

Analog Circuit DESIGN

- ① How to design a analog circuit?
- ② Error budgeting
- ③ Techniques involved in analog circuits.

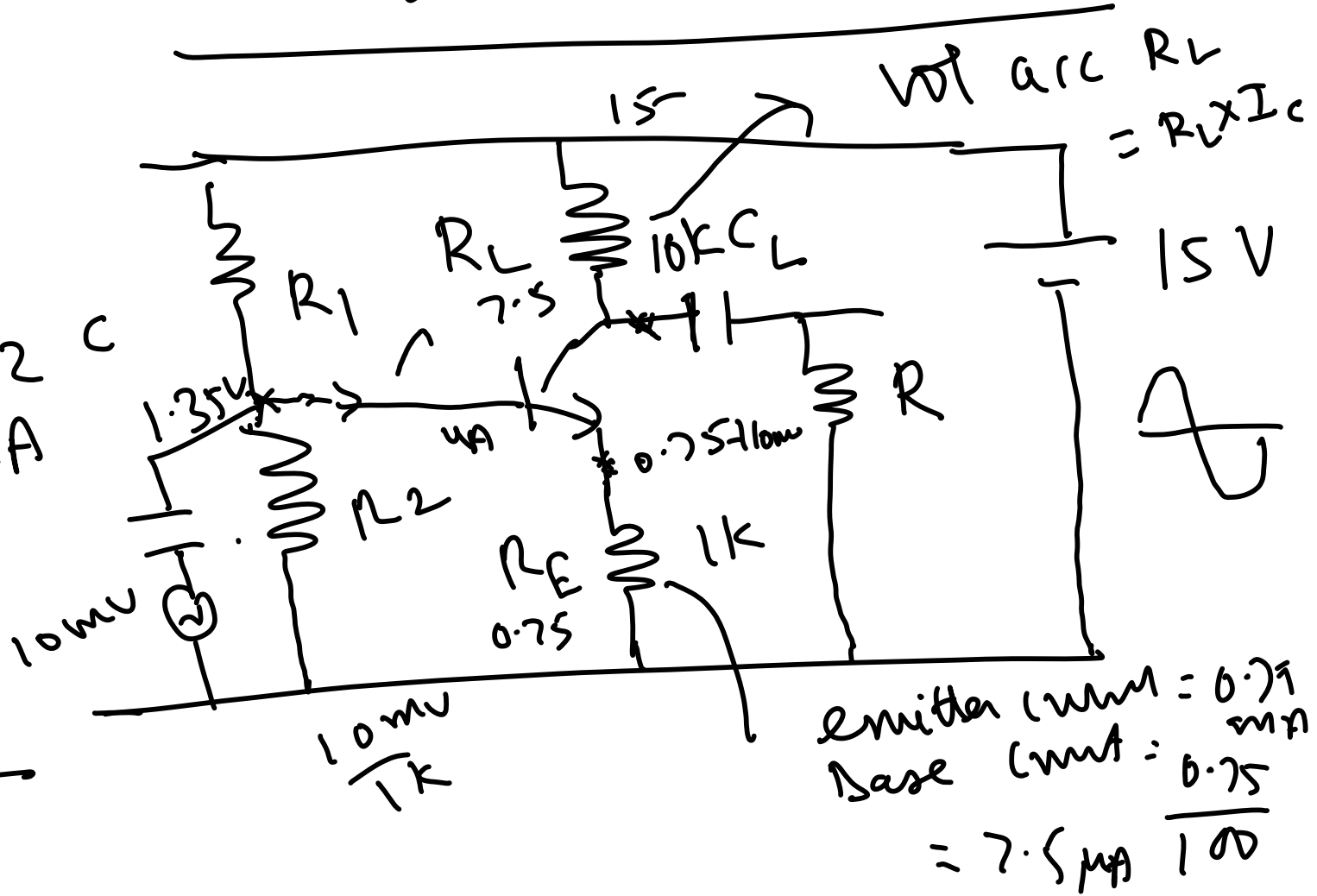
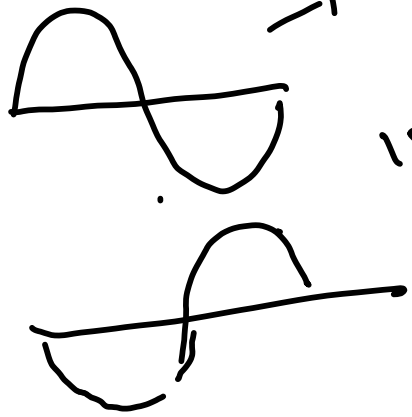
① Designing with
operational amplifiers
and analog integrated
circuits.

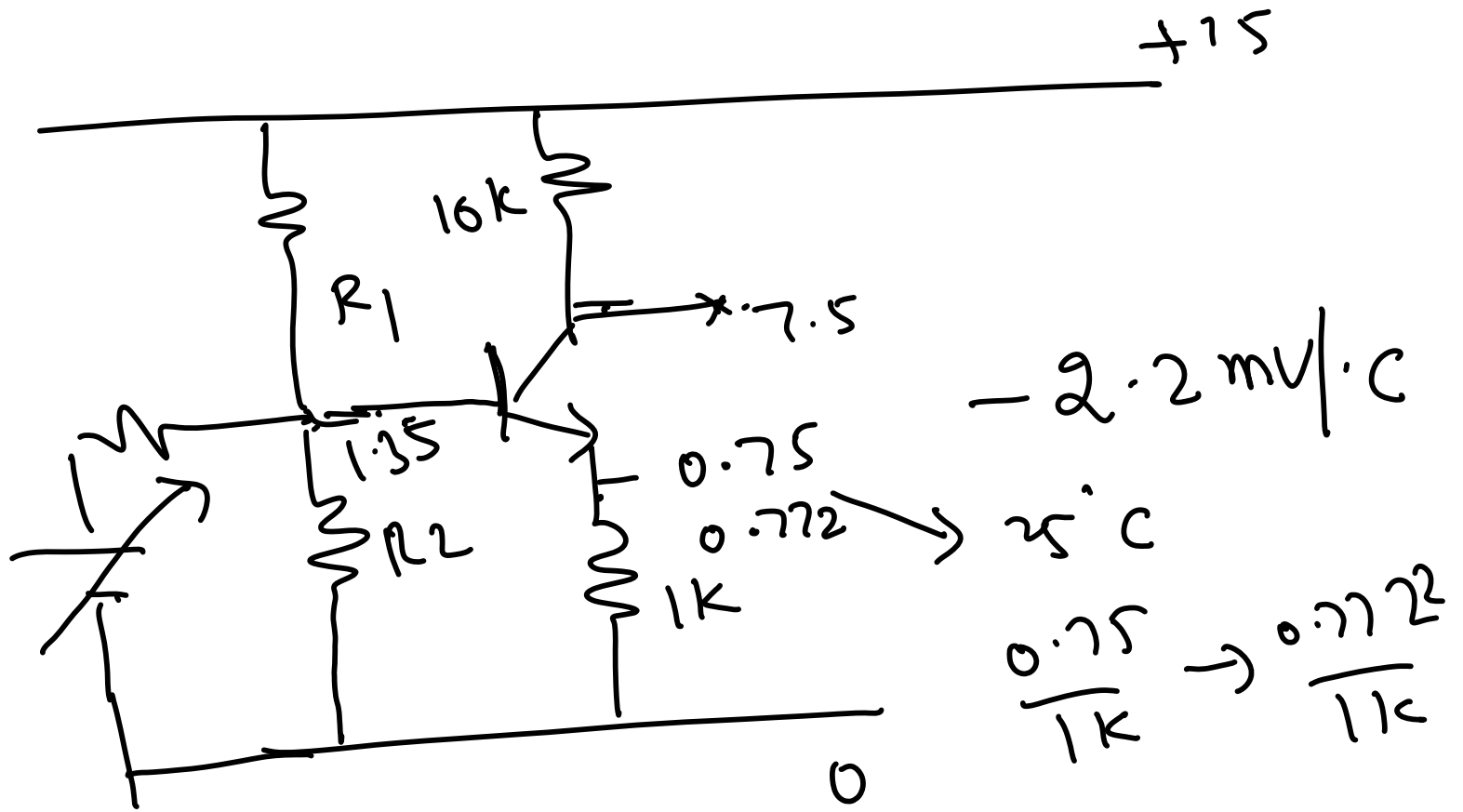
Francis S.

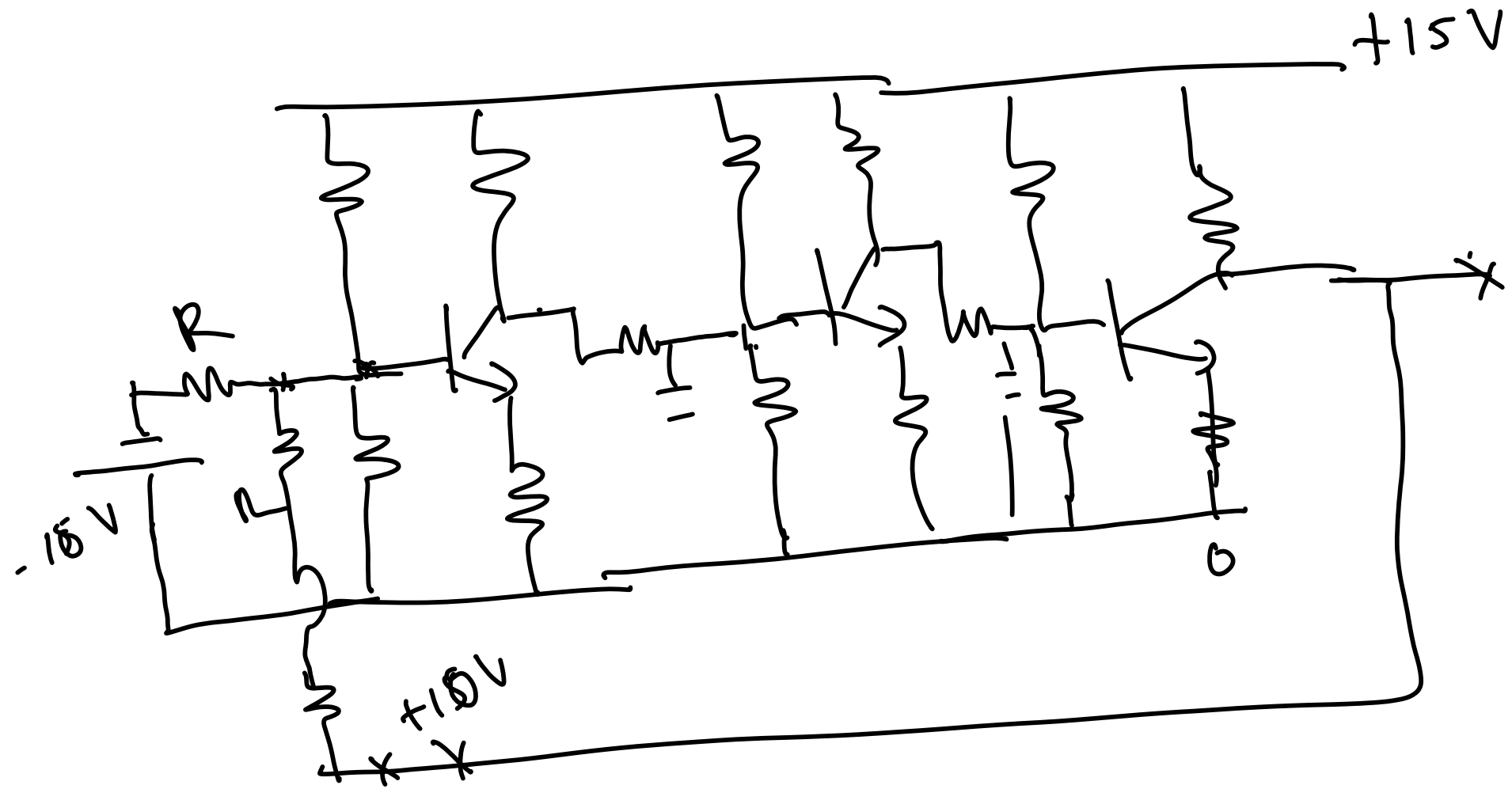
② Paul Horowitz
and Bill
The Art of Electronics

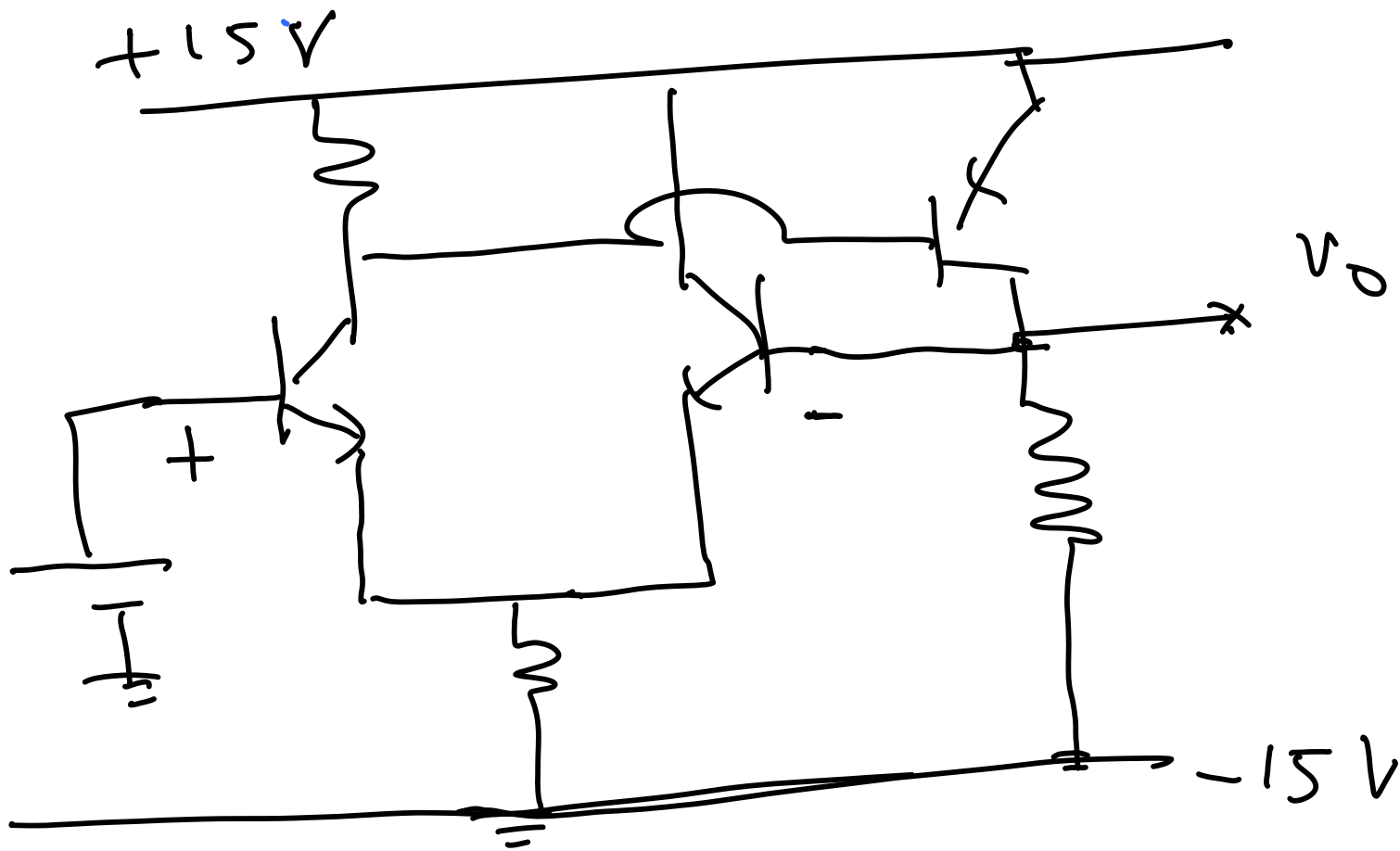
Transistor amplifier

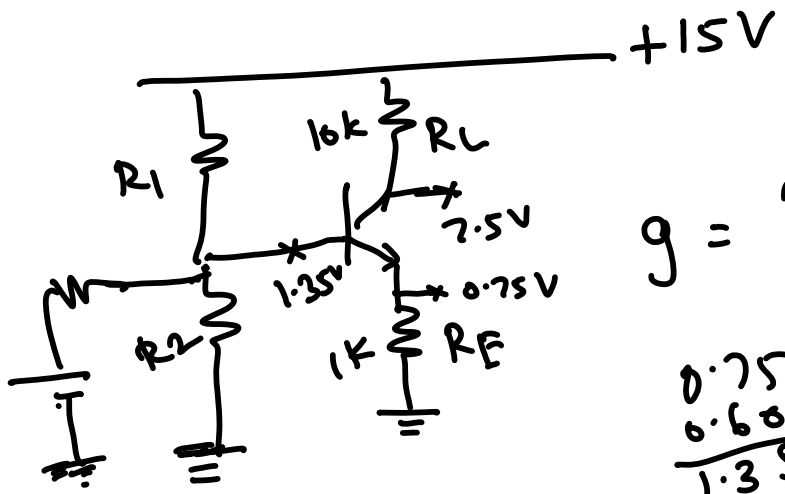
current through R_1 and R_2 $= 7.5 \mu A$





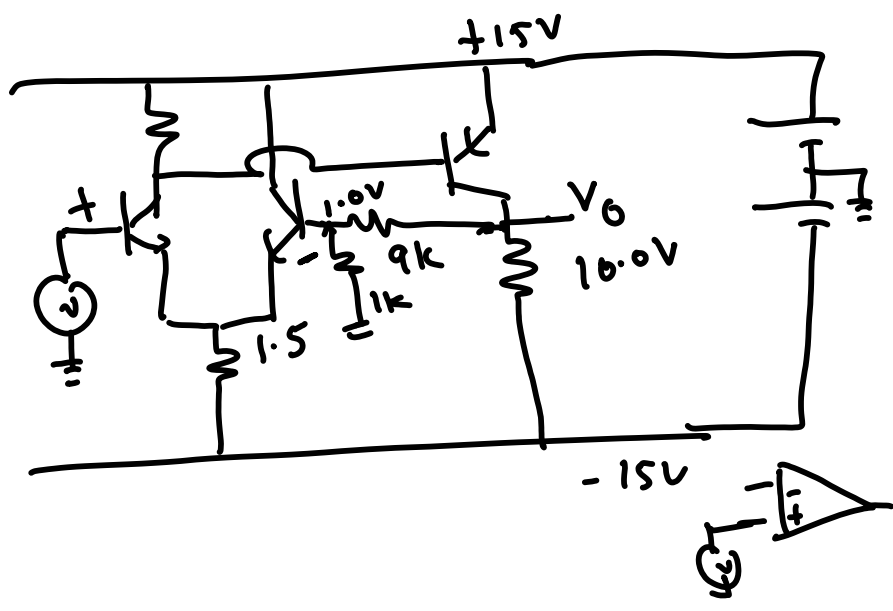


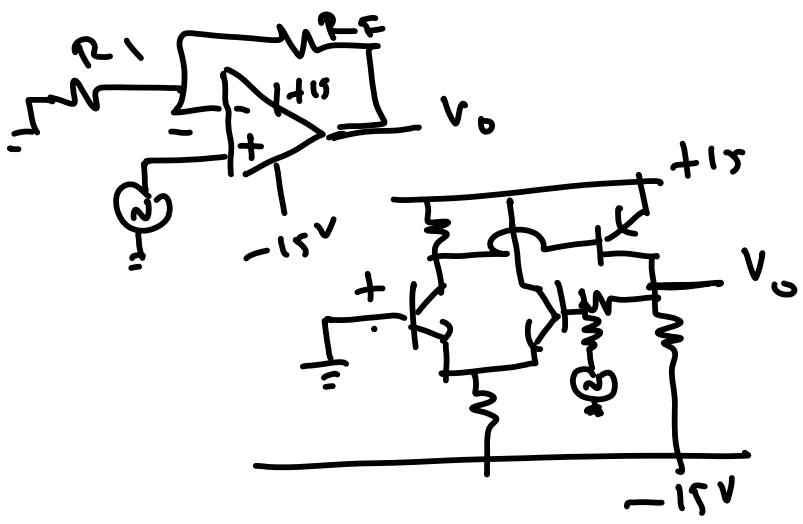


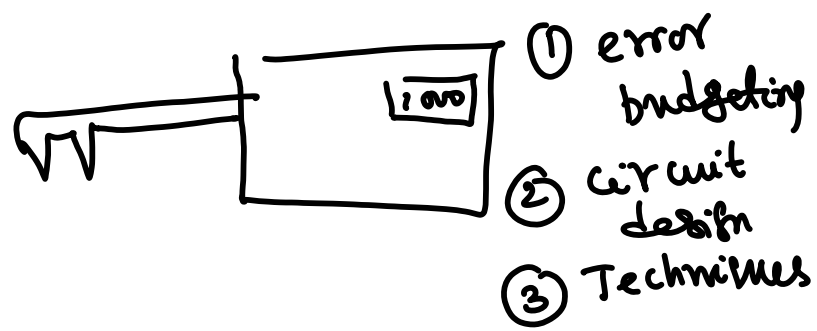


$$g = \frac{R_L}{R_E}$$

$$\frac{0.75}{0.60} = 1.35$$





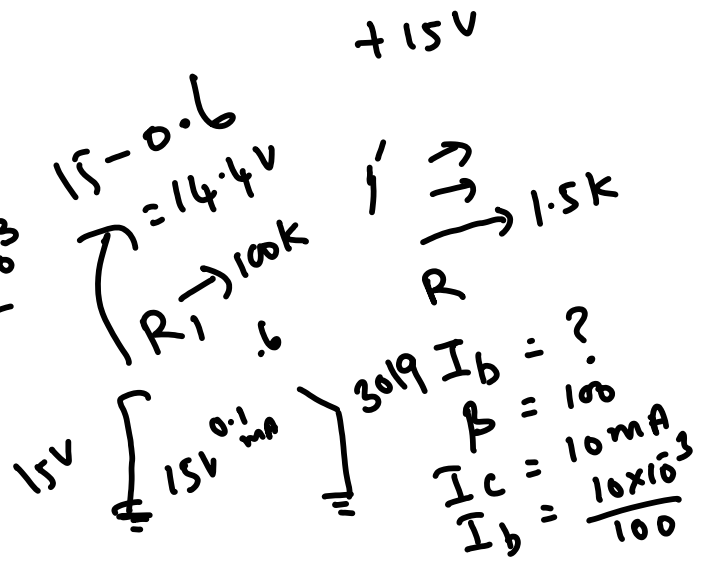


$$V = 14.4V$$

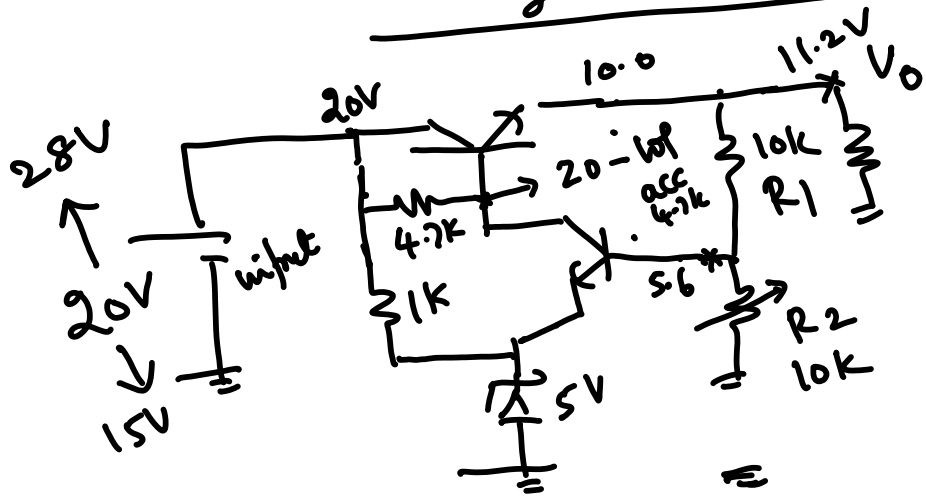
$$I = 0.1mA$$

$$R_1 = \frac{14.4 \times 10^3}{0.1}$$

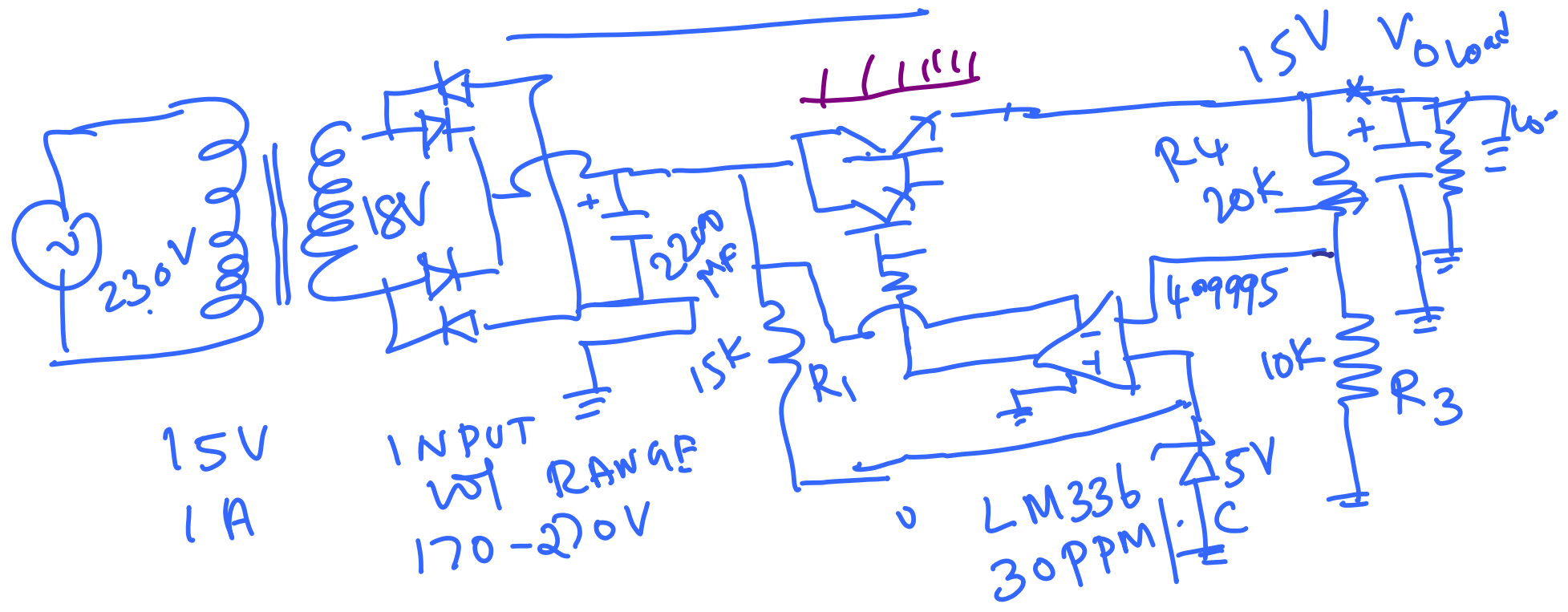
$$= 144K$$

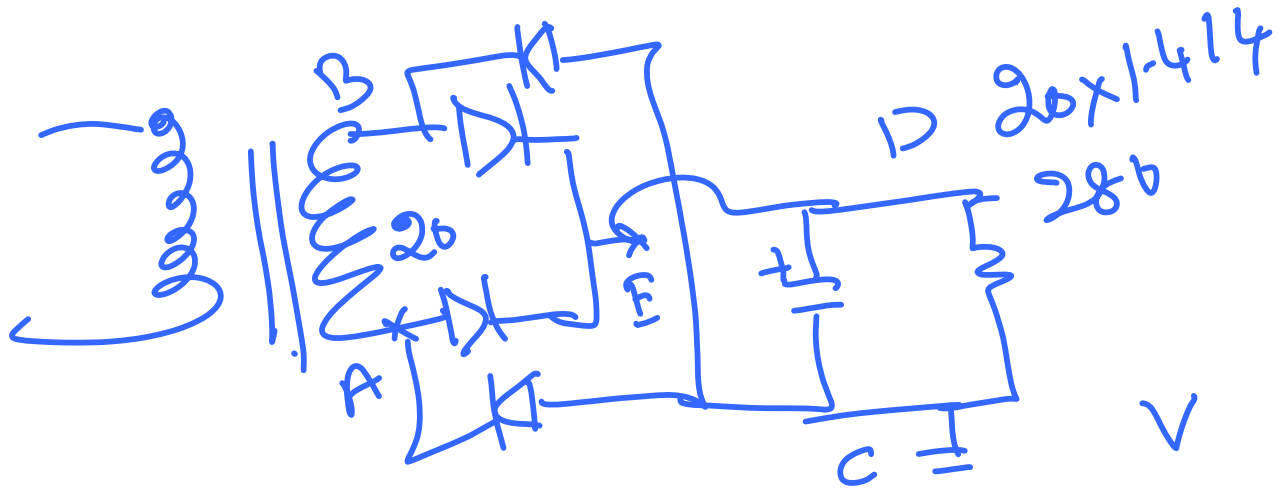


Voltage regulator

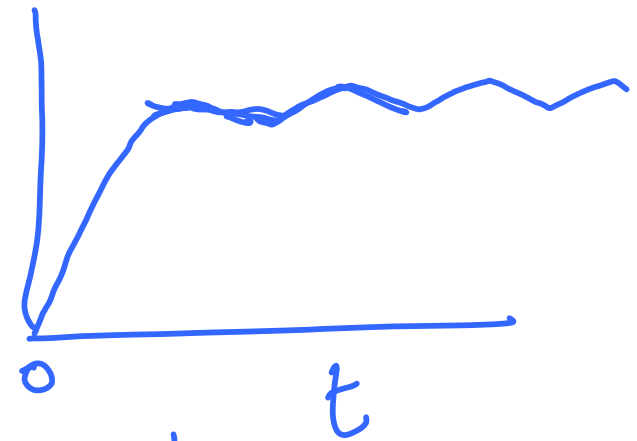
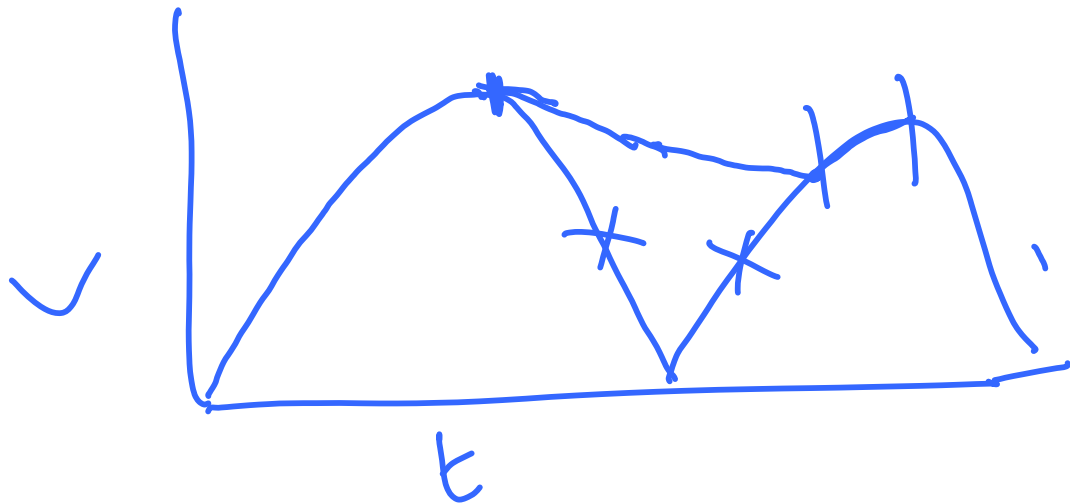


APPLICATIONS OF OP AMP





acc
C and D



At 230V AC input

$$\text{the sec wpt} = \frac{13 \times 230}{170}$$

$$\begin{array}{r} 129 \\ 6 \end{array}$$

=

$$\begin{array}{r} 39 \\ 26 \\ \hline 299 \\ \hline 17 \end{array}$$

$$\approx 18V$$

Pri : 0-230V
Sec = 0-18V

Case 1

Continuous

$$I^2 R = 1^2 \times 1 = 1 \text{ W}$$

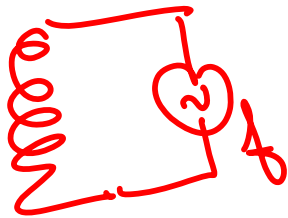
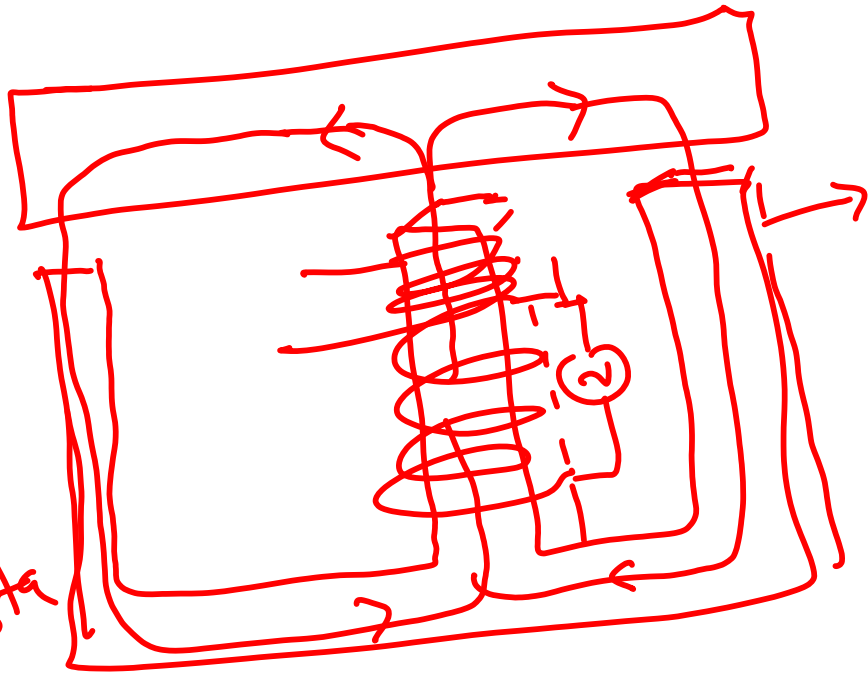
Case 2

3 A for $\frac{1}{3} t$

$$\frac{3^2}{3} \times R = \frac{9 \times 1}{3} = 3 \text{ W}$$

Saturation level
= 1 Tesla

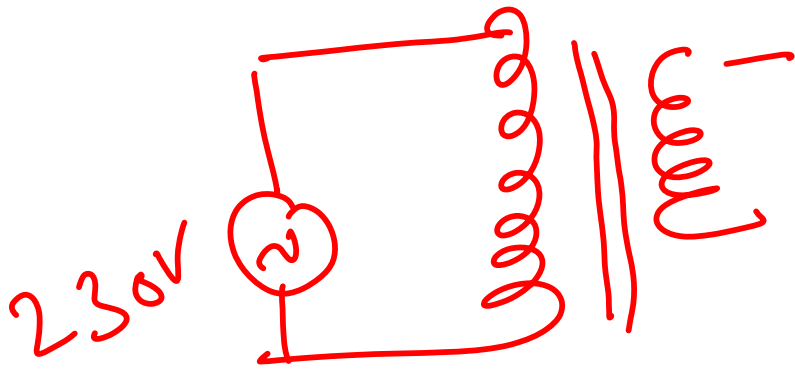
$B = \text{flux density} = 1 \text{ Tesla}$



$$I = \frac{V}{R + L}$$

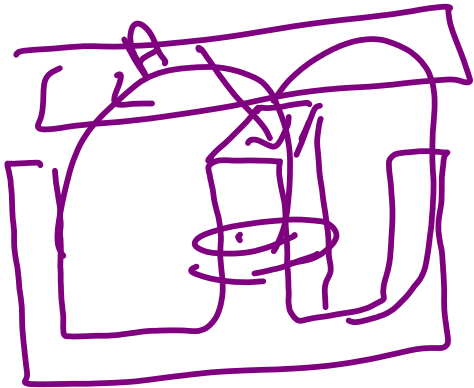
How many
NO. of turns?

- ① CRGO
cold rolled grain oriented
- ② CRNGO
- ③ Dy namo



Basic Concept

Flux $\Phi = I T \mu \mu_0$

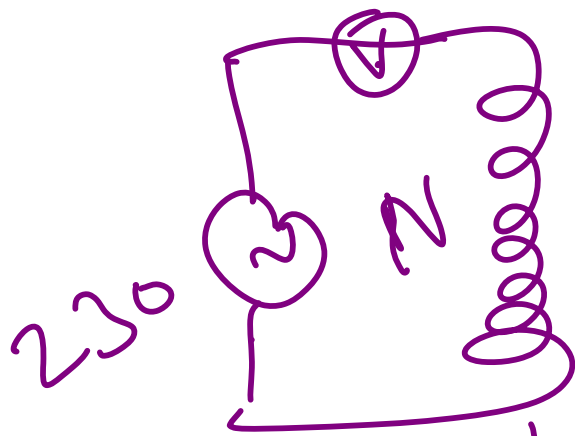


$$B A N \omega = V$$

$$1 \times A \times N \times 2\pi \times 50 = 230$$

$$N = \frac{230}{A \times 2\pi \times 50 \times 1}$$

Thickness of the wire



$$BA N \omega = V$$



$4\pi \times 10^{-7} \text{ H/m}$
3000

$$L = \frac{\mu_0 \mu_r N^2 A}{l}$$



Primary current = $\frac{V}{L \omega}$

① Mag. current
$$j \frac{V}{Lw} = I$$

② Reflected sec current

For 1:1

Reflected current

= Secondary current

$$3 \text{ A} / 1 \text{ mm}^2$$

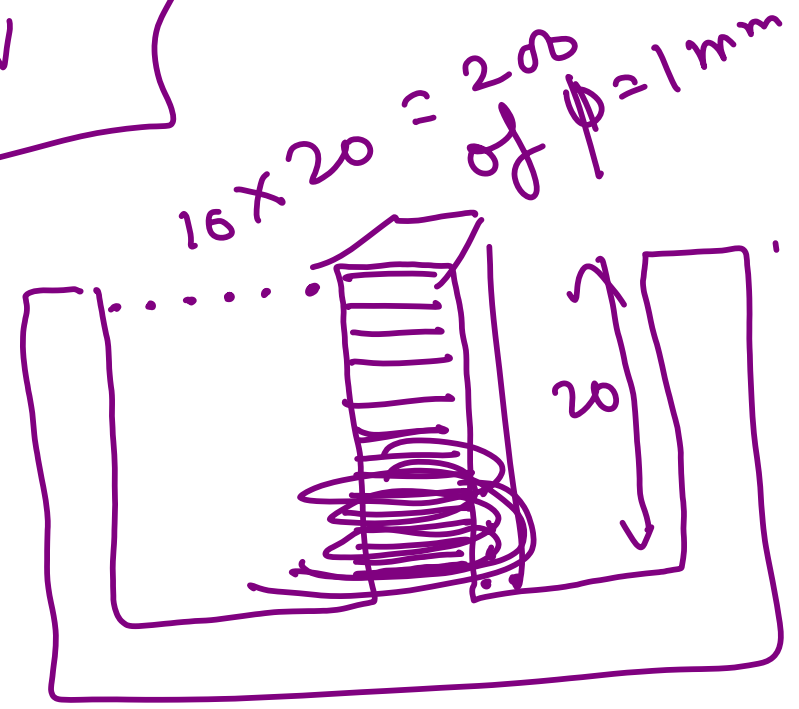
$$\pi r^2 = 1 \text{ mm}^2$$



$$A = 0.3 \text{ mm}^2$$



$B_{ANW} = 230$
 $3A / mm^2$



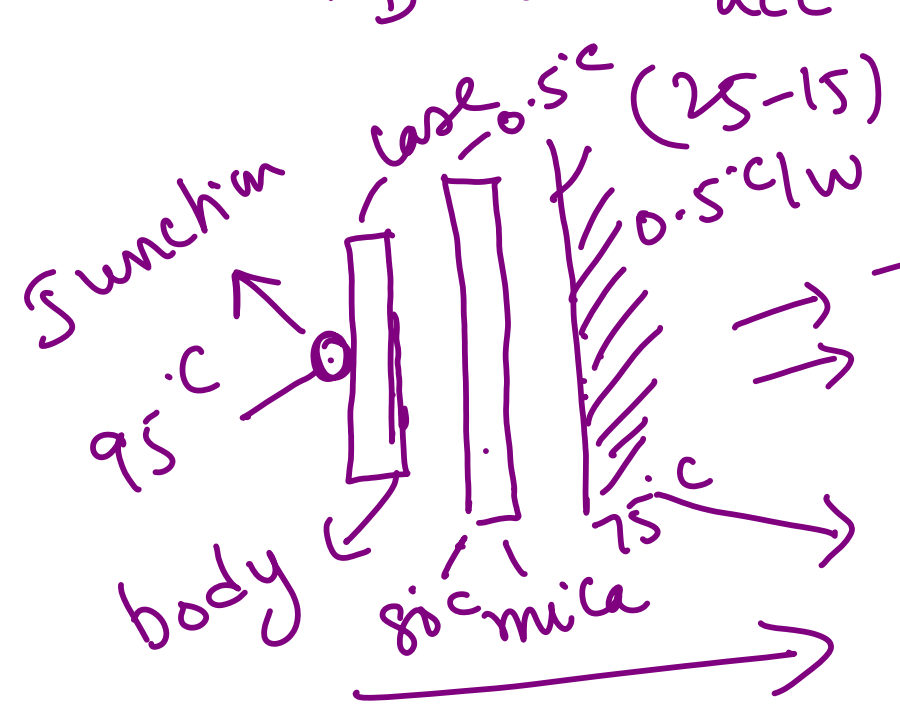
Heat Sink Design

- ① Fix the Junction Temp
Let it be 100°C
- ② What is the max ambient temp?
 - ✓ $0 - 70^{\circ}\text{C}$ — Lab equipment
 - $-20^{\circ}\text{C} - 80^{\circ}\text{C}$ — industrial grade
 - $-40^{\circ}\text{C} - 105^{\circ}\text{C}$ — mil grade

$$T_j = 100^\circ\text{C}$$

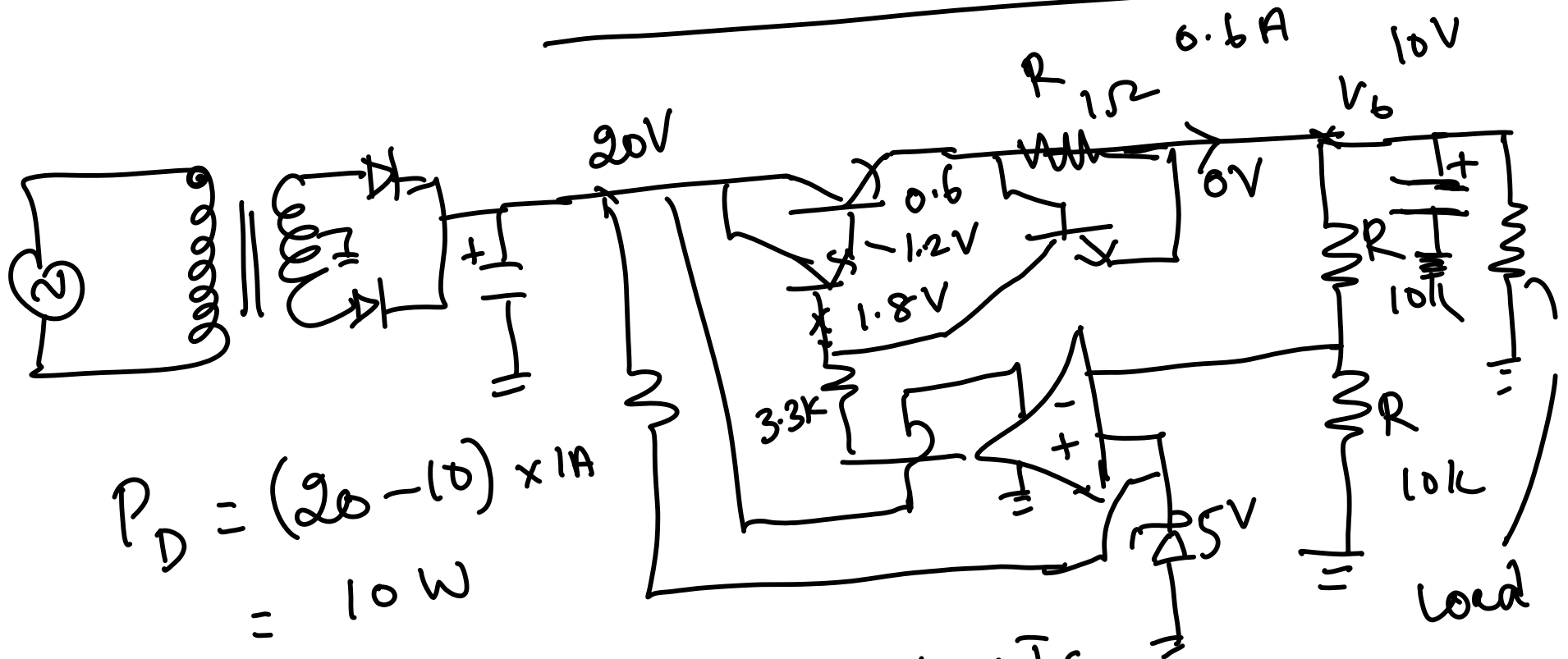
$$T_{\text{amb}} = 70^\circ\text{C}$$

$$P_D = V_{\text{acc}} \times I = 10 \times 1 = 10\text{W}$$



2N3055
Thermal
Resistance
Heat sink from
Jun to case
 $= 1.5^\circ\text{C/W}$
mica $= 0.5^\circ\text{C/W}$

Short circuit protection



$$P_D = (20 - 10) \times 1A$$

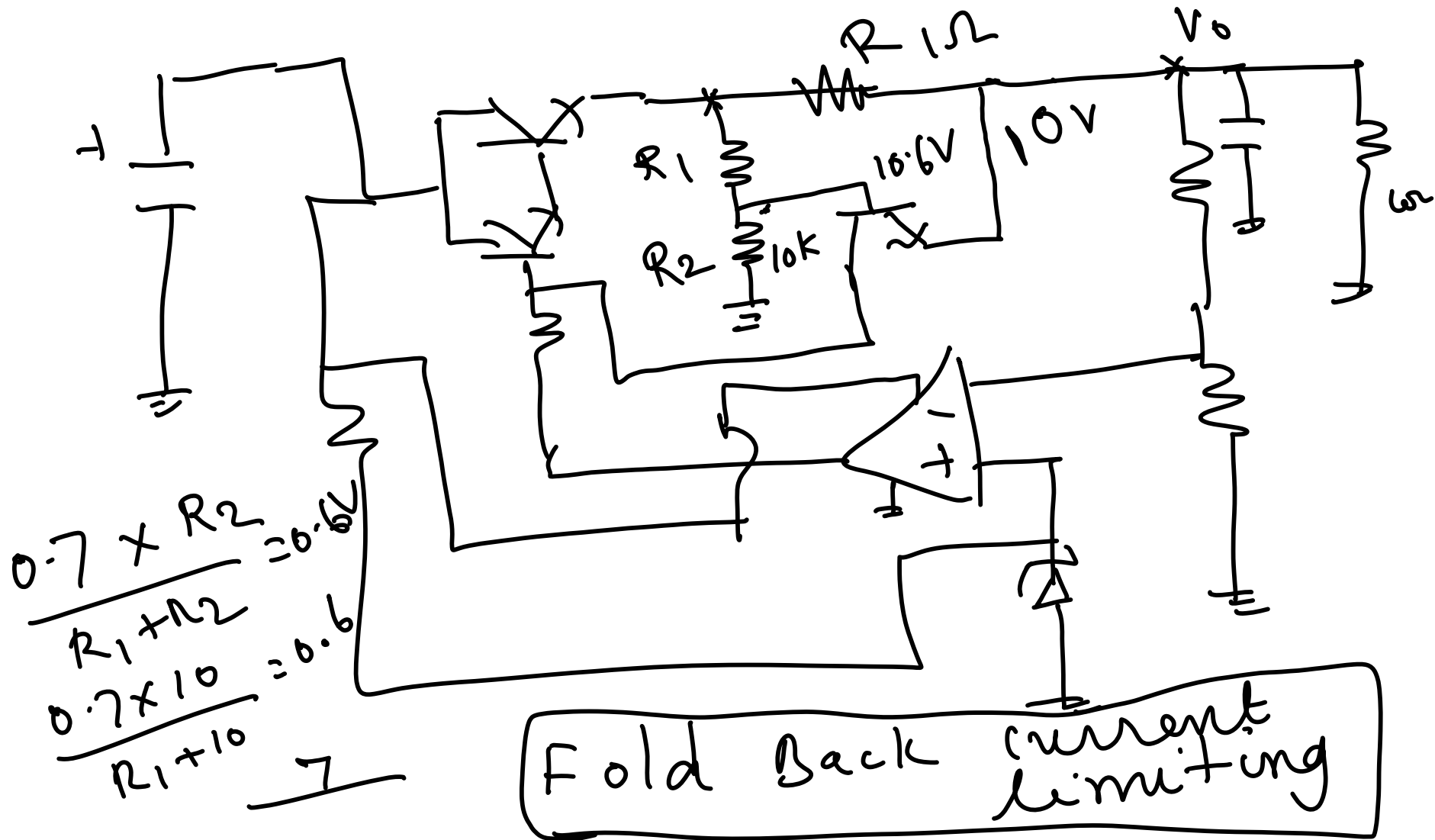
$$= 10W$$

$$0.6V = R \times I_S$$

$$0.6 = 12 \times 0.6A$$

UNDER NORMAL CON $P_W = (20 - 10) \times 0.6 = 6W$

Under Short circuit $P_W = 20 \times 0.6 = 12W$



$$\frac{7}{R_1 + 10} = 0.6$$

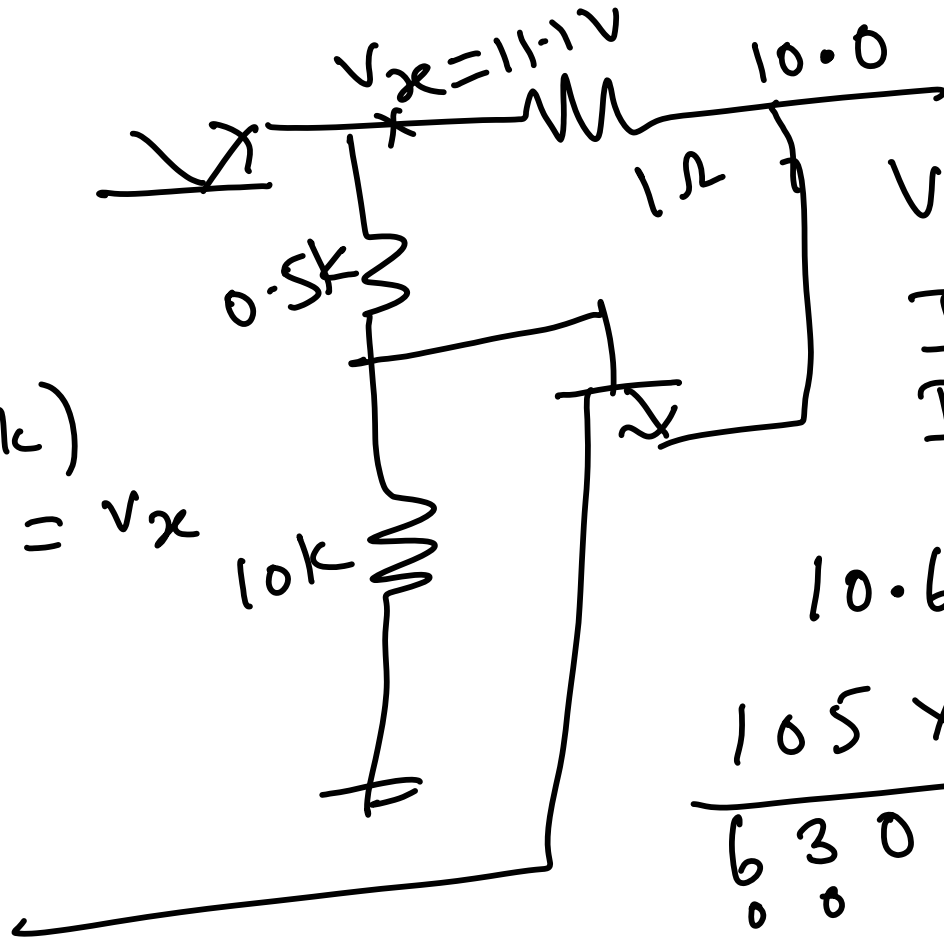
$$7 = 0.6 R_1 + 6$$

$$1 = 0.6 R_1$$

$$R_1 = \frac{1}{0.6}$$

$$= \frac{1000}{600}$$

$$= 0.5k$$



$$V_D = 1.1V$$

$$I = 1.1A$$

$$I_S = 0.7A$$

$$\frac{10.6 (10.5k)}{10k} = V_x$$

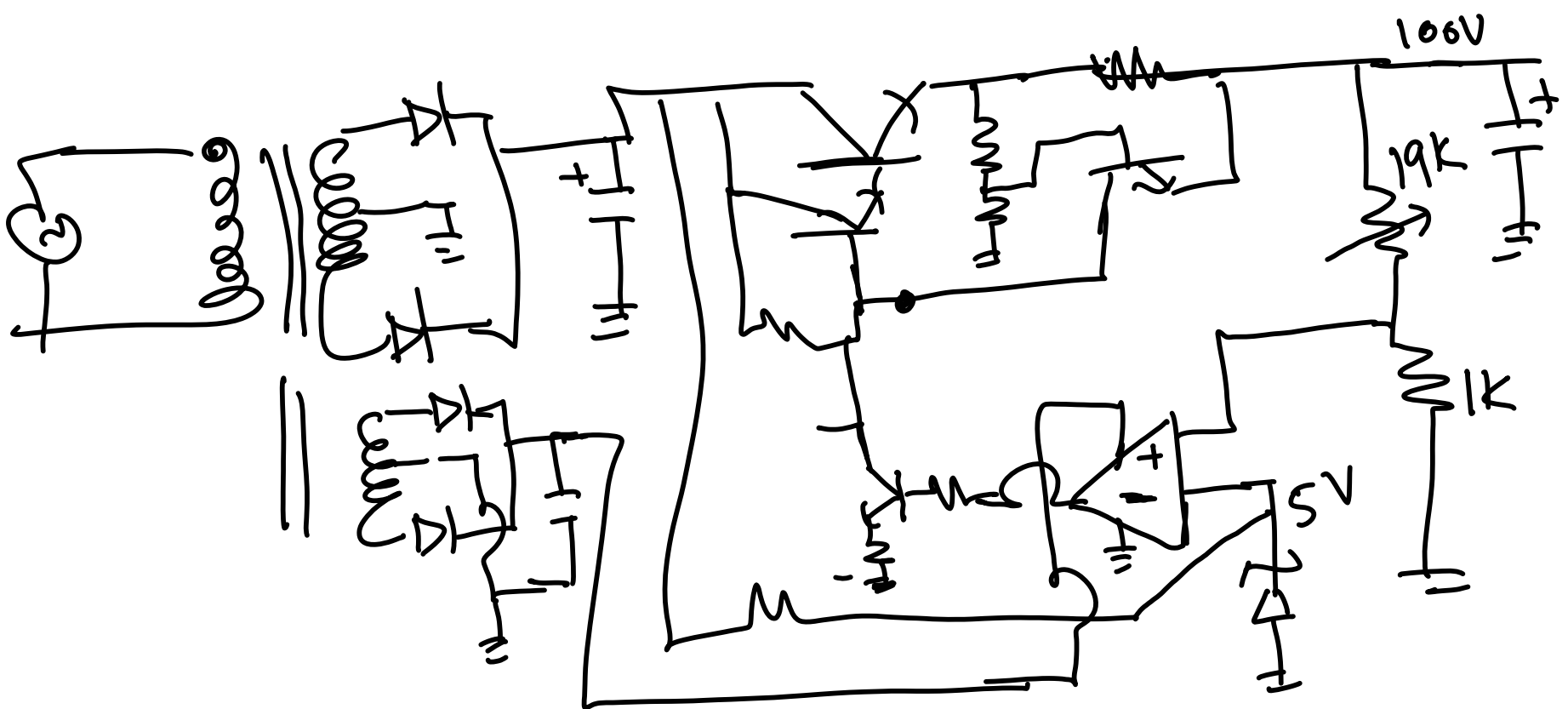
$$\frac{10.6 \times 10.5}{10}$$

$$10.6 \times 1.05$$

$$105 \times 1063$$

$$\begin{array}{r} 630 \\ 00 \end{array}$$

$$\begin{array}{r} 105 \\ \hline 11136 \end{array}$$



Temperature indicator

IC Sensor - LM335



$$-2.2 \text{ mV}/^{\circ}\text{C}$$

at 25°C $V_{BE} = 0.6\text{V}$

35°C $V_{BE} = 0.578$

$R = ?$

$T_H = 100^{\circ}\text{C}$

$T_L = 0^{\circ}\text{C}$

At 0°C w/ acc the sensor = 2.73V

At 100°C

Vol acc the sensor

$$= 3.73 \text{ V} \rightarrow 1.00 \text{ V}$$

$$V_0 = (273 + T_c) \times 10 \text{ mV}$$

$$\text{At } 0^\circ\text{C} = 2.73 \text{ V} \checkmark \rightarrow 0.00 \text{ V}$$

$$\text{At } 1^\circ\text{C} = 2.74 \text{ V}$$

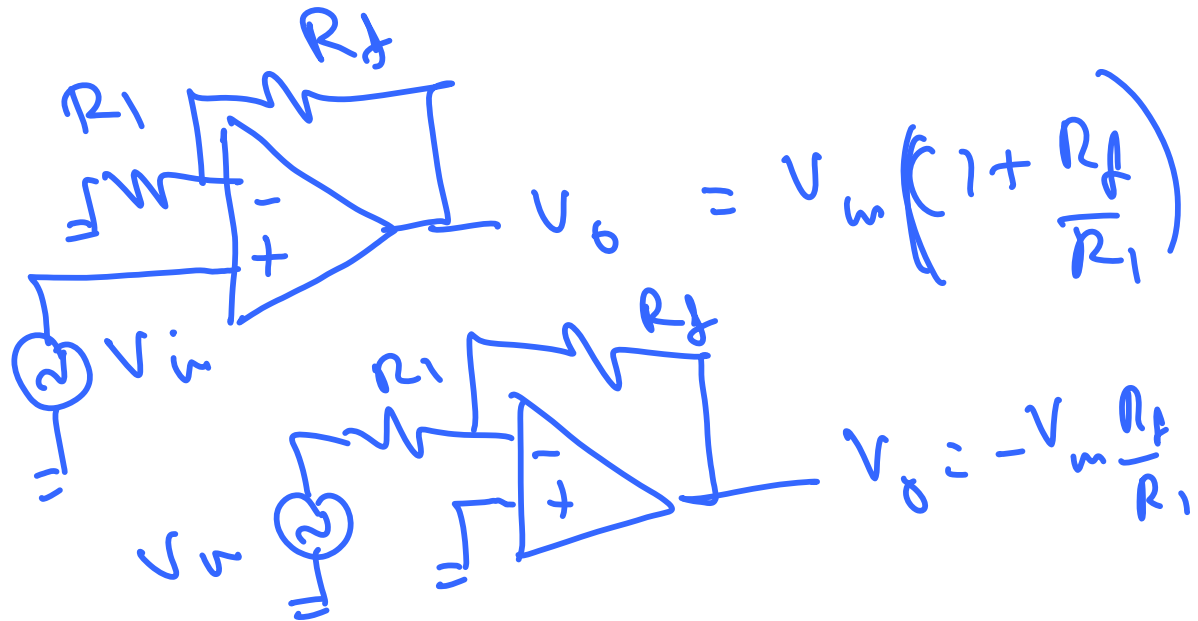
$$2^\circ\text{C} = 2.75 \text{ V}$$

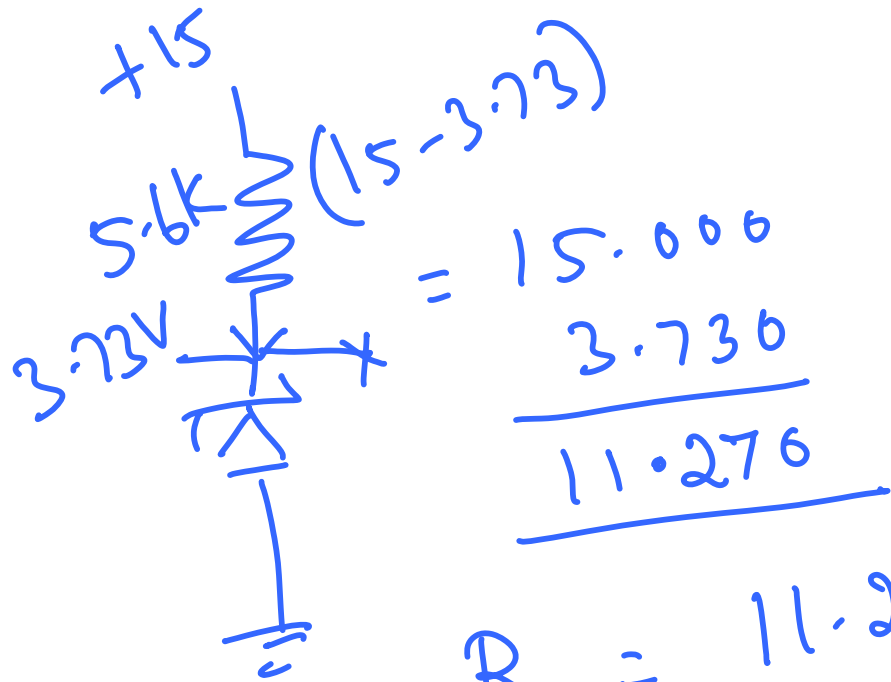
$$25^\circ\text{C} = \begin{array}{r} 2.73 + \\ 0.25 \\ \hline 2.98 \text{ V} \end{array}$$

At 0V \rightarrow 0V

at 1V \rightarrow 1.000V

50V \rightarrow 0.500V





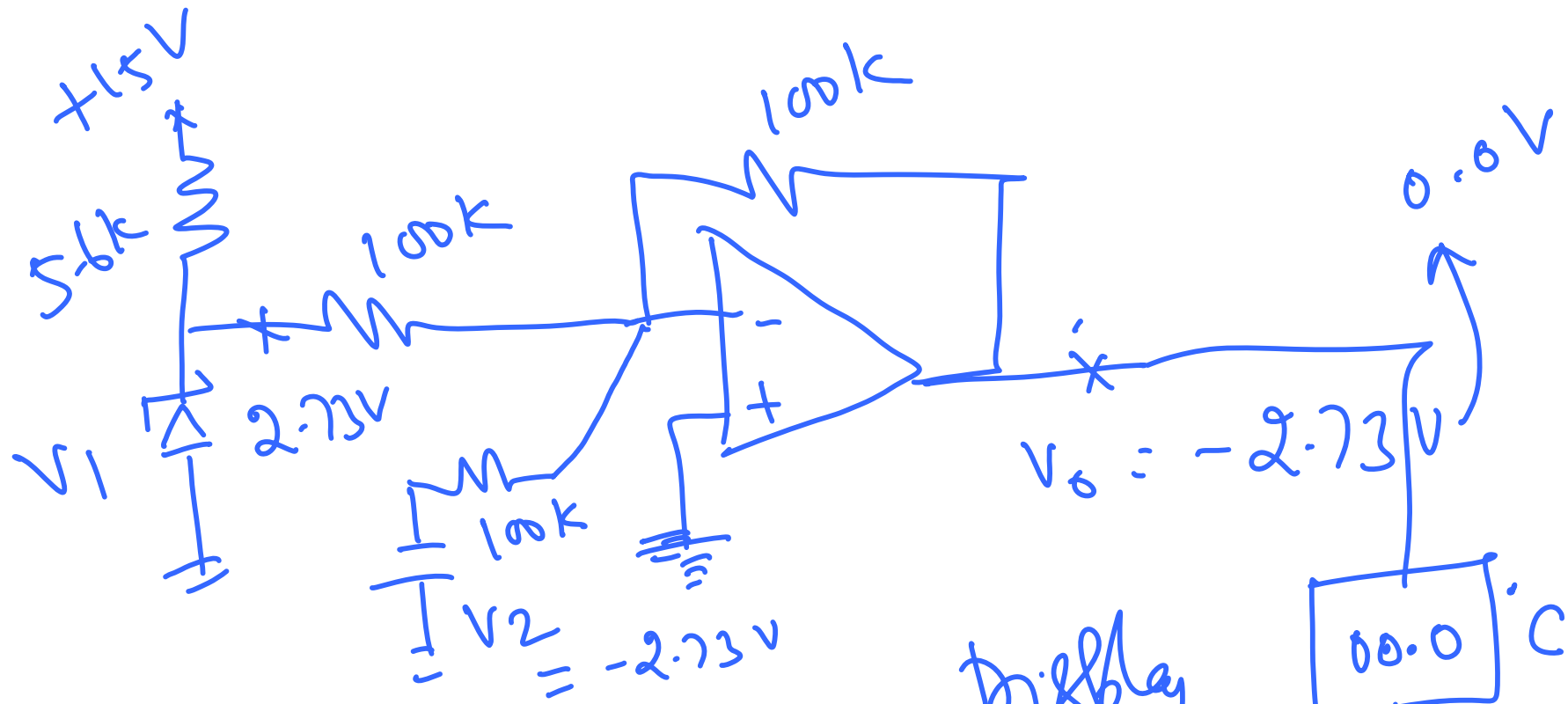
$$= \frac{15.000}{3.730}$$

$$\underline{\underline{11.276}}$$

$$R = \frac{11.270}{\text{current}} = \frac{11.270}{2 \times 10^{-3}}$$

$$= 5.56 k$$

$$= 5.6 k$$



$$-V_1 + V_2 = 0$$

At $100^{\circ}C$

display

Band gap
LM 336

At $t = 0^-$

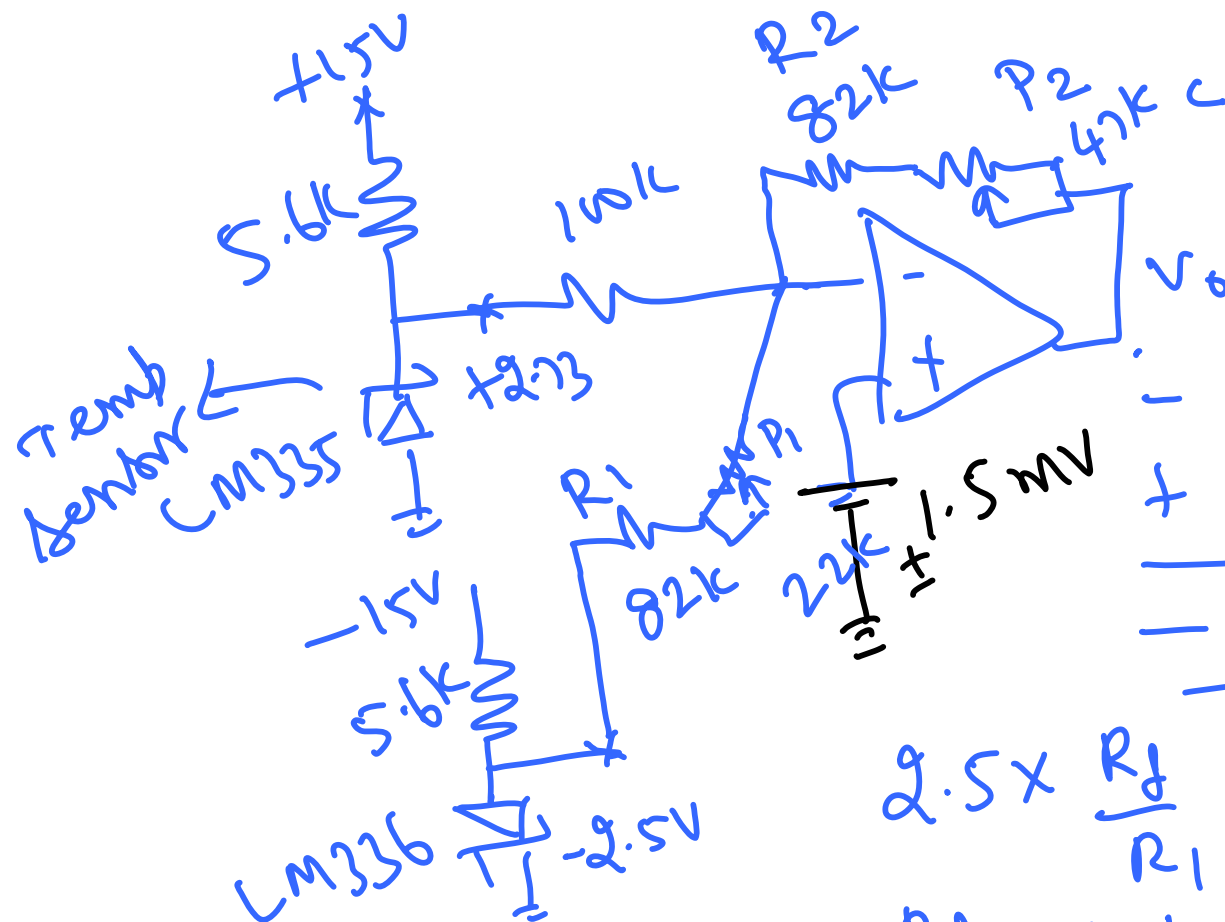
$$V_S = 3.73 \text{ V}$$

$$V_O = -3.73 + 2.73$$

$\downarrow_{V_1} \qquad \qquad \downarrow_2$

$$= -1.0 \text{ V}$$

$$\text{At } \begin{matrix} 0^+ \\ \infty \end{matrix} = \begin{matrix} 0 \text{ V} \\ -1.0 \text{ V} \end{matrix}$$



$$3.72 \times 9 = 3.73$$

$$3.74 \times 9 = 3.73$$

$$\begin{array}{r} -2.73 \\ +2.50 \\ \hline -0.23 \end{array}$$

$$2.5 \times \frac{R_f}{R_1} = 2.73$$

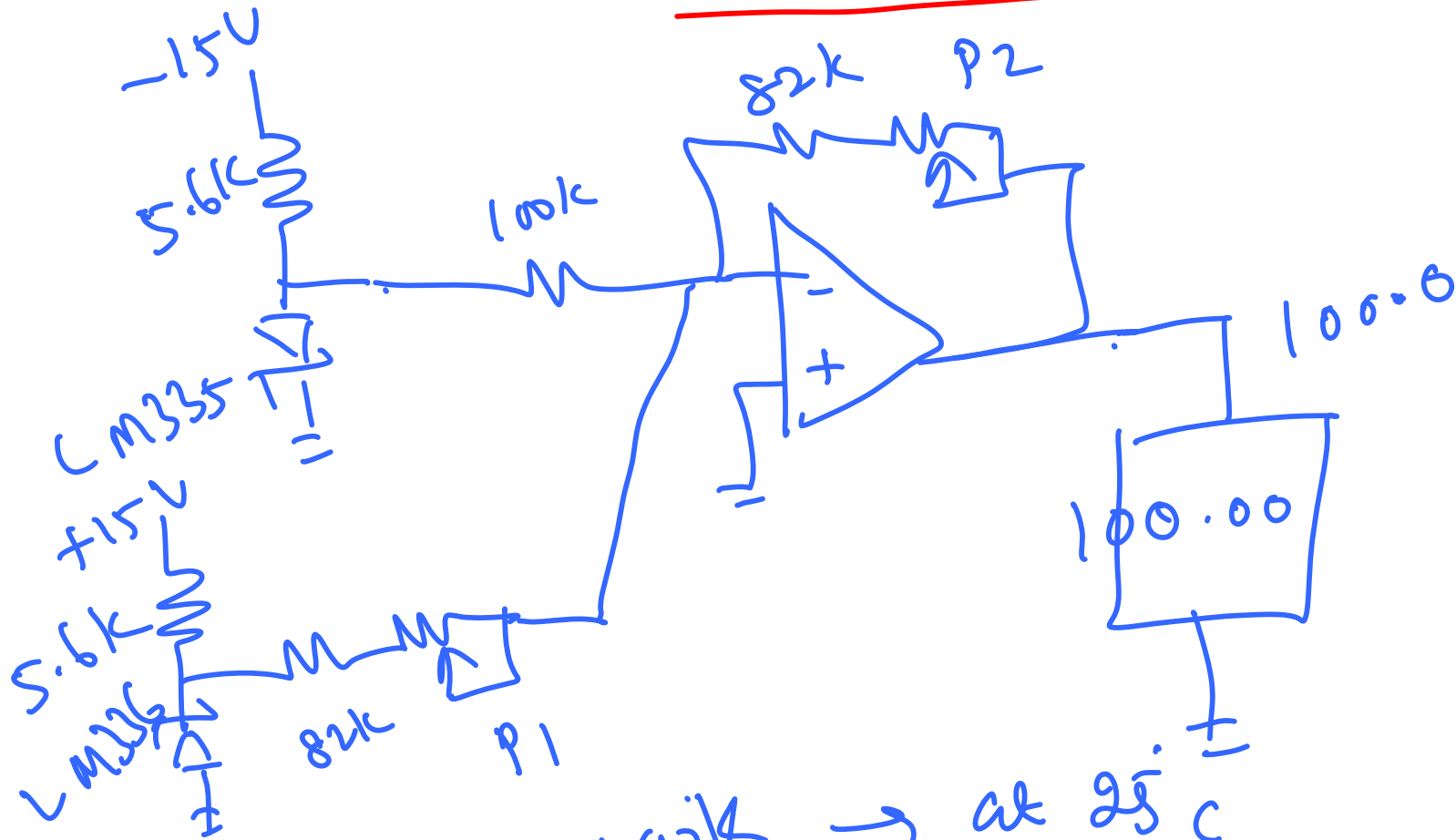
$$R_f = 100k$$

$$2.5 \times \frac{100k}{R_1} = 2.73$$

$$\frac{2.5 \times 100k}{2.73} = R_1$$

- ① Keep the sensor in
ice
Adj P₁ to get $V_0 = 6$
- ② Keep the sensor at 100°C
Adj P₂ to get $V_0 = 1.00\text{V}$
- ③ Repeat ~~step~~ 1 and 2
several times

Error calculations



100k \rightarrow at 25°C

? \rightarrow at 50°C
LM336 temp drift $\pm 30 \text{ ppm}/^\circ\text{C}$
max

working temp range

ambient temp

range $\rightarrow 100^\circ\text{C}$

Temp Drift = $30 \text{ PPM}/^\circ\text{C}$

Total drift = $30 \times 100 \text{ PPM}$

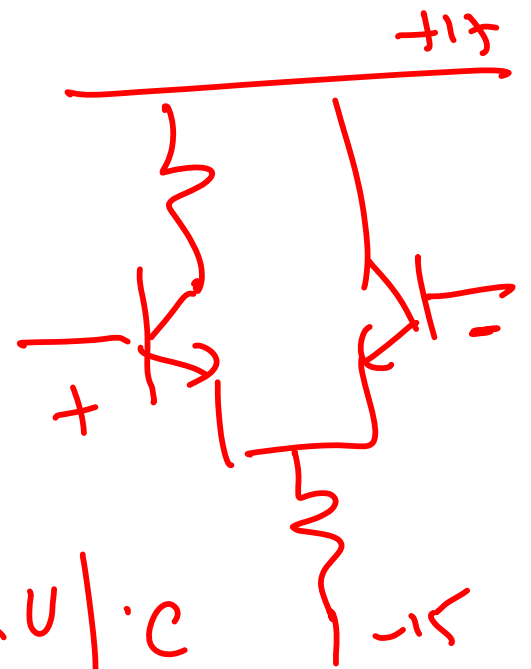
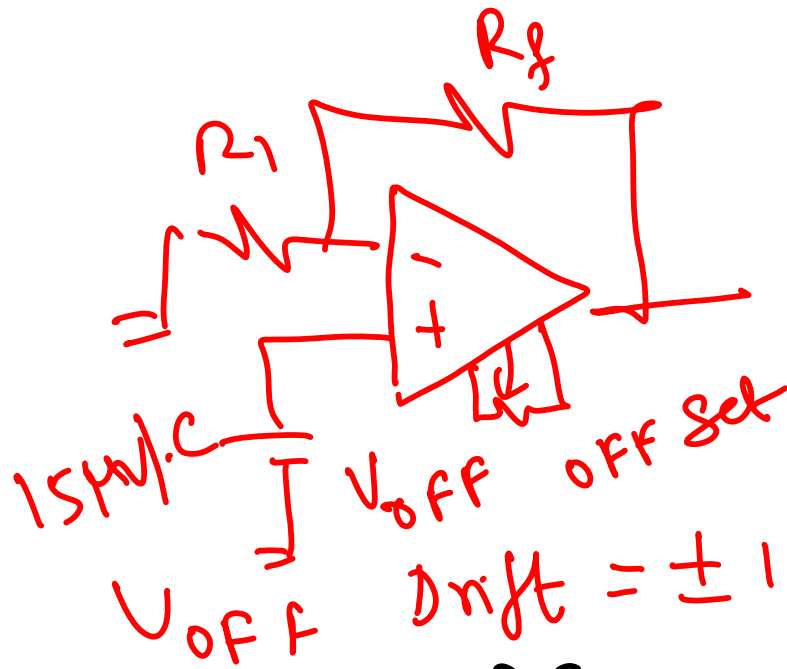
= $\frac{30 \times 100}{10^6}$

drift rel $\omega_f = 2.5 \times 10^{-6}$

Total charge for 2.5 V
for $\Delta T = 100^\circ\text{C}$

$$\begin{aligned} &= \frac{2.5 \times 30 \times 100}{10^6} \text{ V} \\ &= 2.5 \times 3 \times \frac{10^3}{10^6} \\ &= 7.5 \times 10^{-3} \\ &= 7.5 \text{ mV} \end{aligned}$$

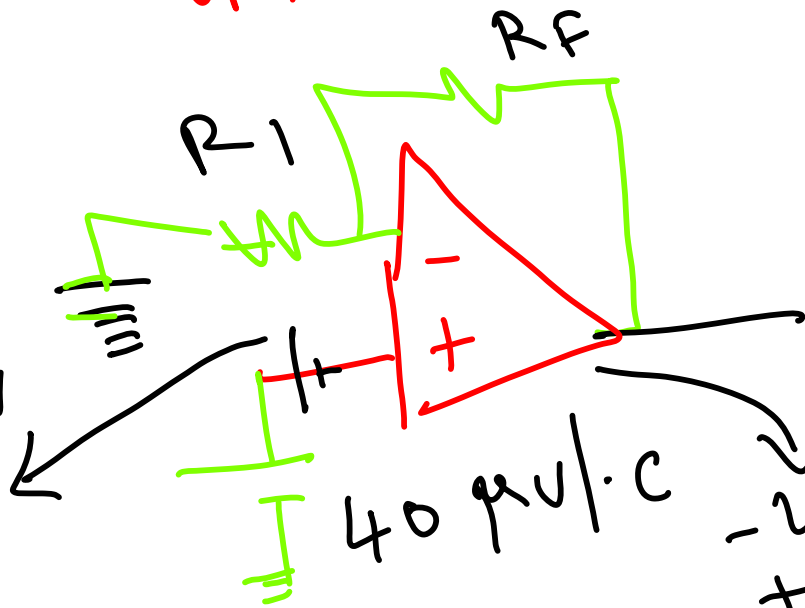
15×10^{-6}
 1.5 mV



$V_{\text{OFF}} \text{ Drift} = \pm 15 \mu\text{V}$

$15 \mu\text{V} \times 100$

$R_{\text{OFF}} = 241$
 1.5 mV

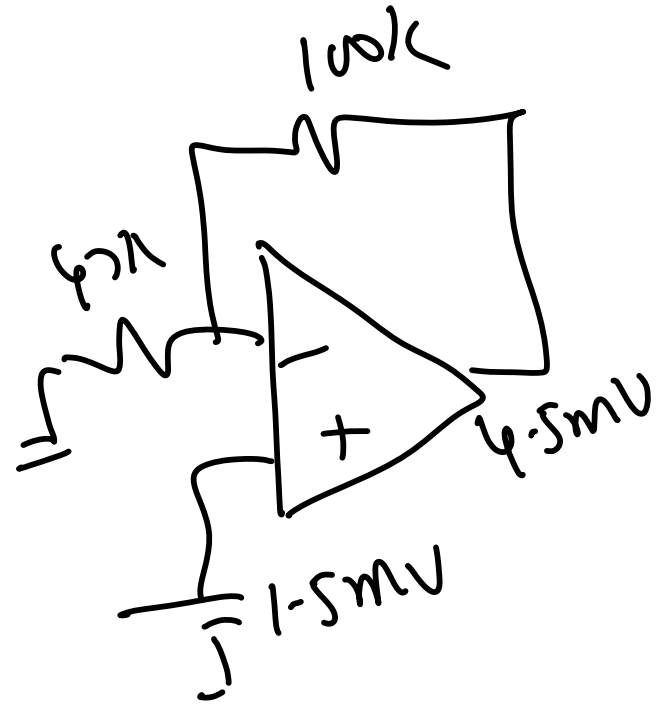
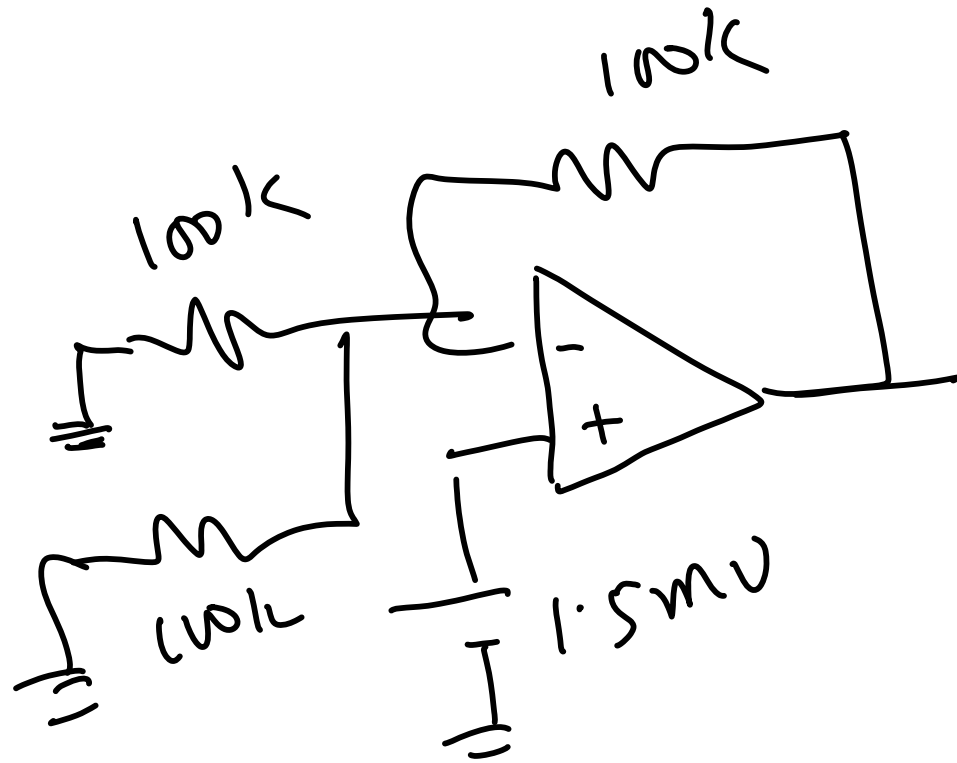


-20°C
 $+80^\circ\text{C}$
 $V_0 = 400 \mu\text{V}$
 $= 400 \mu\text{V} + 15 \text{ mV}$
 $15 \times \frac{1000}{400} = \frac{150}{4}$

$$E_{mr} = \frac{15 \times 1000}{400} = \frac{150}{4} = 37.5^\circ\text{C}$$

Actual temp = 1°C

$$\begin{aligned} \text{What is shown } &= 1^\circ\text{C} + 37.5^\circ\text{C} \\ &= 38.5 \\ &= -36.5^\circ\text{C} \end{aligned}$$

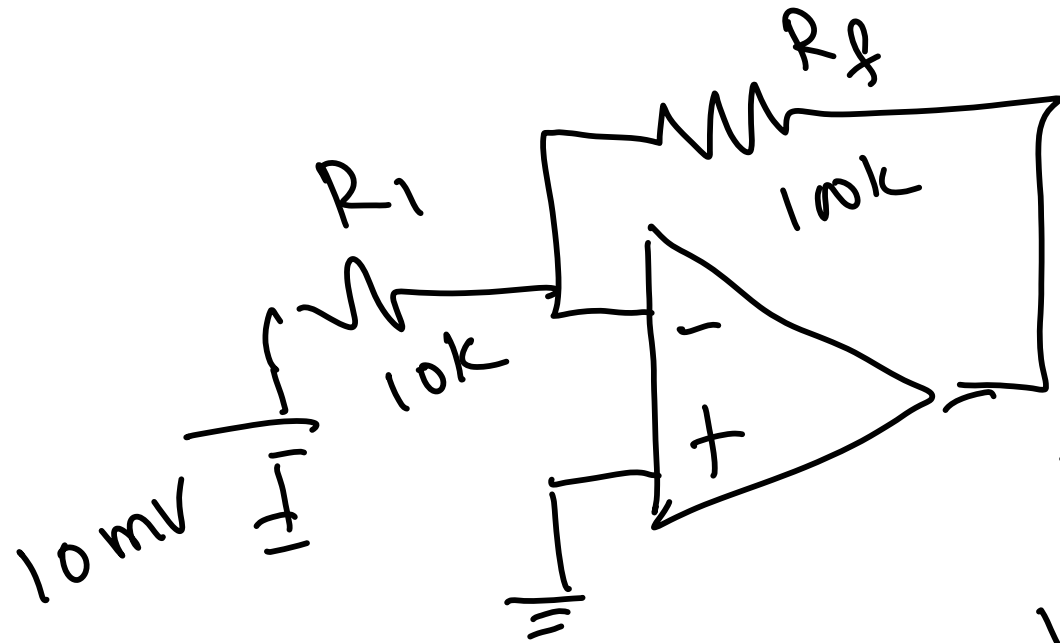


emr due to
 V_{OFF} drift
 emr due to

$$= 4.5 \mu V \quad g = 3 \quad = 0.45^\circ C$$

$$\text{zener drift} = 7.5 \mu V = 0.75^\circ C$$

Resistance drift

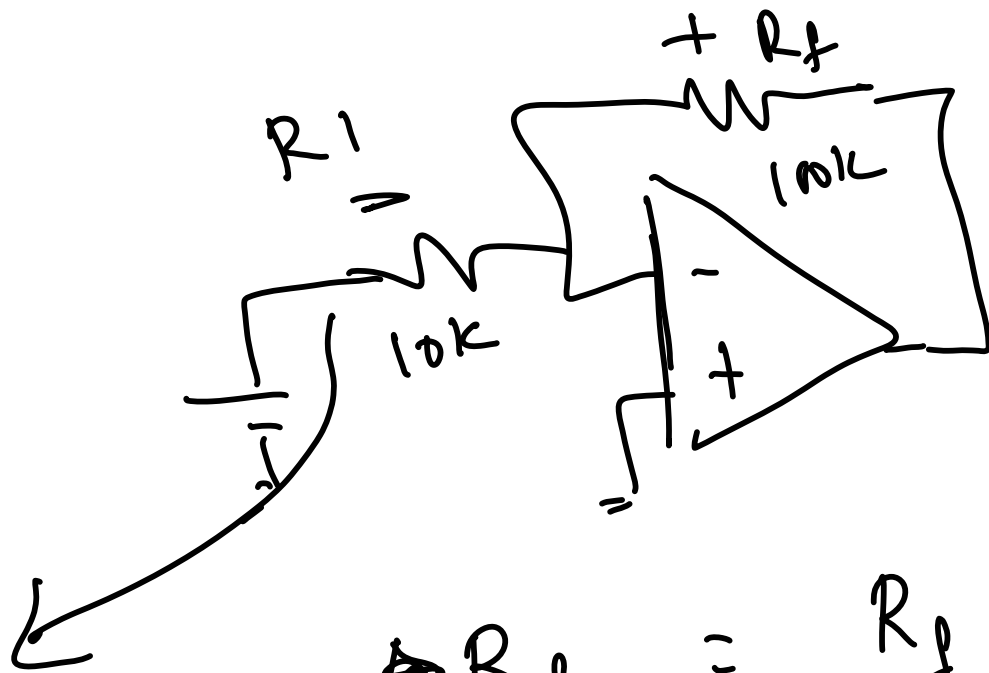


$$g = 10$$

$$V_{in} = 10mV$$

$$V_o = -100mV$$

$$\text{Temp } \omega - \text{eff} = \pm 300 \text{ ppm}/^\circ\text{C}$$



$$R_{ic} = \frac{100k + 3k}{10k - 300\Omega}$$

R_{ic} at ω_{ic}

$$= \frac{10^4 - 10^4 \times 300 \times 10^0}{10^6}$$

$$= \frac{10^4 - 3 \times 10^4}{10^6} = 10k - 300$$

~~R_{ic}~~ $R_{f_{at}}$

$$= R_f = 10^5$$

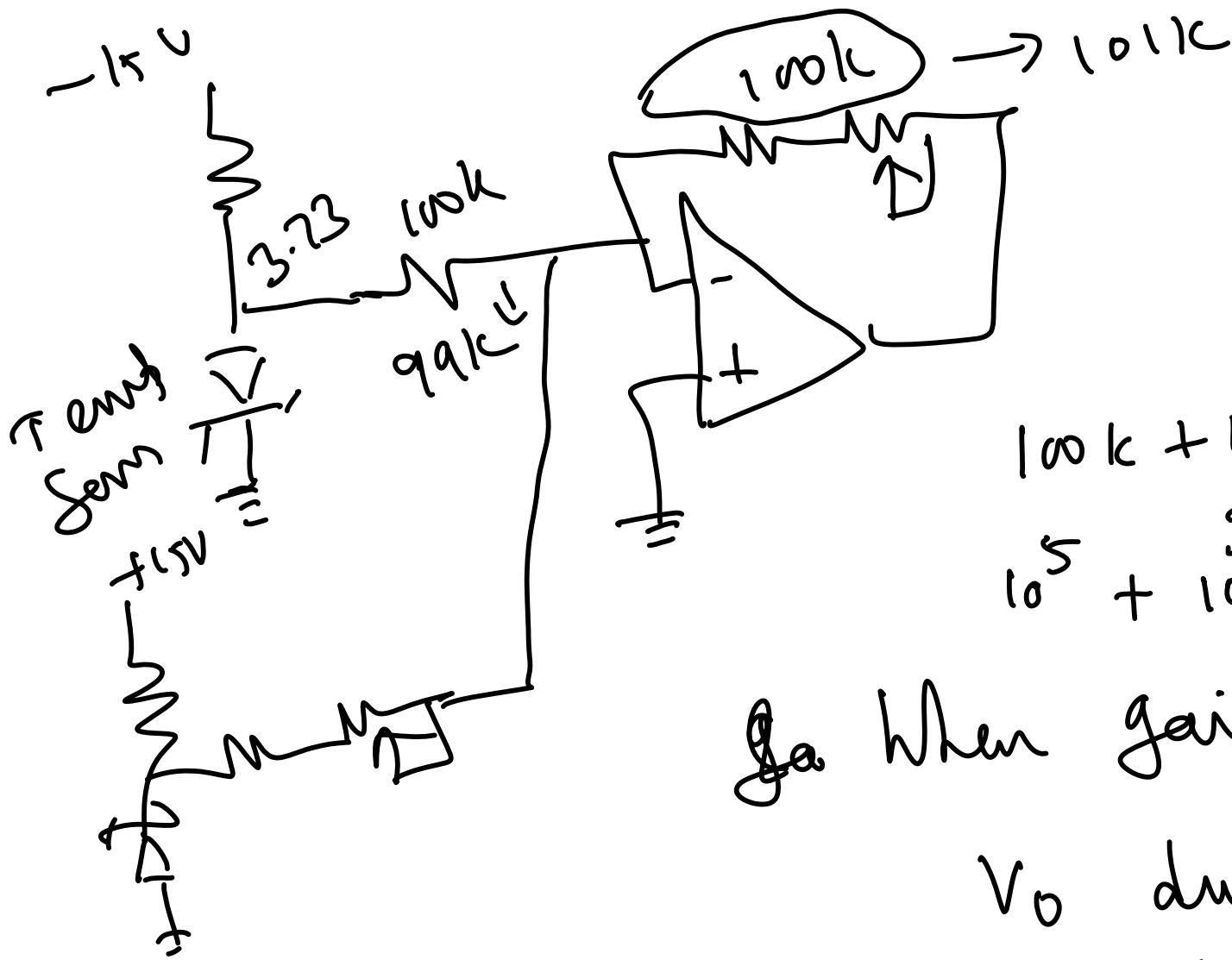
$$+ \frac{R_f \times 300 \times 10^0}{10^6} = 10^5 + \frac{3 \times 10^4}{10^6} = 10^5 + 3 \times 10^{-2}$$

$$= 10^5 + 3 \times 1000 = 100k + 3k$$

= 103
9.7

$$\text{New Gain} = \frac{103}{9.7k}$$

$$\begin{aligned} V_o &= 10 \text{ mV} \times 11 \\ &= 110 \text{ mV} \end{aligned}$$



$$\frac{100k + 10^5}{10^5 + 10^3} \times \frac{100 \times 10^3}{10^6} = 101k$$

So when gain = $\frac{100k}{100k} = 1$

V_o due to sensor = $3.23V$

When gain = $\frac{101}{99}$

$$V_0 = \frac{3.73 \times 101}{99} - 3.$$

$$\text{error} = \frac{3.73 \times 101}{99} - 3.73$$

$$\approx 37 \text{ mV}$$

- ①
- Zener drift error = $7.5 \text{ mV} = 0.75^\circ \text{C}$
 - Resistance drift error = $37 \text{ mV} = 3.7^\circ \text{C}$
 - V₀ R F drift error = $4.5 \text{ mV} = 0.45^\circ \text{C}$

Resistors \rightarrow Carbon Comp
 \downarrow
 $\pm 300 \text{ ppm}/^\circ\text{C}$

\rightarrow Metal film resistors
 \rightarrow
 $\pm 10 \text{ ppm}/^\circ\text{C} \rightarrow 100 \frac{\text{ppm}}{^\circ\text{C}}$

\rightarrow wire wound resistors
 \rightarrow
 $+10 \text{ ppm}/^\circ\text{C}$
 $+ 3000 \text{ ppm}/^\circ\text{C}$

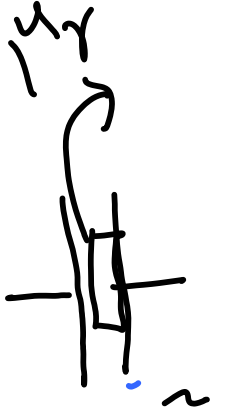
Capacitors

①

Ceramic

Capacitors

no inductance
less



②

Electrolytic

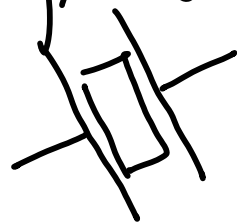
Capacitors



③

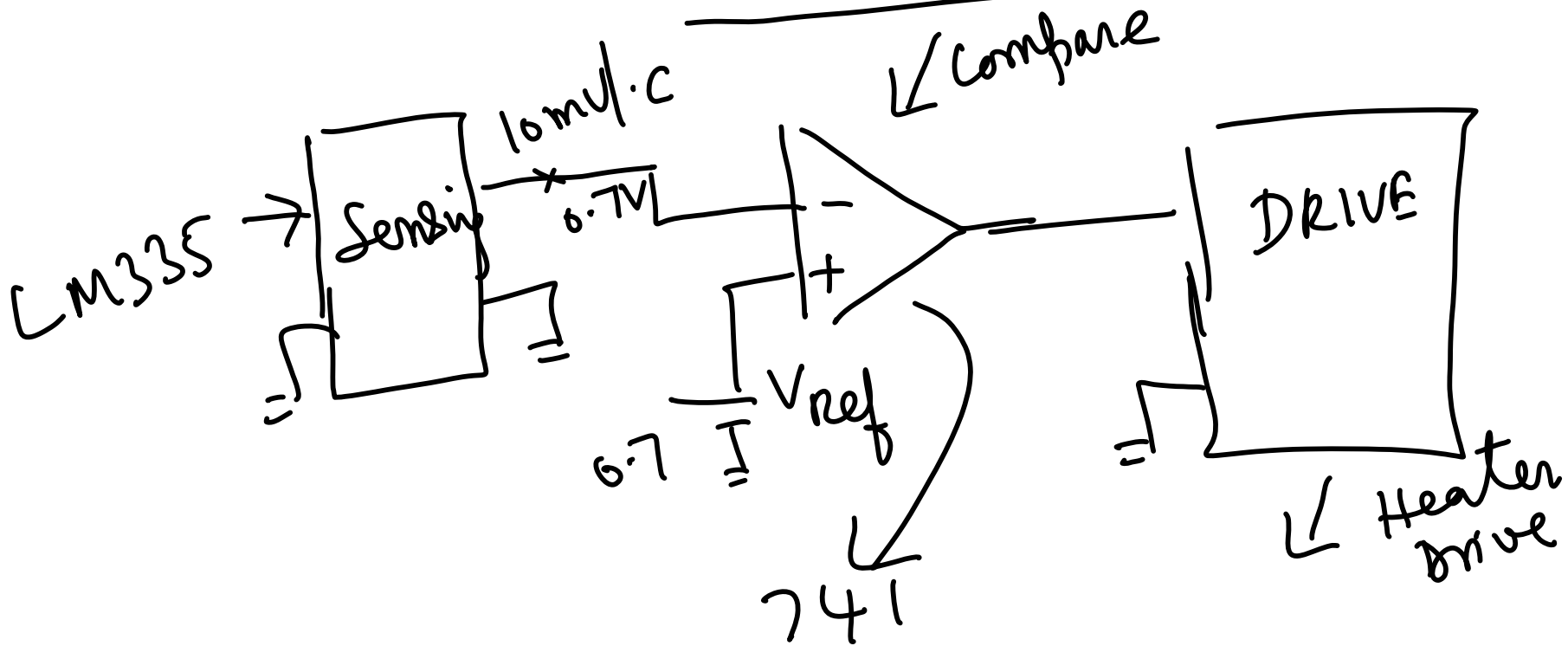
Plastic film

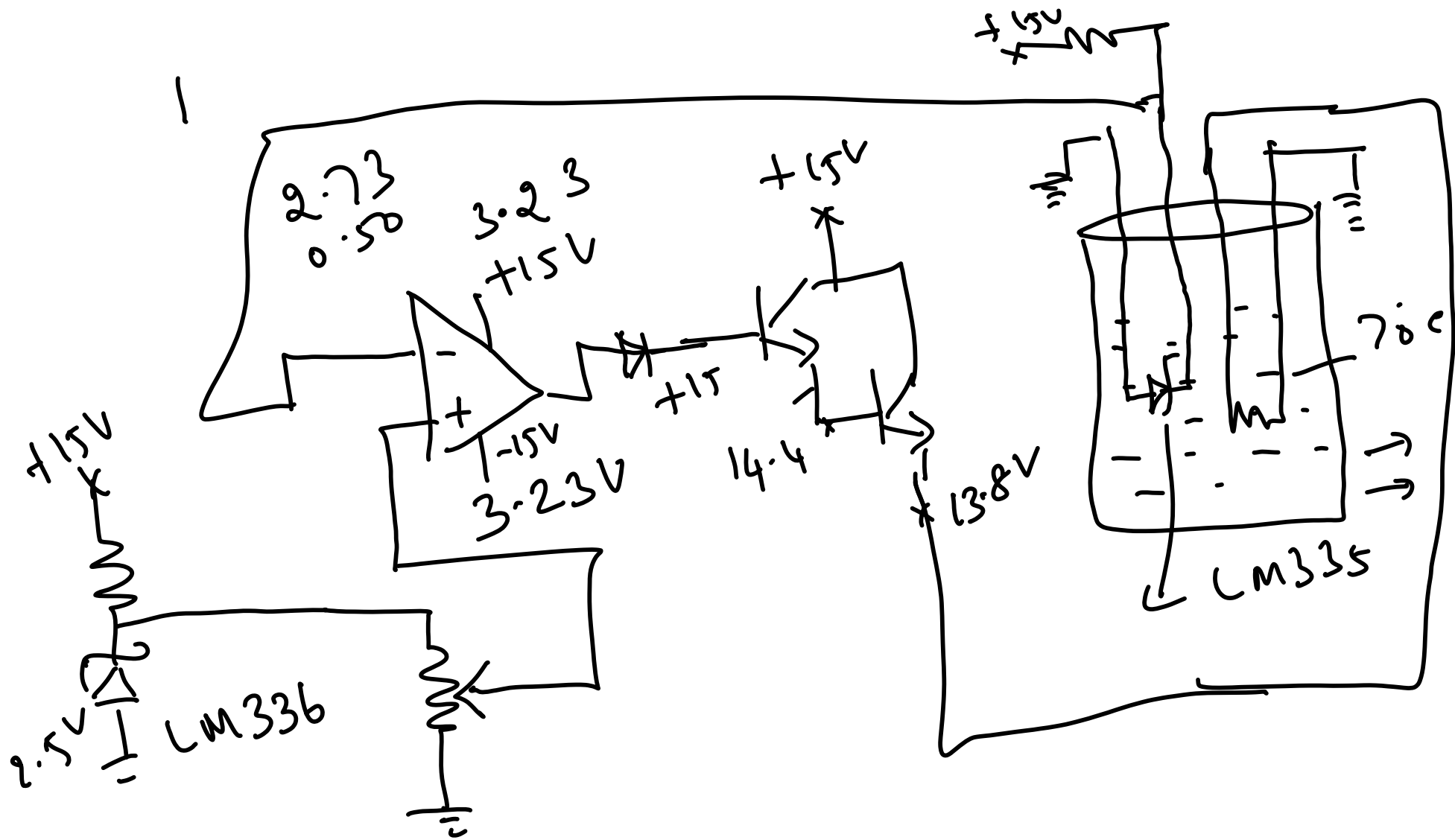
Capacitors

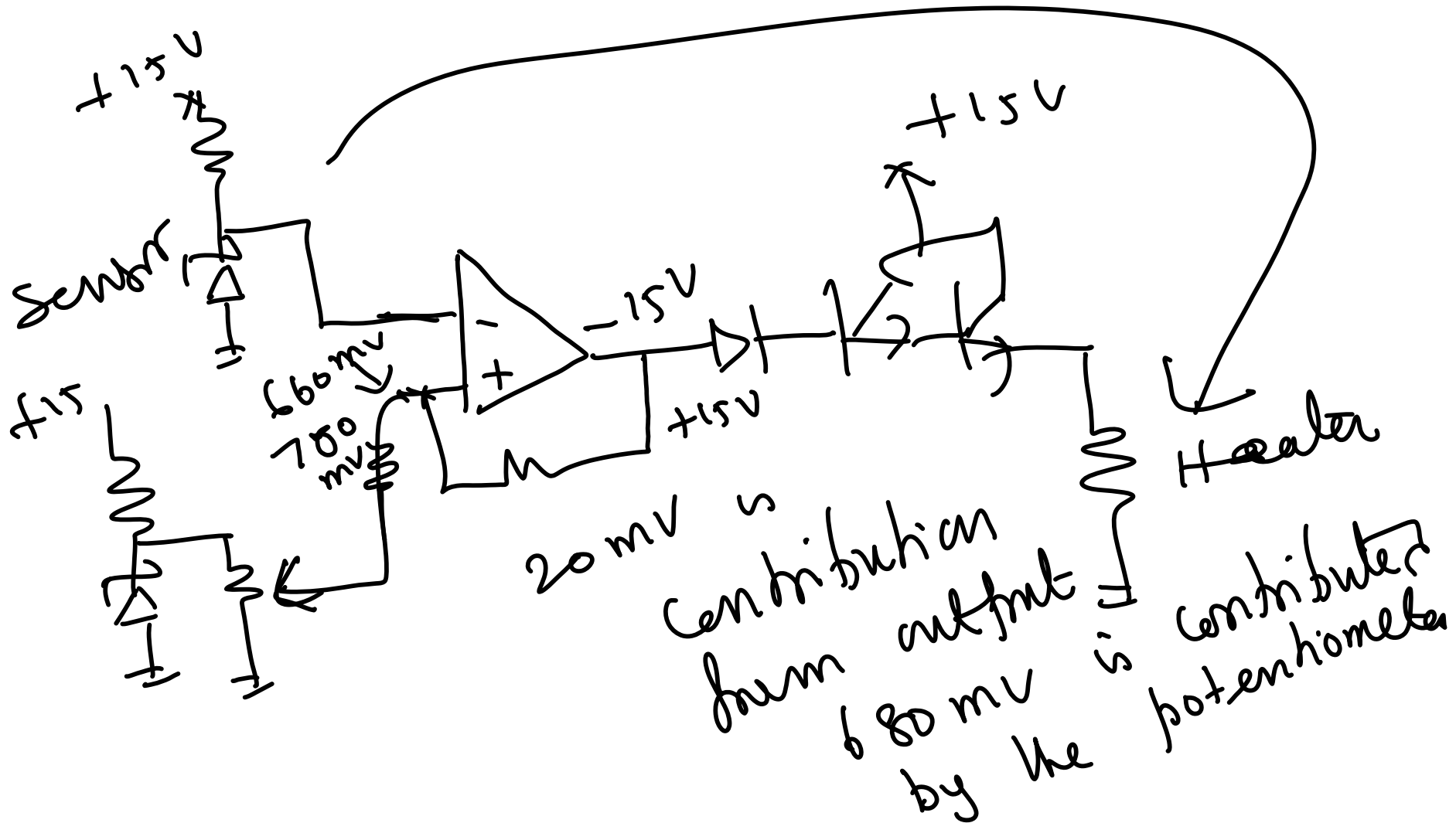


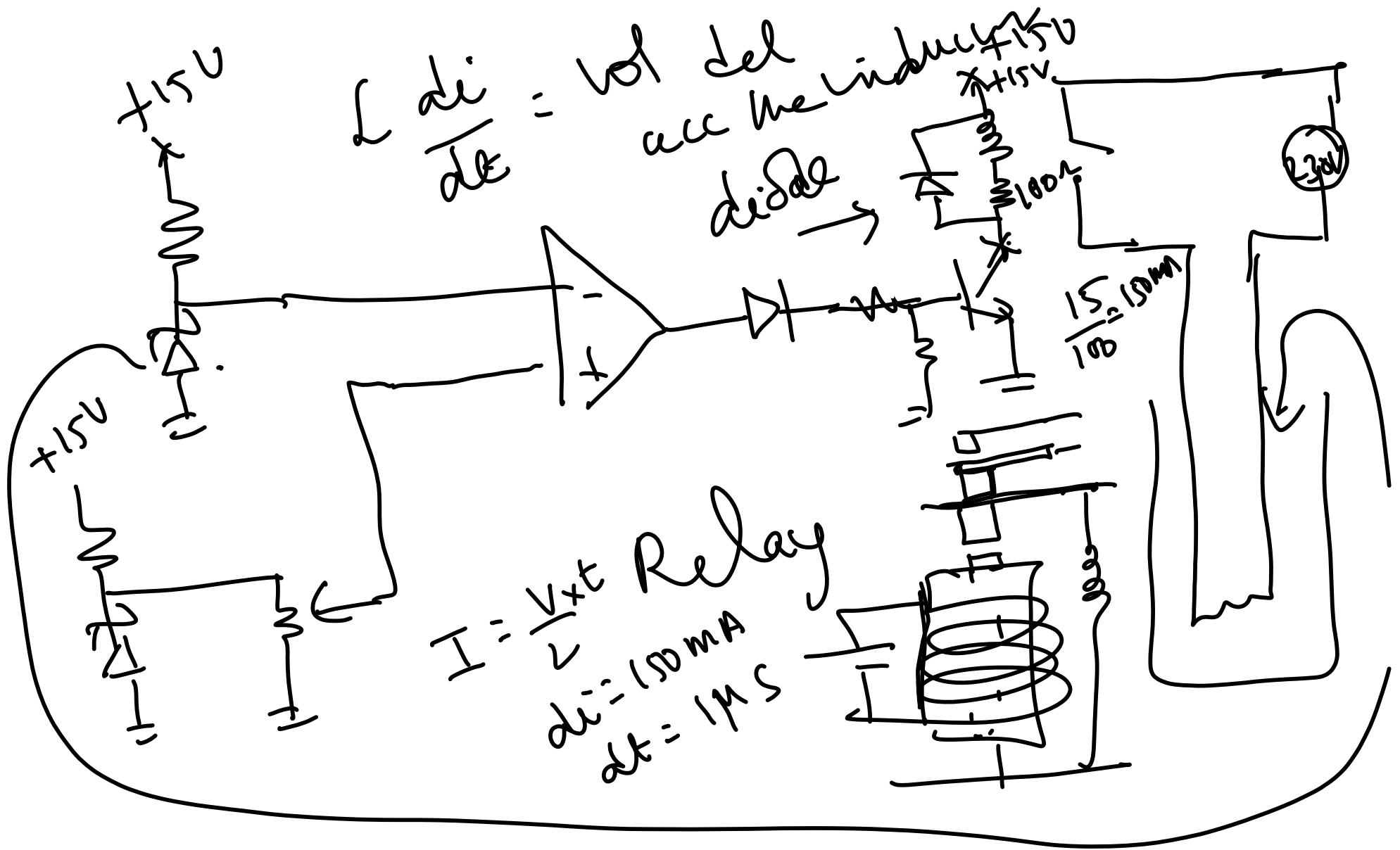
Temperature Controller

ON/OFF CONTROLLER



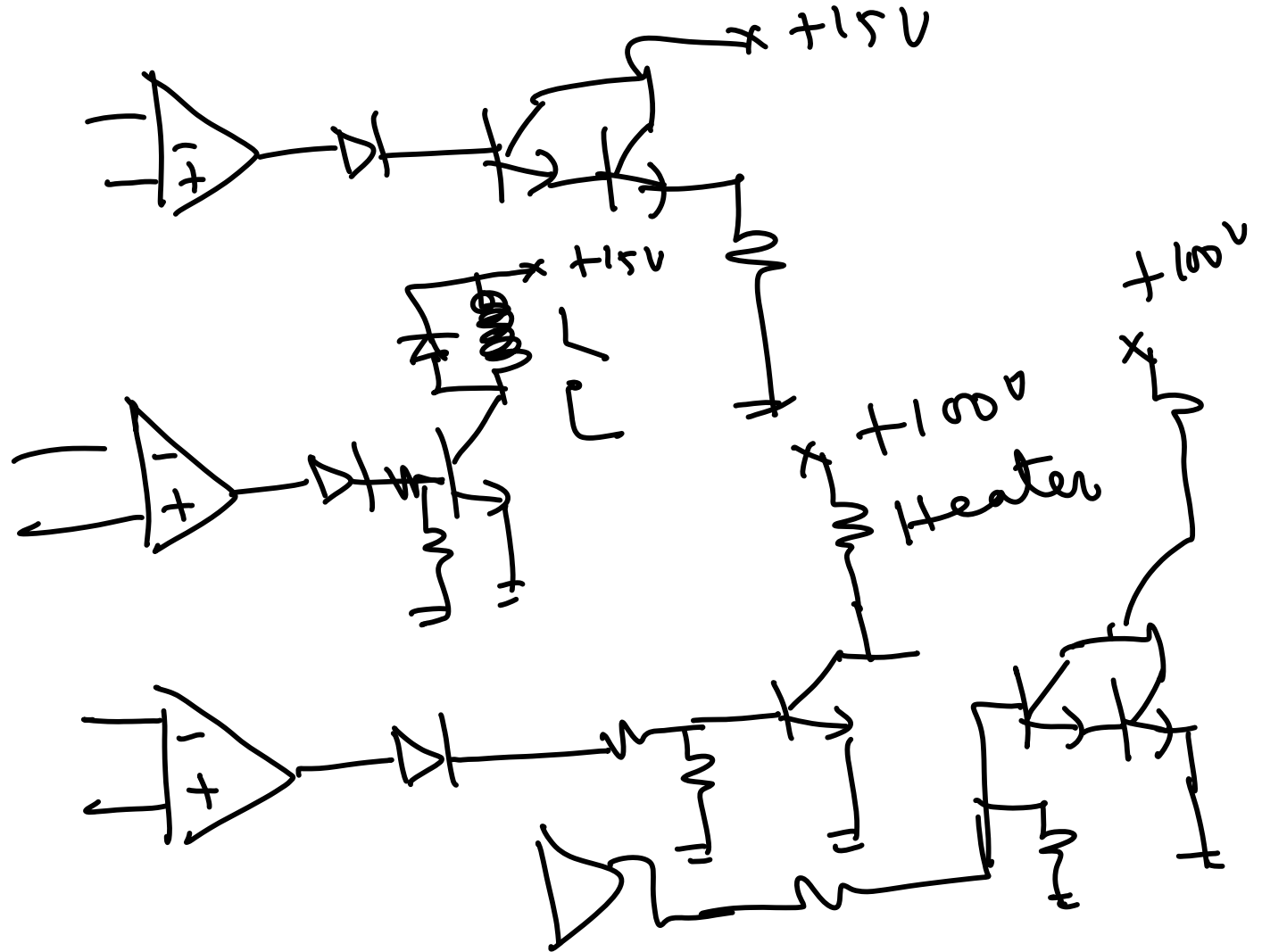


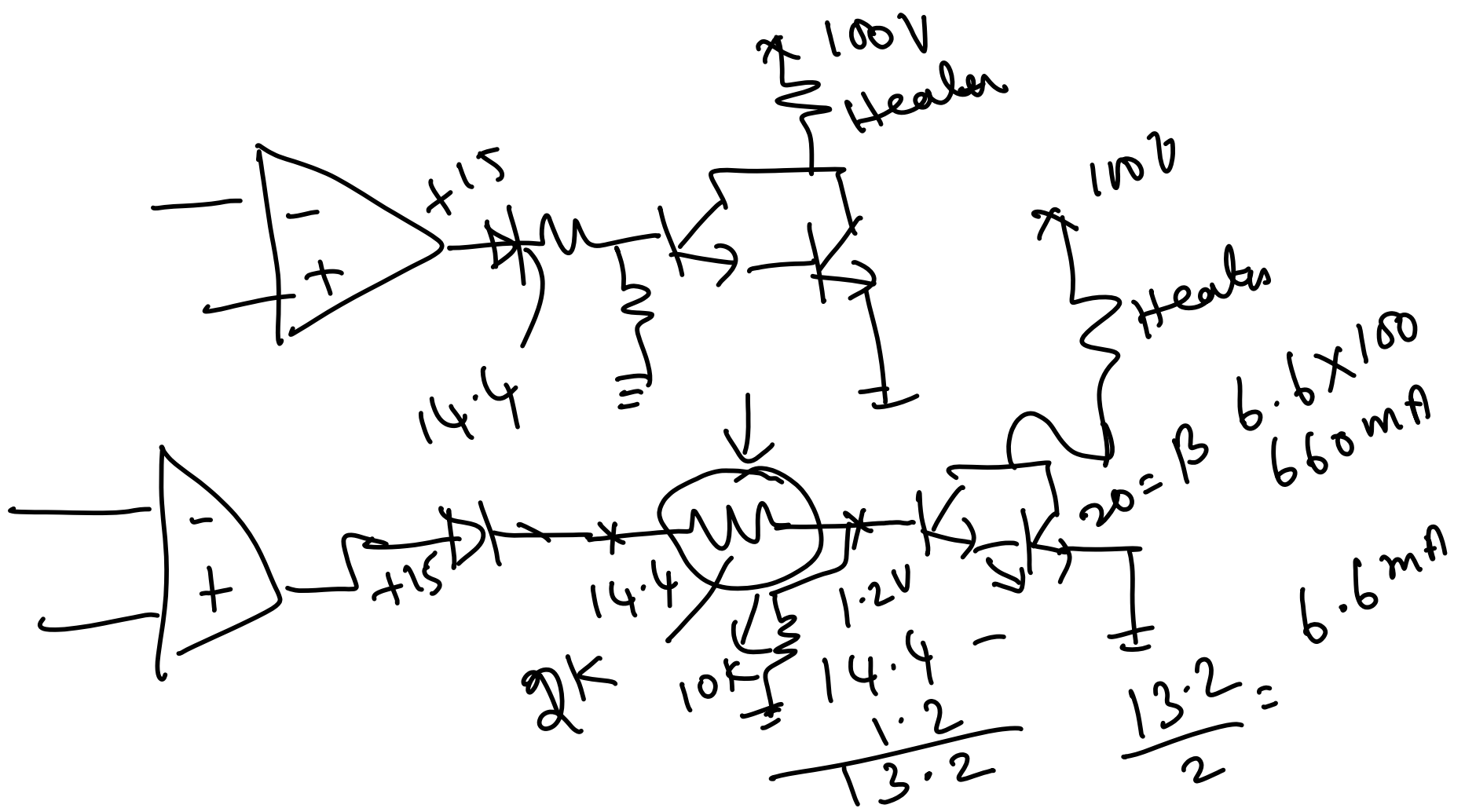




sol

$$\text{acc} = L \frac{di}{dt} = 1 \times 150 \times 10^{-3} \times 10^6 = 150 \times 1000$$





Proportional Temperature Controller

- 1) Thermo Couple as temp sensor
- ② Heater vol as 100 V DC/5A

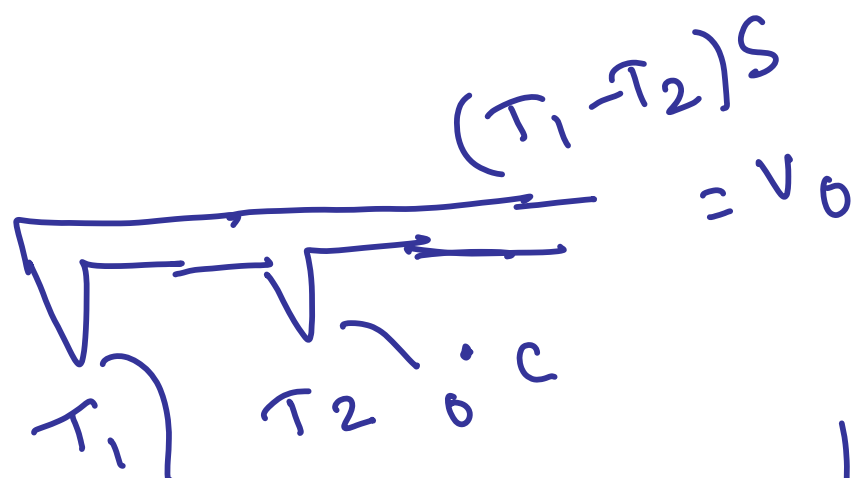
ON/OFF { Temp is low \rightarrow Heater is ON
Temp is high \rightarrow Heater is OFF

Proportional Controller

Heater vol \propto error

$$\text{heater vol} \propto (T_s - T_A) \\ (50 - 30)$$

Heater $\Delta T =$ Difference between
 Set temp and
 actual temp \downarrow sensor

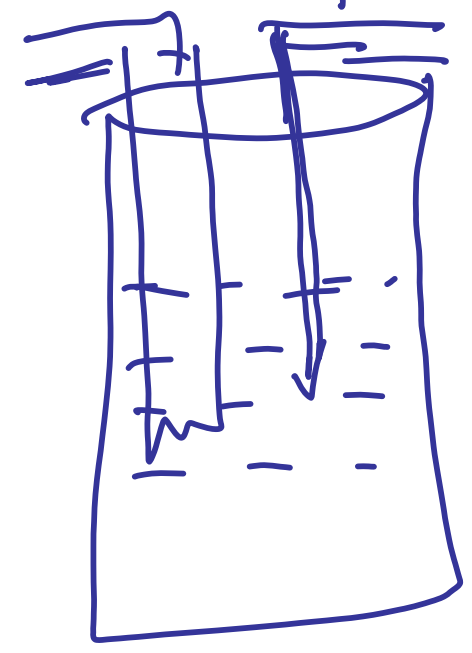


100°C

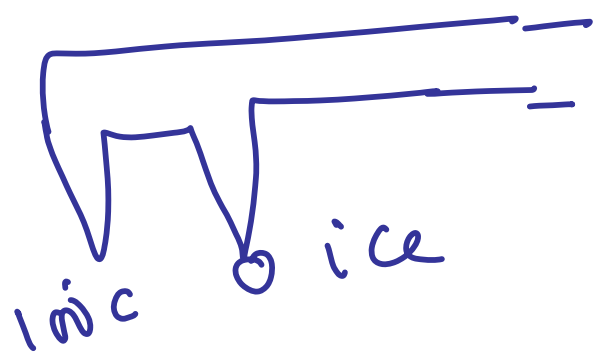
$$S = 40 \mu\text{V}/^{\circ}\text{C}$$

$$(T_1 - T_2) = 100^{\circ}\text{C}$$

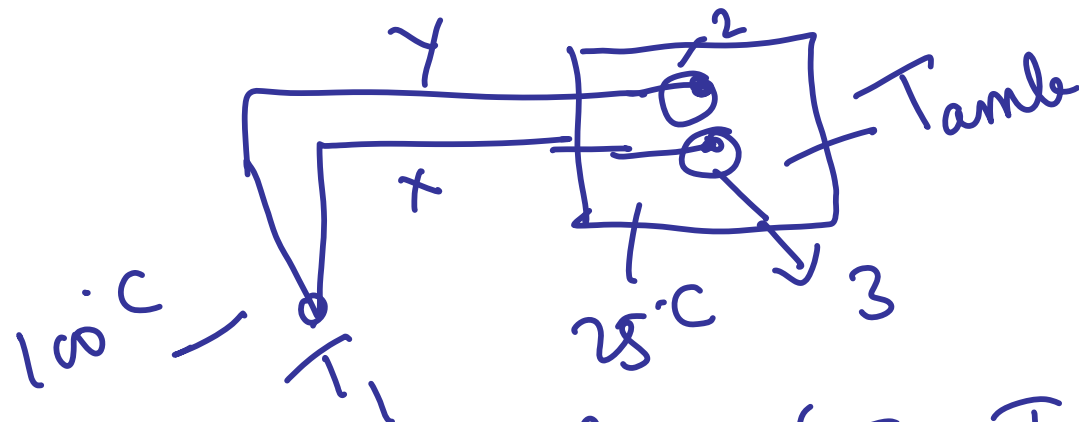
$$= 40 \mu\text{V} \times 100 = 4 \text{mV}$$



$$= 4 \text{mV}$$



Single Junction thermocouple



∴ at 2, and 3 = $(T_1 - T_{amb})S$

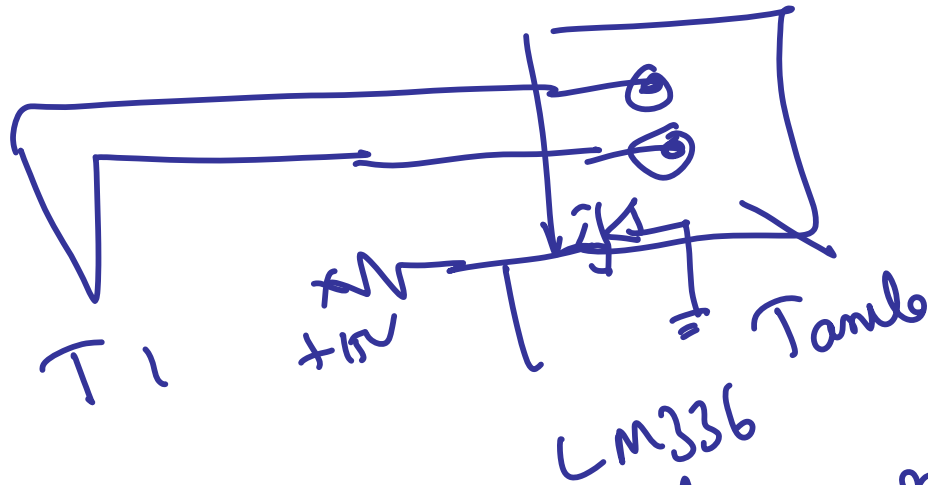
$$S = 40 \mu\text{V}/^\circ\text{C}$$

$$(100 - 25) \times 40 \mu\text{V} = 75 \times 40 \mu\text{V}$$

$$= 3.000 \text{ mV}$$

$$(100 - 50) \times 40 \mu\text{V} = 2.000 \text{ mV}$$

ambient temp compensation



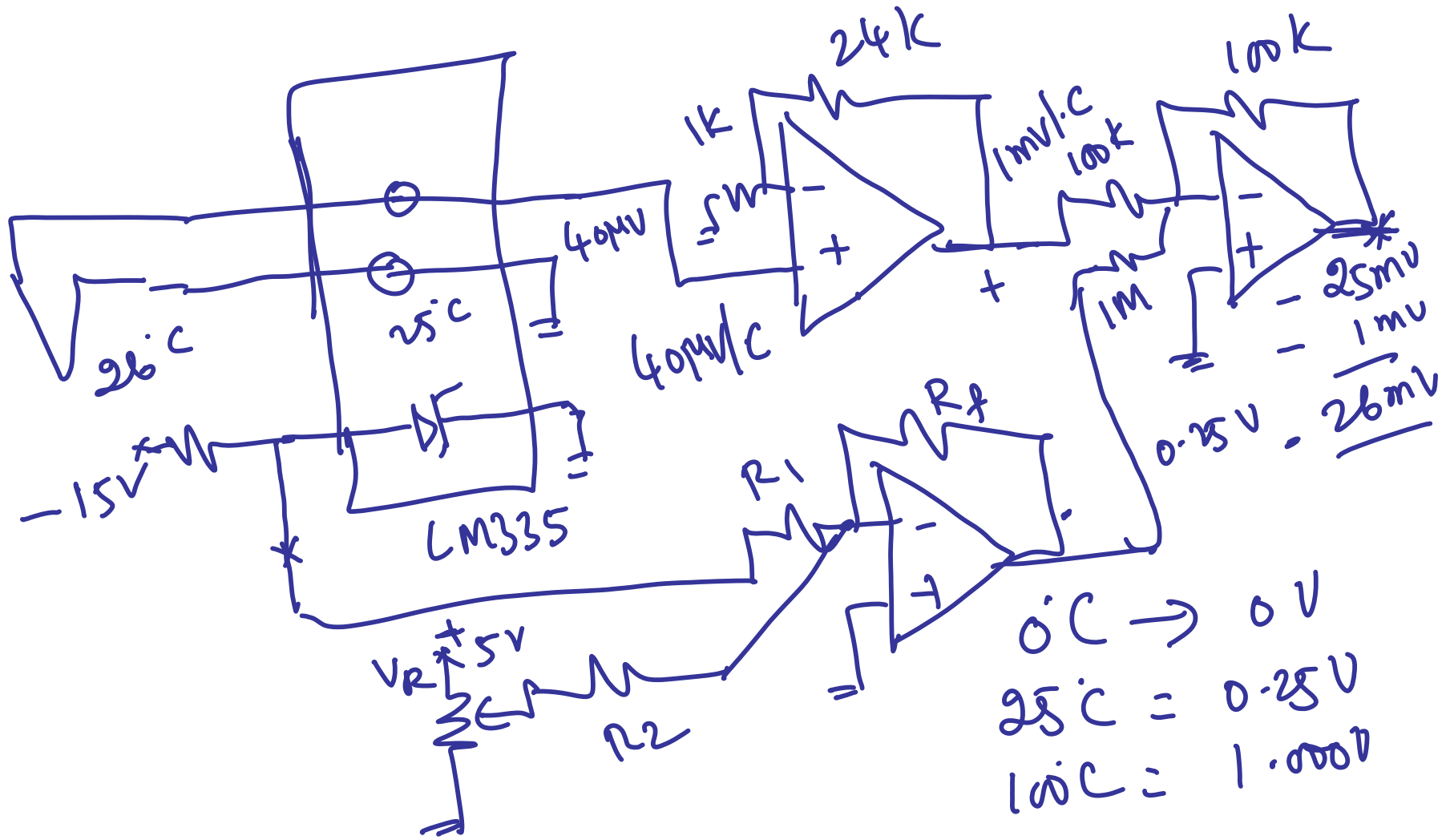
ambient temp must be
measured. use another
sensor

Thermo couple w/

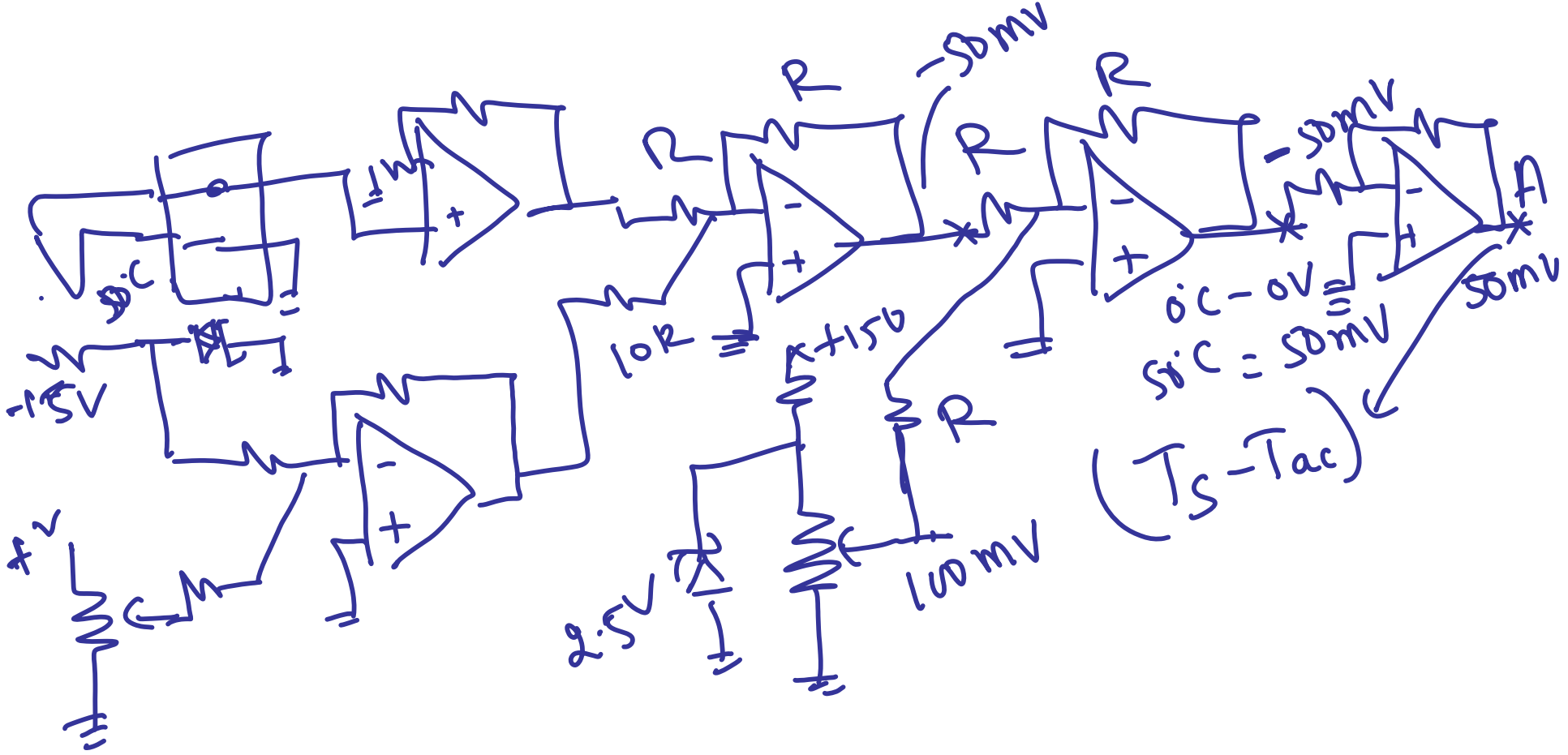
$$V_o \checkmark = (T \checkmark - T_{amb} \checkmark) S \checkmark$$

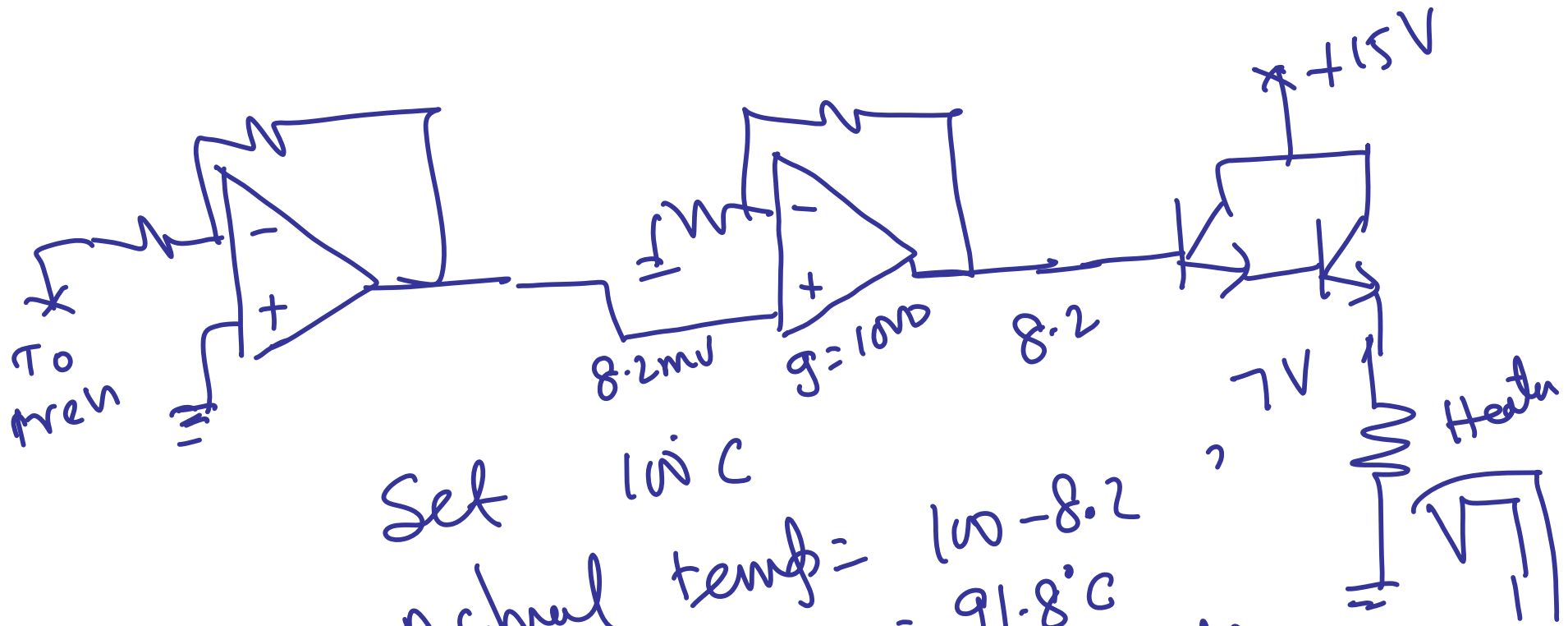
$$\frac{V_o}{S} = T - T_{amb}$$

$$\frac{V_o}{S} + \text{ambient} \checkmark = T$$



$0^{\circ}C \rightarrow 0V$
 $25^{\circ}C = 0.25V$
 $100^{\circ}C = 1.000V$





Set 100°C

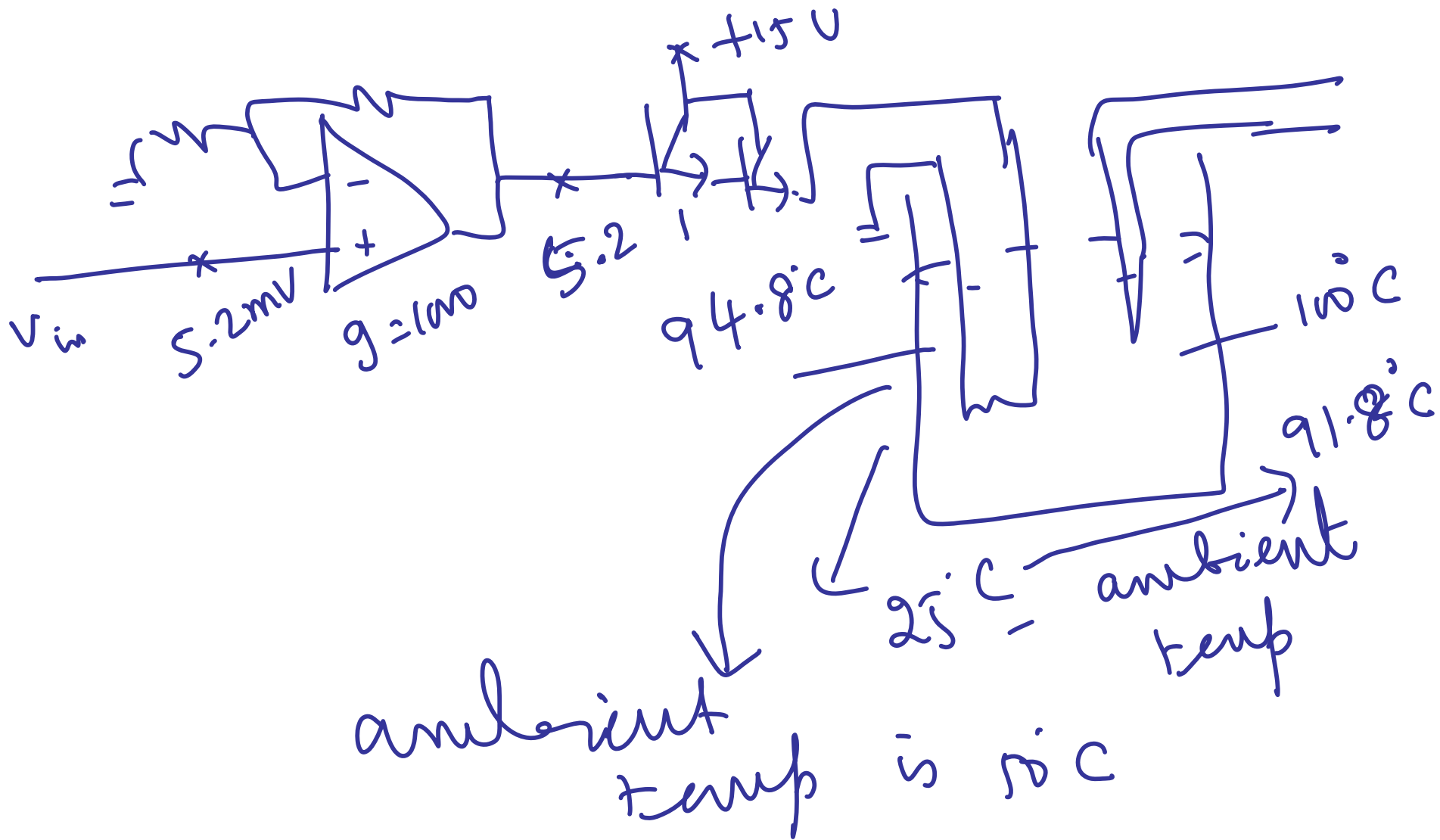
$$\text{Actual temp} = 100 - 8.2 = 91.8^{\circ}\text{C}$$

In proportional controller
 Set temp is not equal
 to actual temp. Stabilized

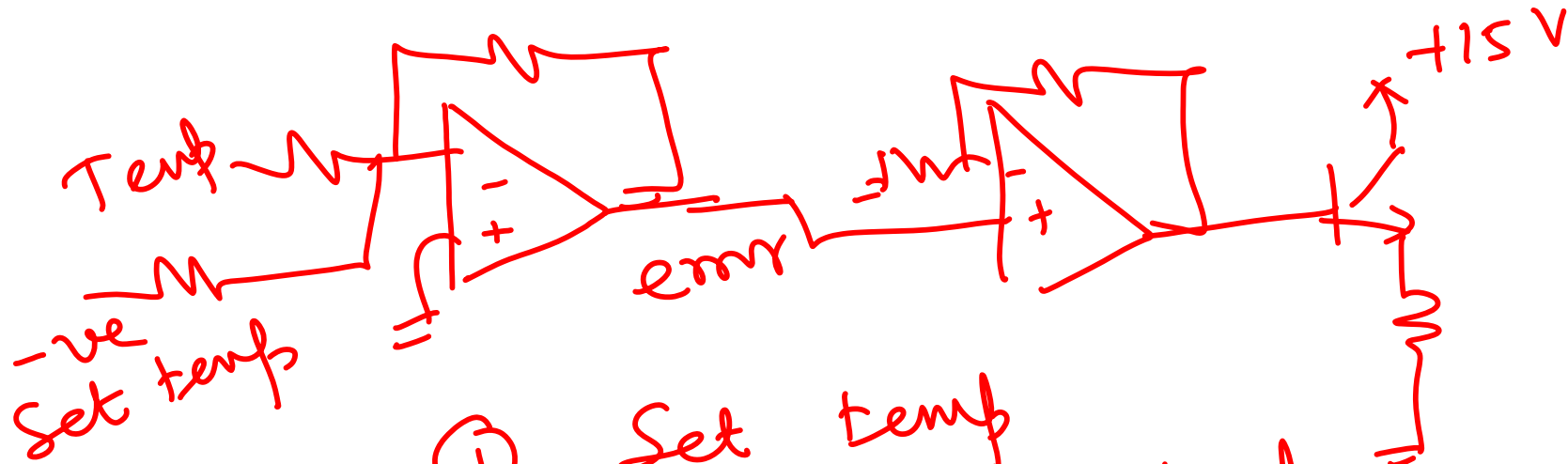
Set temp is different
from actual stabilized
temp.

This difference only driving
the heater.

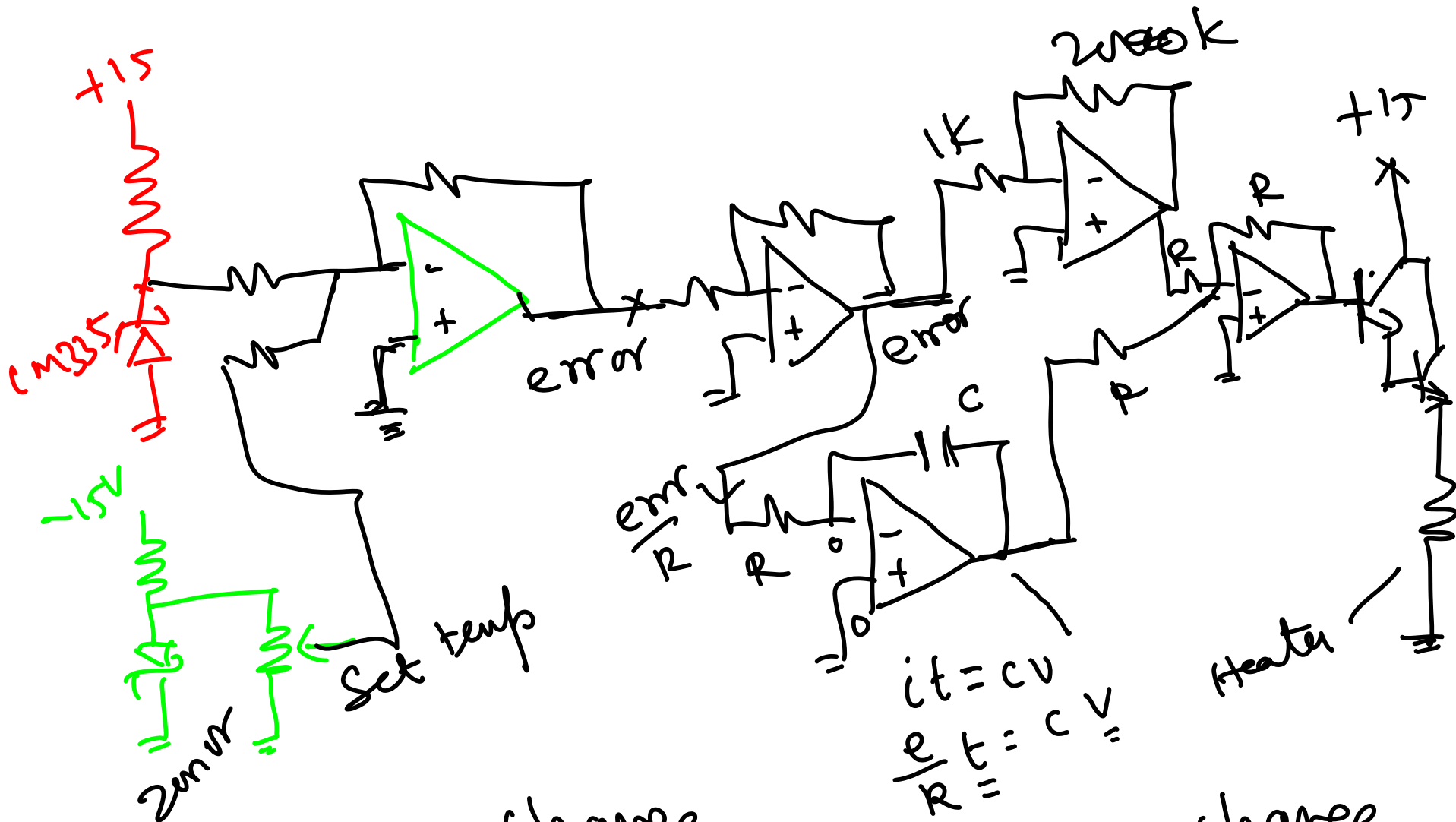
This difference produces
secondary effect



PI Temperature Controller



① $\text{Set temp} = \text{actual temp}$
 $\text{error} \times \text{gain} = \text{Heater vol}$

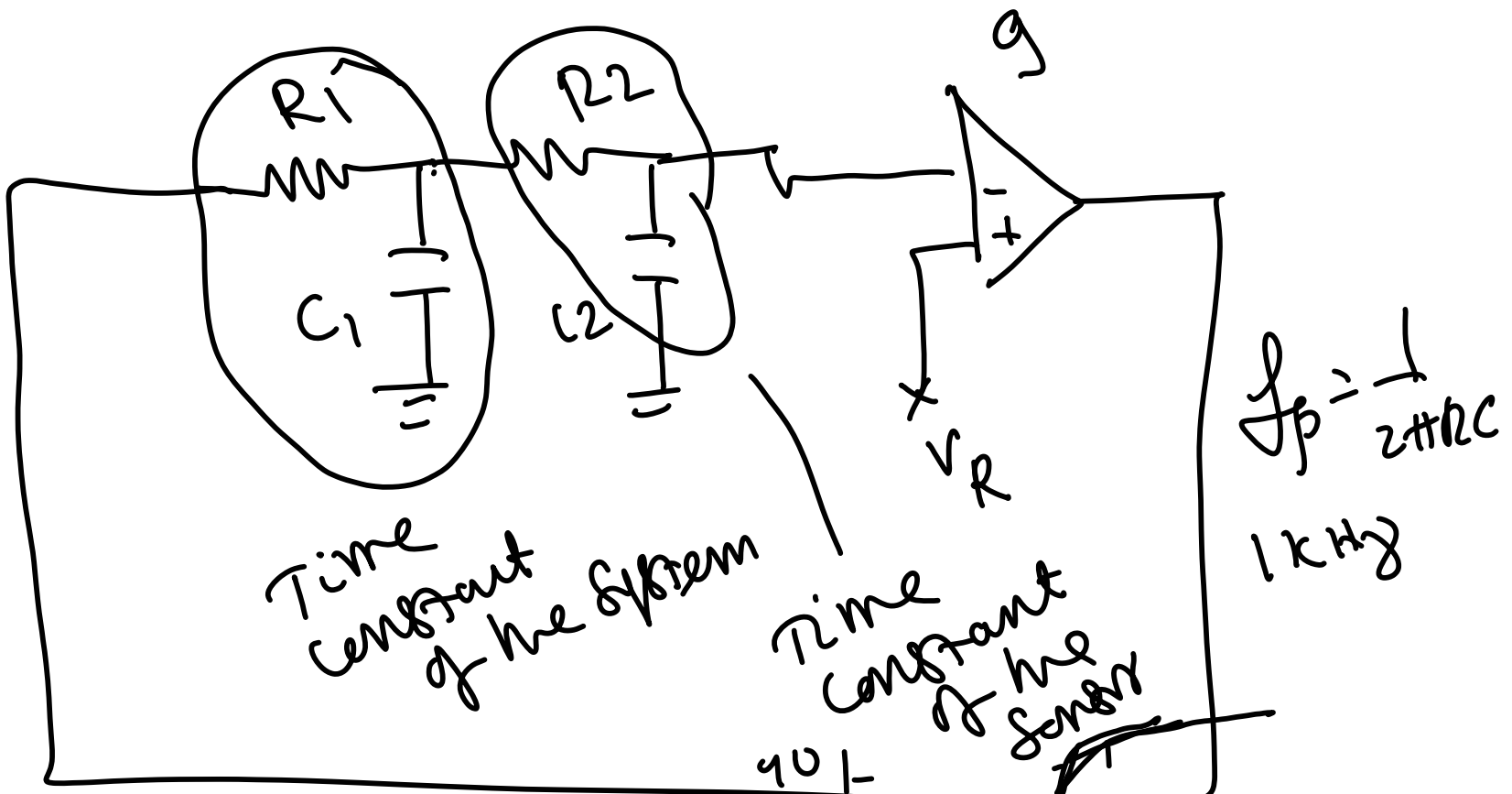


$$i_t = c v$$

$$\frac{e}{R} t = c v$$

10mV change should produce 20V change at the heater

electronic gain = $\frac{20V}{10mV} = 2000$



Time constant of the system

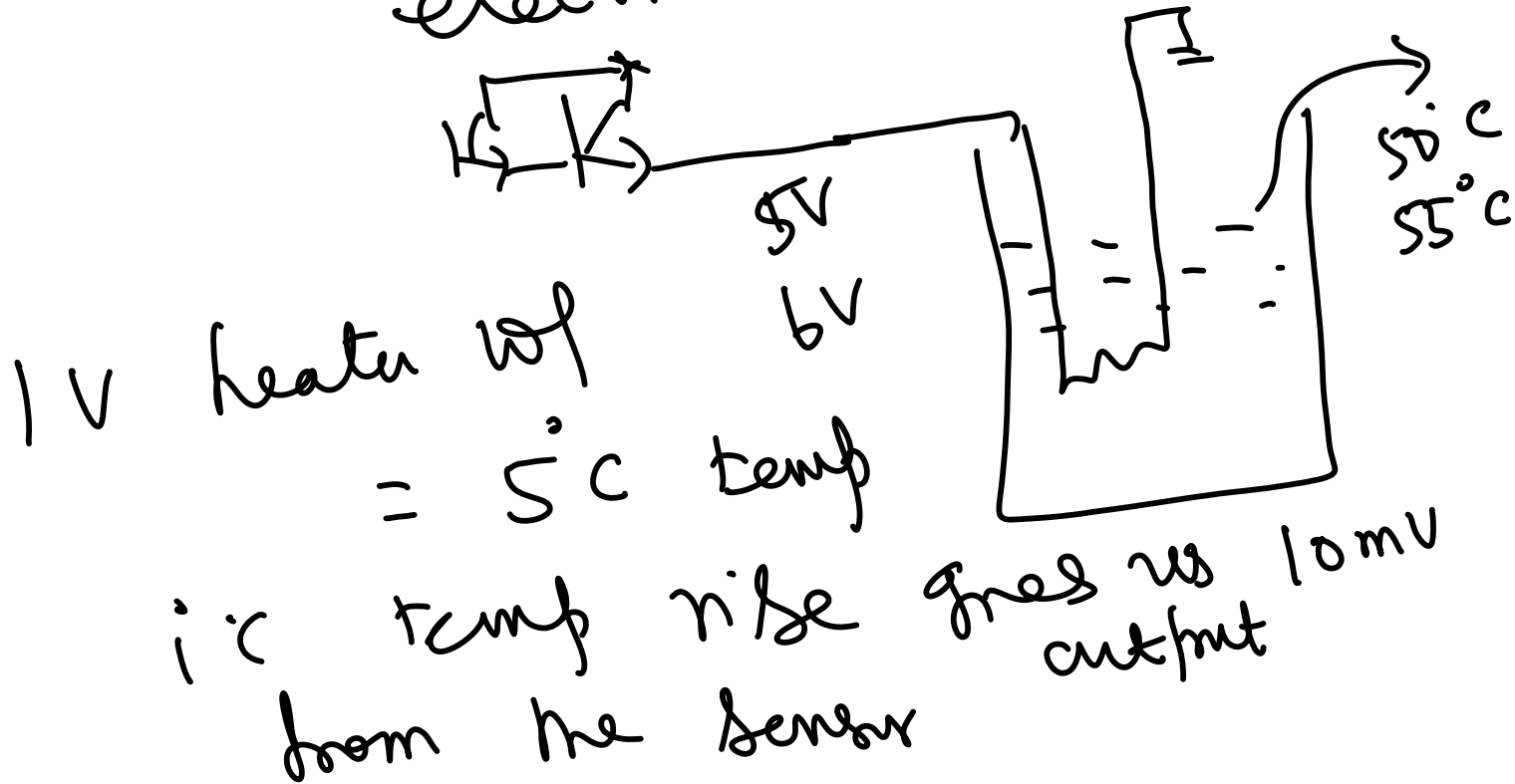
Time constant of the sensor

$$A = \left(\frac{g}{f_p} \right)$$

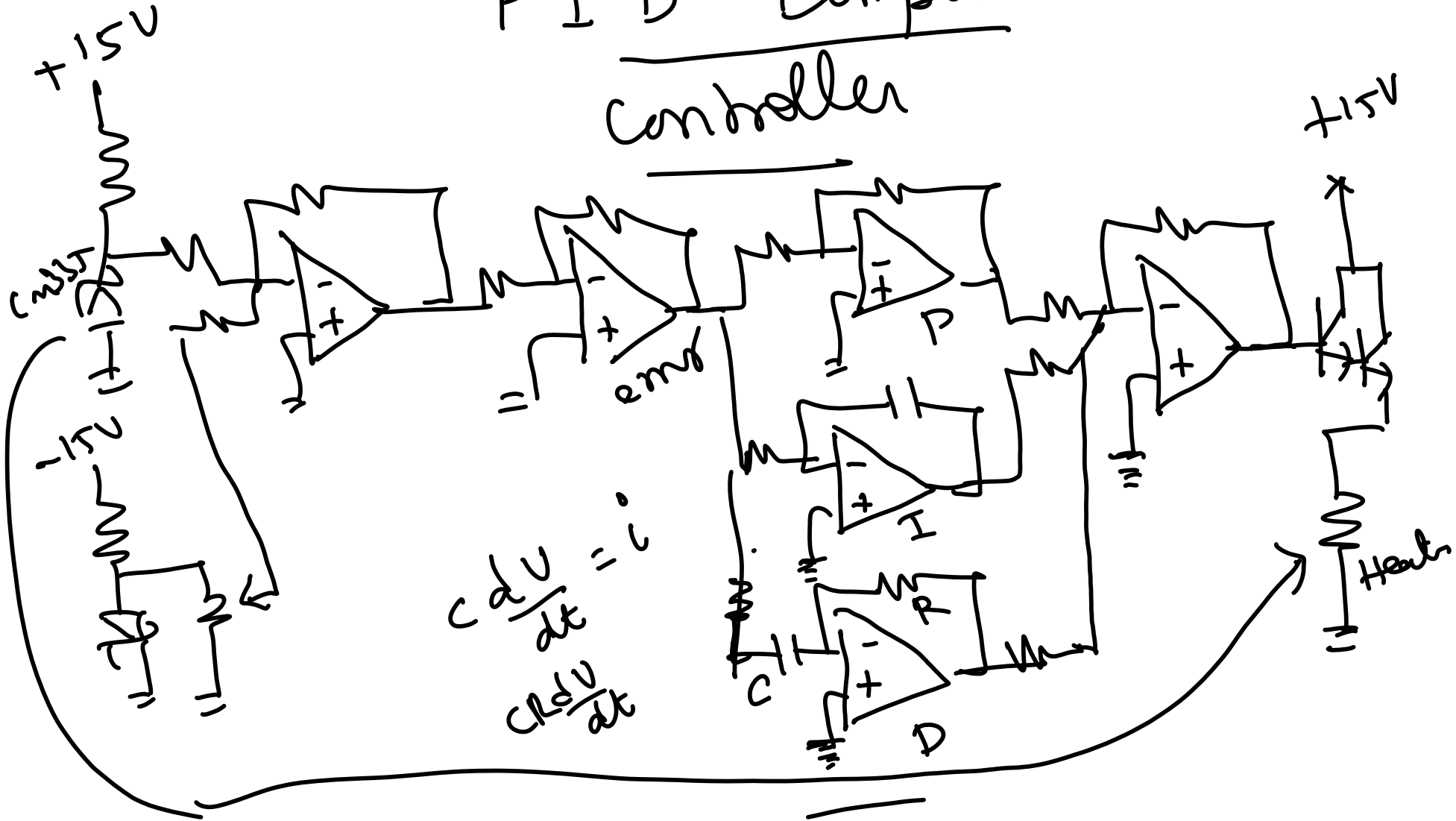


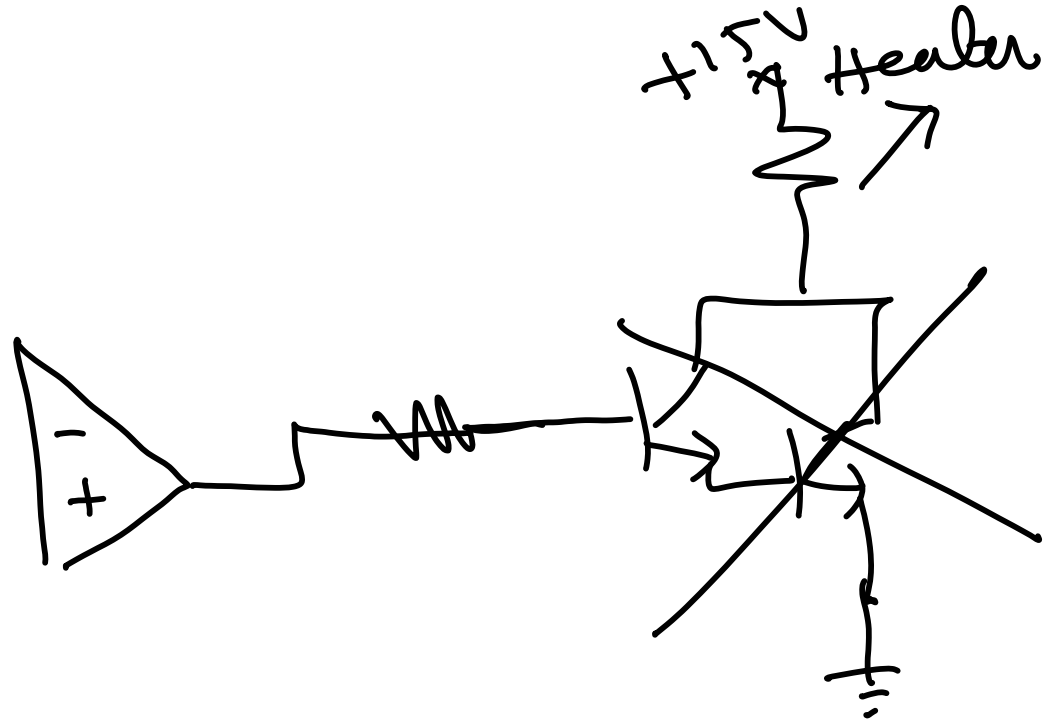
$$\frac{100}{1} = \frac{\text{System time constant} \times \text{gain}}{\text{Sensor time const}}$$

How to convert
temperature gain into
electronic gain?

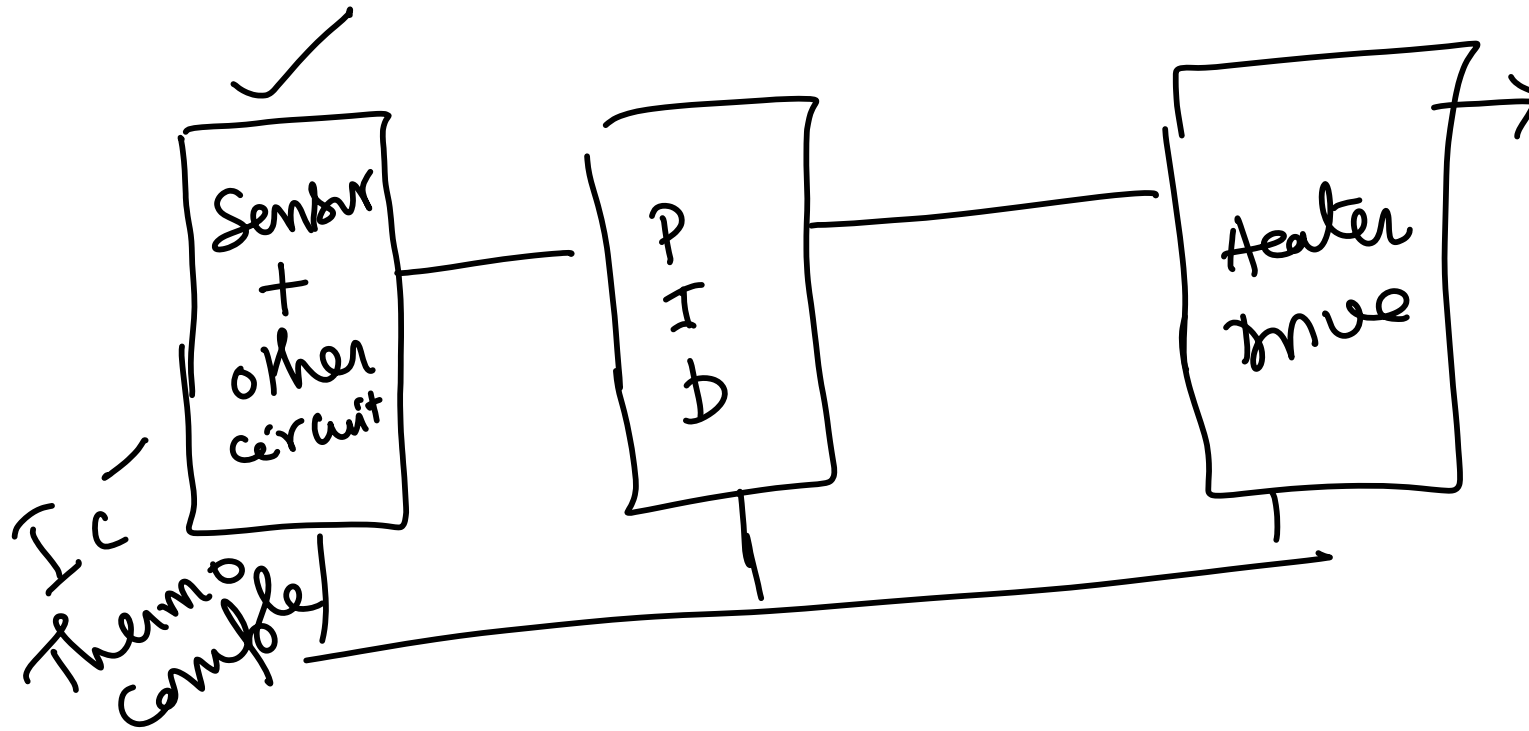


PID Temperature Controller

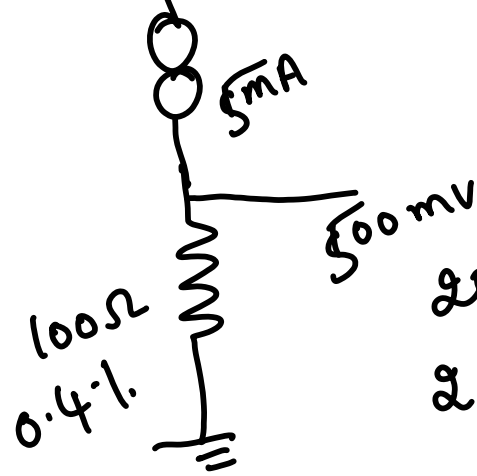




PID Controller

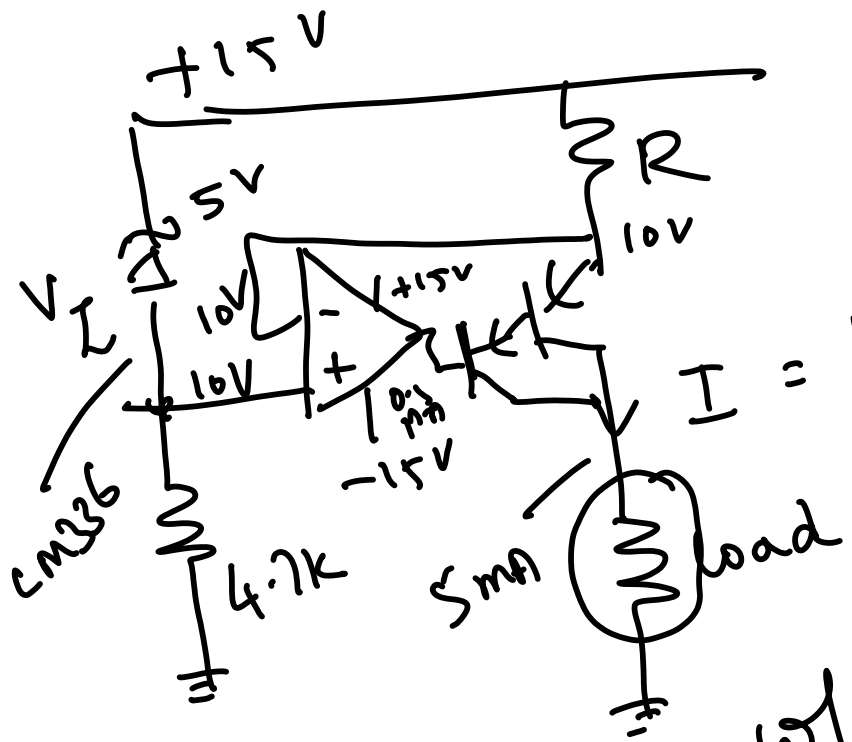


+15V Platinum resistance thermometer



25°C → 500 mV
 26°C → 100.4 Ω →

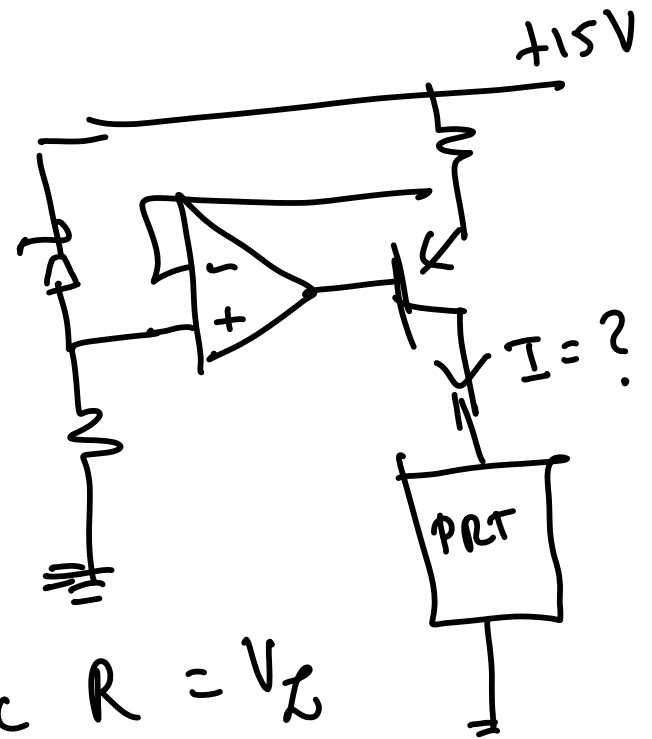
Sensitivity = $\frac{100.4 \times 5}{500} \text{ mV}$
~~0.4 mV/C~~
 = 2 mV/C

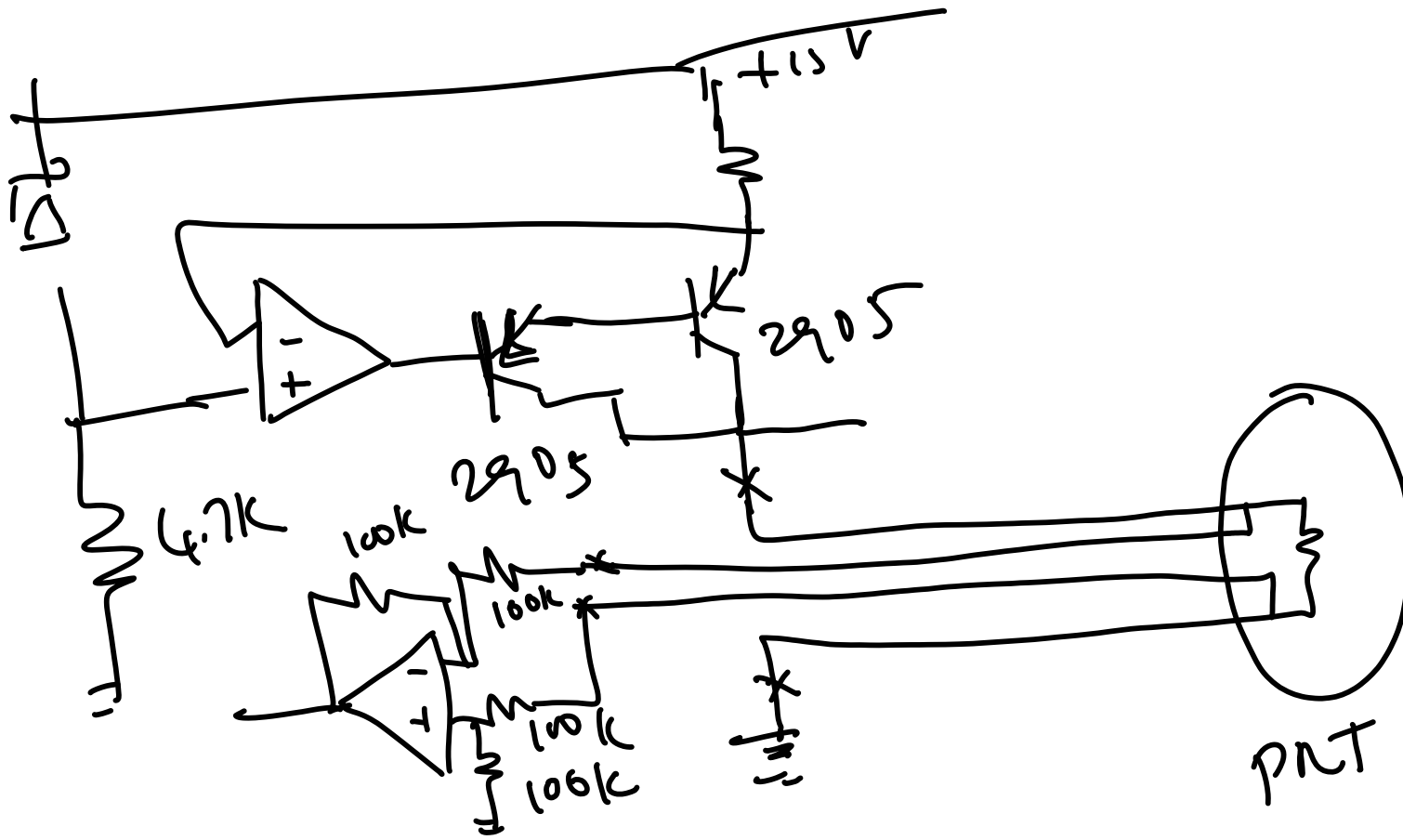


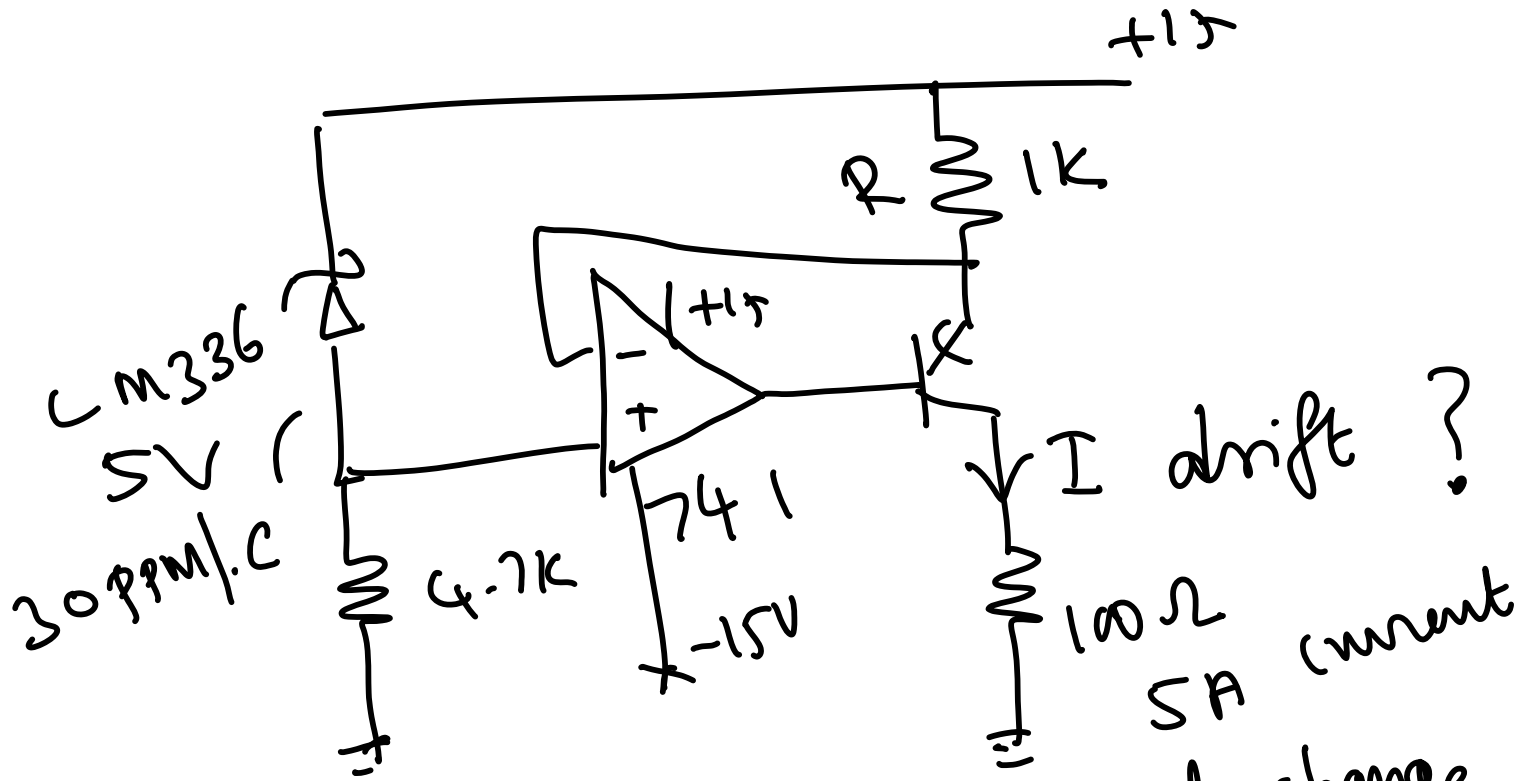
$$I = \frac{V_Z}{R}$$

W/ acc $R = \frac{V_Z}{I}$

$$I_R = \frac{V_Z}{R} = \frac{5V}{1K} = 5mA$$







For 100°C ambient temp change

$$V_2 \text{ drift} = 5V \times 30 \times 100$$

$$= \frac{15}{10^3} = \frac{15}{10^6} = 15 \text{ mV}$$

current drift due to V_2 drift

$$= \frac{15 \text{ mV}}{1 \text{ k}} = 15 \mu\text{A}$$

Current drift due to V_2 drift = $15 \mu\text{A}$

w/ change acc PRT due to $15 \mu\text{A}$

$$\begin{aligned} \text{Current drift} &= 15 \times 10^{-6} \times 100 \\ &= 1500 \mu\text{V} = 1.5 \text{ mV} \end{aligned}$$

Sensitivity of PRT = $2 \text{ mV}/^\circ\text{C}$

So error in temp due to

$$1.5 \text{ mV drift} = \frac{1.5}{2} = 0.75^\circ\text{C}$$

Temp error due to R change

$$R = 1000 \Omega$$

$$\text{Temp Co-eff} = \pm 300 \text{ ppm}/^\circ\text{C}$$

$$\Delta T = 100^\circ\text{C}$$

$$\Delta R = 1000 \times \frac{300 \times 100}{10^6}$$

$$\Delta R = 3 \times \frac{10^7}{10^6} = 30 \Omega$$

$$\Delta I = \frac{V_Z}{R} = \frac{5}{1000 + 30}$$

$$= \frac{5}{1030} = \frac{5000}{1030} = 4.86 \text{ mA}$$

$$\Delta I = 0.14 \text{ mA}$$

$$\begin{array}{r} 5000 \\ \underline{4120} \\ 8800 \\ \underline{8240} \\ 6600 \end{array}$$

Voltage error for 0.14 mA

$$\begin{aligned} \text{Current change in PRT} &= 0.14 \times 100 \\ &= 14 \text{ mV} \end{aligned}$$

$$\text{Sensitivity} = 2 \text{ mV/}^\circ\text{C}$$

$$\text{Total temp error} = \frac{14}{2} = 7^\circ\text{C}$$

For ± 25 ppm drift resistance

Error due to offset voltage
drift of the op amp

$$V_{\text{OFF}} \text{ drift of } 741 = \pm 15 \mu\text{V/}^\circ\text{C}$$

$$\Delta T = 100^\circ\text{C}$$

$$\begin{aligned} \text{Total } V_{\text{OFF}} \text{ drift} &= 15 \times 100 \\ &= 1.5 \text{ mV} \end{aligned}$$

Current error due to

V_{off} drift of 241

$$= \frac{1.5 \times 10^{-3}}{1k} = 1.5 \mu A$$

Change in wf

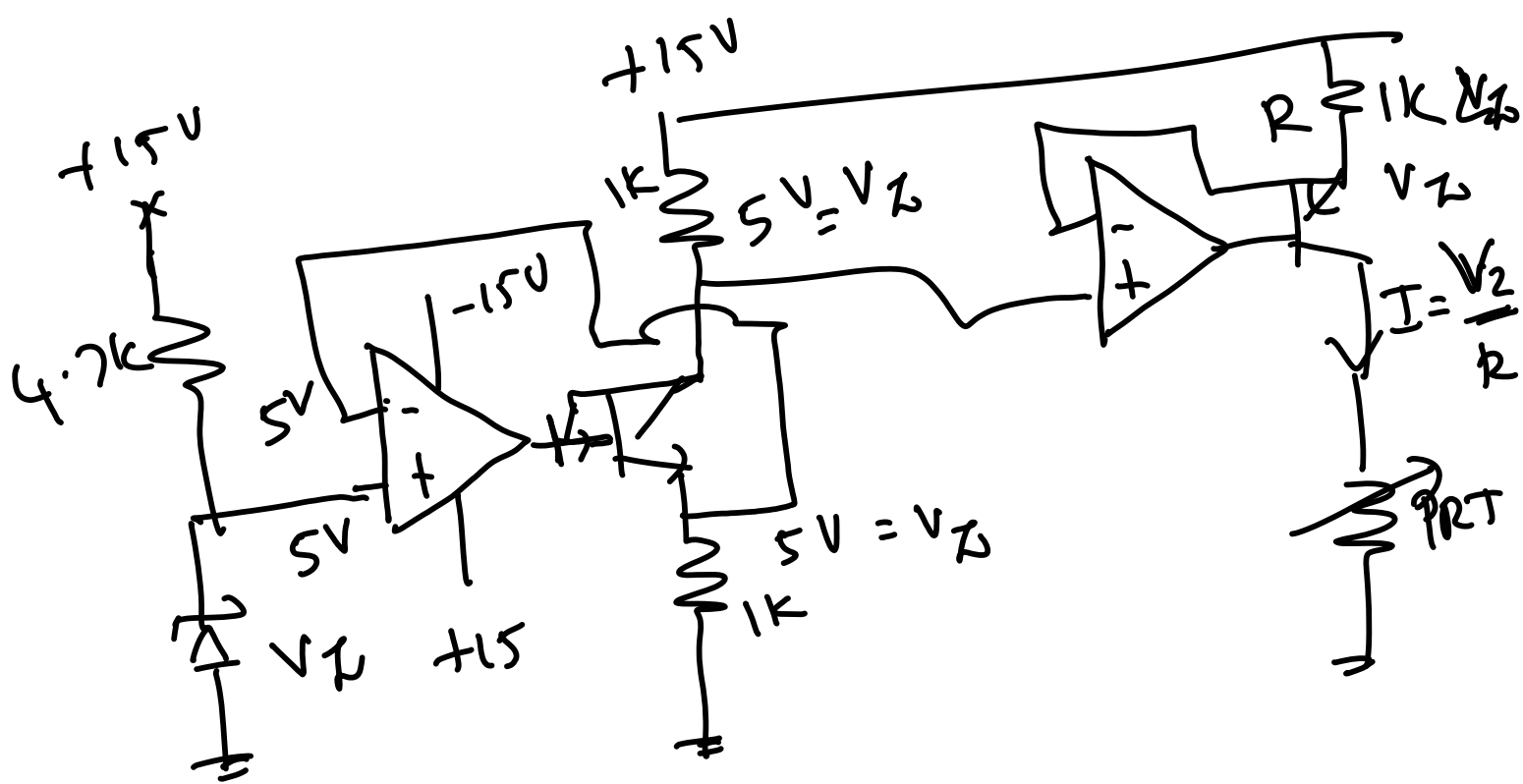
$$\text{acc } 10 \Omega \text{ PRT} = 1.5 \mu A \times 100$$
$$= 150 \mu V$$

$$\text{Sensitivity} = 2 \text{ mV} / \text{C}$$

$$150 \mu V = \frac{0.15}{2} = \frac{15}{200} = \frac{7.5}{100} = 0.075$$

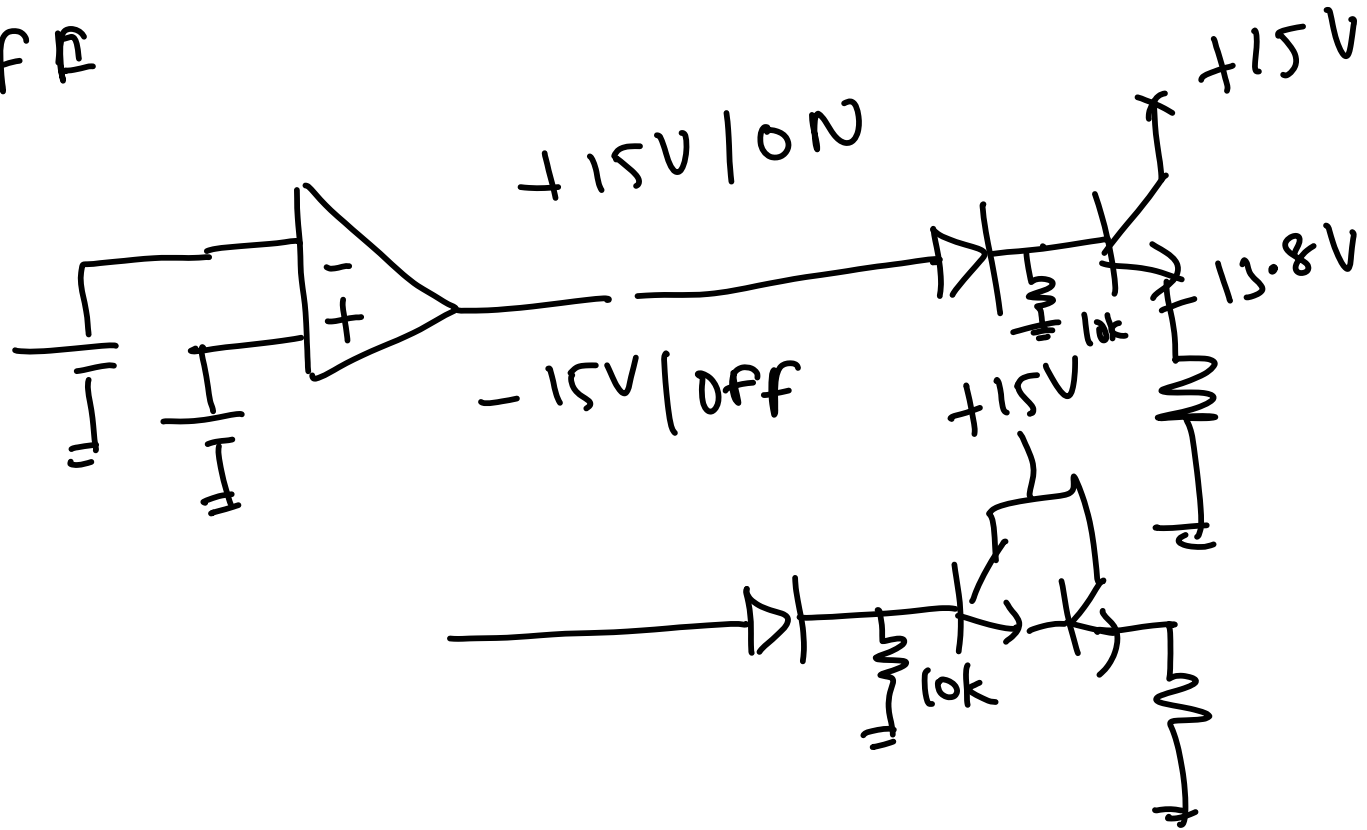
Temp error due to

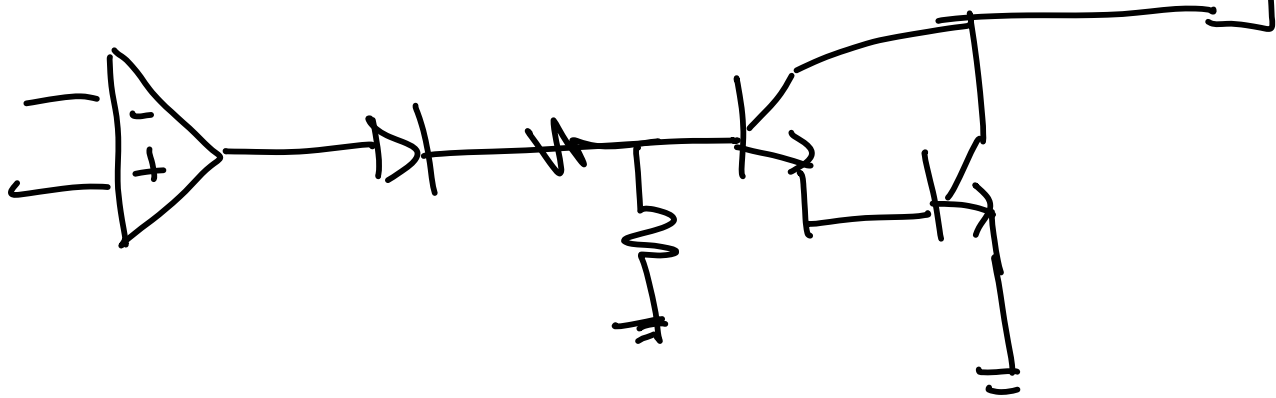
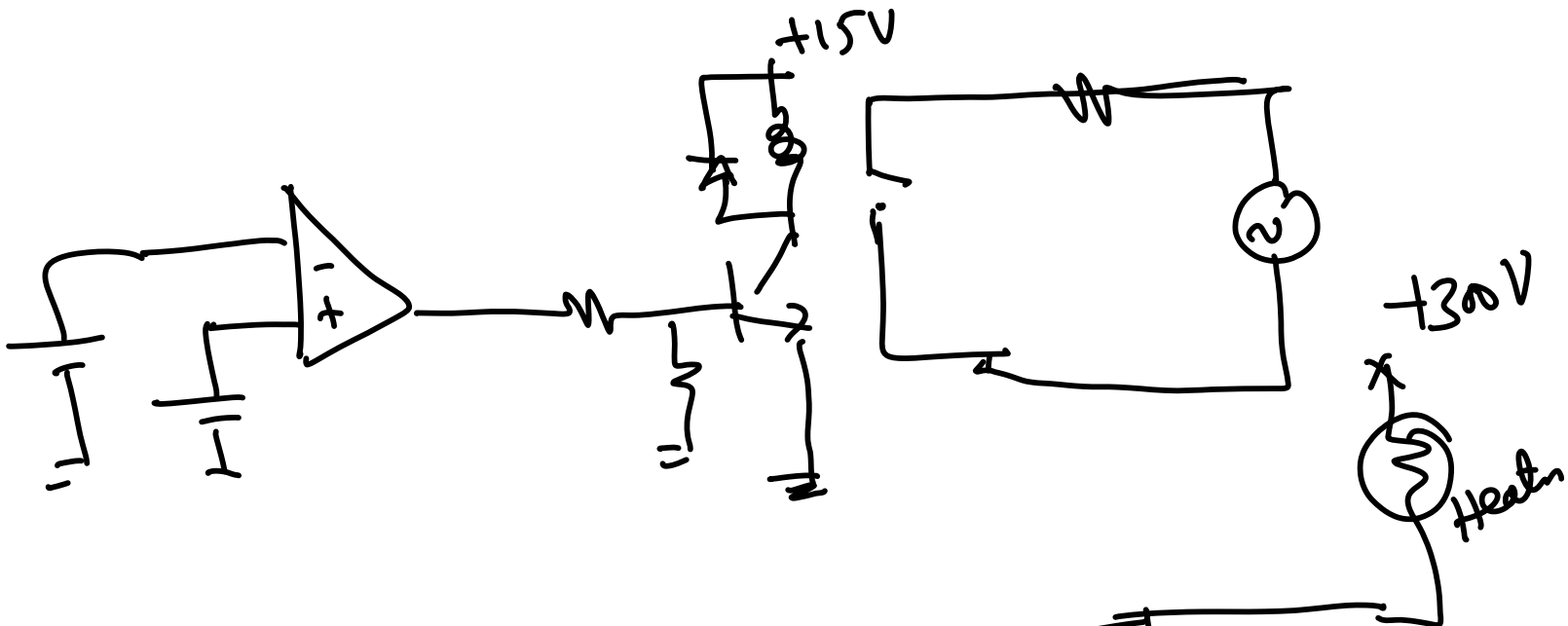
offset wf drift of 0.075C

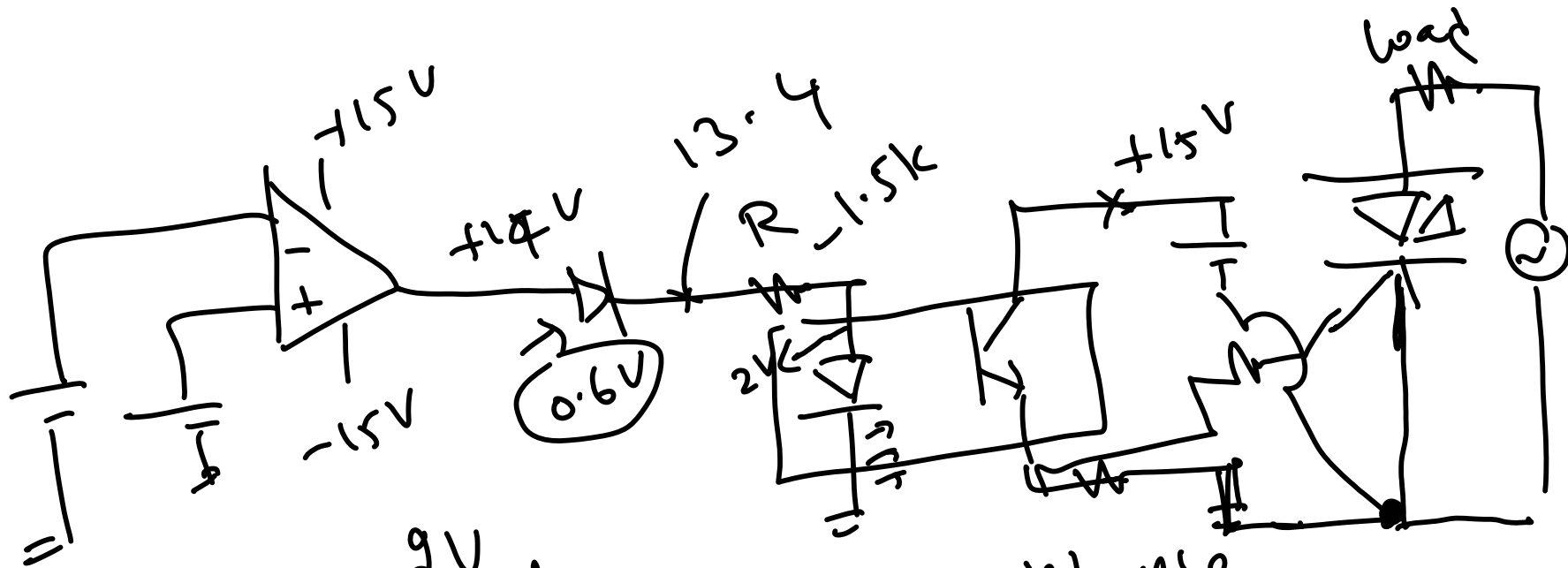


Heater Drive

ON/OFF







$$13.4 - 2V$$

$$11.4 = V$$

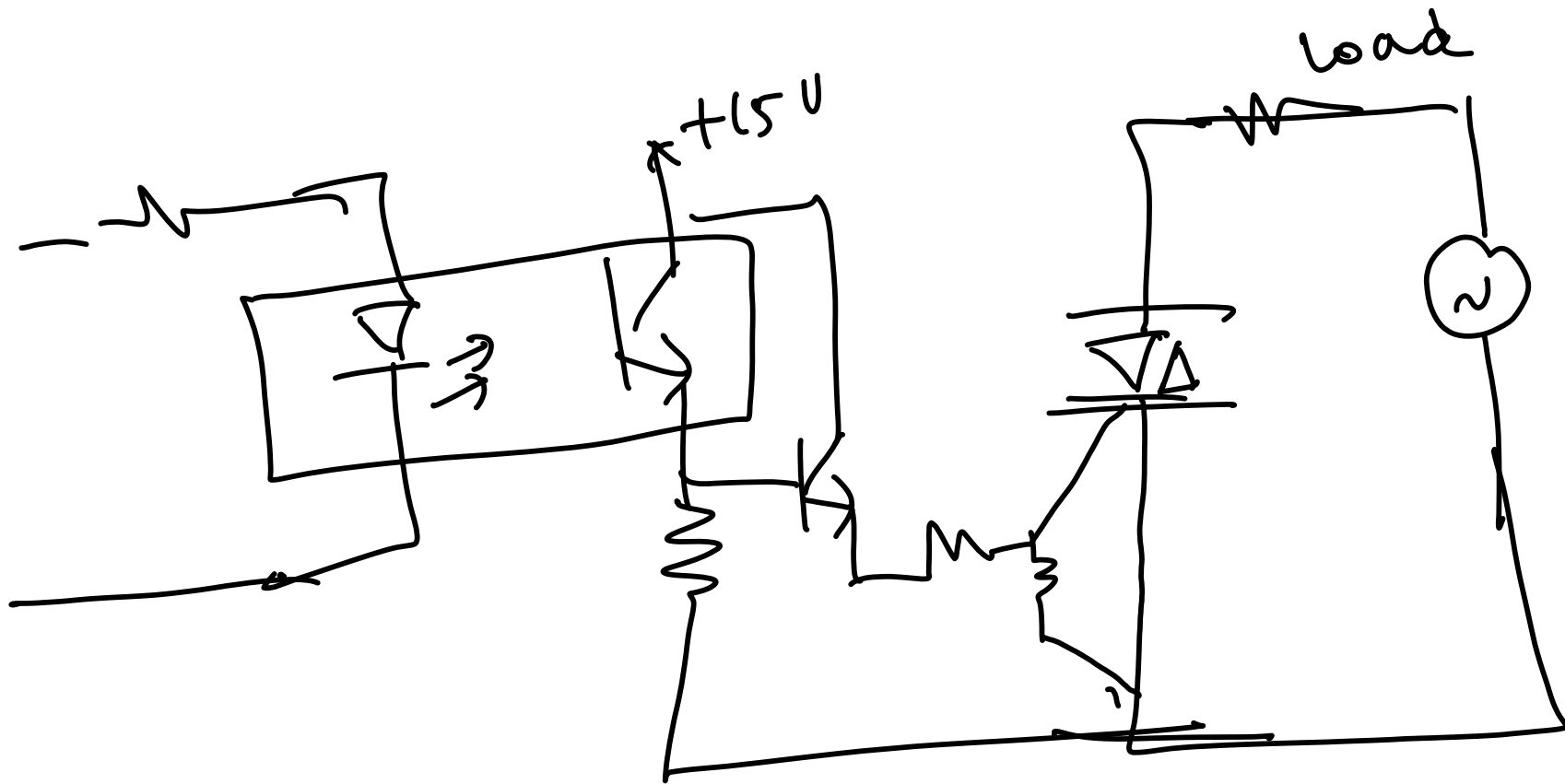
For

8mA current

$$R = \frac{11.4 \times 10^3}{8} = 1.5k$$

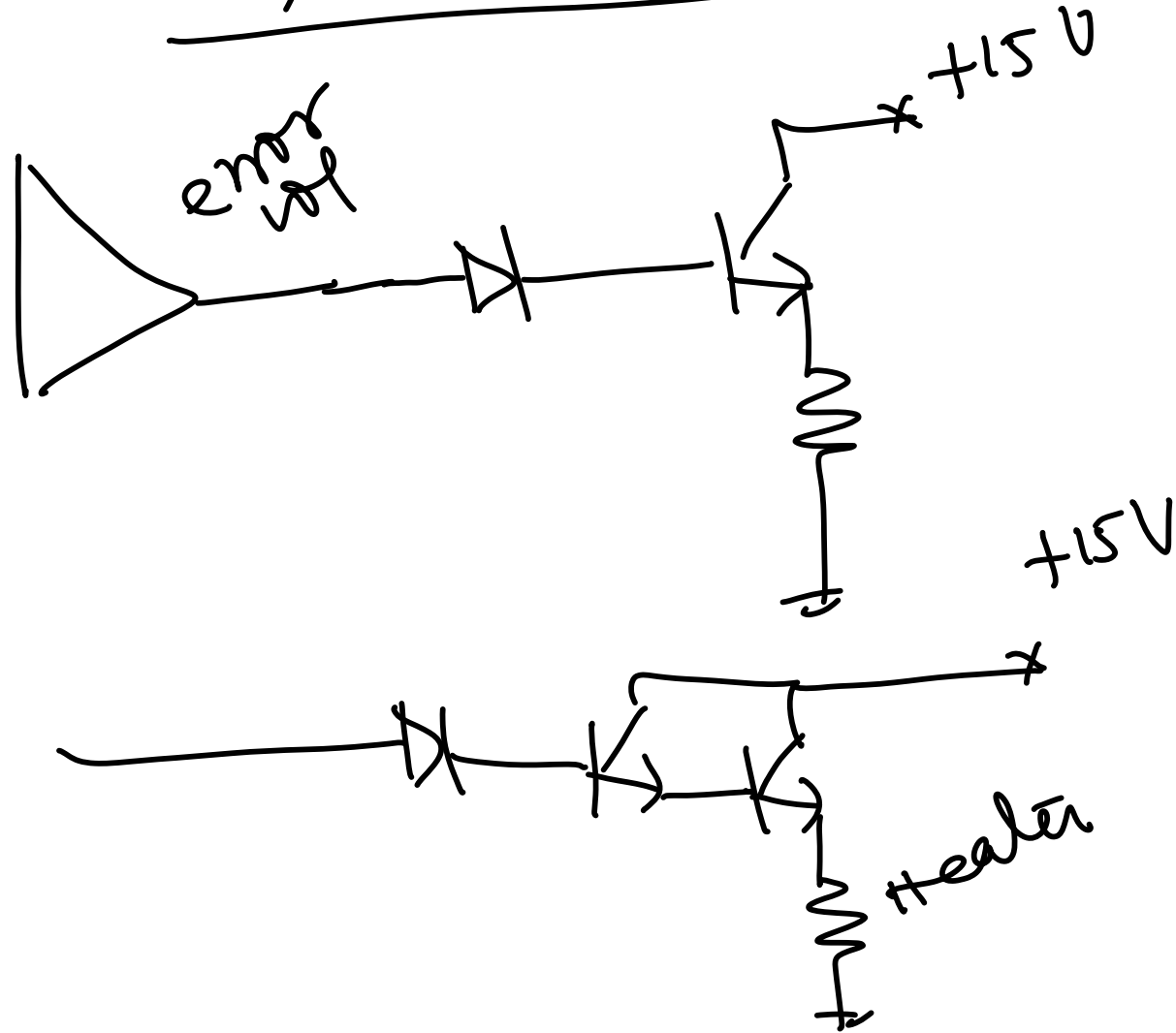
acc the resistance

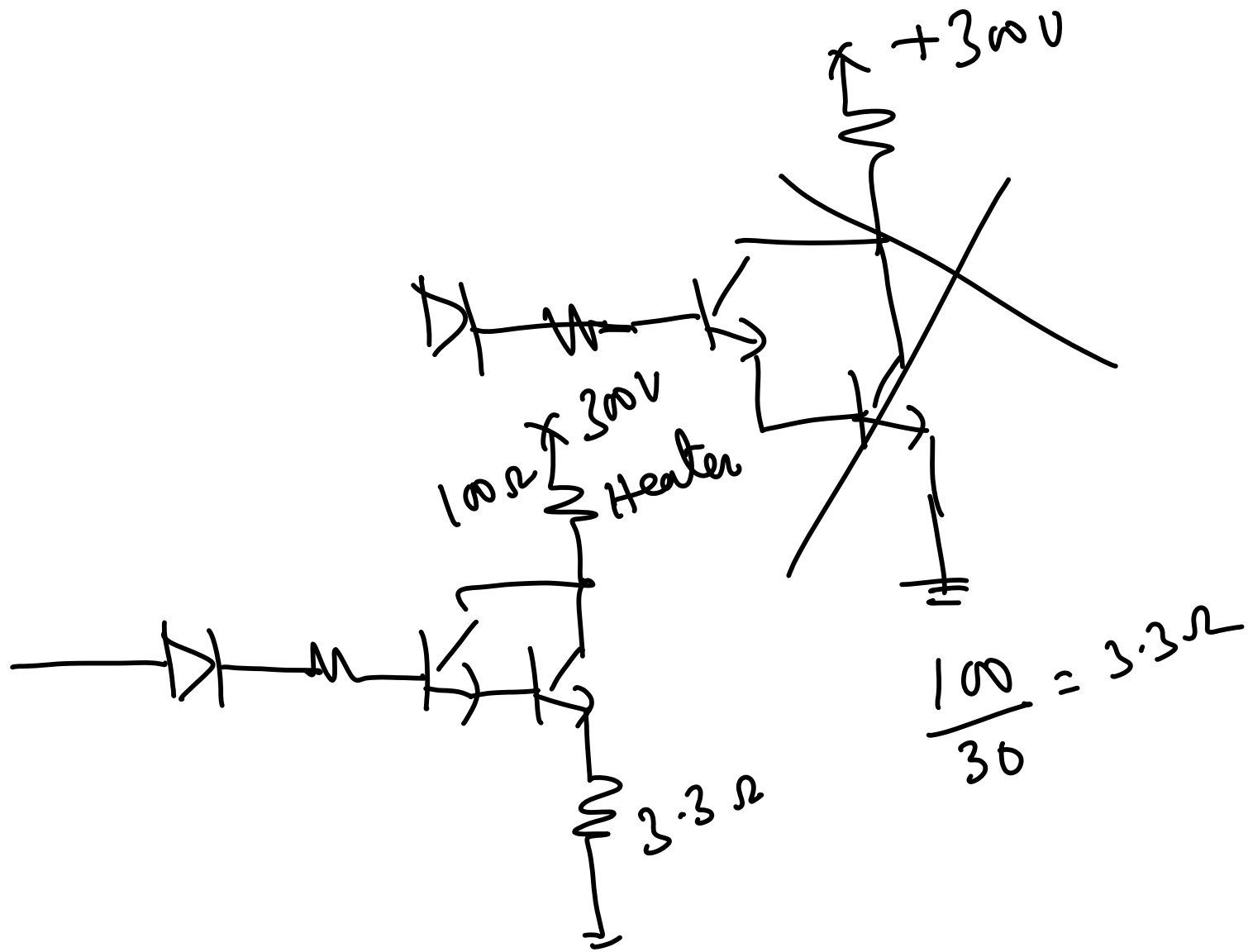
acc the resis

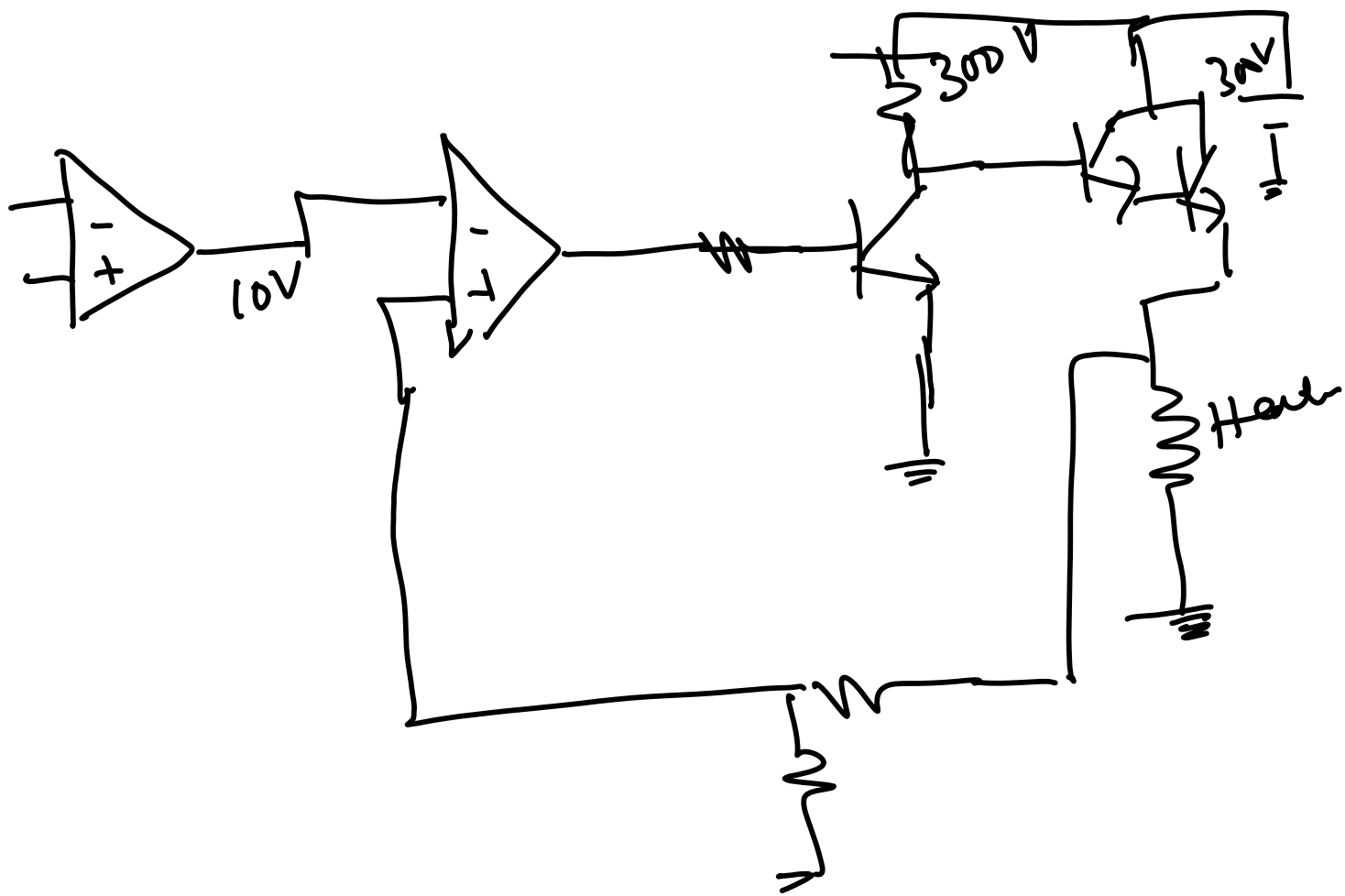


Heater drive drv

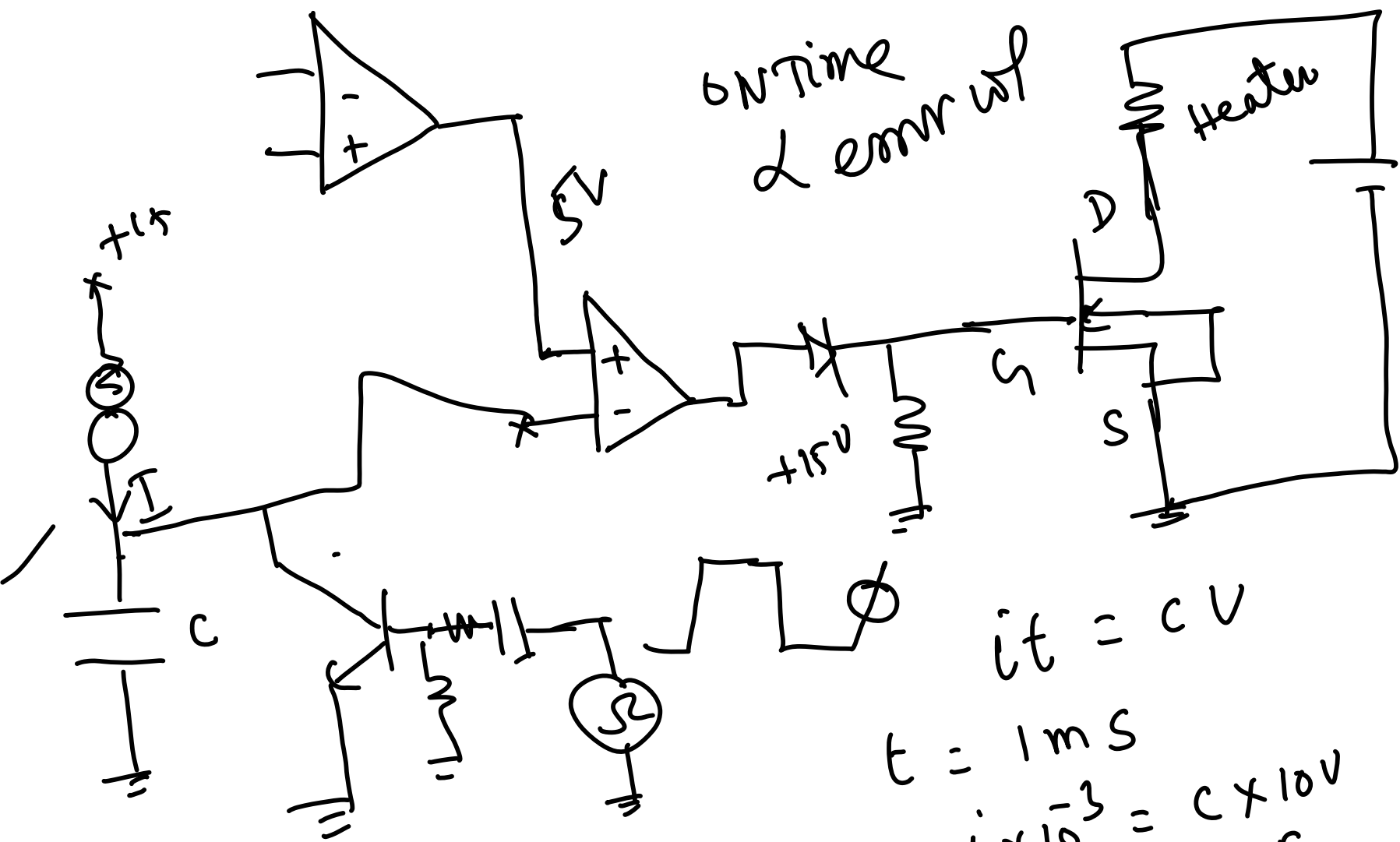
P, PI, PD, PID







PWM Technique



ON time
& error w/p

$$i t = C V$$

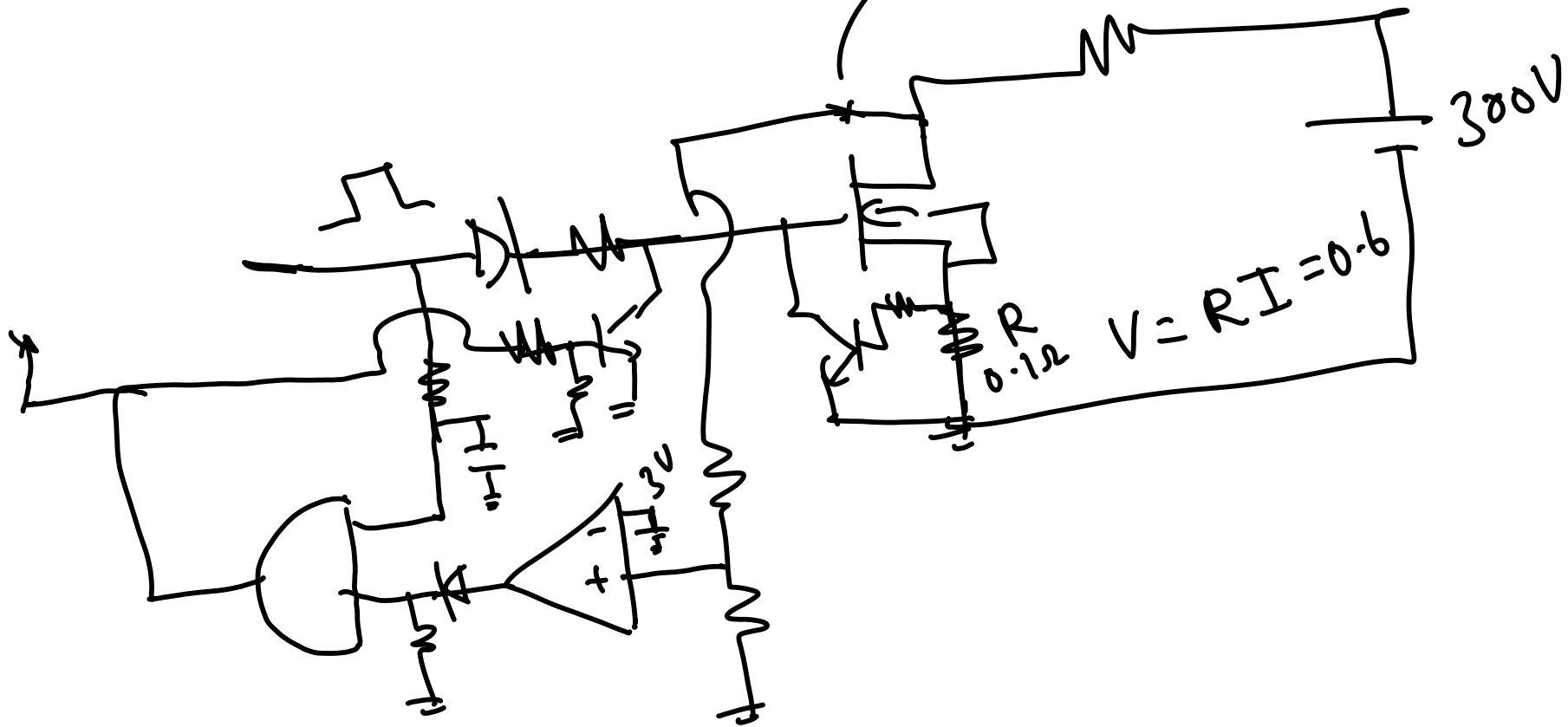
$$t = 1 \text{ ms}$$

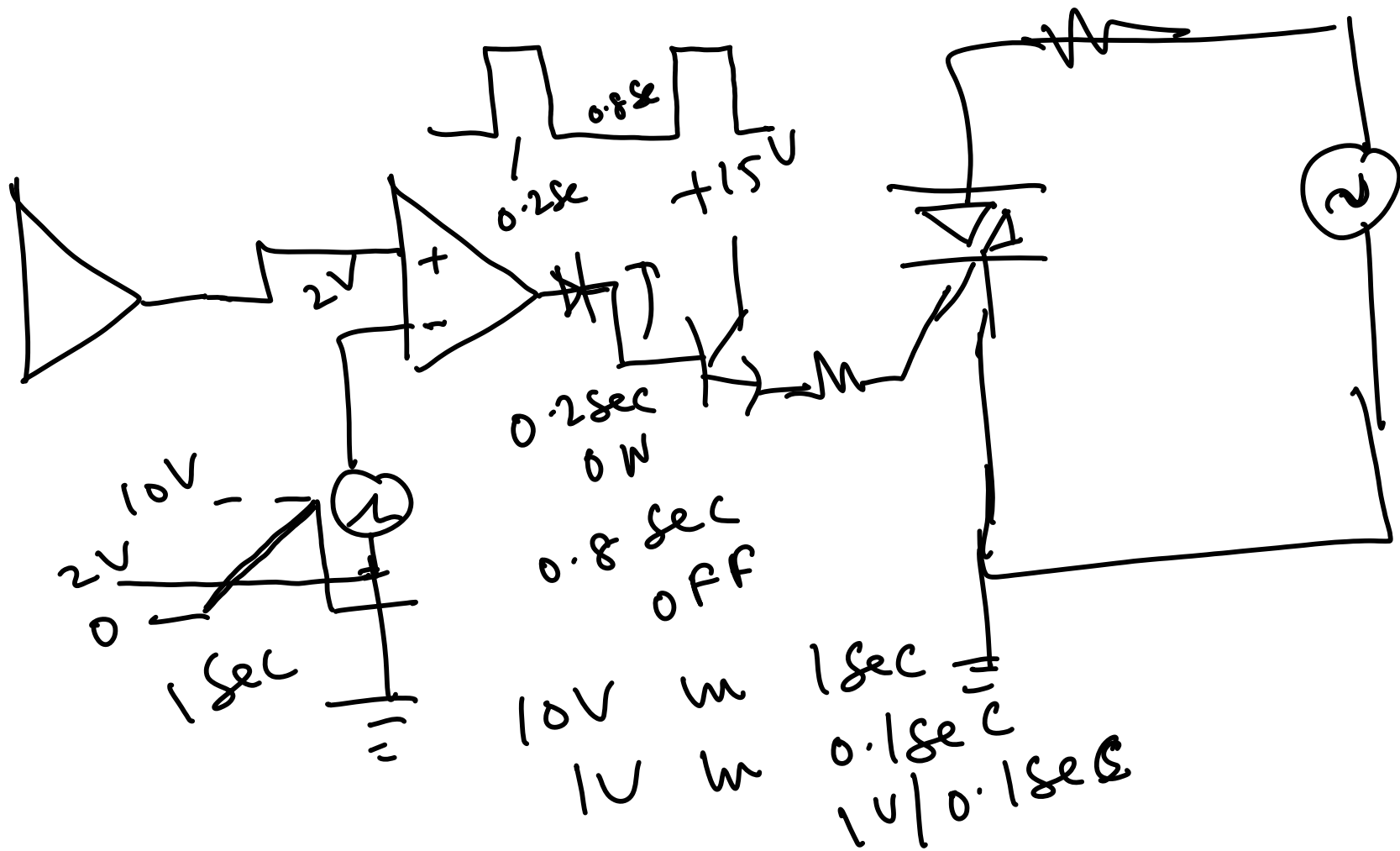
$$i \times 10^{-3} = C \times 10 \text{ V}$$

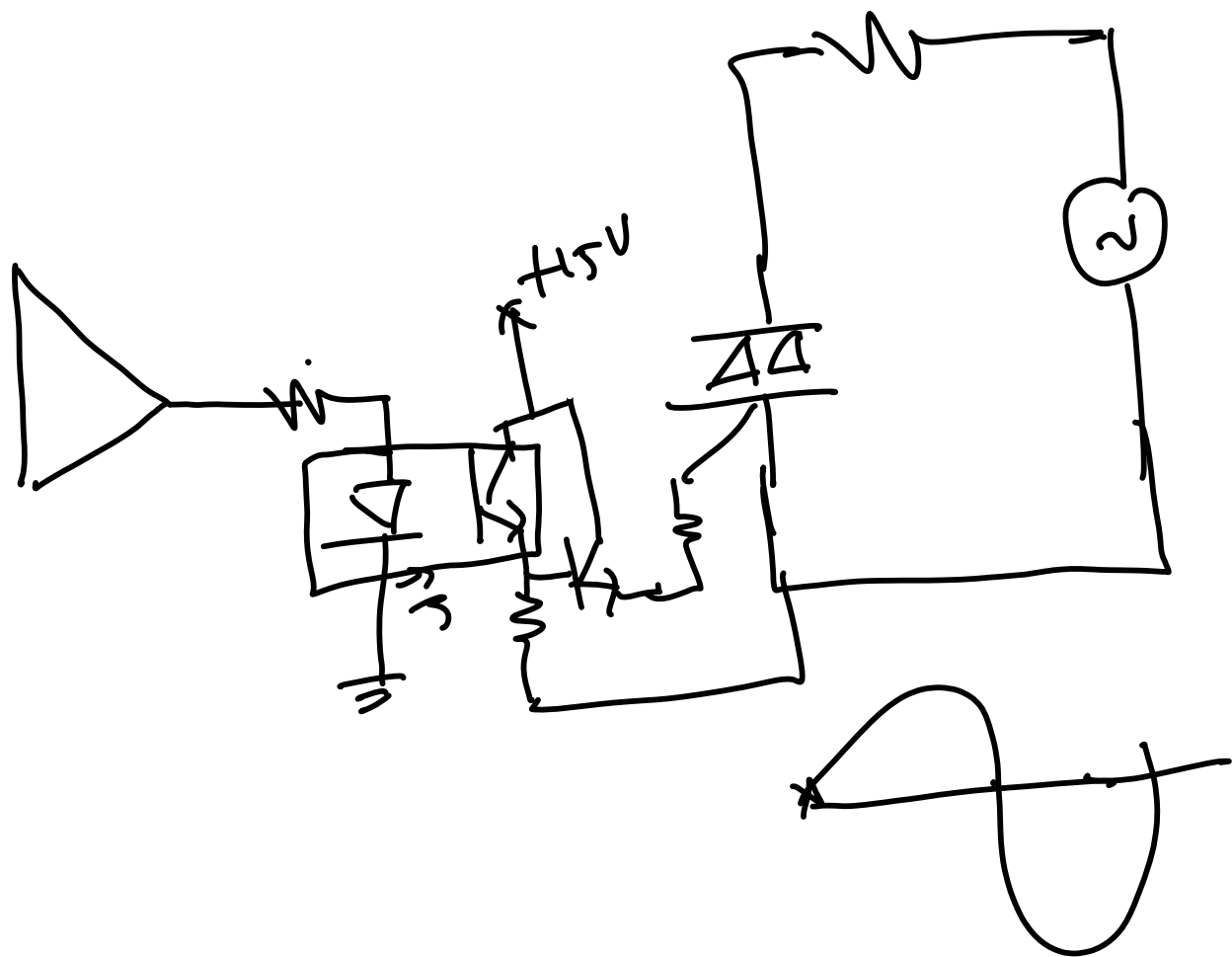
$$C = 1 \mu \text{ F}$$

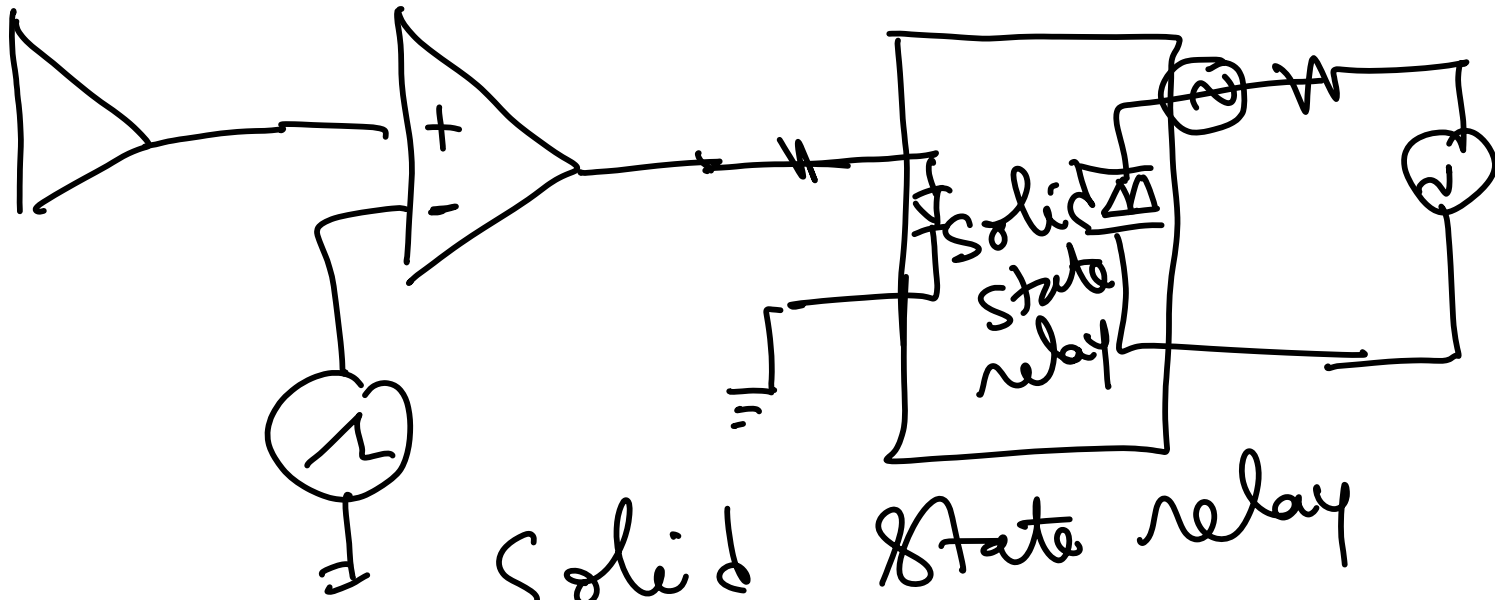
Short circuit protection for MOSFET

$$6A \times 300V = 1800W$$



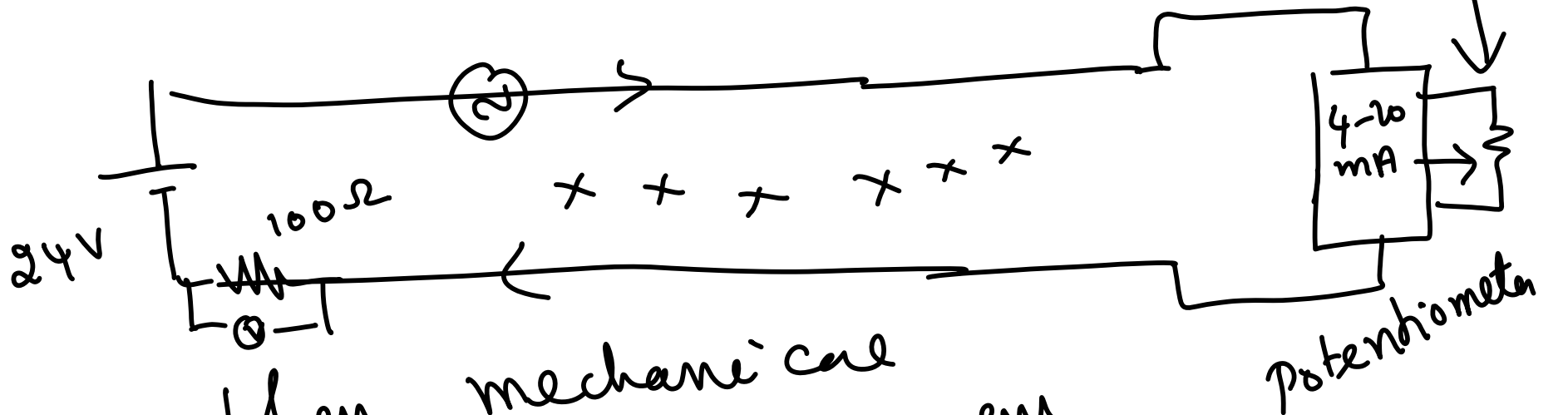






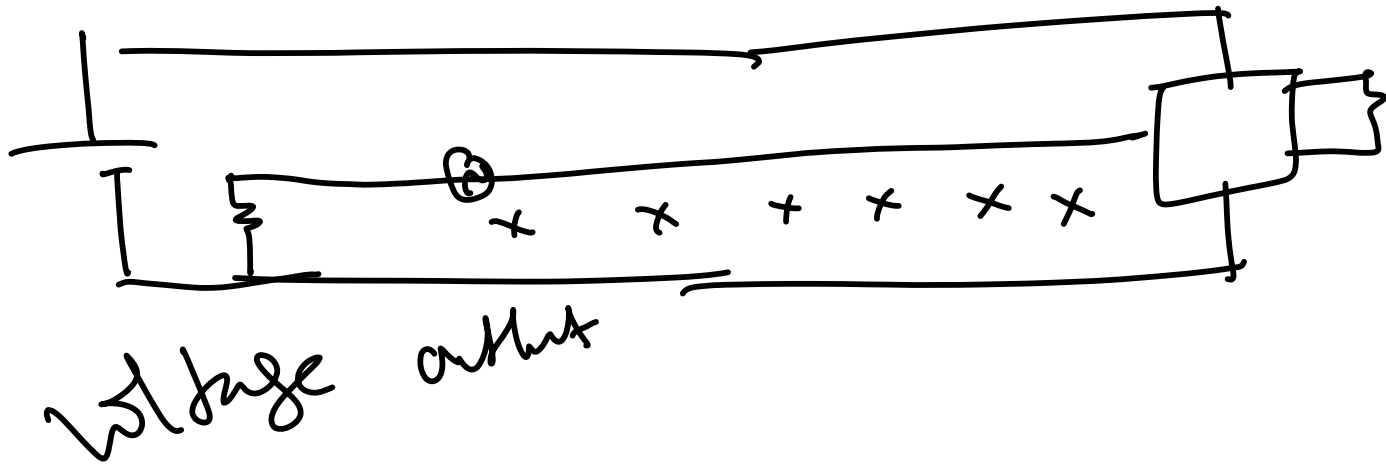
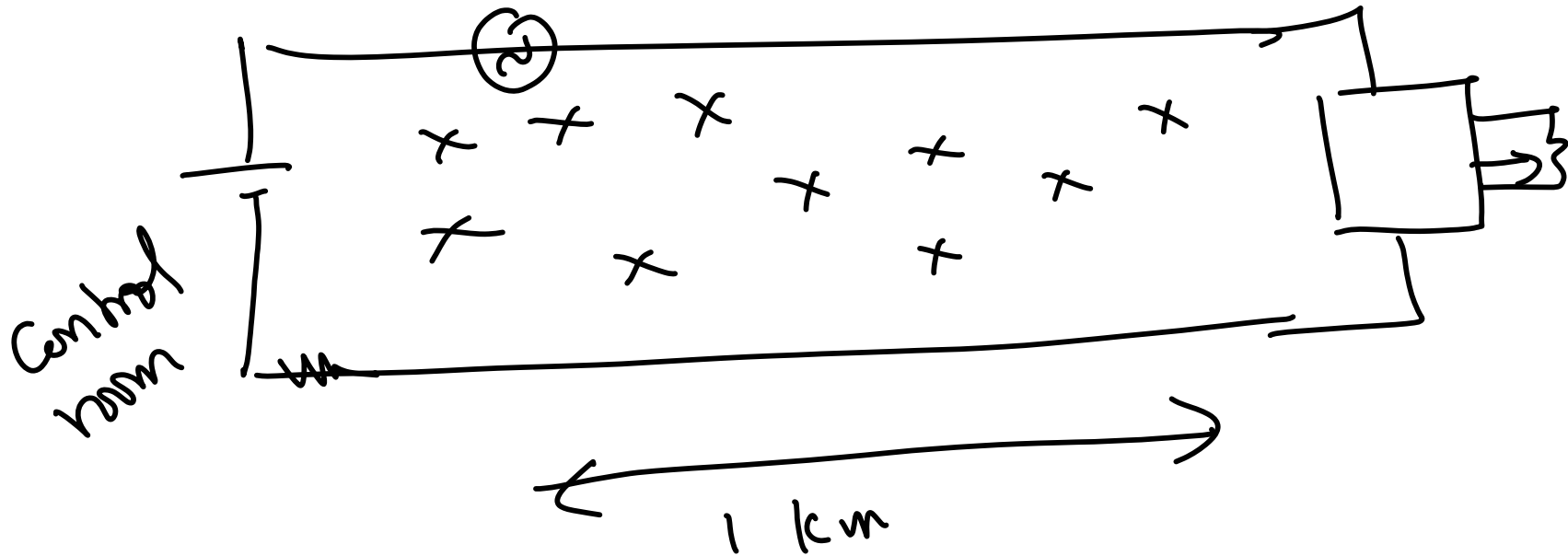
Solid State relay
with zero crossing

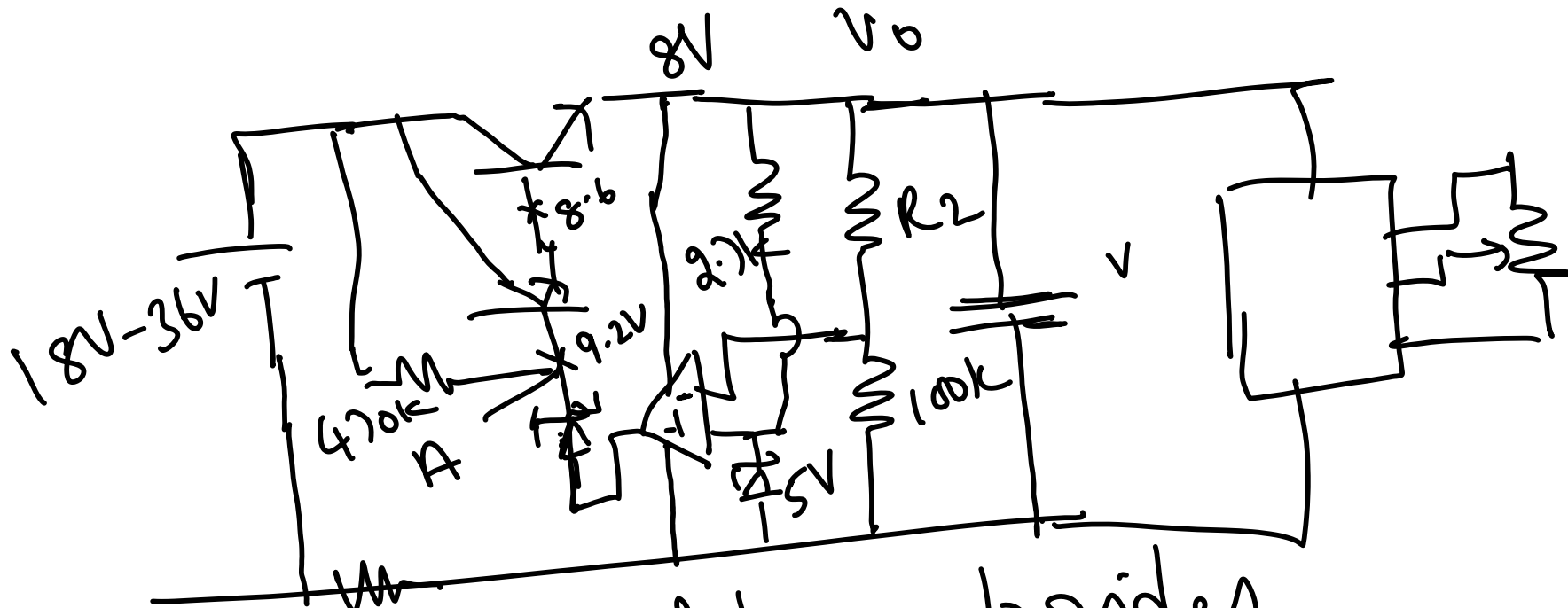
4 - 20 mA current transmitters



When mechanical system at zero end = 4 mA

- | | | |
|-----|--------|------------------------------------|
| 0% | → 4 mA | At the other end I should be 20 mA |
| 25% | → 8 mA | 50% = 12 mA |
| | | 75% = 16 mA |
| | | 100% = 20 mA |





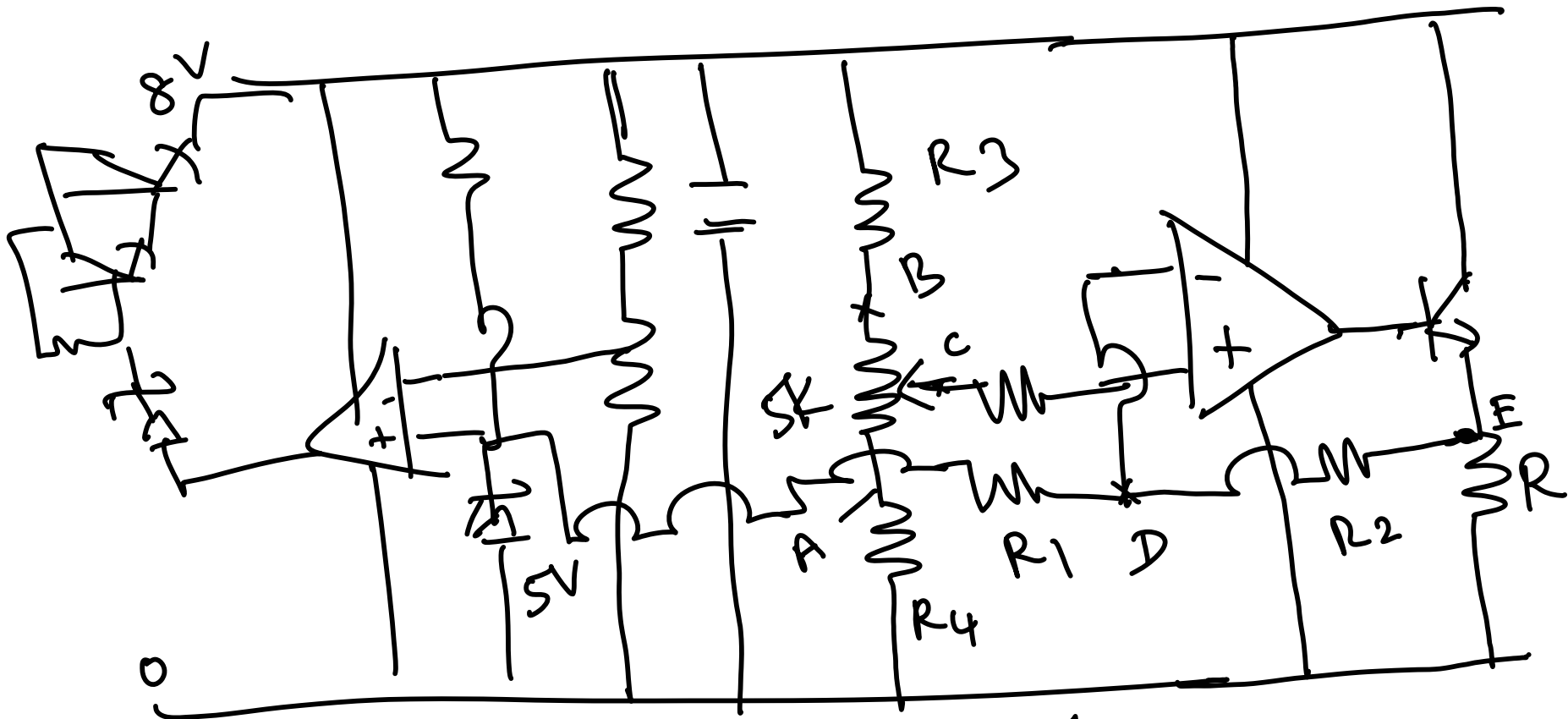
Zener voltage provides
 extra voltage i.e.
 V_{at A} = OP amp output
 + V_{across Zener}
 V_{across Zener} ≠ breakdown
 V_{of the Zener}

Wf acc $100k = 5V$

So output Wf = $\frac{5V \times (100k + x)}{100k}$

x can be ≈ 8 calculated

Design of a current
transmitter



Select R_4 , R_3 , pot
 such that $V_A = 2V$
 $V_B = 4V$
 V_C acc the potentiometer
 becomes $2V$

The expected charge at $D = 2V$
= charge at C

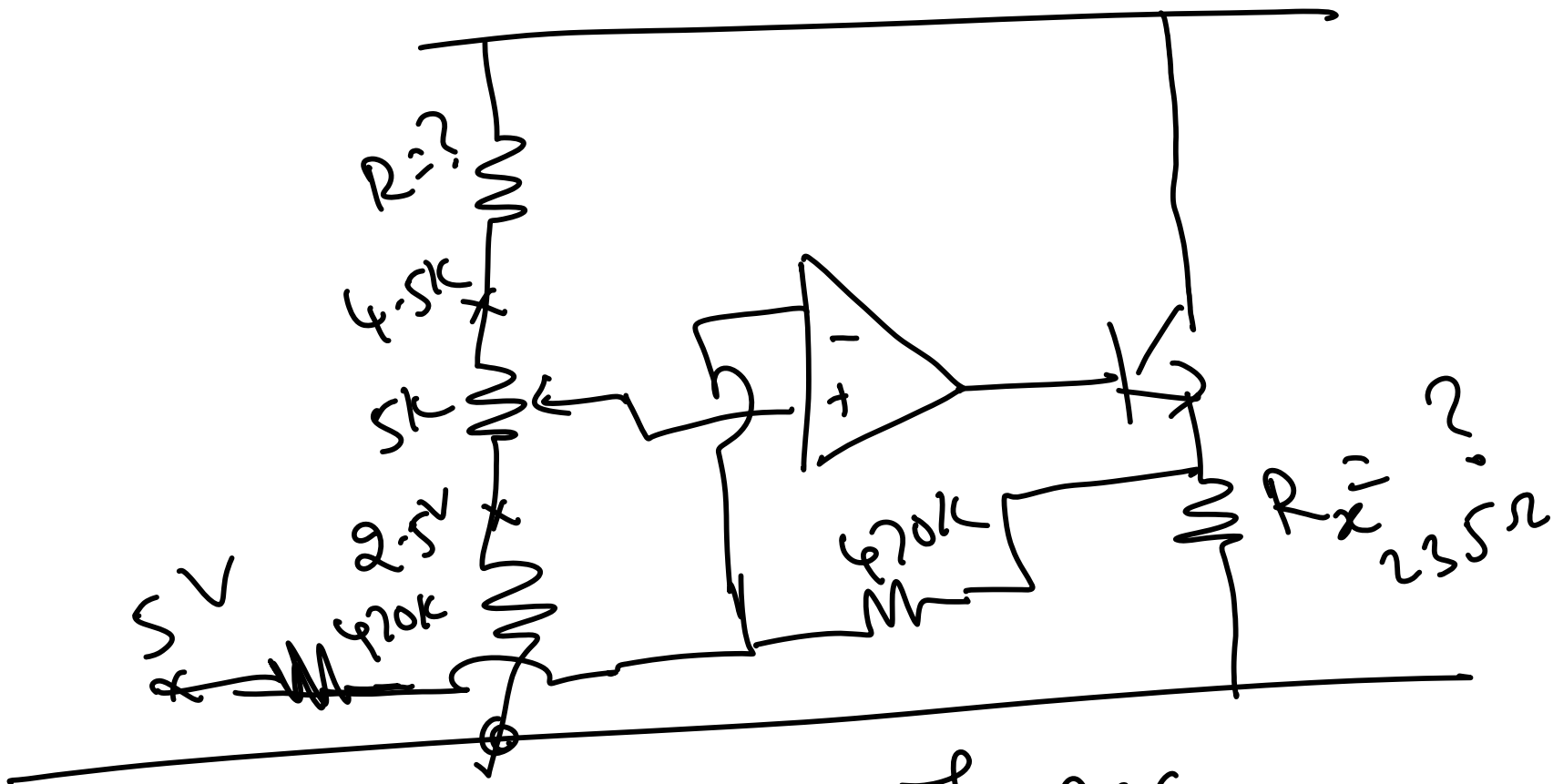
$$\Delta R_1 \approx R_2$$

Keep A at $2.5V$

Then $R_1 = R_2 = 470k$

B at $4.5V$

Po tenhio meta $Wf = 2V$



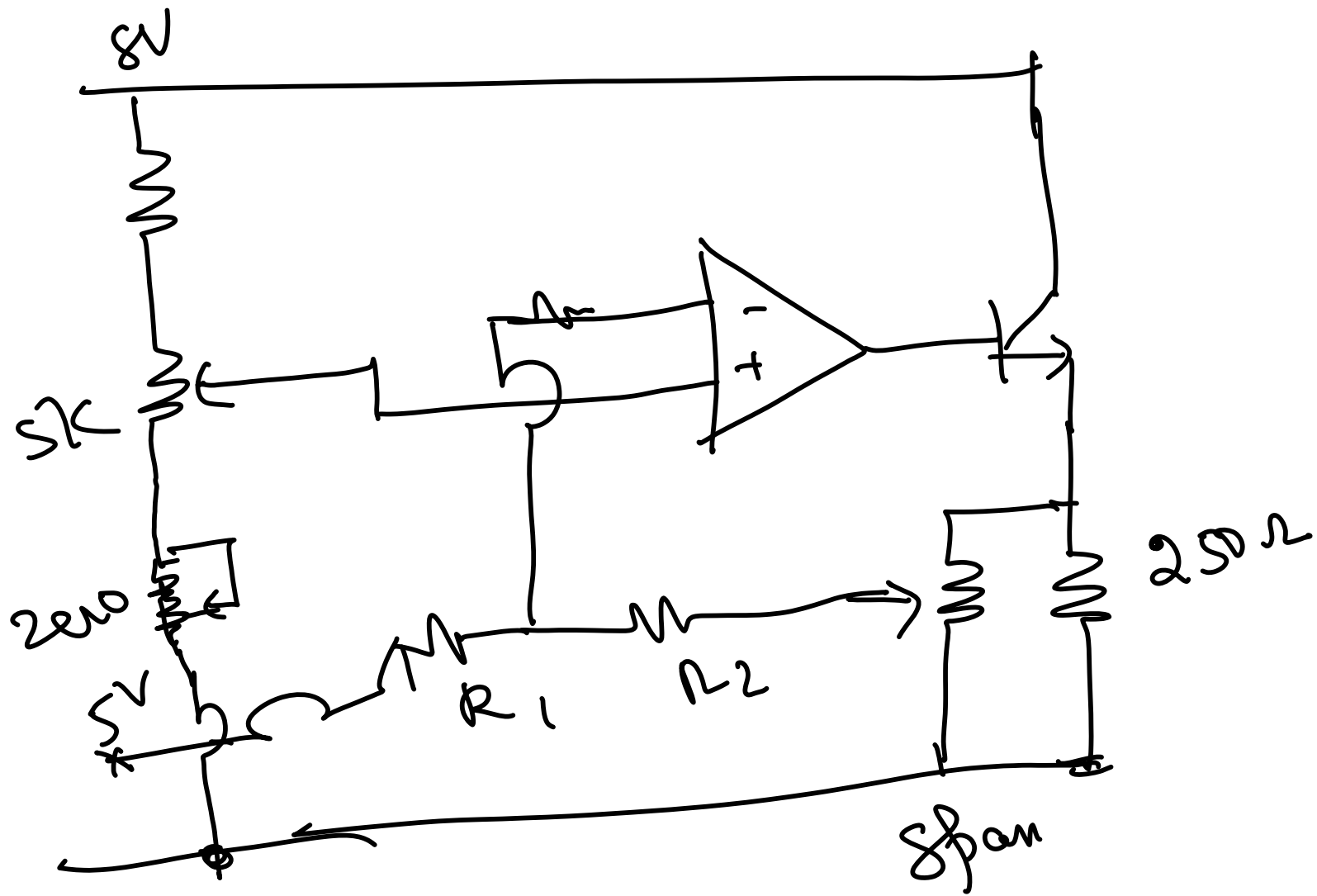
Required w/ acc
 $R_x = 4V$ at $17mA$

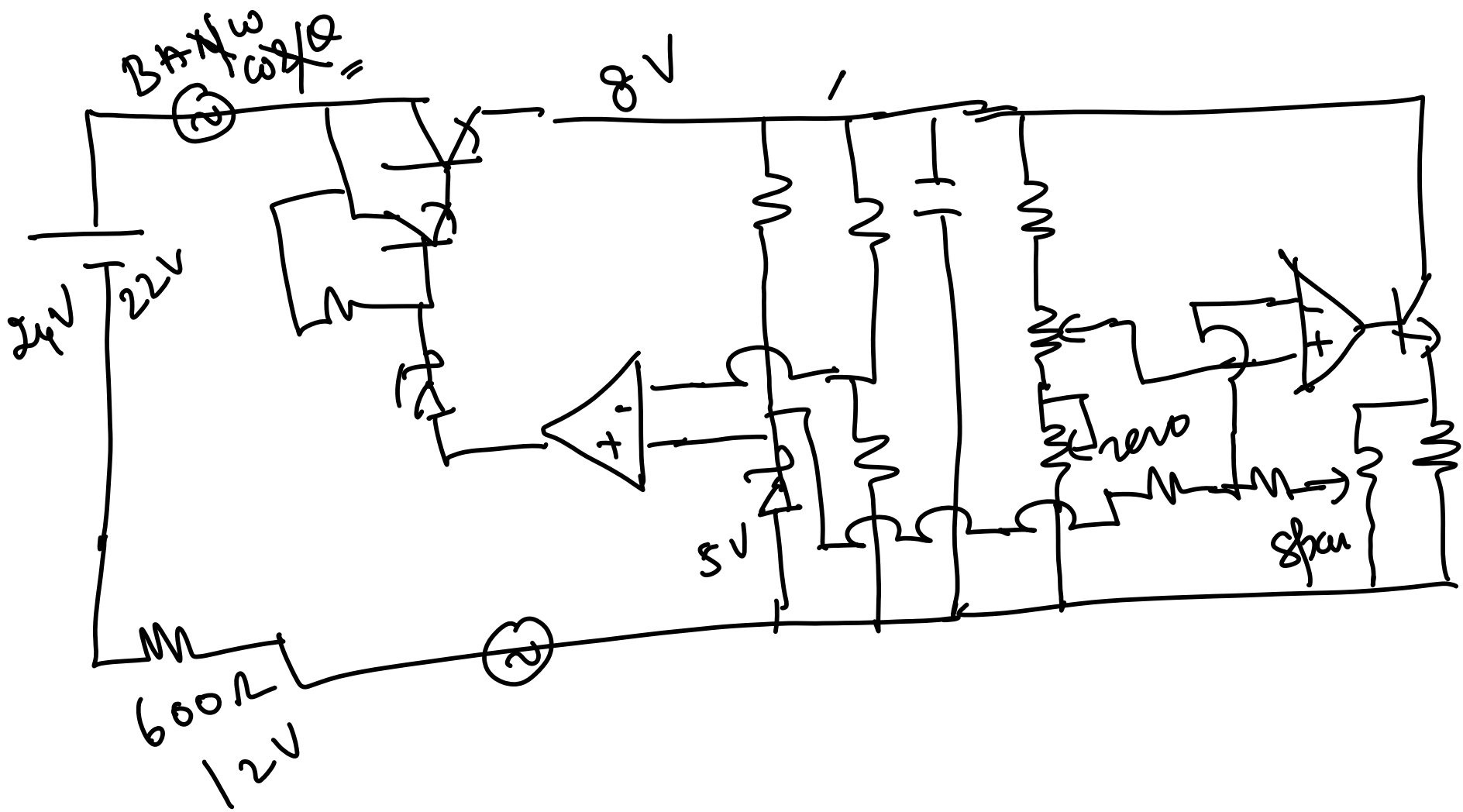
Required w/ acc
 $R_x \geq 0V$
 at $1mA$ or less

$$R_x \times 17 \text{ mA} = 4 \text{ V}$$

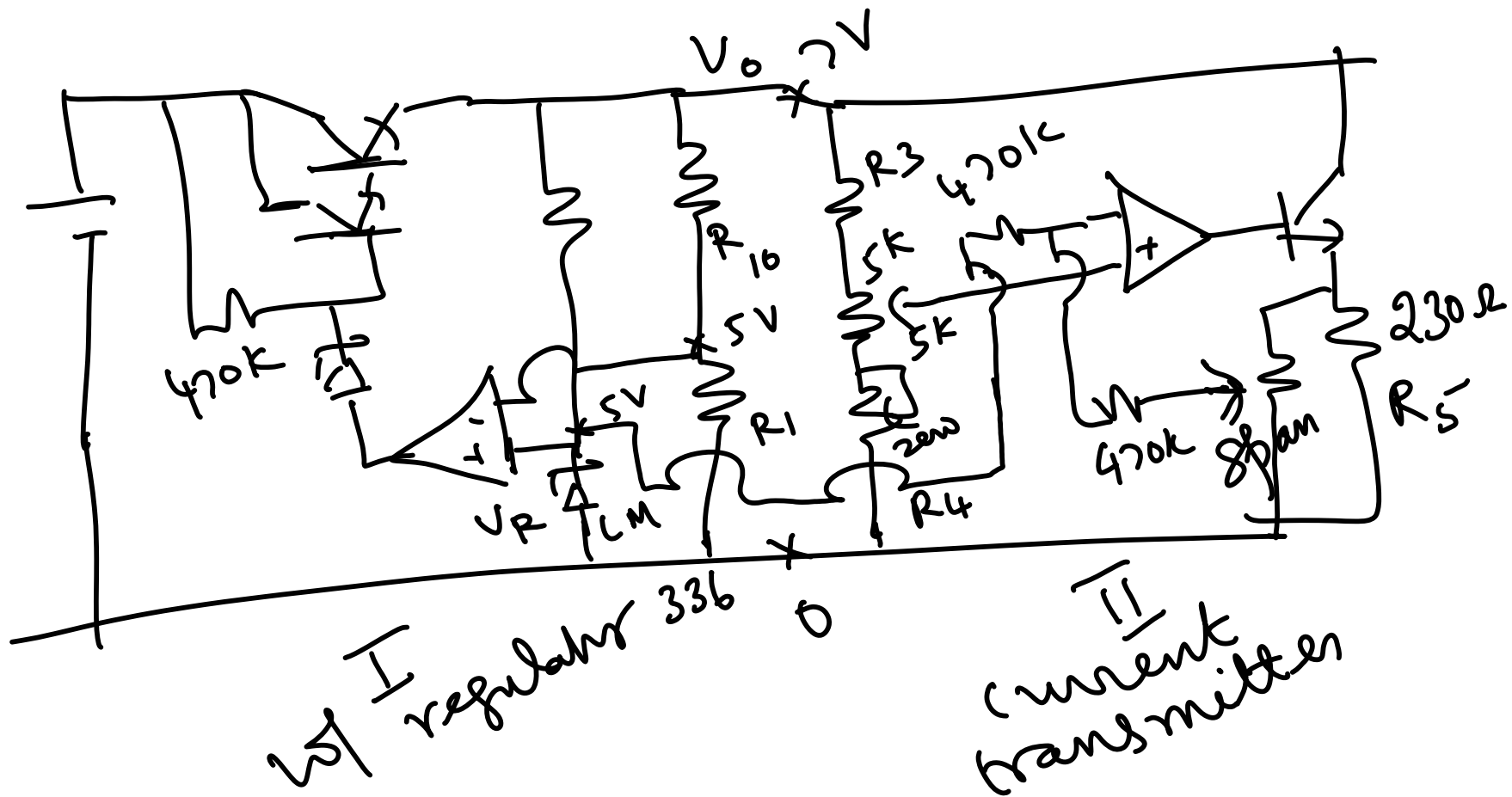
$$R_x = \frac{4 \text{ V}}{17} = \frac{4 \text{ mV}}{17} = \underline{\underline{235 \Omega}}$$

60





Error budgeting for 4-20mA current transmitter



LM336 Zener 5V 30 PPM/C

Drift = 30 PPM/C
Assuming ambient Temp
change = 100°C

Vol of the Zener initially be
= 5V

ΔV of the Zener

V × PPM × DC

$$= \frac{5 \times 30 \times 100}{10^6}$$

$$\Delta V = \frac{15 \times 10^3}{10^6}$$

$$= 15 \times 10^{-3} \text{ V}$$
$$= \pm 15 \text{ mV}$$

Δv of the zener = $\pm 15 \text{ mV}$

S_o regulated output voltage

$$\text{change} = \frac{15 \text{ mV} \times (R_1 + R_{10})}{R_1}$$

$$7 \text{ V} = 5 \times \frac{(R_1 + R_{10})}{R_1}$$

$$\frac{7 \text{ V}}{5 \text{ V}} = \frac{(R_1 + R_{10})}{R_1}$$

$$\Delta v_o = 15 \times 10^{-3} \times \frac{7}{5} = 21 \text{ mV}$$

$$\text{W/ acc } R_3 = R_4 = 2.5 \text{ V}$$

For 5k the w/p
drop = 2V

$$\text{So } R_3 = \frac{5k \times 2.5}{2} = \frac{12.5}{2} = 6.25k$$

$$R_3 = R_4 = 6.25k$$

w/p at the potentiometer

$$\text{top end} = 2.5 + 2.0 = 4.5V$$

(This corresponds to current of
20 mA)

For ΔV_o of 21 mV the corresponding
voltage change at the top

end of the potentiometer

$$= \frac{21 \times 4.5}{7.0} \text{ mV}$$

$$= 3 \times 4.5 \text{ mV} = \underline{13.5 \text{ mV}}$$

Assuming the span pot
at the top end the w/ ΔV
change at, at inverting
input = 13.5 mV = w/ change
at the non-inverting input

at -ve input $\Delta V = 13.5 \text{ mV}$
So w/ change acc RS
 $= 2 \times 13.5 = 27 \text{ mV}$

w/ change acc R_5

$$\approx 27 \text{ mV}$$

$$\text{So current change} = \frac{27 \times \text{mV}}{230}$$

$$= \frac{27}{230} = \pm 0.08 \text{ mA}$$

II
calculate the current
drift due to R_1 ; R_{10} change

$$R_1 = 100 \text{ k}$$

$$R_{10} = \frac{5 \times (R_1 + R_{10})}{R_1} = 7 \text{ V}$$

$$= \frac{5 (10^5 + R_{10})}{10^5} = 7 \text{ V}$$

$$7 = \frac{5 \times (10^5 + R_{10})}{10^5}$$

$$7 \times 10^5 = 5 \times 10^5 + 5 \times R_{10}$$

$$\frac{2 \times 10^5}{5} = R_{10}$$

$$R_{10} = \frac{200 \times 10^3}{5} = 40 \text{ k}$$

Assume R_1, R_{10} drifts by 50 ppm/°C

Assume R_1 is decreasing and R_{10} is increasing with temp

$$\Delta R_1 \text{ change} = - \frac{100 \times 10^3 \times 50 \times 100}{10^6}$$

$$= \frac{5 \times 10^8}{10^6} = -500 \Omega$$

$$\Delta R_{10} = \frac{40 \times 10^3 \times 50 \times 100}{10^6}$$

$$= 20 \times \frac{10^7}{10^6} = 200 \Omega$$

R_1 decreases by 500Ω

R_{10} increases by 200Ω

So change in regulated
voltage = $\frac{5V (R_1 + R_{10})}{R_1}$

$$\text{New } V_0 = \frac{5 (100 \times 10^3 - 500 + 40200)}{99500}$$

$$= 5 \frac{(99500 + 40200)}{99500} \quad \begin{array}{r} 99500 \\ 40200 \\ \hline 139700 \end{array}$$

$$= 5 \times \frac{139700}{99500} = \frac{1397}{995} \times 5 = \frac{1397}{199}$$

$$\text{New } V_0 = \frac{1397}{199} \approx \frac{1397}{200} = \underline{\underline{6.985 \text{ V}}}$$

$$\begin{aligned} \text{Change in } V_0 &= 7 - 6.985 \\ &= 15 \text{ mV} \end{aligned}$$

So the expected
current change in
 $20 \text{ mA} = 0.08 \text{ mA}$

III
Error due to V_{offset} of
Wt regulator stage

Let $V_{\text{offset}} = 15 \mu\text{V}/\text{C}$

For 100 C total offset voltage

$$\text{Change} = 15 \times 100 = 1.5 \text{ mV}$$

For 1.5 mV at the input of
the regulator of amp the
expected change at the output
of the regulator $= 1.5 \times \frac{7}{5} \text{ mV}$
 $= 2.1 \text{ mV}$

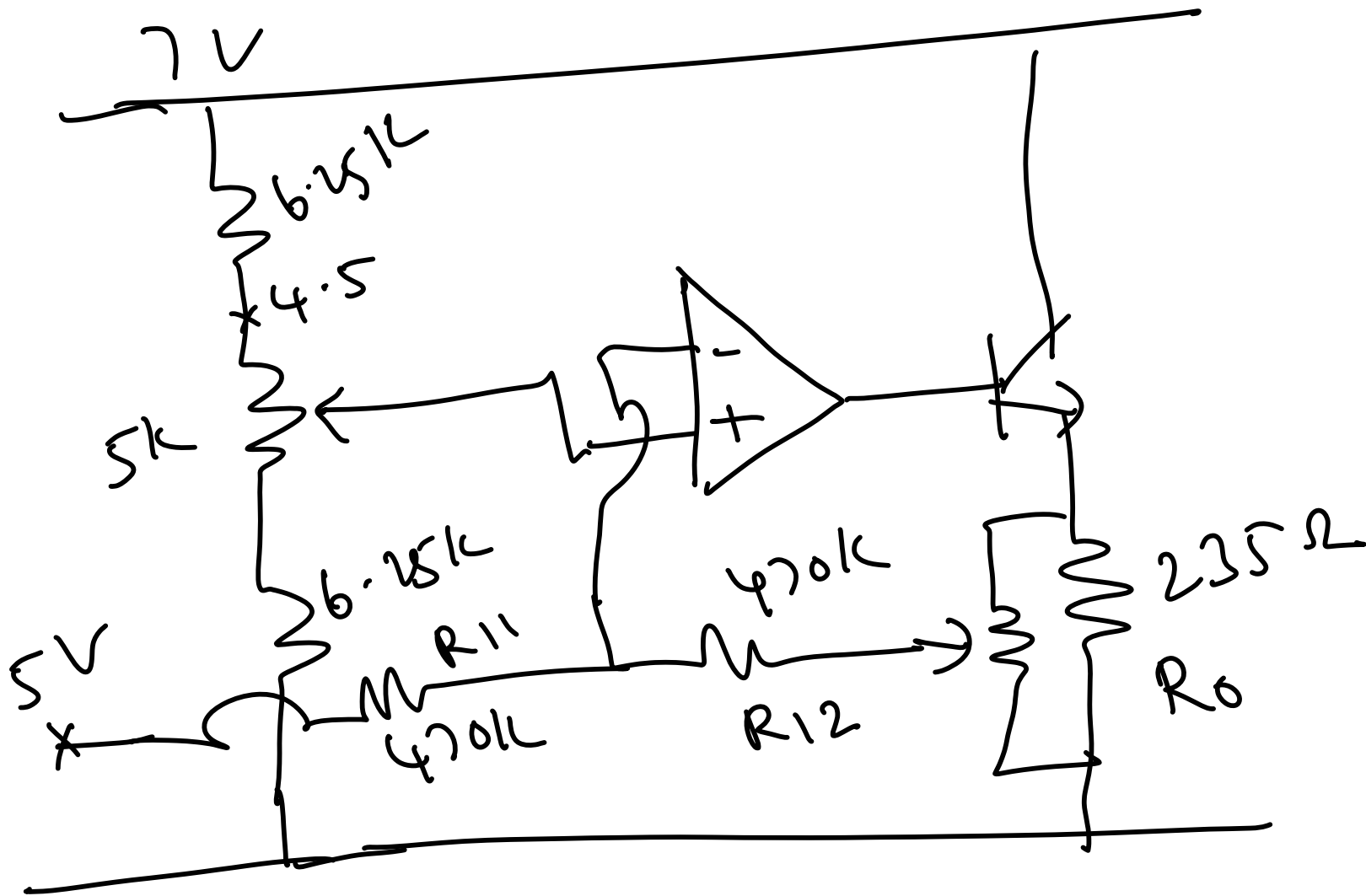
So current change in
the 20mA output

$$= \frac{0.08 \times 2.1}{15}$$

$$= \frac{0.16}{15} = 0.01 \text{ mA}$$

Error in the Current Converter

Stage



① Error due to offset
voltage drift of current
converter of amp

$$V_{\text{offset}} = 15 \mu\text{V} \cdot \text{C}$$

Total offset voltage

$$\text{Change} = \pm 1.5 \text{ mV} \\ (15 \mu\text{V} \times 100)$$

So the expected change in

the non-inverting input = 1.5 mV
= Expected change

in the inverting input = 1.5 mV

So the expected change

$$\text{across } R_0 = \frac{1.5 \times 470 + 470k}{470}$$

$$= 3 \text{ mV}$$

So the expected current change

$$\text{in } 20 \text{ mA} = \frac{3 \times 10^{-3}}{230} = \frac{3000}{230} \mu\text{A} = 12 \mu\text{A}$$

②

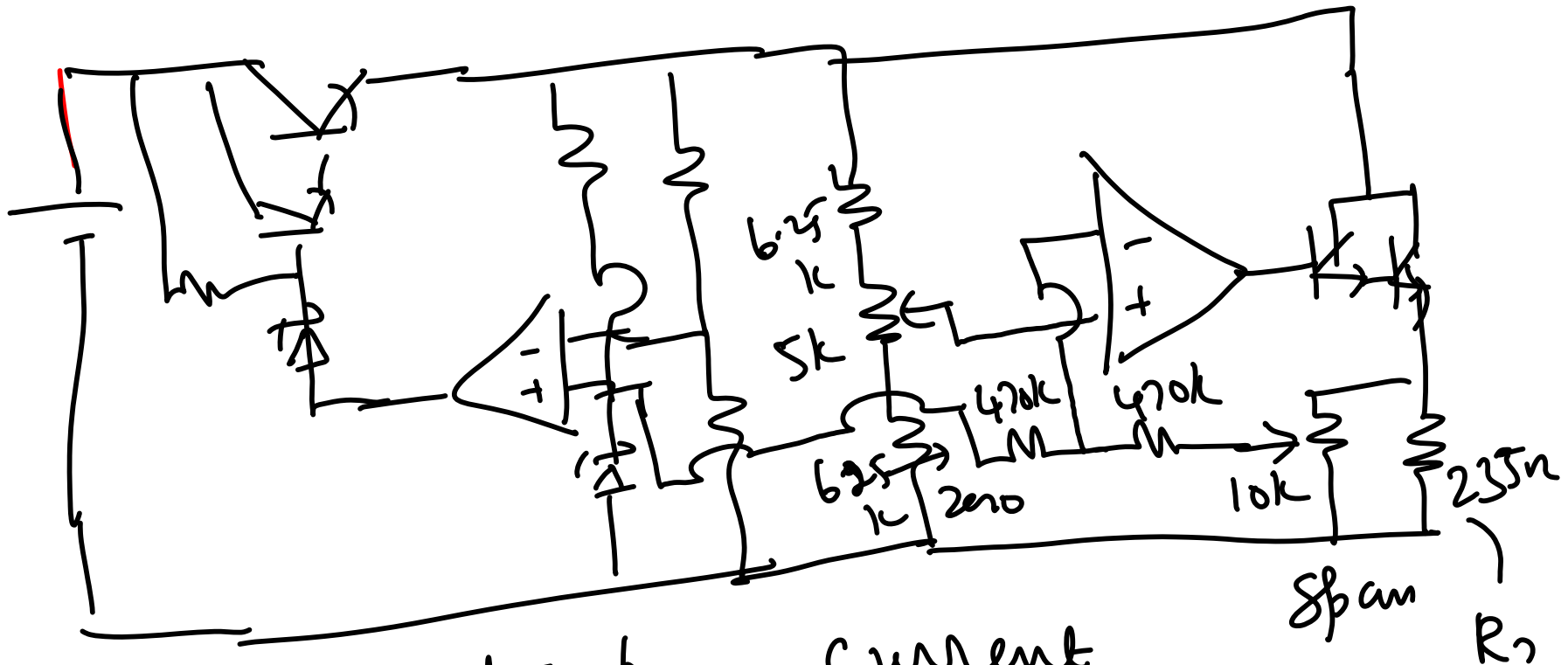
change in current
due to zero w/ change

③

change in current
due to R_{11} , R_{12} change

④

change in current due to
 235Ω resistance change



Calculate the current drift due to drift in R_7

Let the TC of

$$R_7 = 50 \text{ PPM}/^\circ\text{C}$$

For $\Delta T = 10^\circ\text{C}$

$$\Delta R = \frac{235 \times 50 \times 100}{10^6 - 3}$$

$$= 235 \times 5 \times 10^{-3}$$

$$= 1.175 \Omega$$

Assuming 16 mA current in R_7

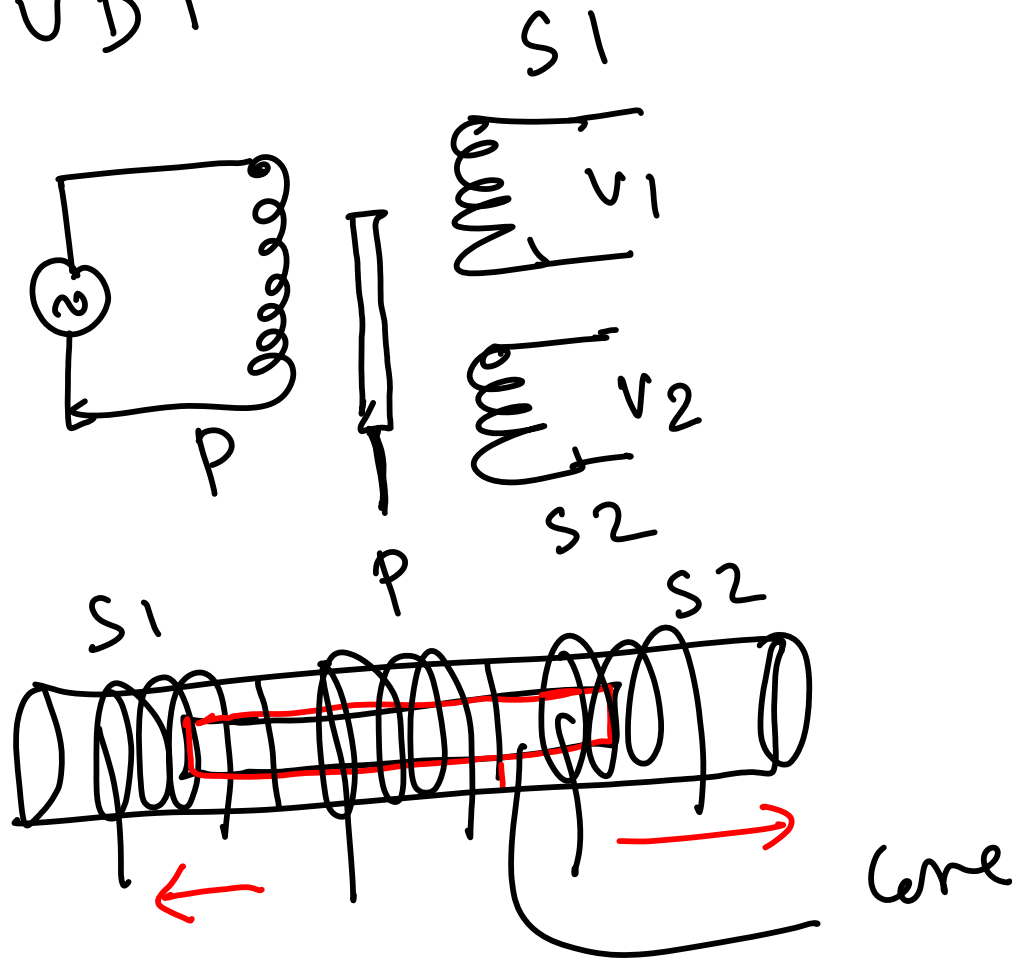
Then for 1.175Ω change the

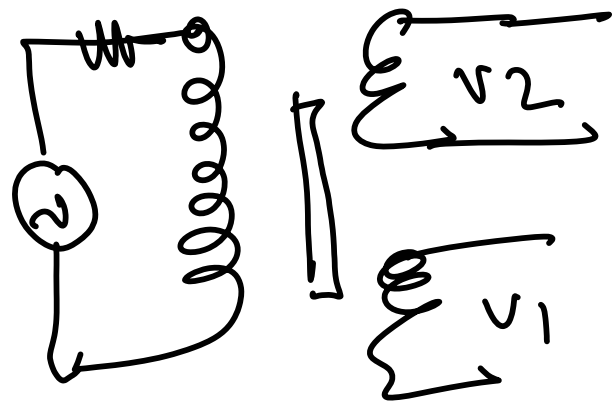
expected current change

$$= \frac{16 \times 1.1}{235} = \frac{17.6}{235} \text{ mA}$$
$$= \frac{1}{15} \text{ mA} = 0.06 \text{ mA}$$

Design of LVDT based position transmitter

① LVDT





$$|V_2| - |V_1| = \text{displace}$$

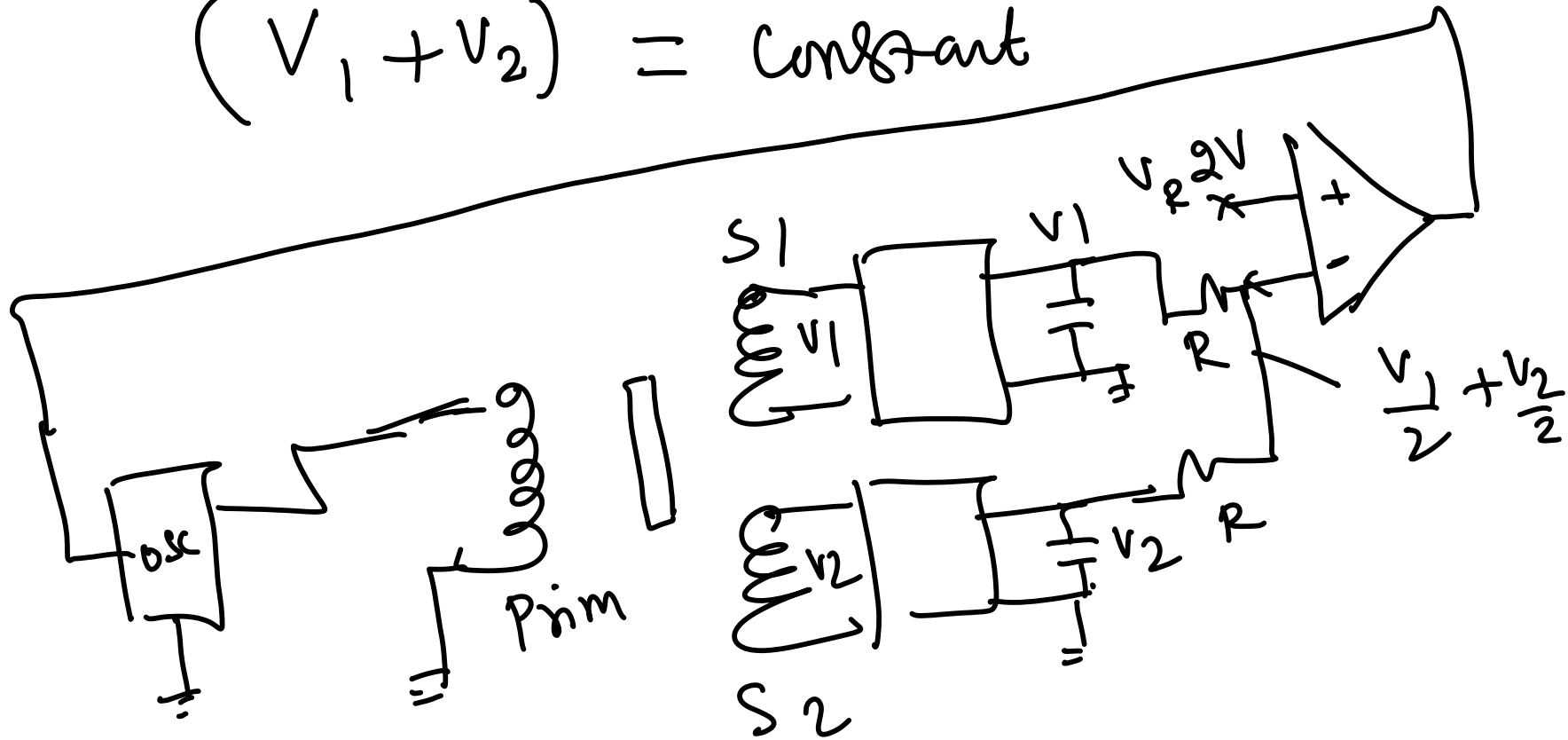
(1) Convert V_1 and V_2 into DC

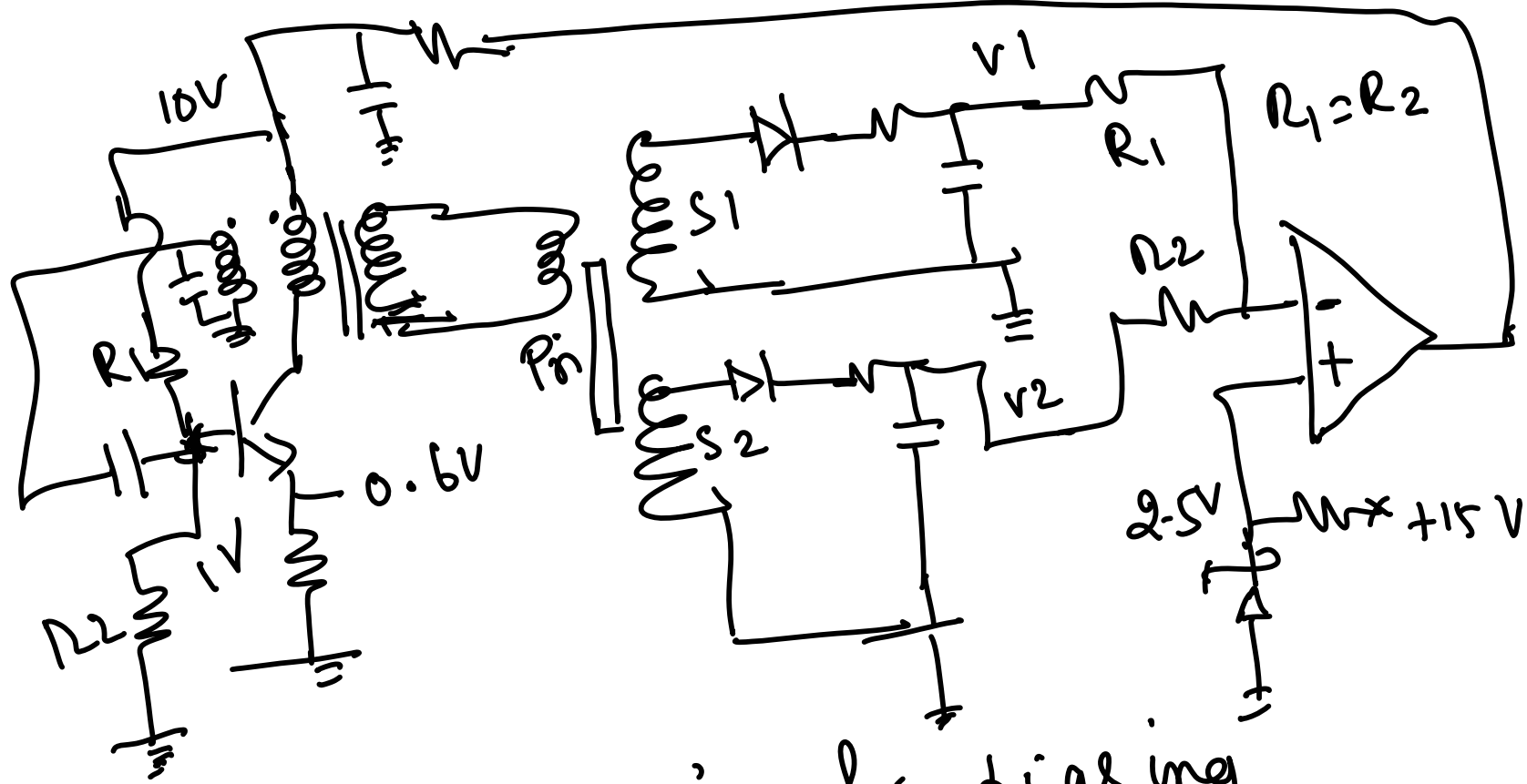
This dc w/ difference alone give you the displacement

(2) $|V_2 - V_1|$ changes with temp

How to make $(V_2 - V_1)$ independent of Temp?

$$(V_1 + V_2) = \text{constant}$$





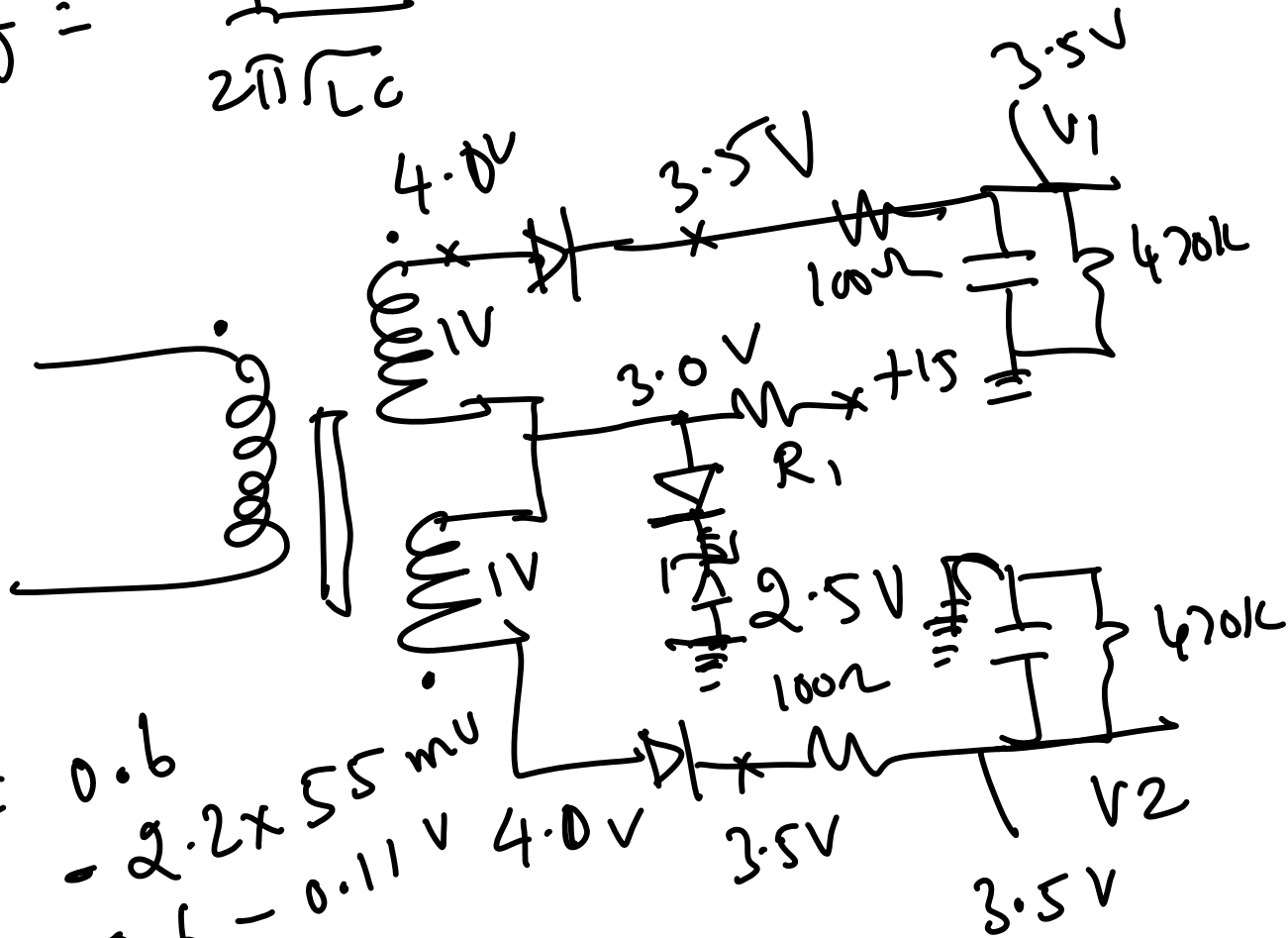
- R_1, R_2 is for biasing
- ① The emitter current increases
 - ② This produces increased mag field in the coil

③ This increases base vol of the transistor

④ This increase in base vol again increases the emitter current.

⑤ Again mag field in the primary increases

$$f = \frac{1}{2\pi RC}$$



Wol acc
he did

$$= 0.6$$

$$= 2.2 \times 55 \mu$$

$$= 0.6 - 0.11 \text{ V}$$

$$= 0.49 \text{ V}$$

At room temp

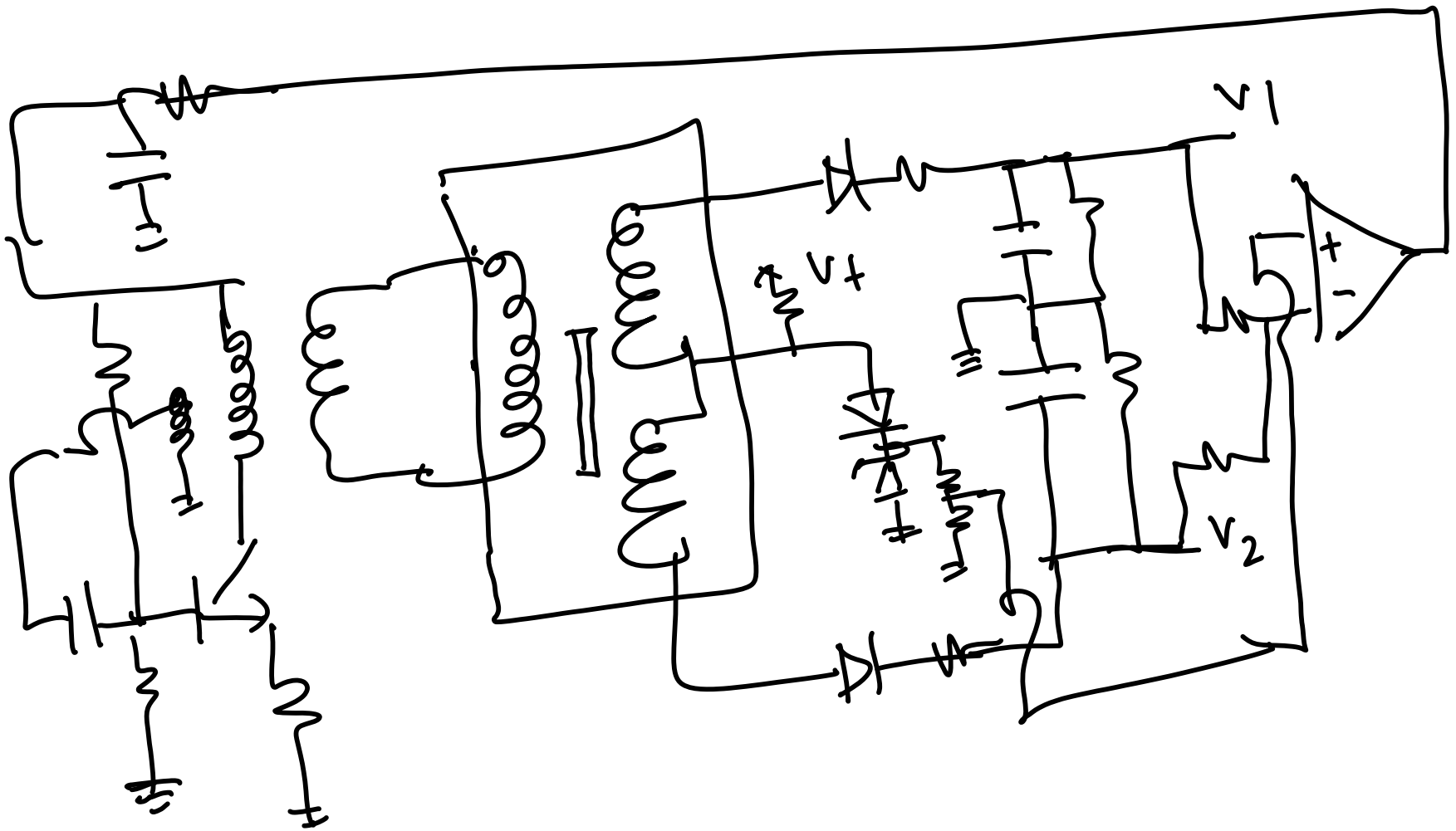
$$V_1 = 3.5 \text{ V}$$

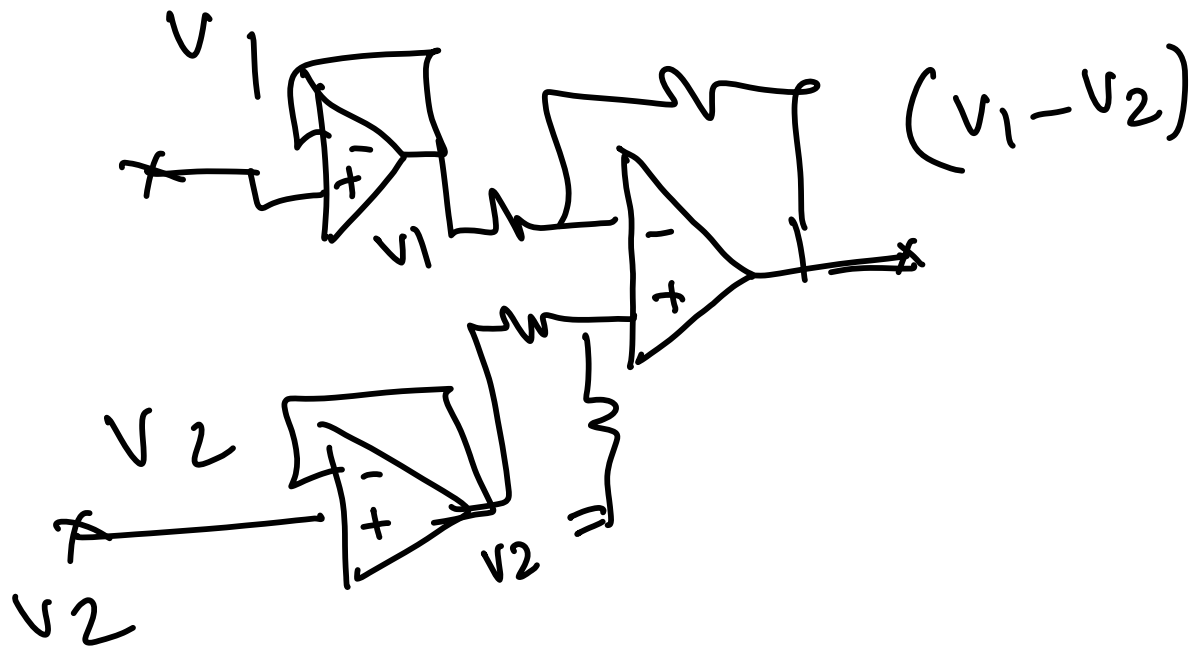
$$V_2 = 3.5 \text{ V}$$

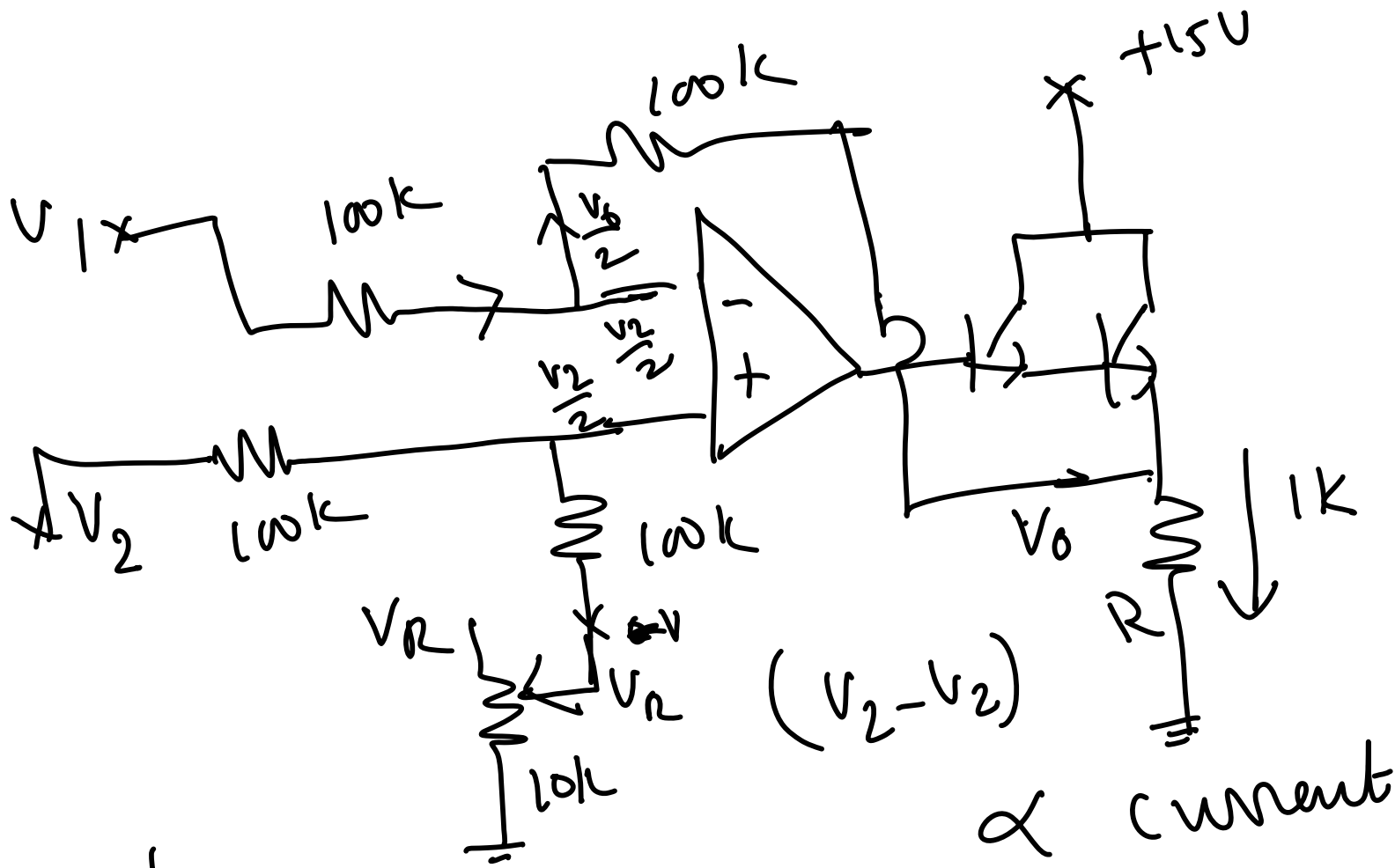
At 80°C ambient temp

$$V_1 = ? = 3.5 \text{ V}$$

$$V_2 = ? = 3.5$$







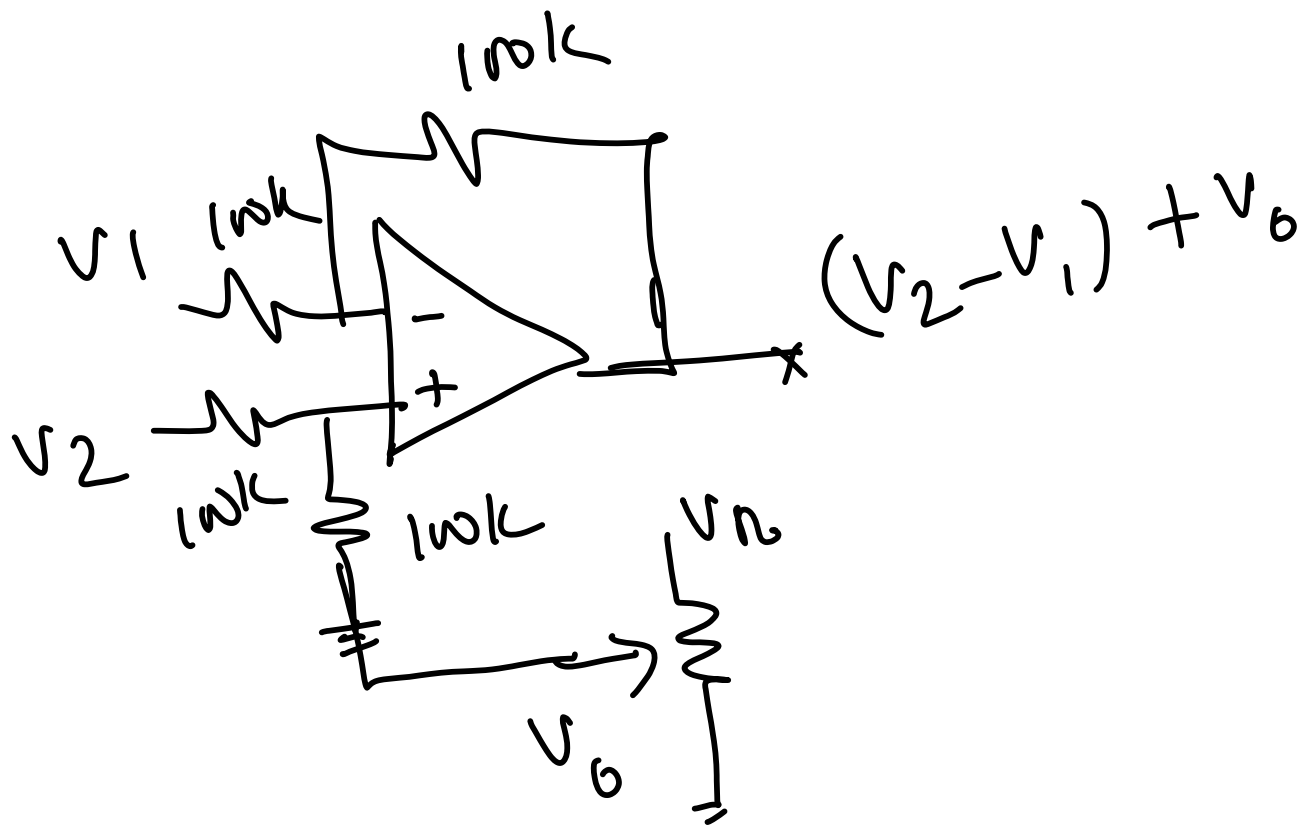
At inverting terminal

$$\frac{V_1}{2} + \frac{V_0}{2}$$

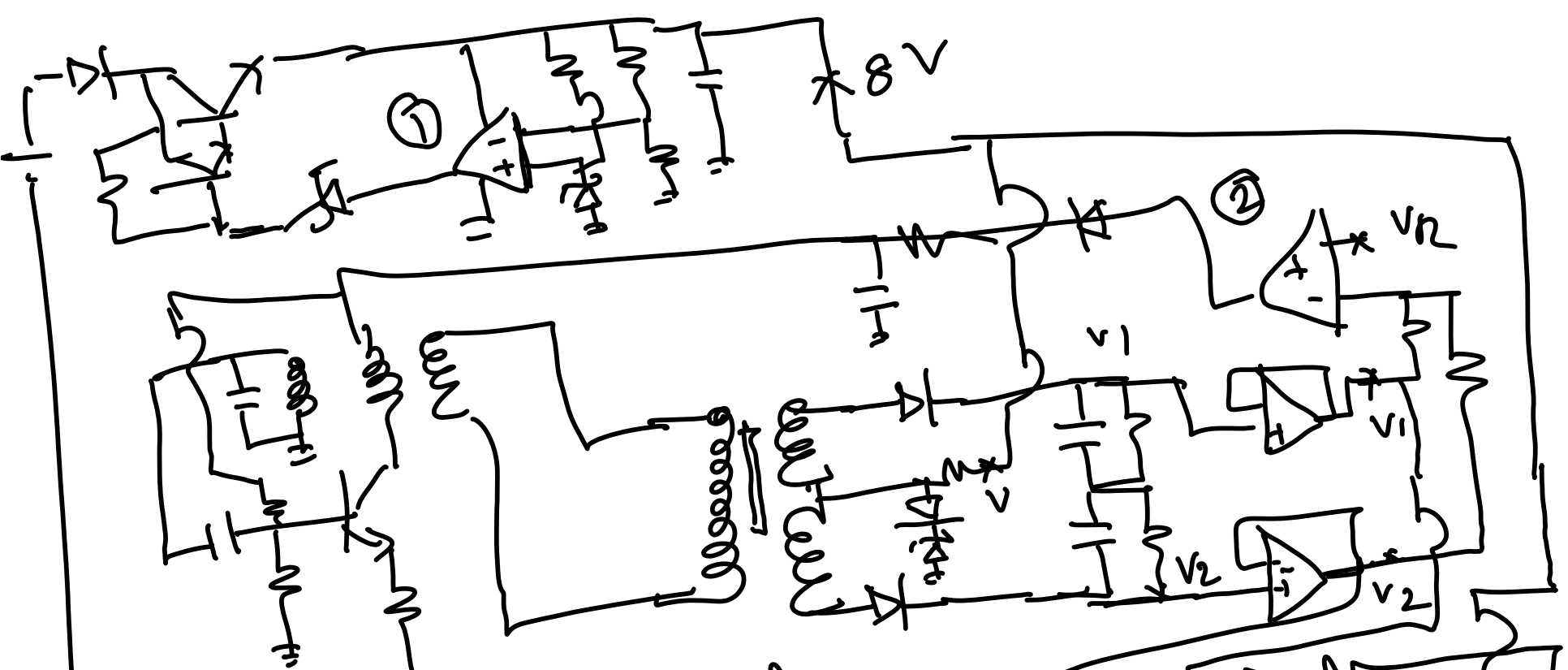
At + terminal = $\frac{V_2}{2} + \frac{V}{2}$

$$\frac{V_1}{2} + \frac{V_0}{2} = \frac{V_2}{2} + \frac{V}{2}$$

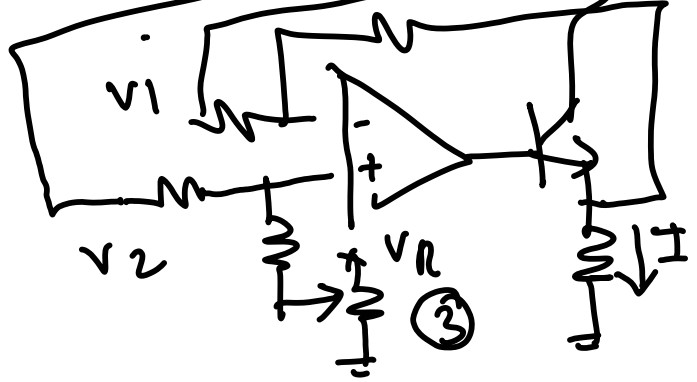
$$V_2 - V_1 = V_0 - V$$



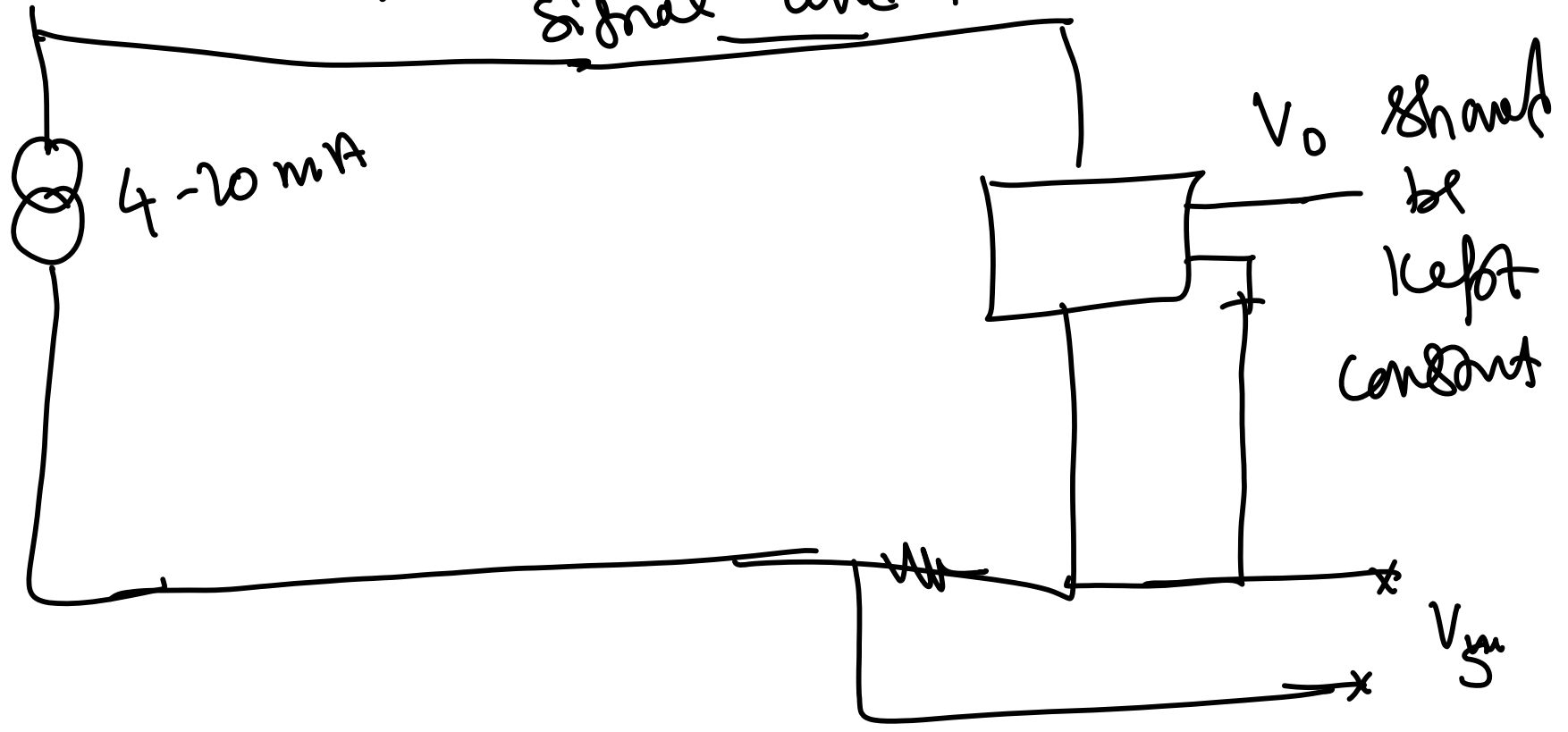
- ① LVDT excitation using sine wave
- ② Temperature compensation
- ③ $(V_1 - V_2)$ \propto displacement
- ④ $(V_1 - V_2)$ is converted into proportional current



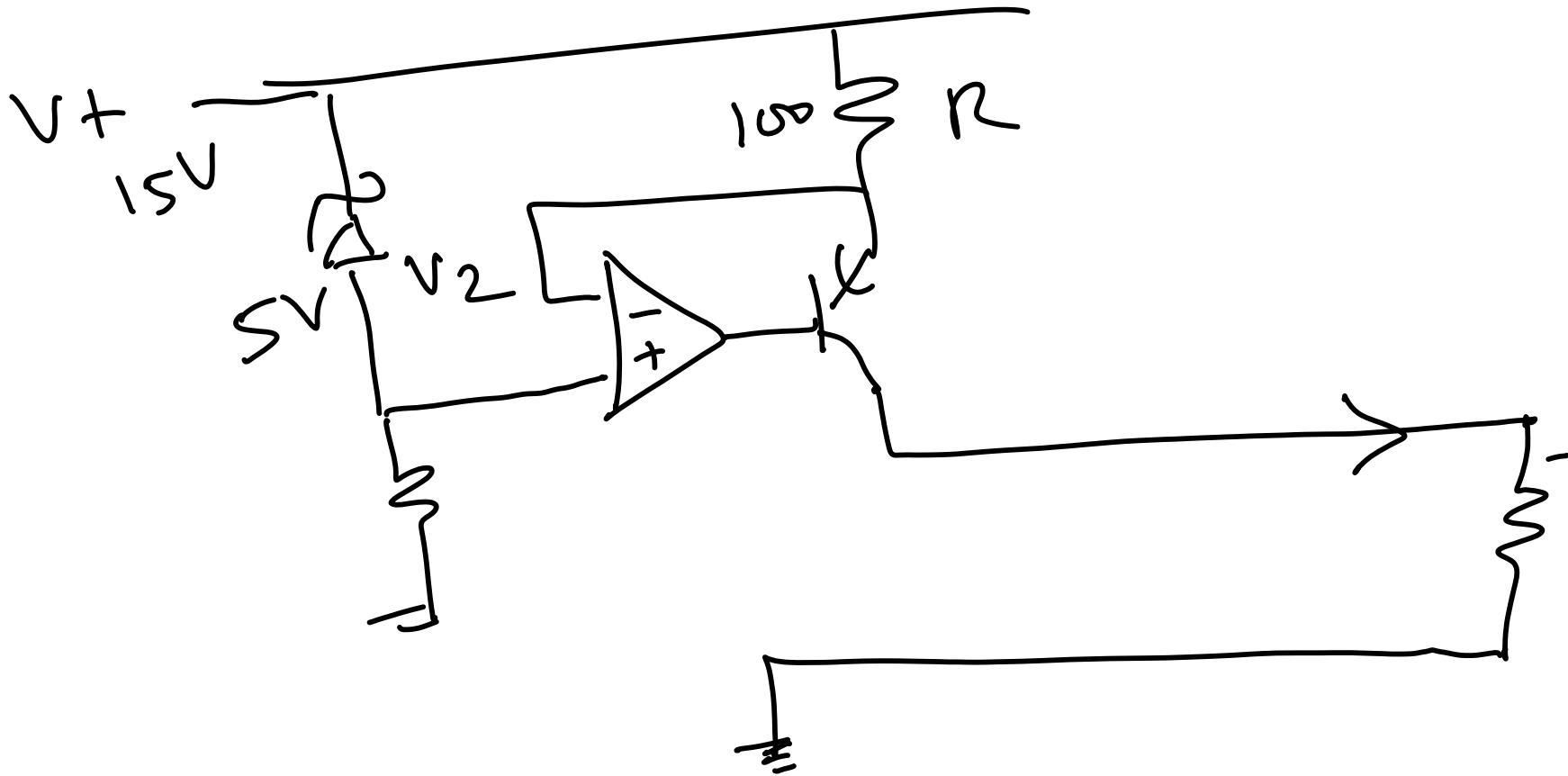
- ① op-amp ① → v_1 reg
- ② op-amp ② → $(v_1 + v_2)$ constant
- ③ op-amp ③ → $(v_1 - v_2) \propto I$

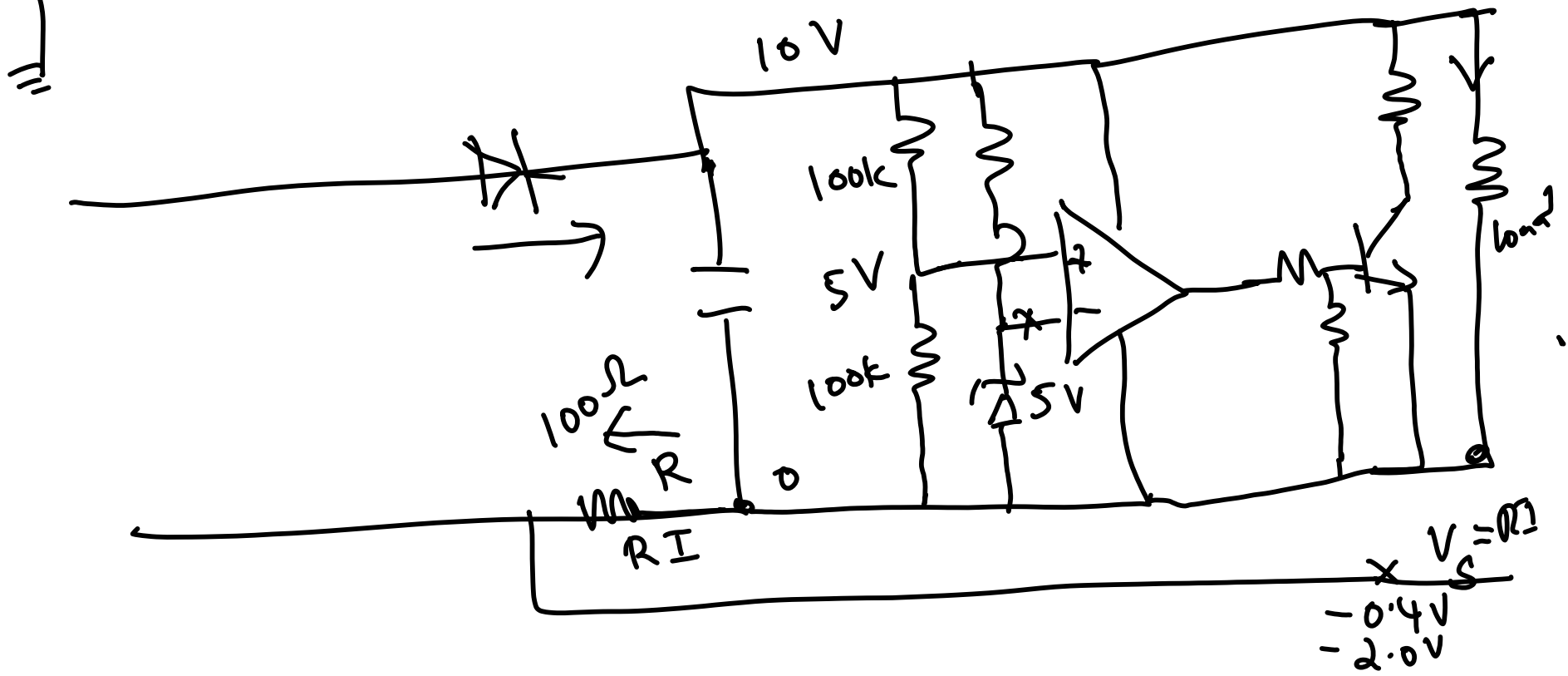
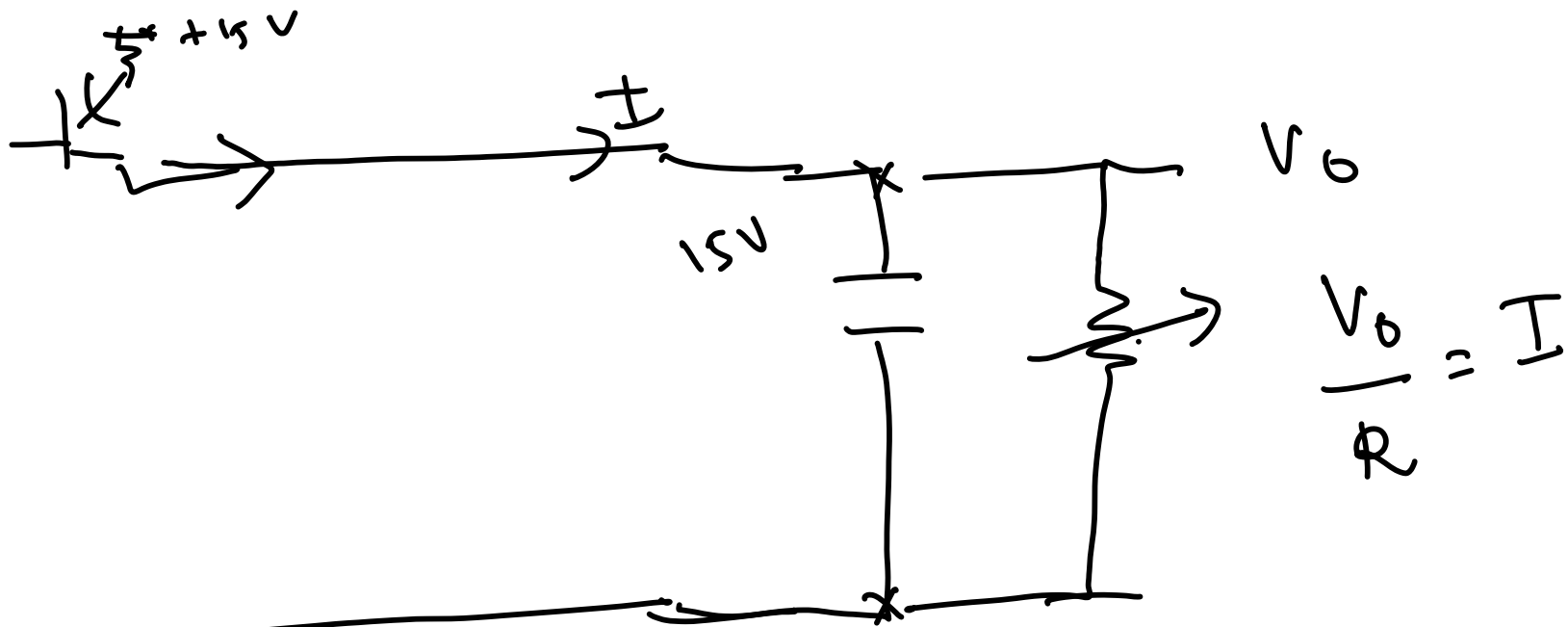


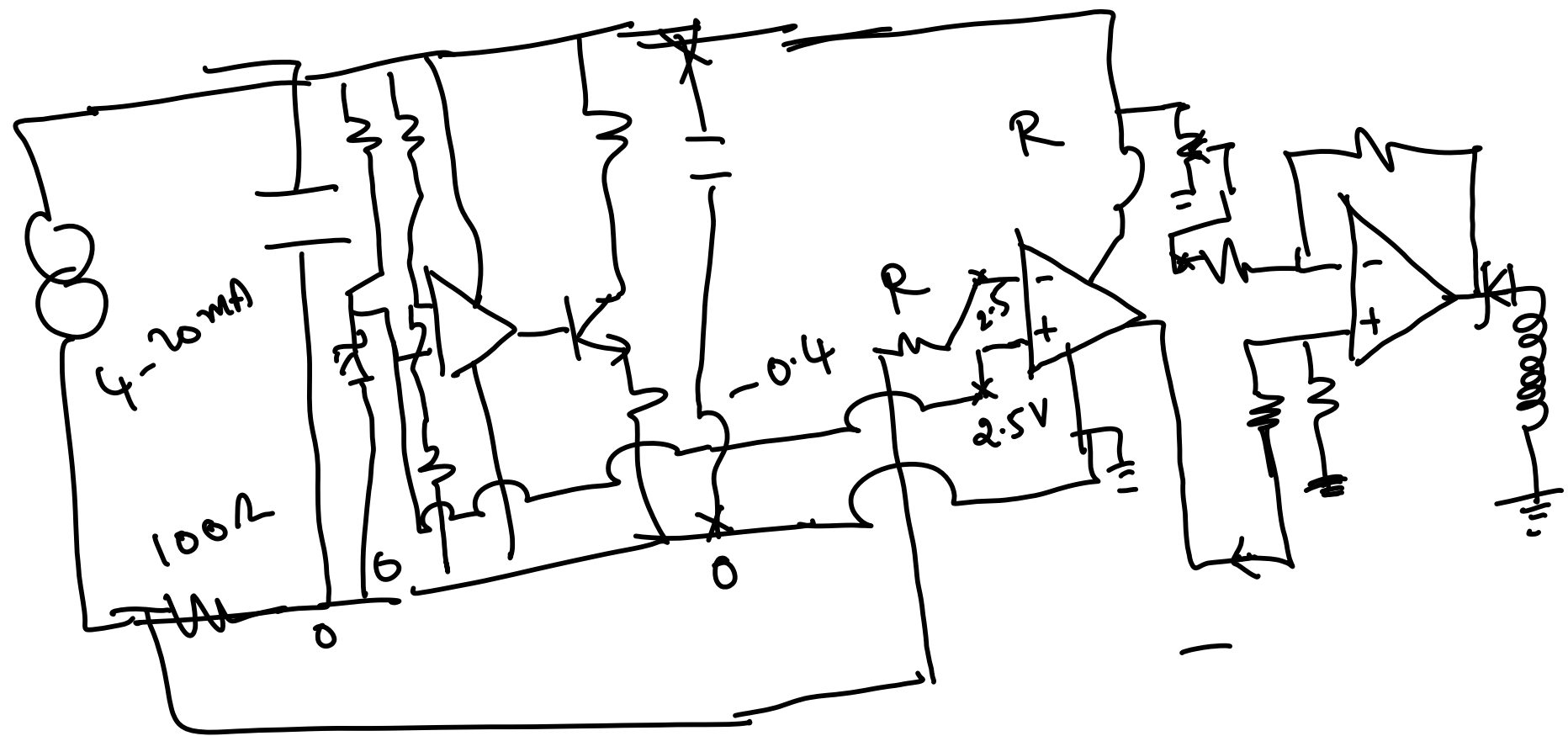
Splitting the current into
signal and power

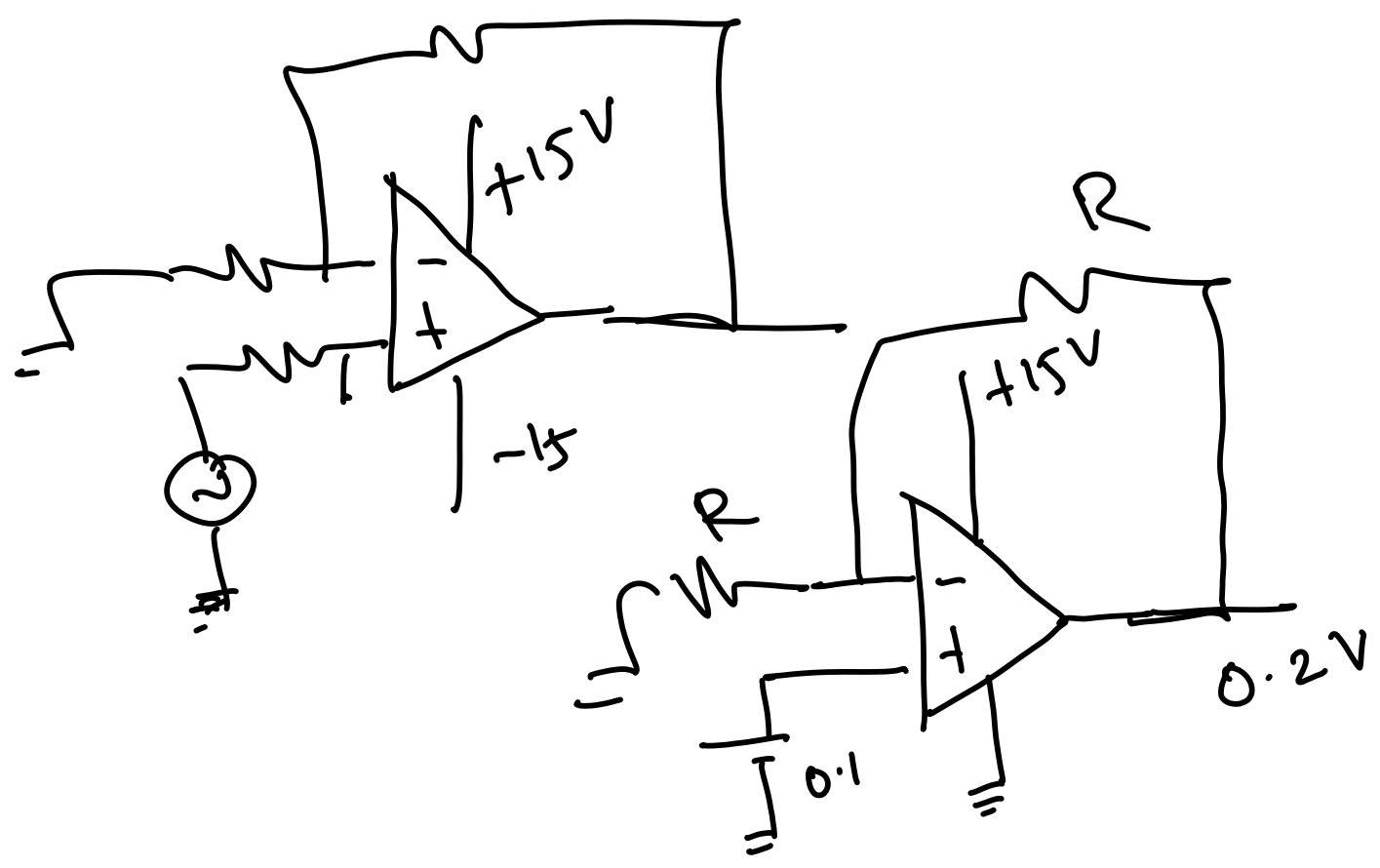


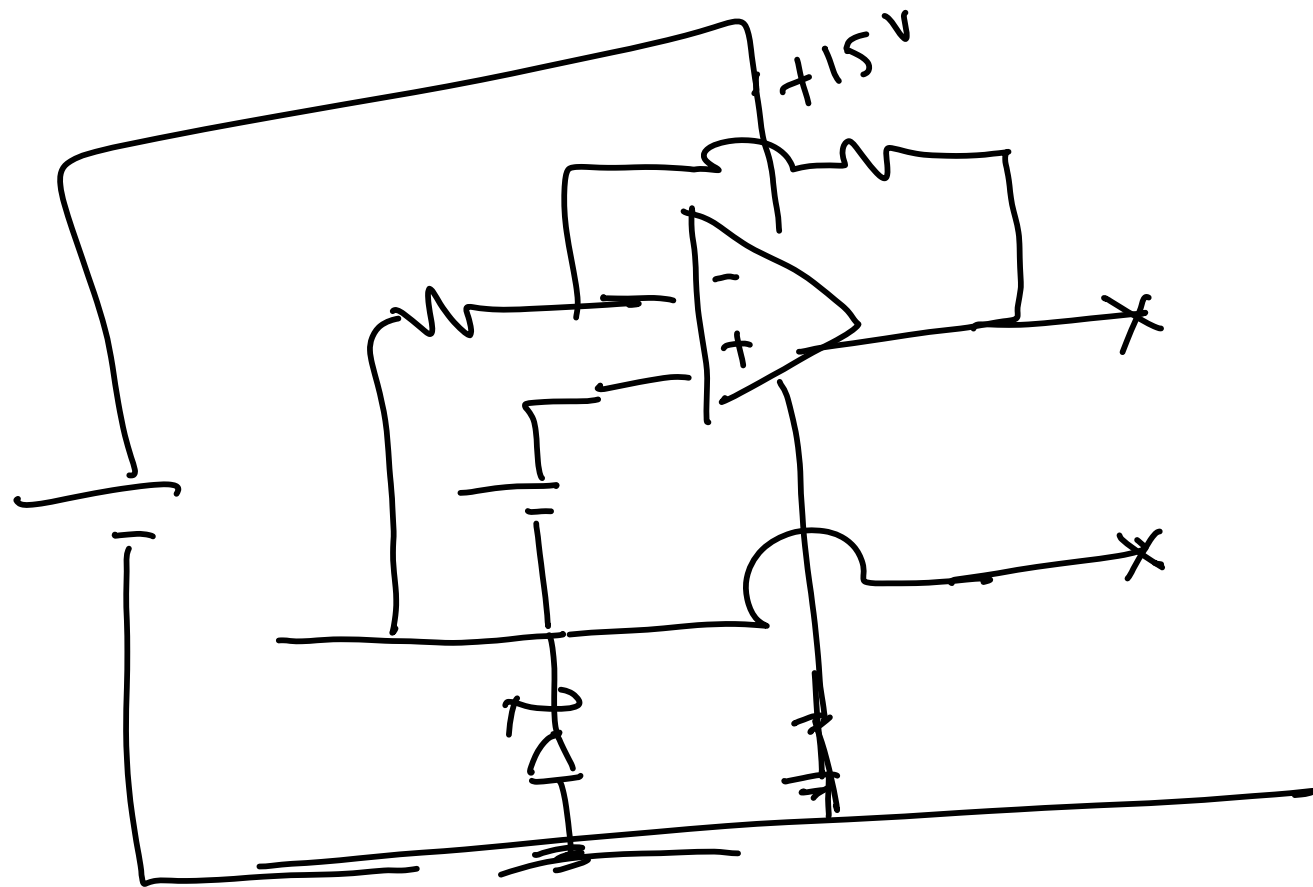
Constant current source



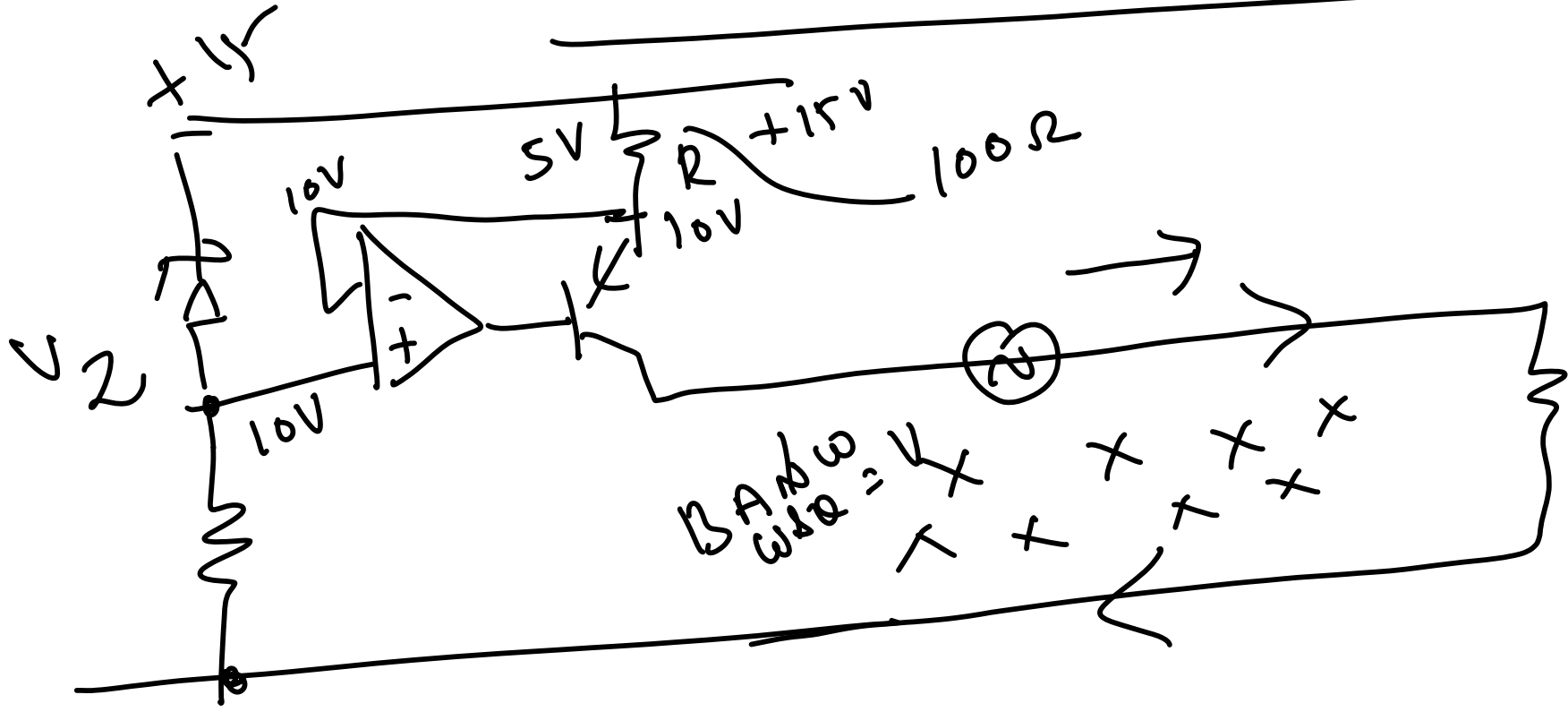


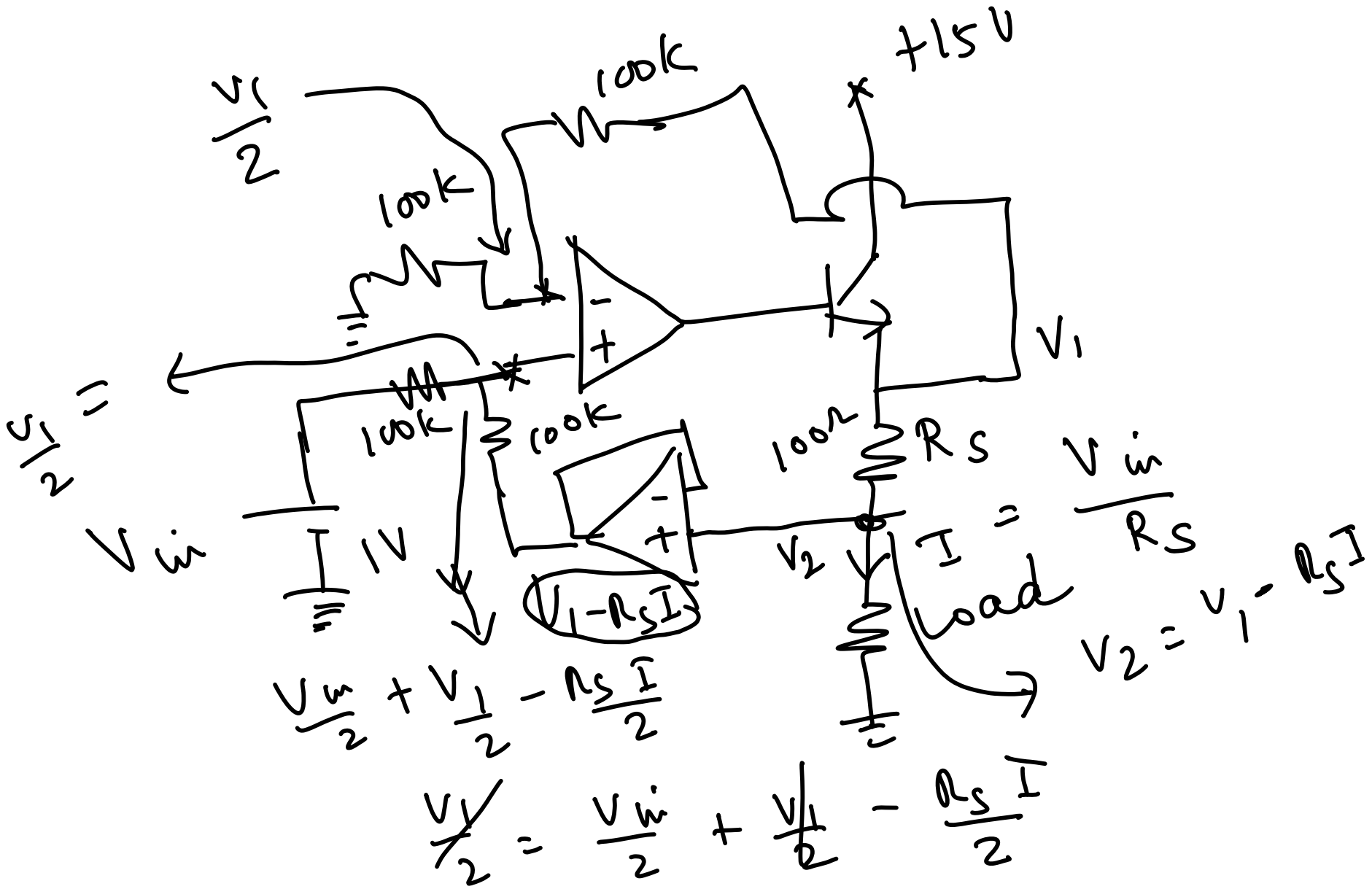






Constant current source

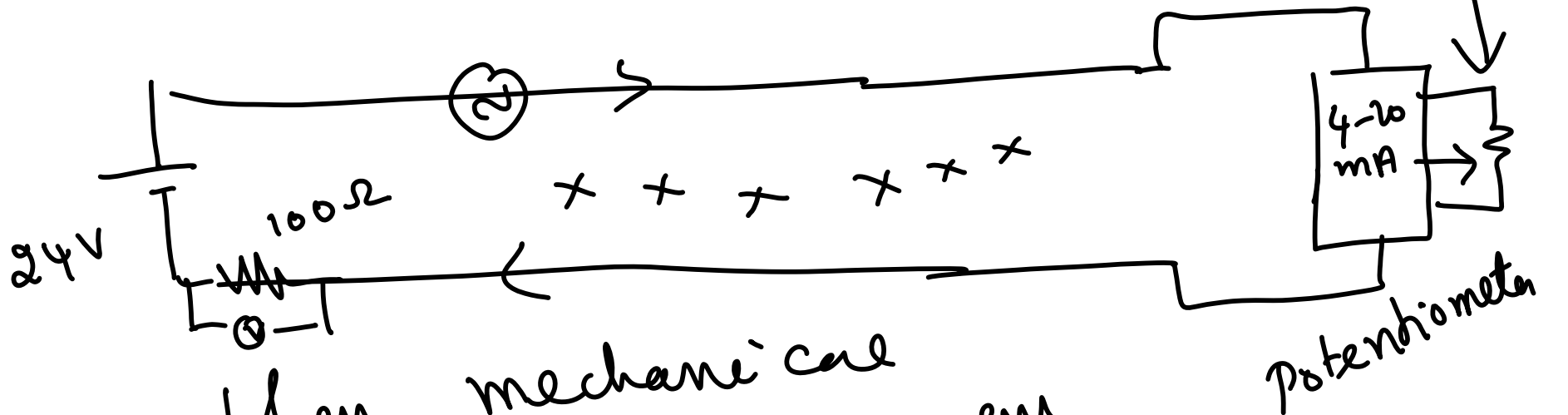




$$R_S I = V_{in}$$

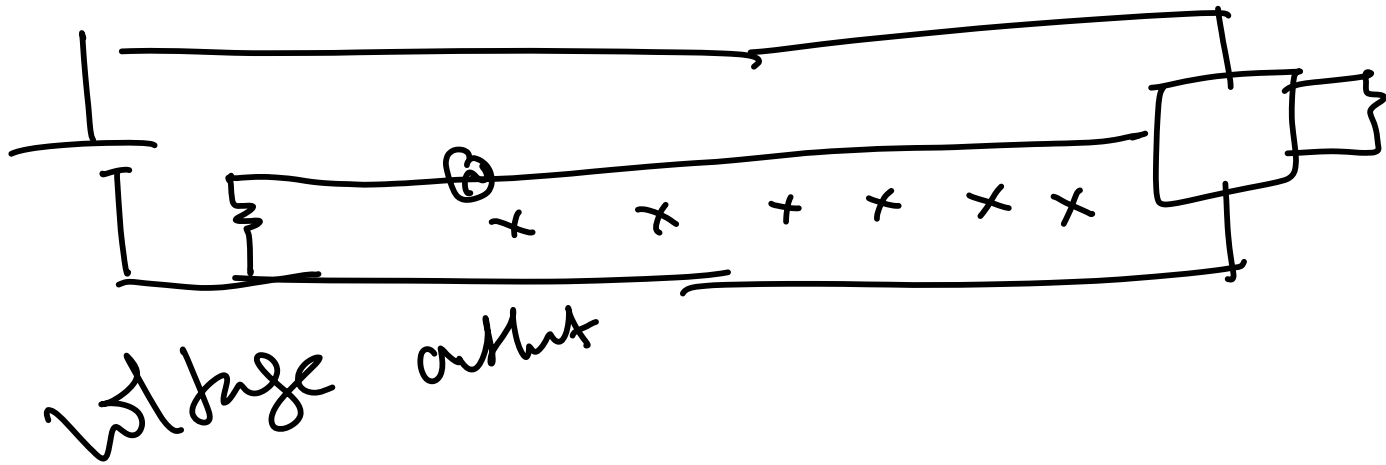
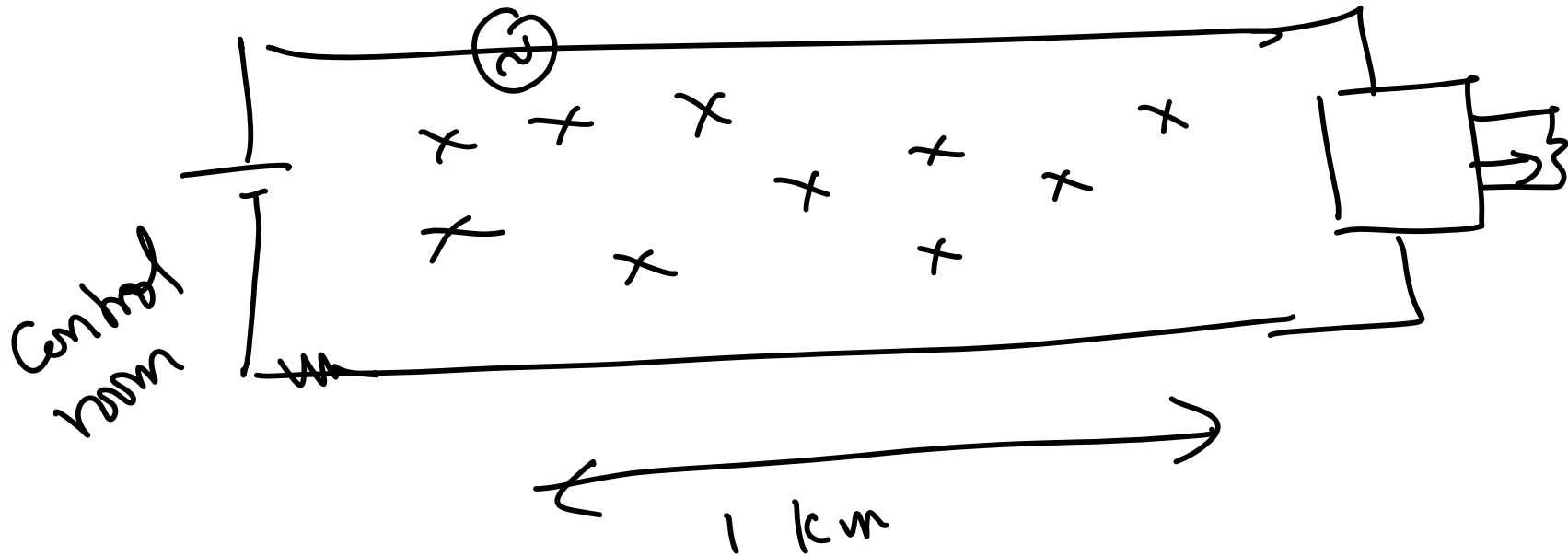
$$I = \frac{V_{in}}{R_S}$$

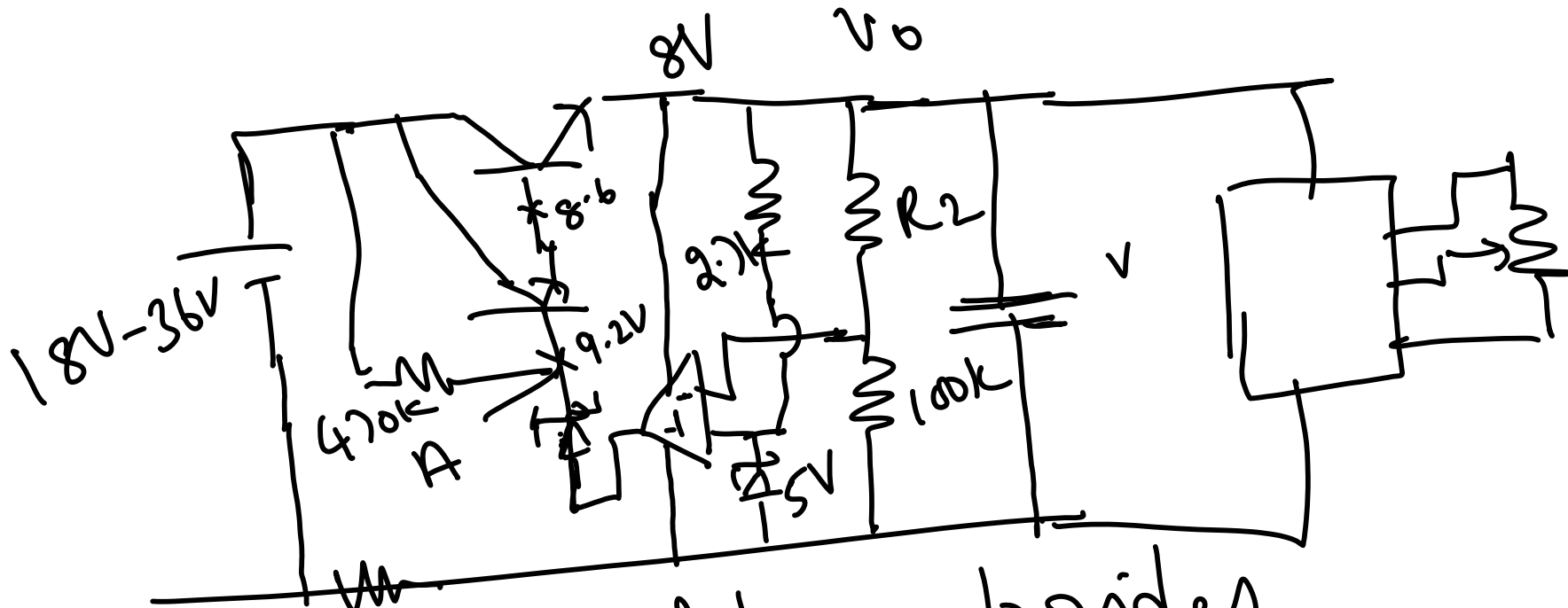
4 - 20 mA current transmitters



When mechanical system at zero end = 4 mA

- | | | |
|-----|--------|------------------------------------|
| 0% | → 4 mA | At the other end I should be 20 mA |
| 25% | → 8 mA | 50% = 12 mA |
| | | 75% = 16 mA |
| | | 100% = 20 mA |





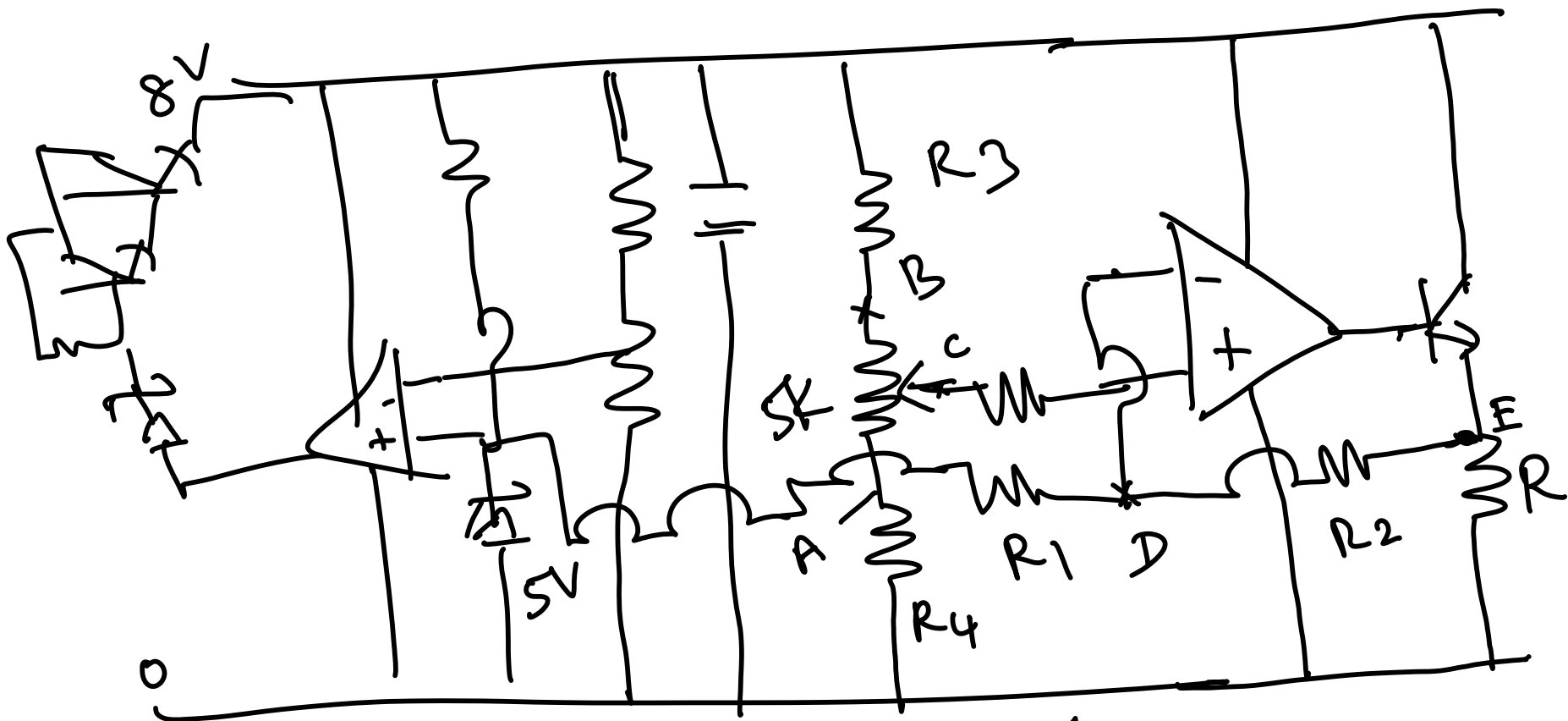
Zener voltage provides
 extra voltage i.e.
 V_{at A} = OP amp output
 + V_{acc the zener}
 V_{acc the zener} ≠ break down
 V_{of the}
 Zener

Wf acc $100k = 5V$

So output Wf = $\frac{5V \times (100k + x)}{100k}$

x can be ≈ 8 calculated

Design of a current
transmitter



Select R_4, R_3 , pot
 such that $v_A = 2V$
 $v_B = 4V$
 v_C acc the potentiometer
 becomes $2V$

The expected charge at $D = 2V$
= charge at C

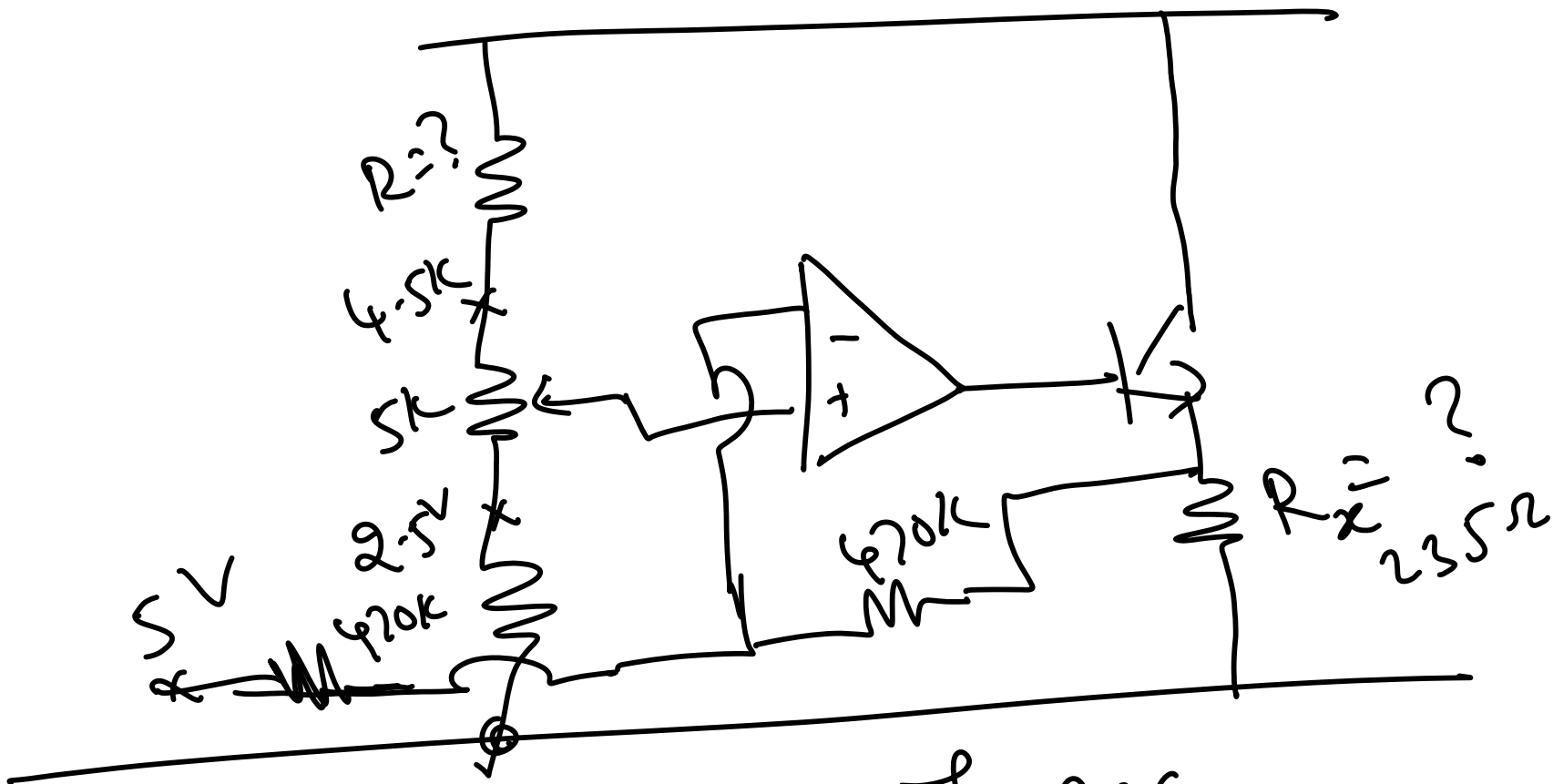
$$\Delta R_1 \approx R_2$$

Keep A at $2.5V$

Then $R_1 = R_2 = 470k$

B at $4.5V$

Po tenhio meta $wf = 2V$



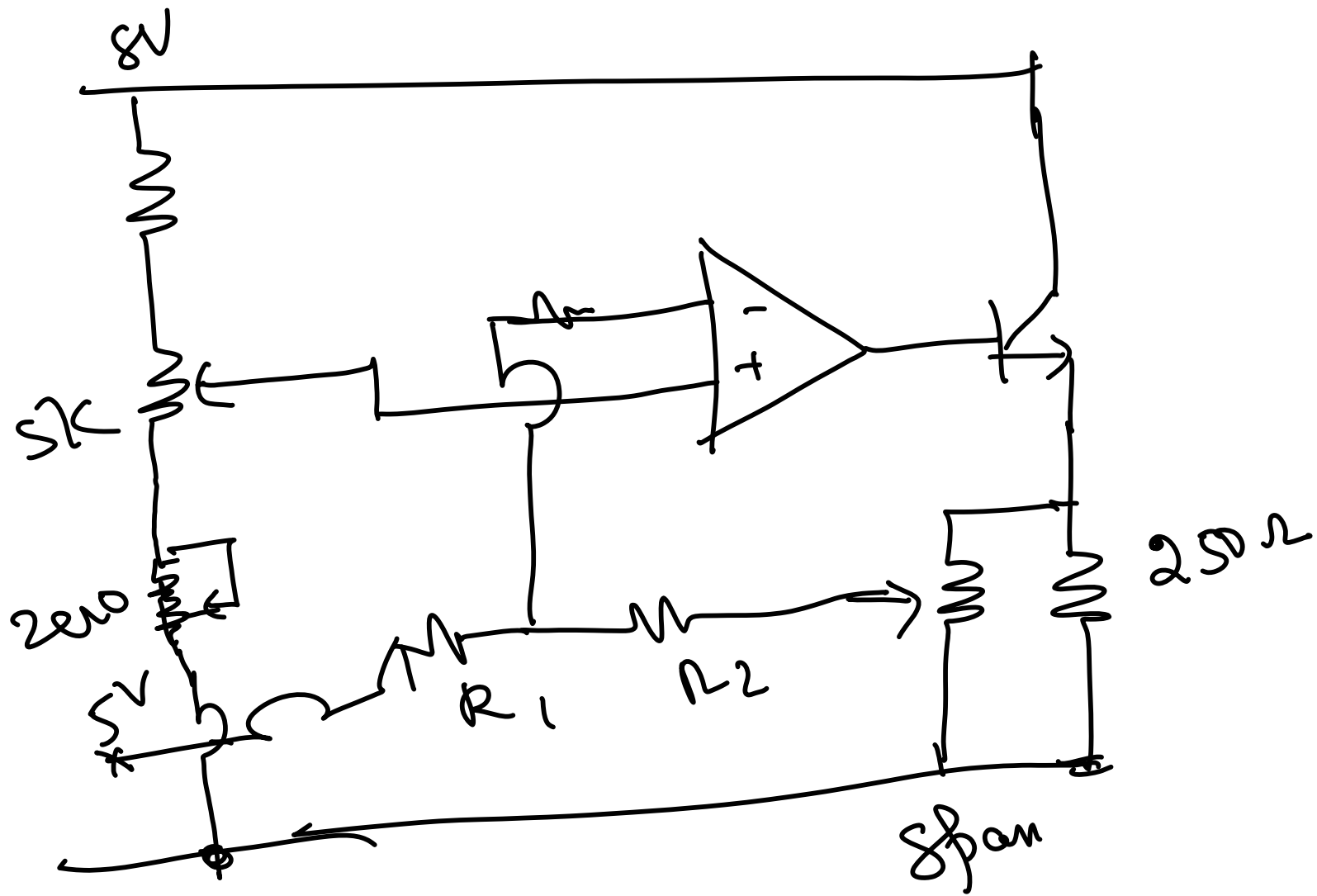
Required w/ acc
 $R_x = 4V$ at 17mA

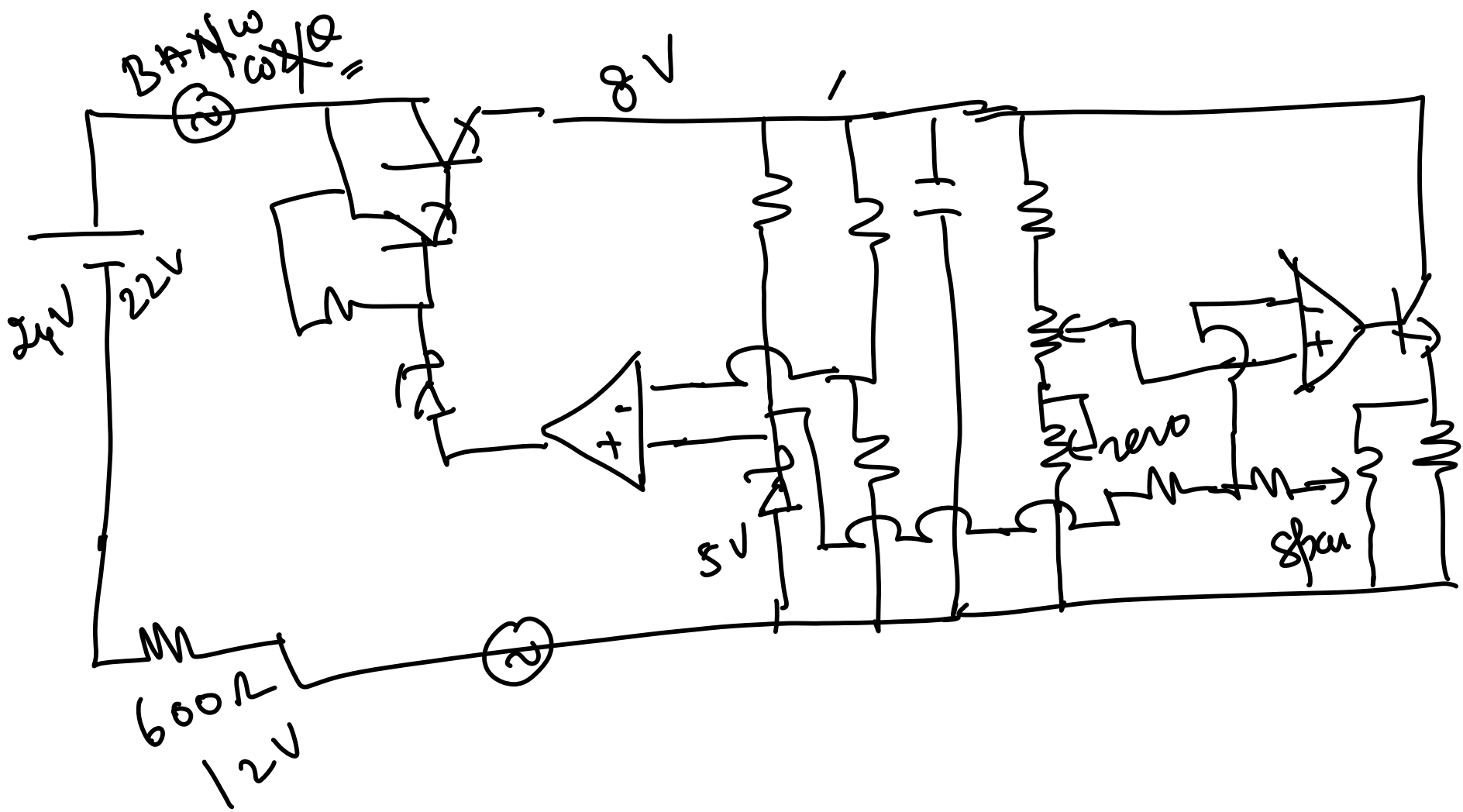
Required w/ acc
 $R_x \geq 0V$
 at 1mA or less

$$R_x \times 17 \text{ mA} = 4 \text{ V}$$

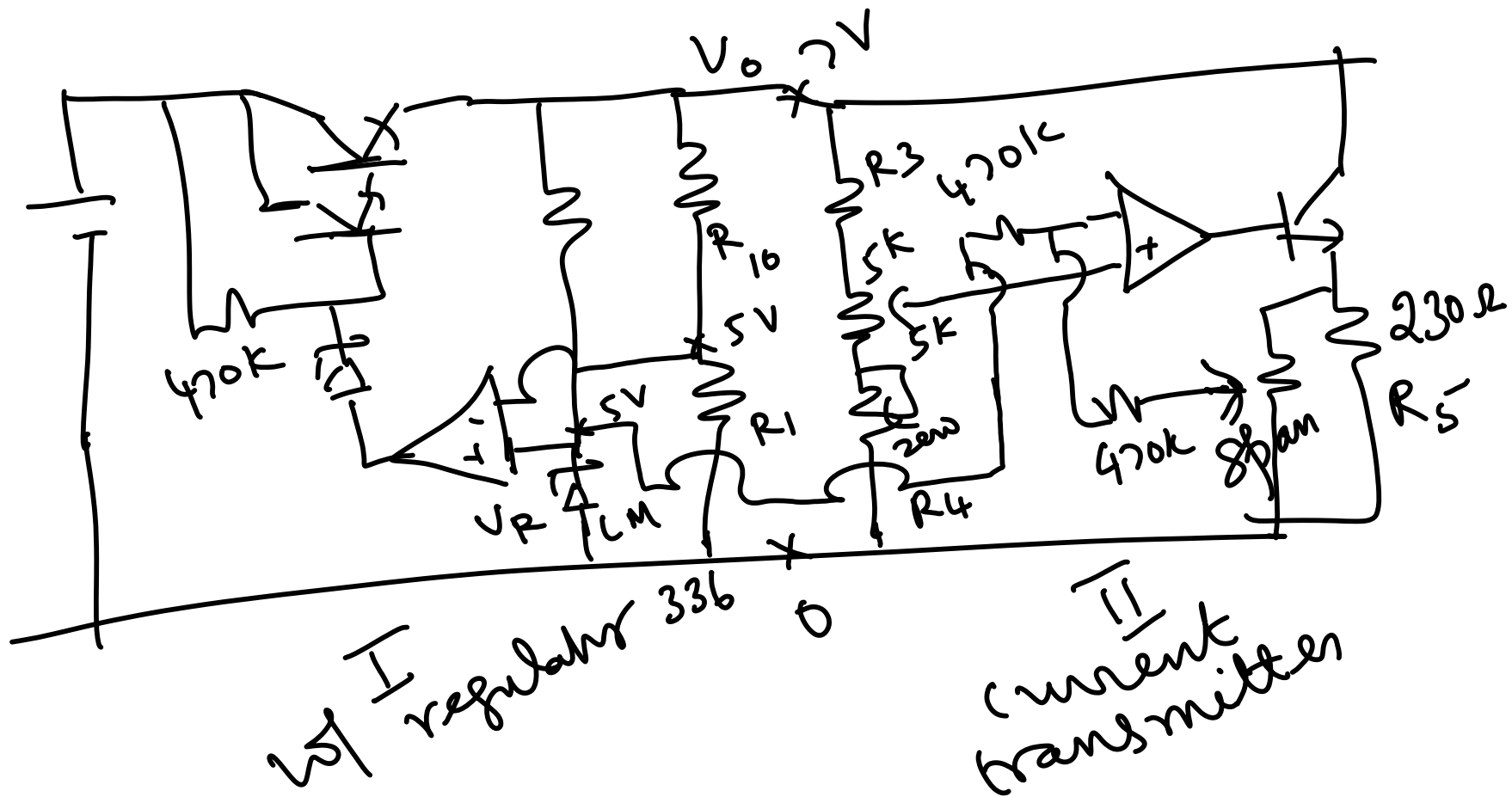
$$R_x = \frac{4 \text{ V}}{17} = \frac{4 \text{ mV}}{17} = \underline{\underline{235 \Omega}}$$

60





Error budgeting for 4-20mA current transmitter



LM336 Zener 5V 30PPM/C

Drift = 30 PPM/C
Assuming ambient Temp
change = 100°C

Vol of the Zener initially be
= 5V

ΔV of the Zener

V × PPM × ΔC

$$= \frac{5 \times 30 \times 100}{10^6}$$

$$\Delta V = \frac{15 \times 10^3}{10^6}$$

$$= 15 \times 10^{-3} \text{ V}$$
$$= \pm 15 \text{ mV}$$

Δv of the zener = $\pm 15 \text{ mV}$

S_o regulated output voltage

$$\text{change} = \frac{15 \text{ mV} \times (R_1 + R_{10})}{R_1}$$

$$7 \text{ V} = 5 \times \frac{(R_1 + R_{10})}{R_1}$$

$$\frac{7 \text{ V}}{5 \text{ V}} = \frac{(R_1 + R_{10})}{R_1}$$

$$\Delta v_o = 15 \times 10^{-3} \times \frac{7}{5} = 21 \text{ mV}$$

$$\text{W/ acc } R_3 = R_4 = 2.5 \text{ V}$$

For 5k the w/p
drop = 2V

$$\text{So } R_3 = \frac{5k \times 2.5}{2} = \frac{12.5}{2} = 6.25k$$

$$R_3 = R_4 = 6.25k$$

w/p at the potentiometer

$$\text{top end} = 2.5 + 2.0 = 4.5V$$

(This corresponds to current of
20 mA)

For ΔV_o of 21 mV the corresponding
voltage change at the top

end of the potentiometer

$$= \frac{21 \times 4.5}{7.0} \text{ mV}$$

$$= 3 \times 4.5 \text{ mV} = \underline{13.5 \text{ mV}}$$

Assuming the span pot
at the top end the w/ ΔV
change at, at inverting
input = 13.5 mV = w/ change
at the non-inverting input

ie at -ve input $\Delta V = 13.5 \text{ mV}$
So w/ change acc RS
 $= 2 \times 13.5 = 27 \text{ mV}$

w/ change acc R_5

$$\approx 27 \text{ mV}$$

$$\text{So current change} = \frac{27 \times \text{mV}}{230}$$

$$= \frac{27}{230} = \pm 0.08 \text{ mA}$$

II
calculate the current
drift due to R_1 ; R_{10} change

$$R_1 = 100 \text{ k}$$

$$R_{10} = \frac{5 \times (R_1 + R_{10})}{R_1} = 7 \text{ V}$$

$$= \frac{5 (10^5 + R_{10})}{10^5} = 7 \text{ V}$$

$$7 = \frac{5 \times (10^5 + R_{10})}{10^5}$$

$$7 \times 10^5 = 5 \times 10^5 + 5 \times R_{10}$$

$$\frac{2 \times 10^5}{5} = R_{10}$$

$$R_{10} = \frac{200 \times 10^3}{5} = 40 \text{ k}$$

Assume R_1, R_{10} drifts by 50 ppm/°C

Assume R_1 is decreasing and R_{10} is increasing with temp

$$\Delta R_1 \text{ change} = - \frac{100 \times 10^3 \times 50 \times 100}{10^6}$$

$$= \frac{5 \times 10^8}{10^6} = -500 \Omega$$

$$\Delta R_{10} = \frac{40 \times 10^3 \times 50 \times 100}{10^6}$$

$$= 20 \times \frac{10^7}{10^6} = 200 \Omega$$

R_1 decreases by 500Ω

R_{10} increases by 200Ω

So change in regulated
voltage = $\frac{5V (R_1 + R_{10})}{R_1}$

$$\text{New } V_0 = \frac{5 (100 \times 10^3 - 500 + 40200)}{99500}$$

$$= 5 \frac{(99500 + 40200)}{99500} \quad \begin{array}{r} 99500 \\ 40200 \\ \hline 139700 \end{array}$$

$$= 5 \times \frac{139700}{99500} = \frac{1397}{995} \times 5 = \frac{1397}{199}$$

$$\text{New } V_0 = \frac{1397}{199} \approx \frac{1397}{200} = \underline{\underline{6.985 \text{ V}}}$$

$$\begin{aligned} \text{Change in } V_0 &= 7 - 6.985 \\ &= 15 \text{ mV} \end{aligned}$$

So the expected
current change in
 $20 \text{ mA} = 0.08 \text{ mA}$

III
Error due to V_{offset} of
Wt regulator stage

Let $V_{\text{offset}} = 15 \mu\text{V}/\text{C}$

For 100 C total offset voltage

$$\text{Change} = 15 \times 100 = 1.5 \text{ mV}$$

For 1.5 mV at the input of
the regulator of amp the
expected change at the output
of the regulator $= 1.5 \times \frac{7}{5} \text{ mV}$
 $= 2.1 \text{ mV}$

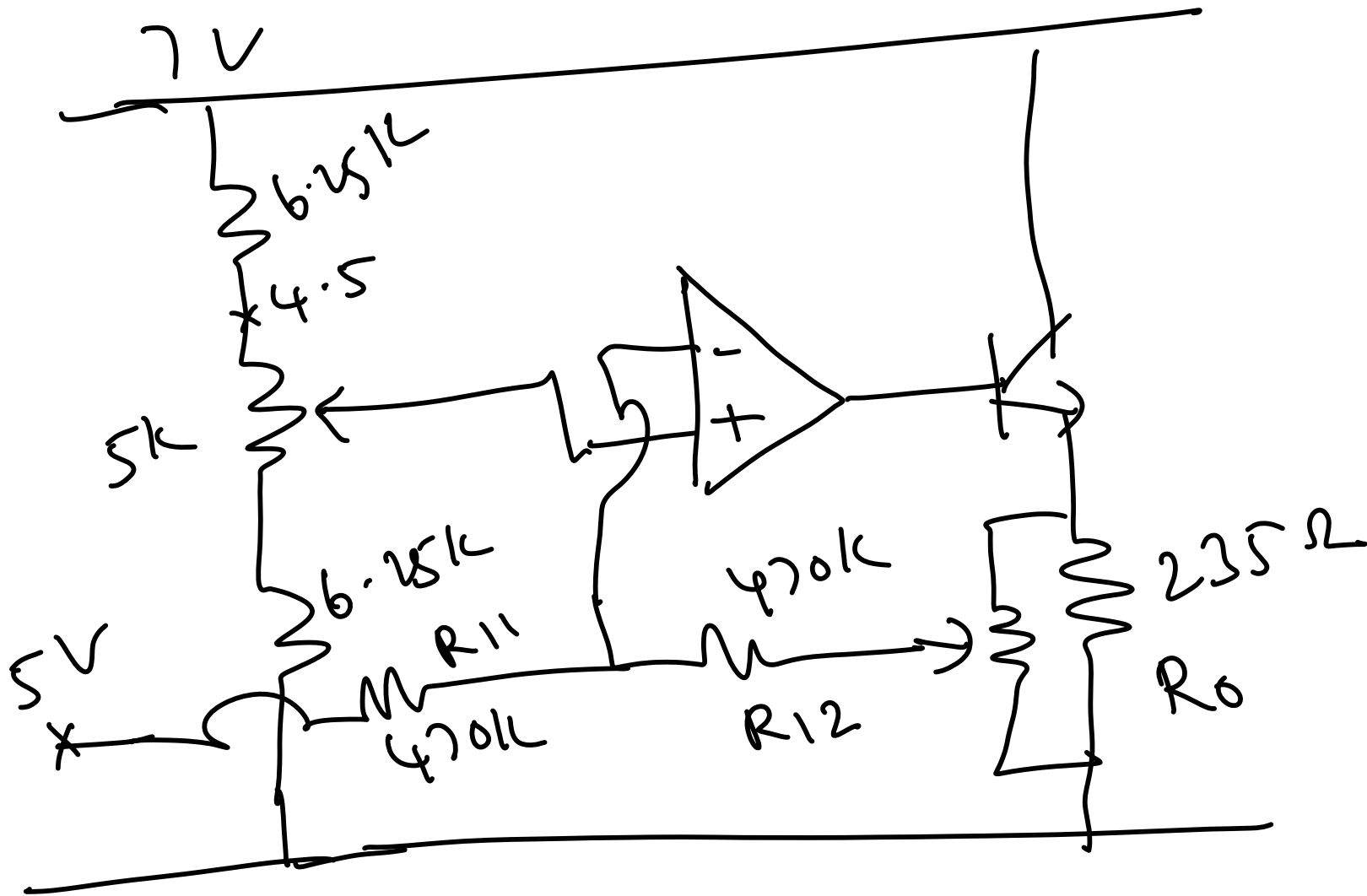
So current change in
the 20mA output

$$= \frac{0.08 \times 2.1}{15}$$

$$= \frac{0.16}{15} = 0.01 \text{ mA}$$

Error in the Current Converter

Stage



① Error due to offset
voltage drift of current
converter of amp

$$V_{\text{offset}} = 15 \mu\text{V} \cdot \text{C}$$

Total offset voltage

$$\text{Change} = \pm 1.5 \text{ mV} \\ (15 \mu\text{V} \times 100)$$

So the expected change in

the non-inverting input = 1.5 mV
= Expected change

in the inverting input = 1.5 mV

So the expected change

$$\text{across } R_0 = \frac{1.5 \times 470 + 470k}{470}$$

$$= 3 \text{ mV}$$

So the expected current change

$$\text{in } 20 \text{ mA} = \frac{3 \times 10^{-3}}{230} = \frac{3000}{230} \mu\text{A} = 12 \mu\text{A}$$

②

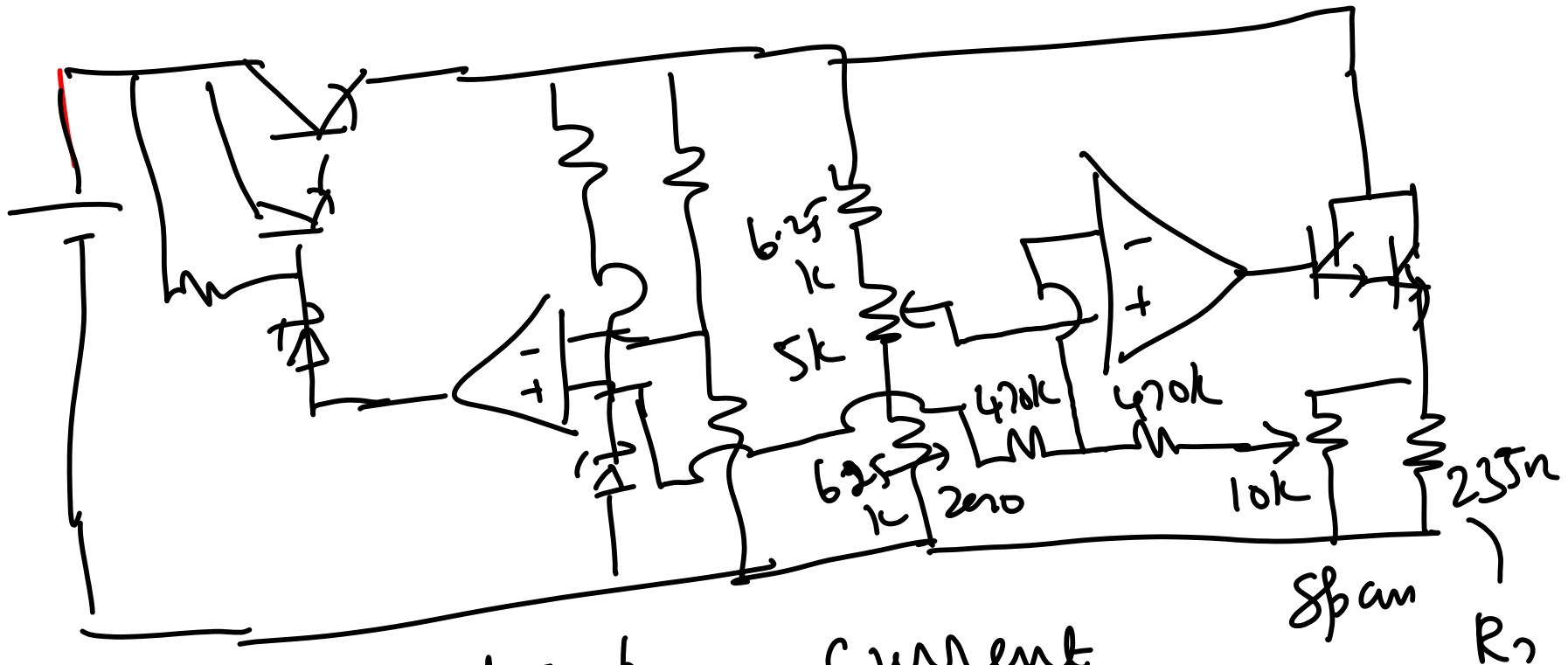
change in current
due to zero w/ change

③

change in current
due to R_{11} , R_{12} change

④

change in current due to
 235Ω resistance change



Calculate the current drift due to drift in R_7

Let the TC of

$$R_7 = 50 \text{ PPM}/^\circ\text{C}$$

For $\Delta T = 10^\circ\text{C}$

$$DR = \frac{235 \times 50 \times 100}{10^6}$$

$$= 235 \times 5 \times 10^{-3}$$

$$= 1.175 \Omega$$

Assuming 16 mA current in R_7

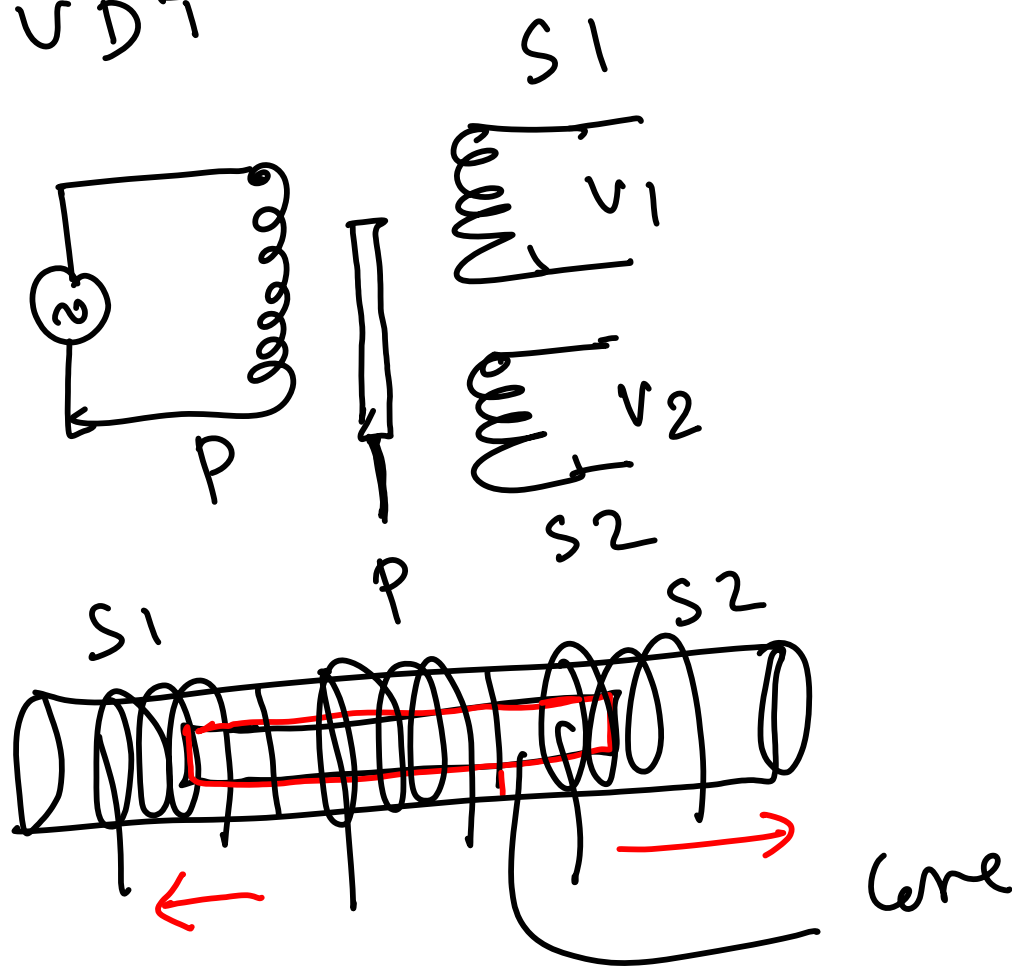
Then for 1.175Ω change the

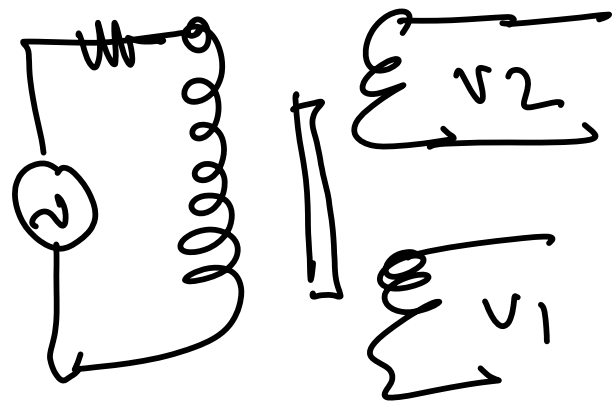
expected current change

$$= \frac{16 \times 1.1}{235} = \frac{17.6}{235} \text{ mA}$$
$$= \frac{1}{15} \text{ mA} = 0.06 \text{ mA}$$

Design of LVDT based position transmitter

① LVDT





$$|V_2| - |V_1| = \text{displace}$$

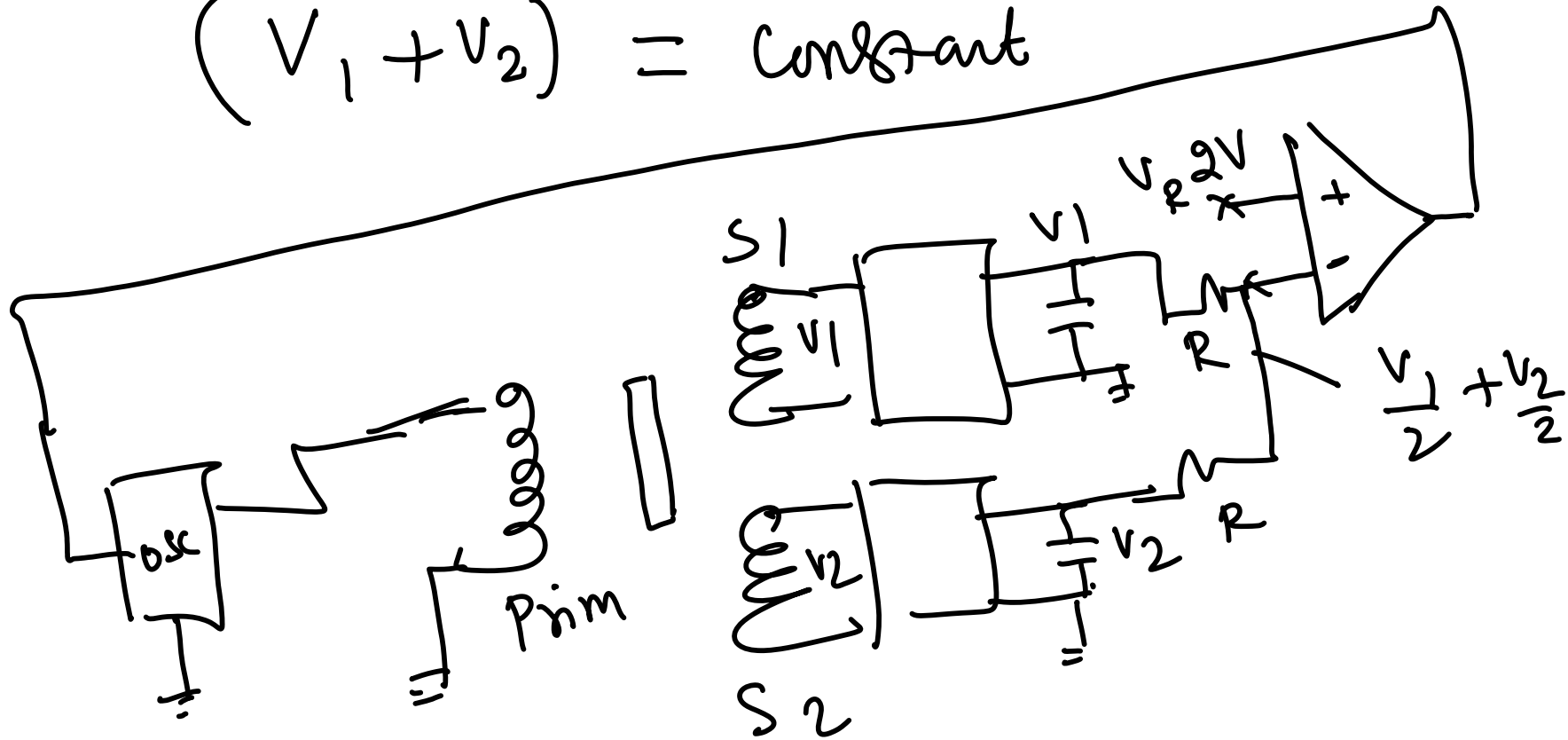
① Convert V_1 and V_2 into DC

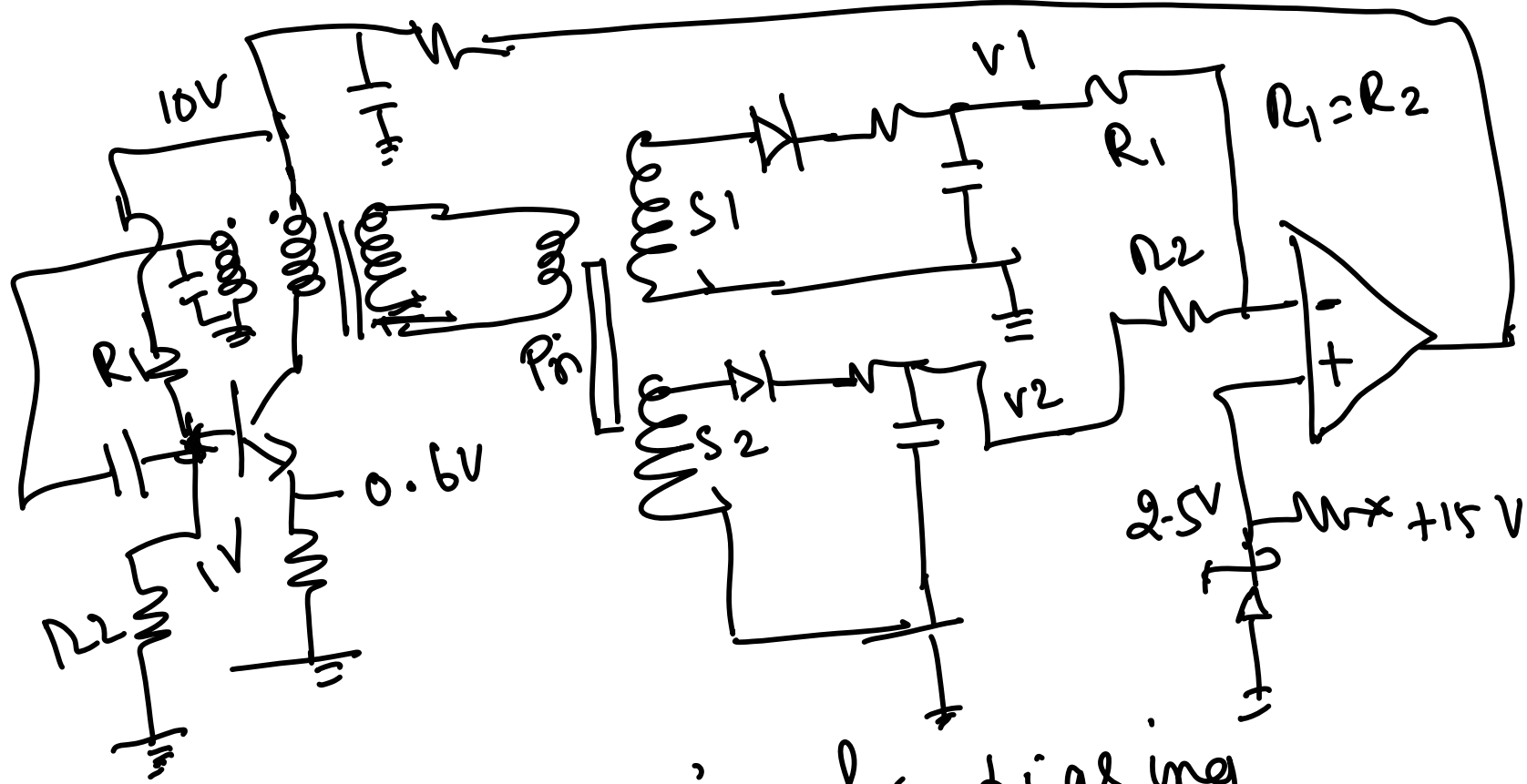
This dc w/ difference alone give you the displacement

② $|V_2 - V_1|$ changes with temp

How to make $(V_2 - V_1)$ independent of Temp?

$$(V_1 + V_2) = \text{constant}$$





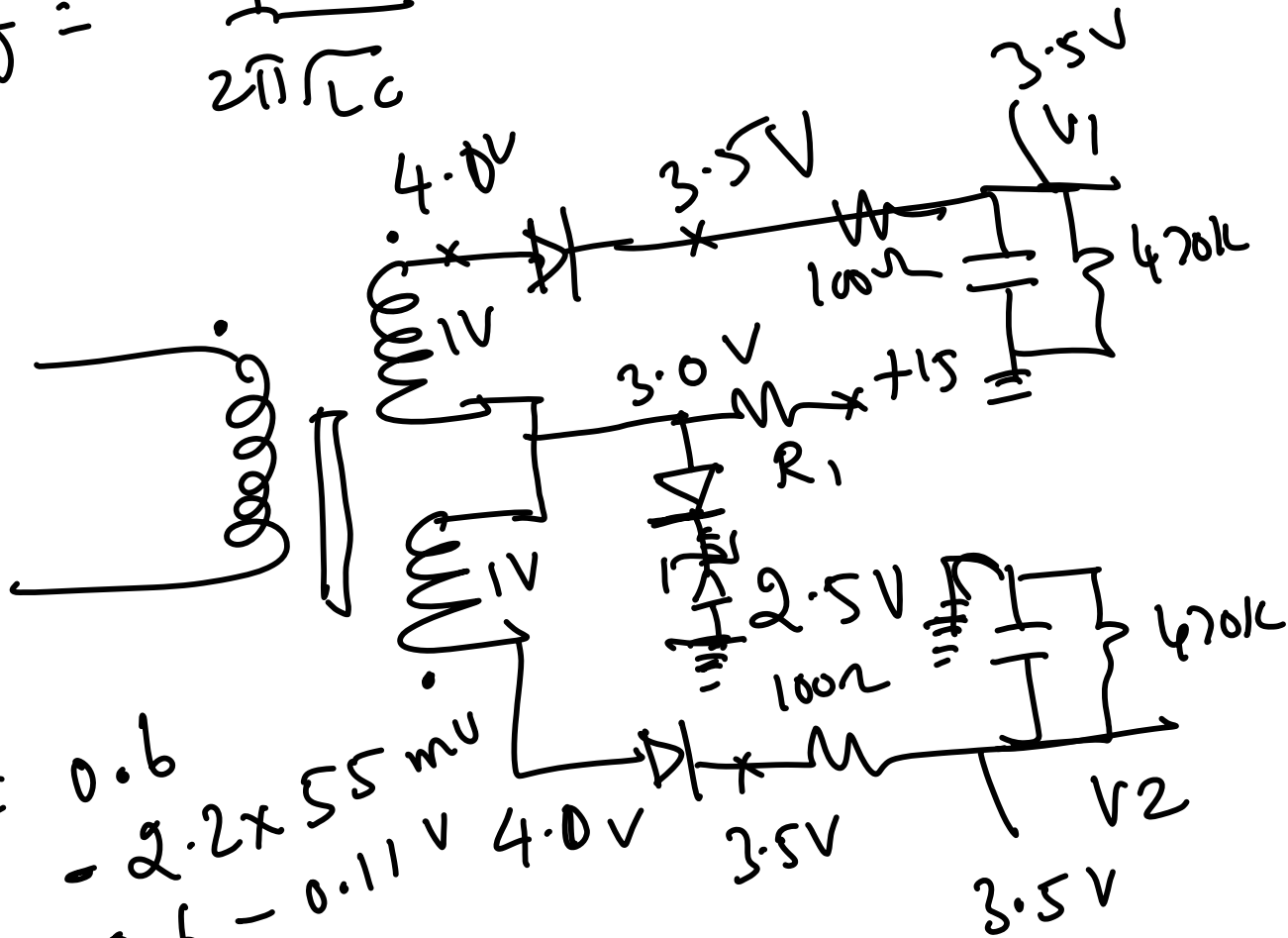
- R_1, R_2 is for biasing
- ① The emitter current increases
 - ② This produces increased mag field in the coil

③ This increases base vol of the transistor

④ This increase in base vol again increases the emitter current.

⑤ Again mag field increases in the primary

$$f = \frac{1}{2\pi RC}$$



Wol acc
he did

$$= 0.6$$

$$= 2.2 \times 55 \mu\text{V}$$

$$= 0.6 - 0.11 \text{ V}$$

$$= 0.49 \text{ V}$$

At room temp

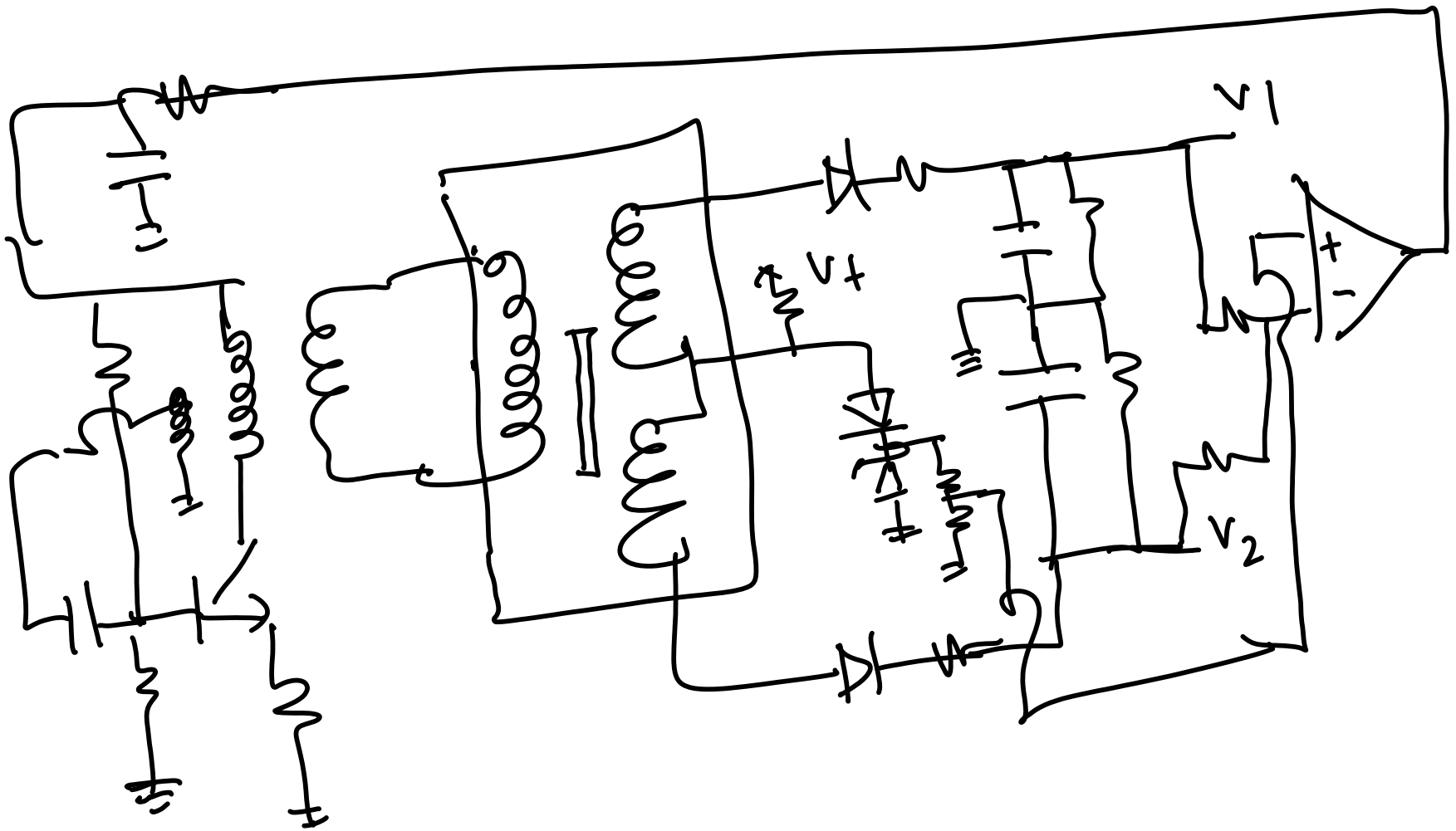
$$V_1 = 3.5 \text{ V}$$

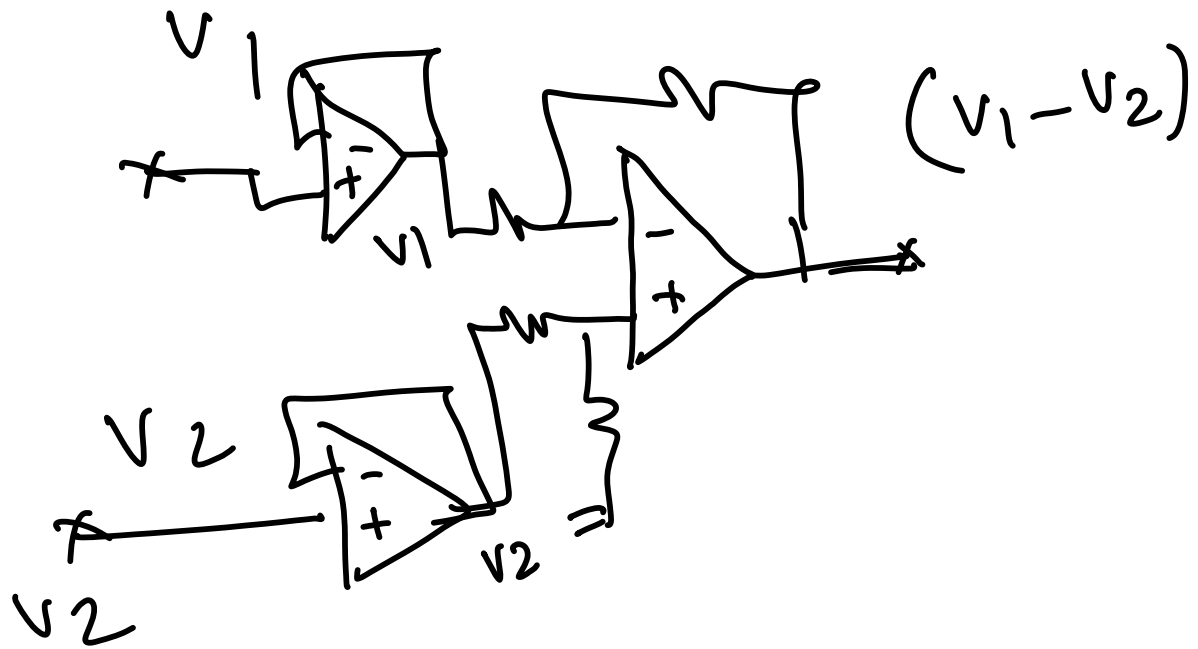
$$V_2 = 3.5 \text{ V}$$

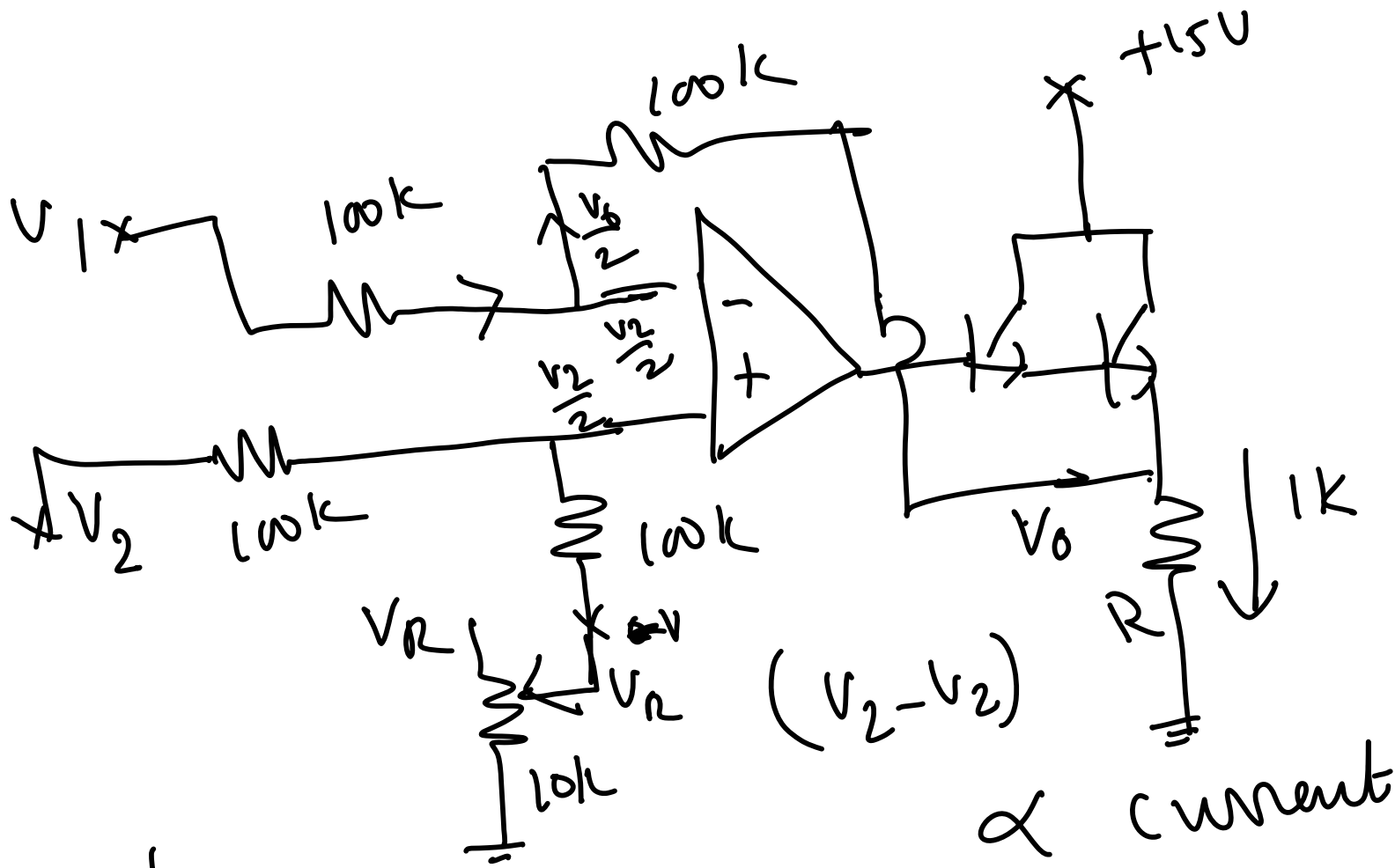
At 80°C ambient temp

$$V_1 = ? = 3.5 \text{ V}$$

$$V_2 = ? = 3.5$$

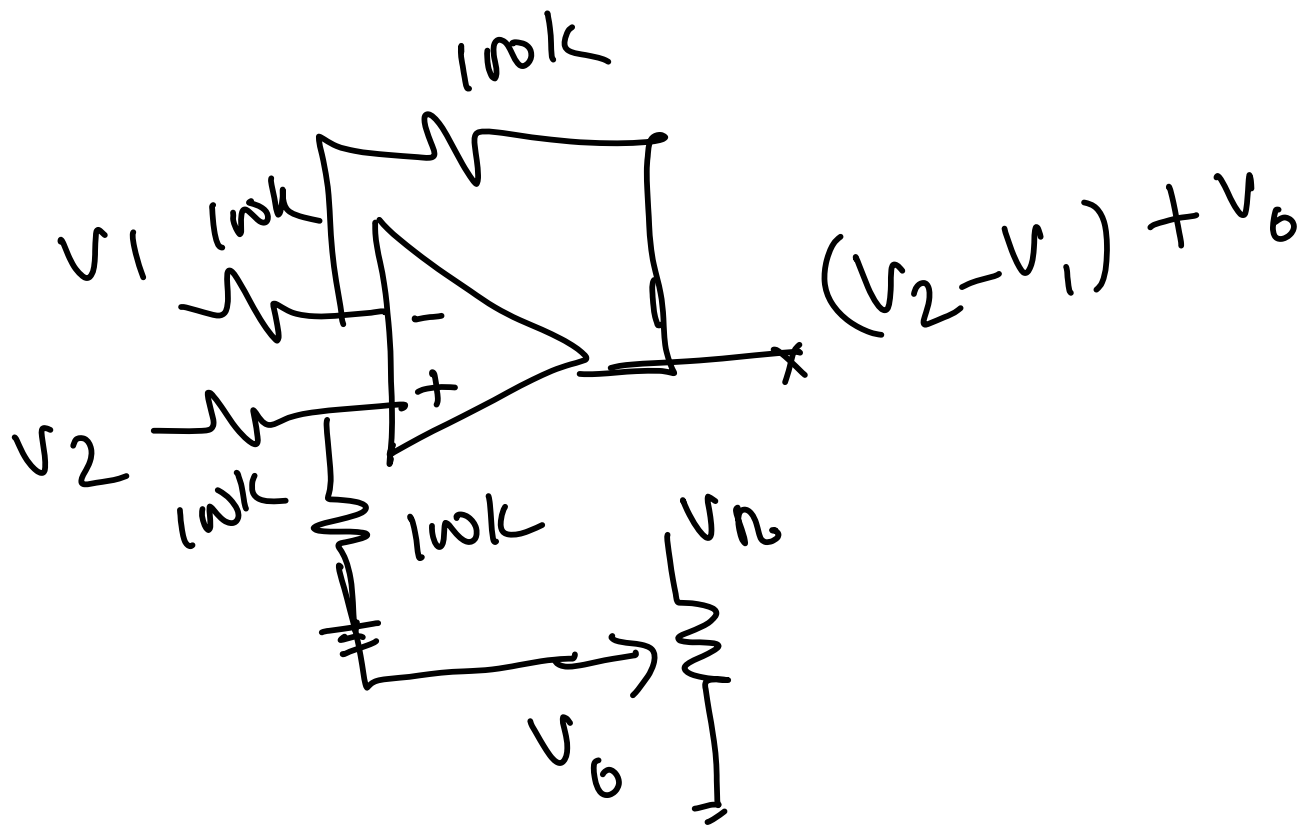




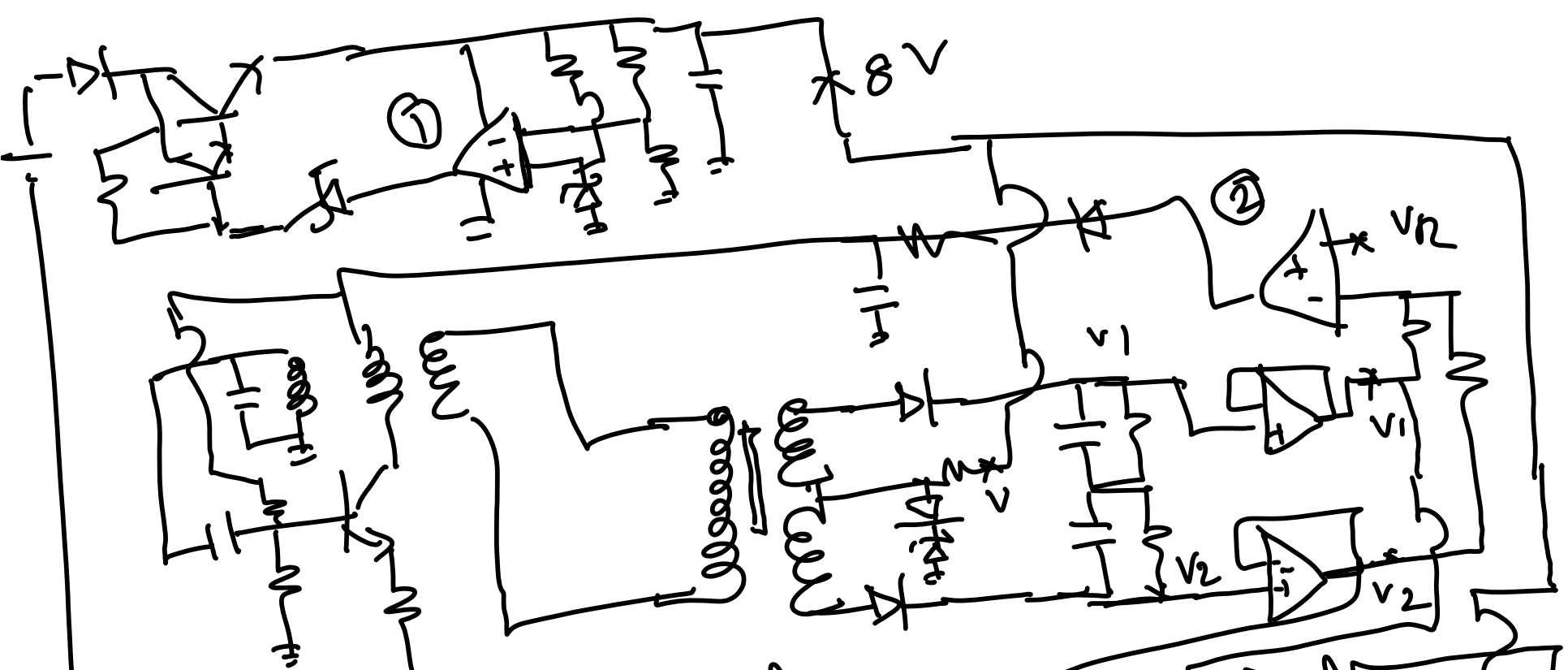


At inverting terminal

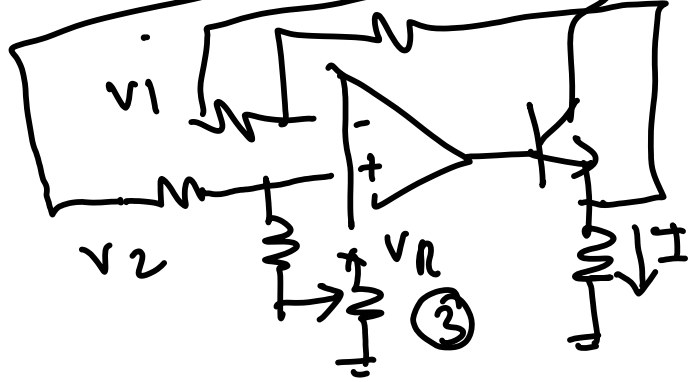
$$\begin{aligned}
 \text{At } + \text{ terminal} &= \frac{V_1}{2} + \frac{V_0}{2} \\
 \frac{V_1}{2} + V_0 &= V_2 + V_R \\
 V_2 - V_1 &= V_0 - V_R
 \end{aligned}$$



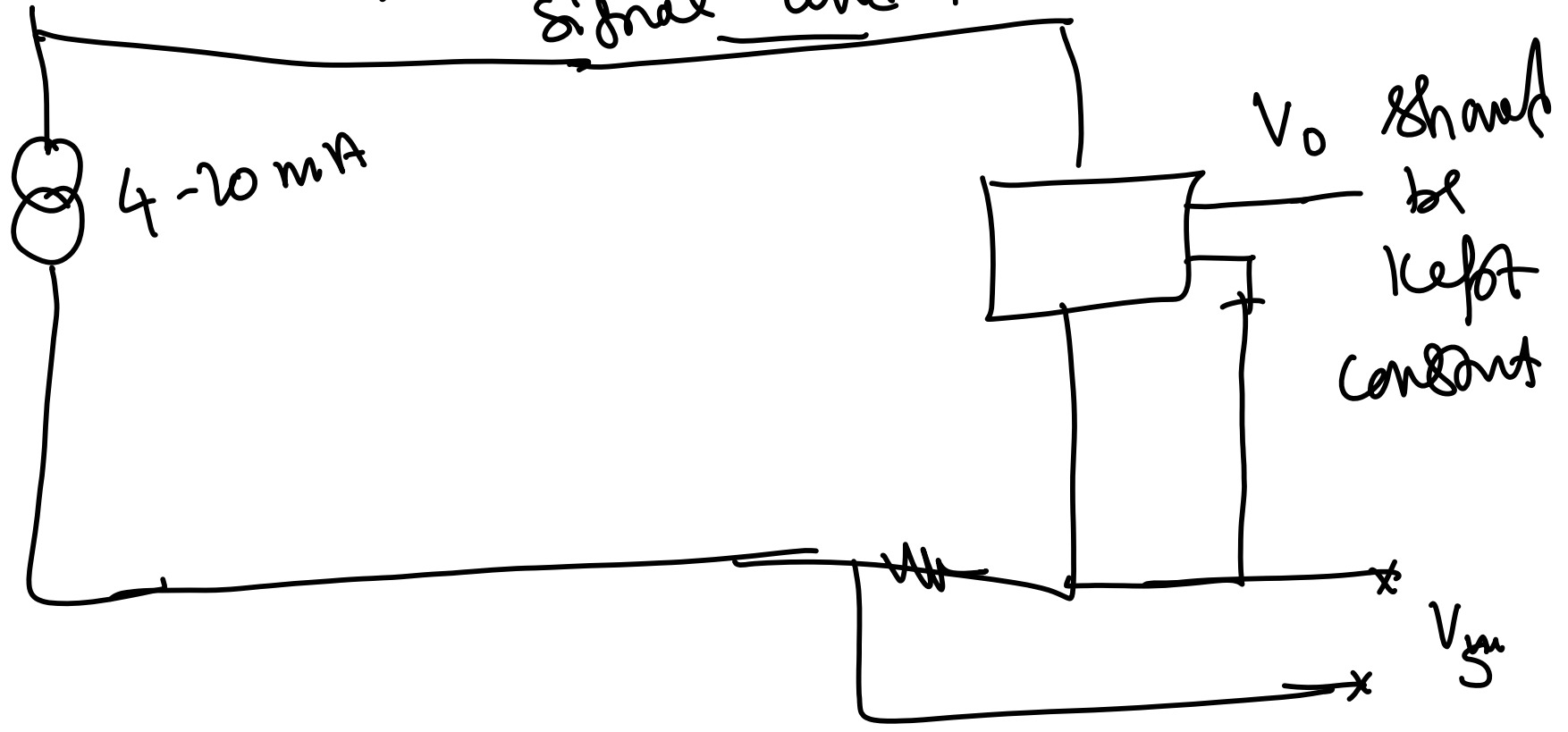
- ① LVDT excitation using sine wave
- ② Temperature compensation
- ③ $(V_1 - V_2)$ \propto displacement
- ④ $(V_1 - V_2)$ is converted into proportional current



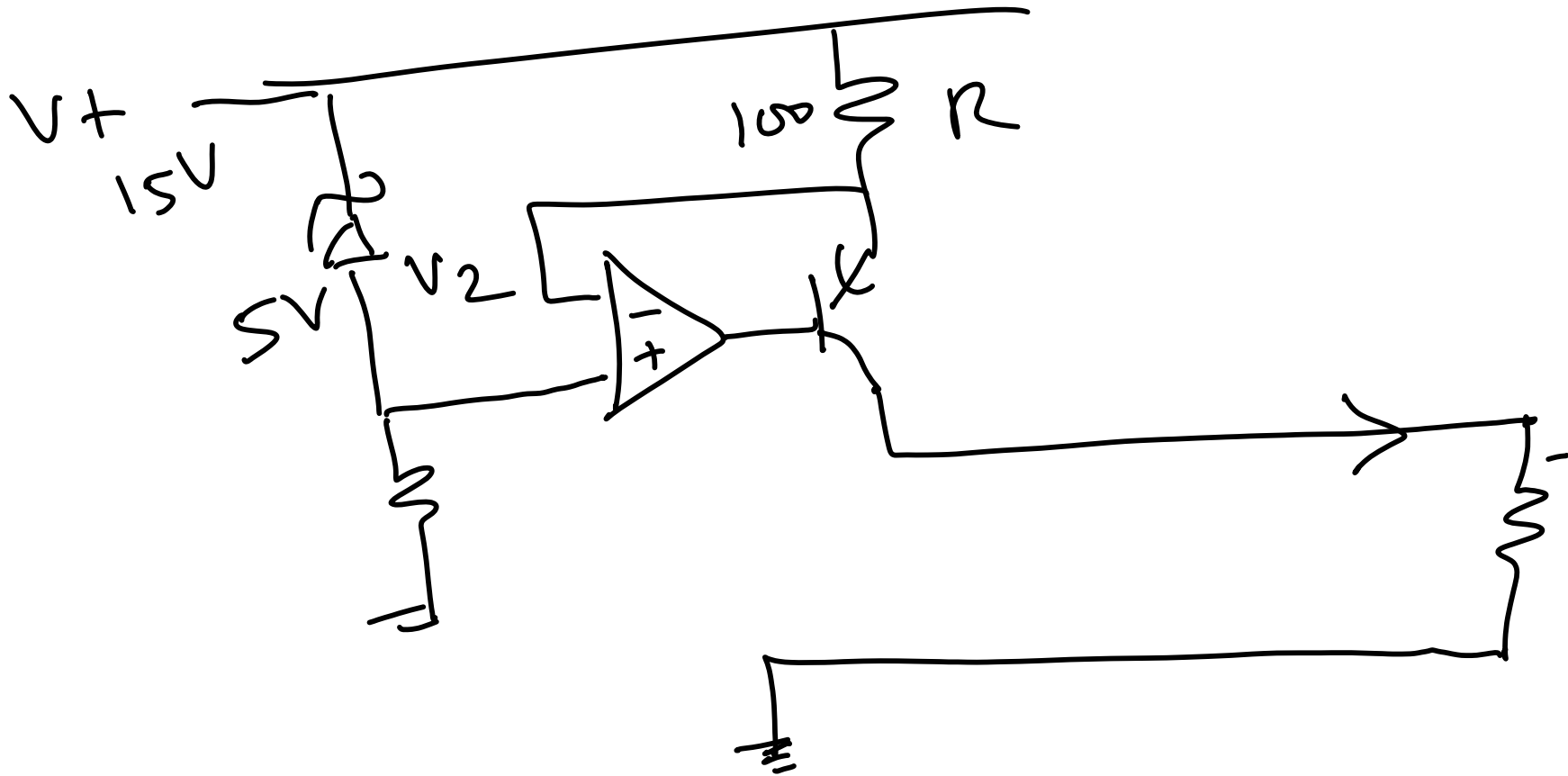
- ① op-amp ① → V_{ref}
- ② op-amp ② → $(V_1 + V_2)$ constant
- ③ op-amp ③ → $(V_1 - V_2) \propto I$

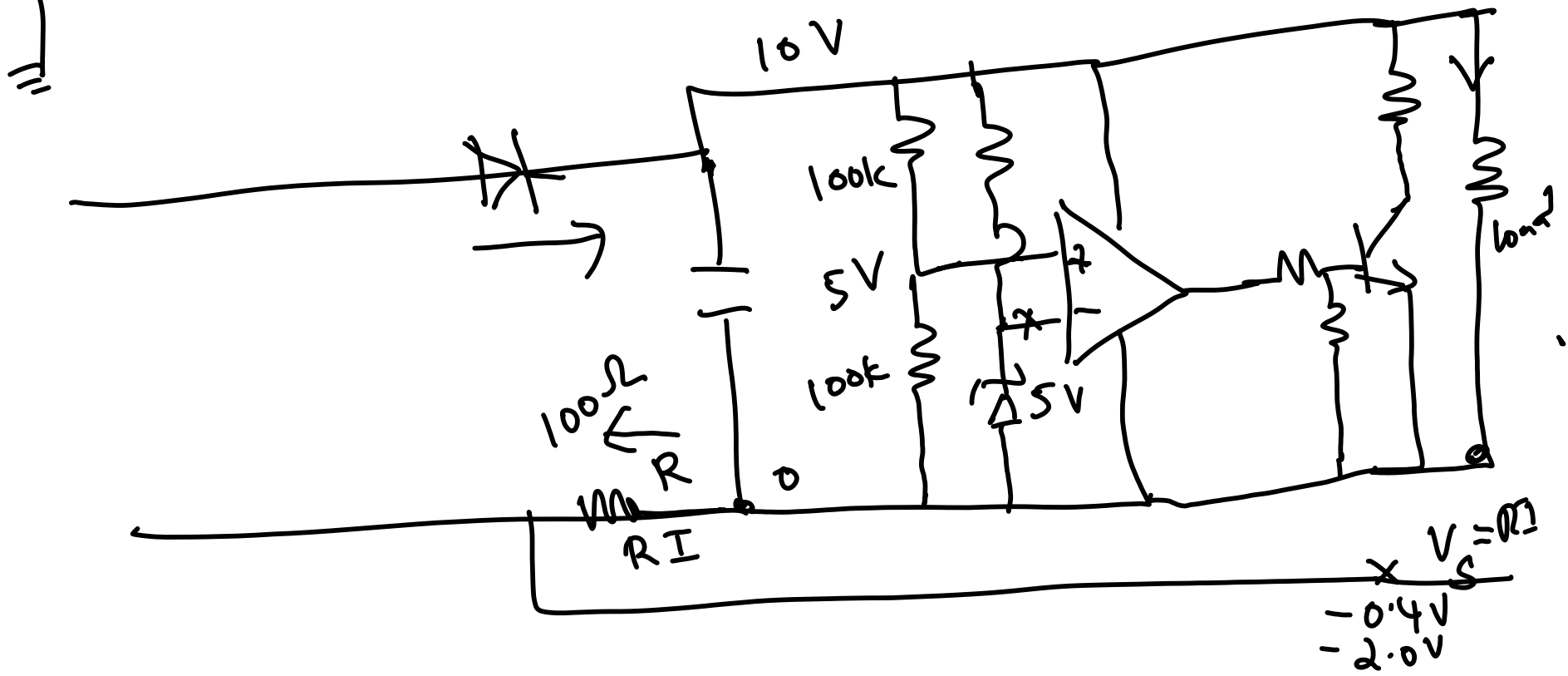
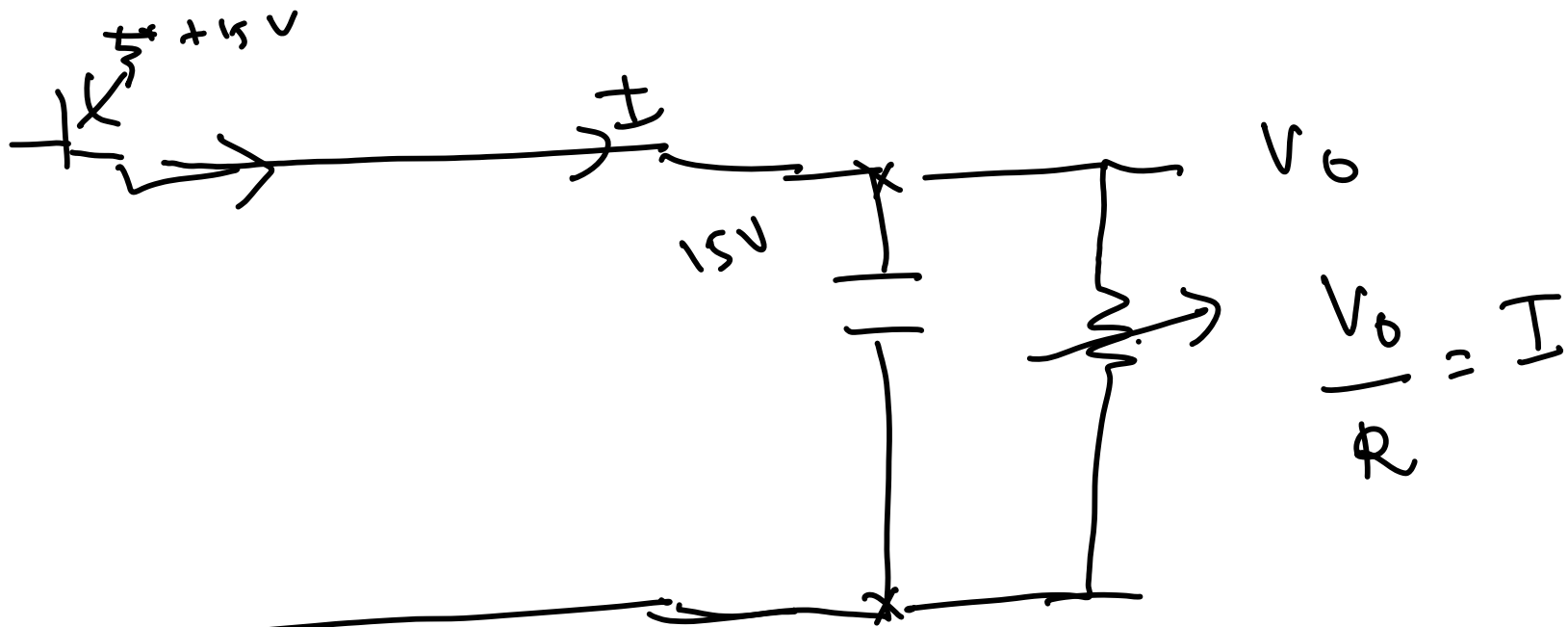


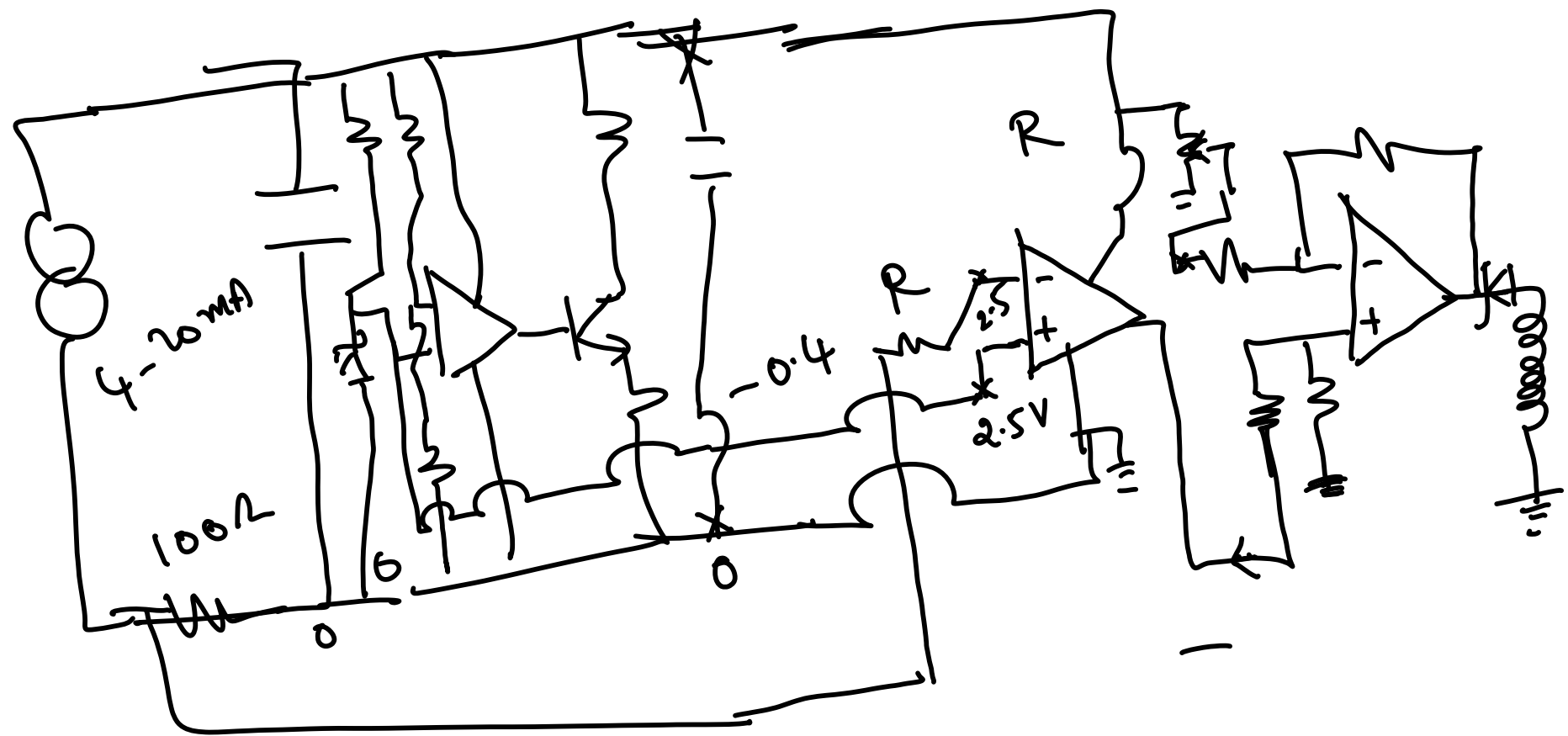
Splitting the current into
signal and power

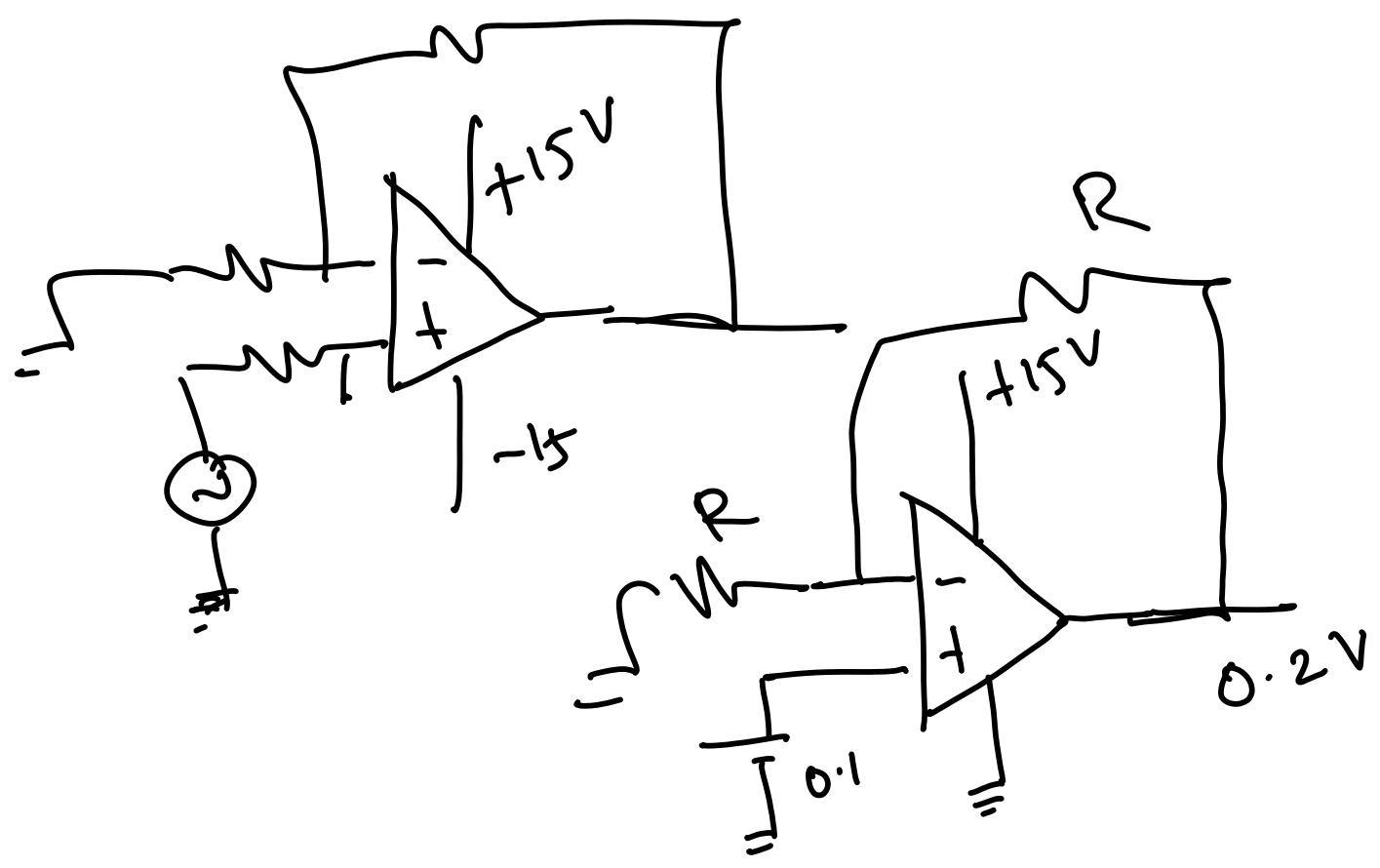


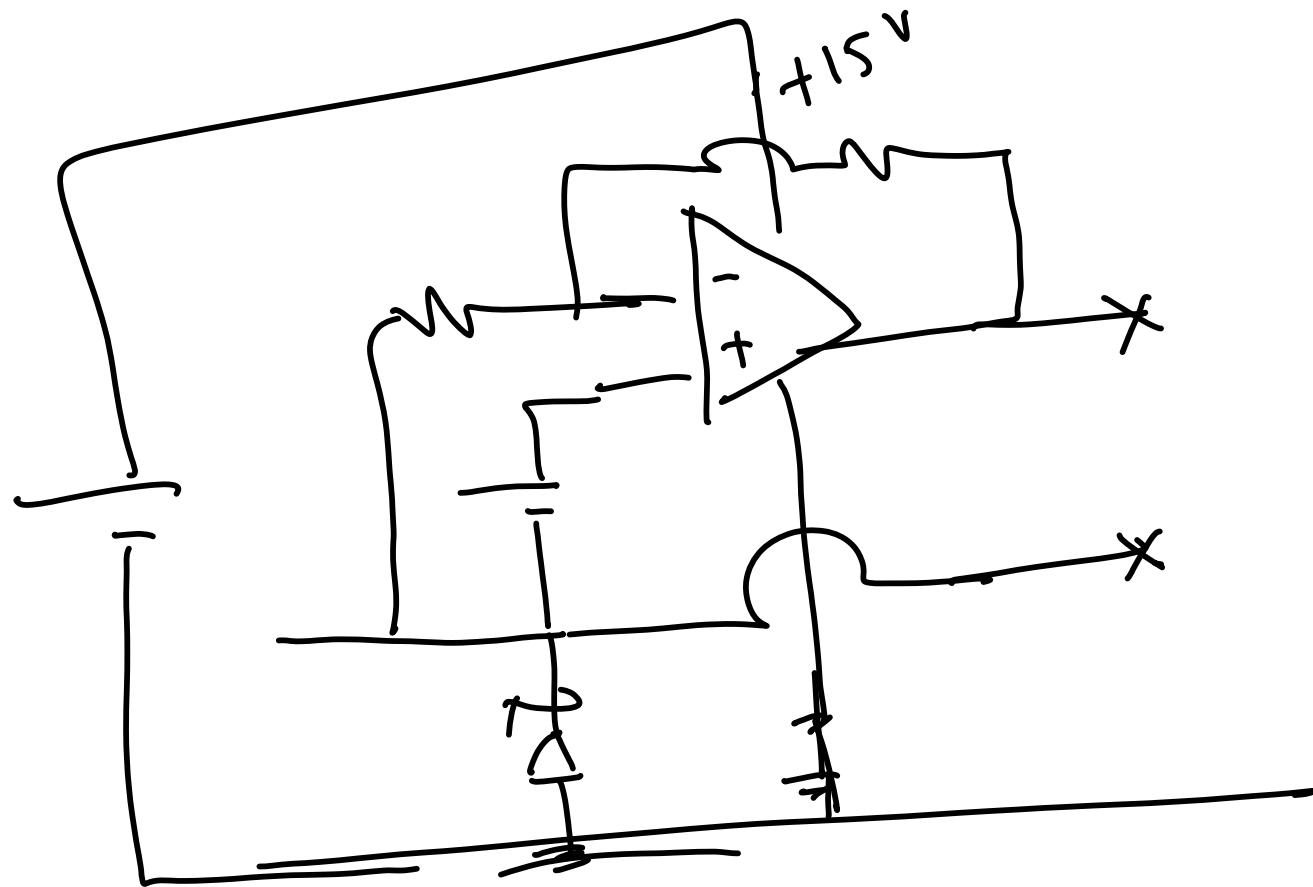
Constant current source



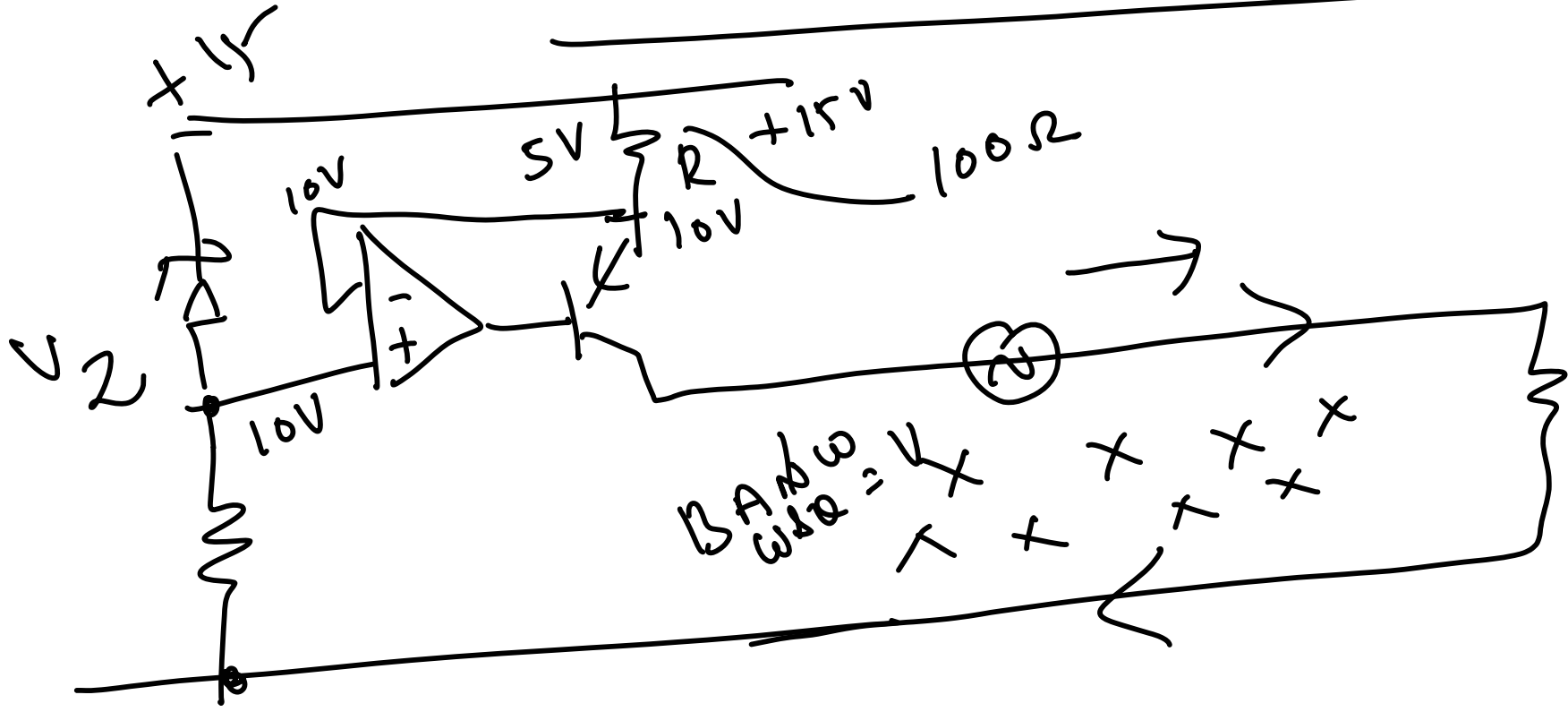


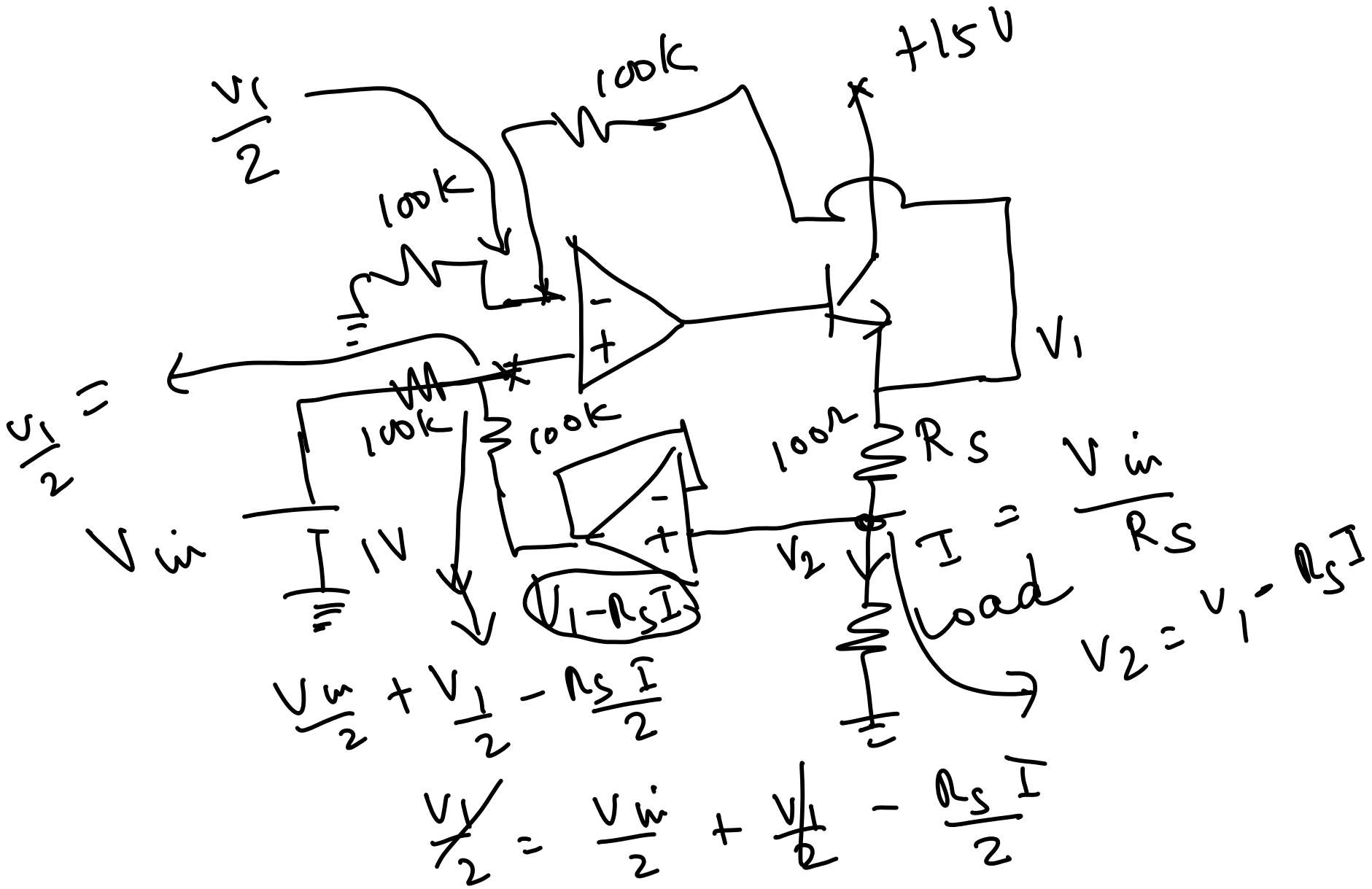






Constant current source





$$R_S I = V_{in}$$

$$I = \frac{V_{in}}{R_S}$$

Application of transistors

① Transistor as an amplifier.

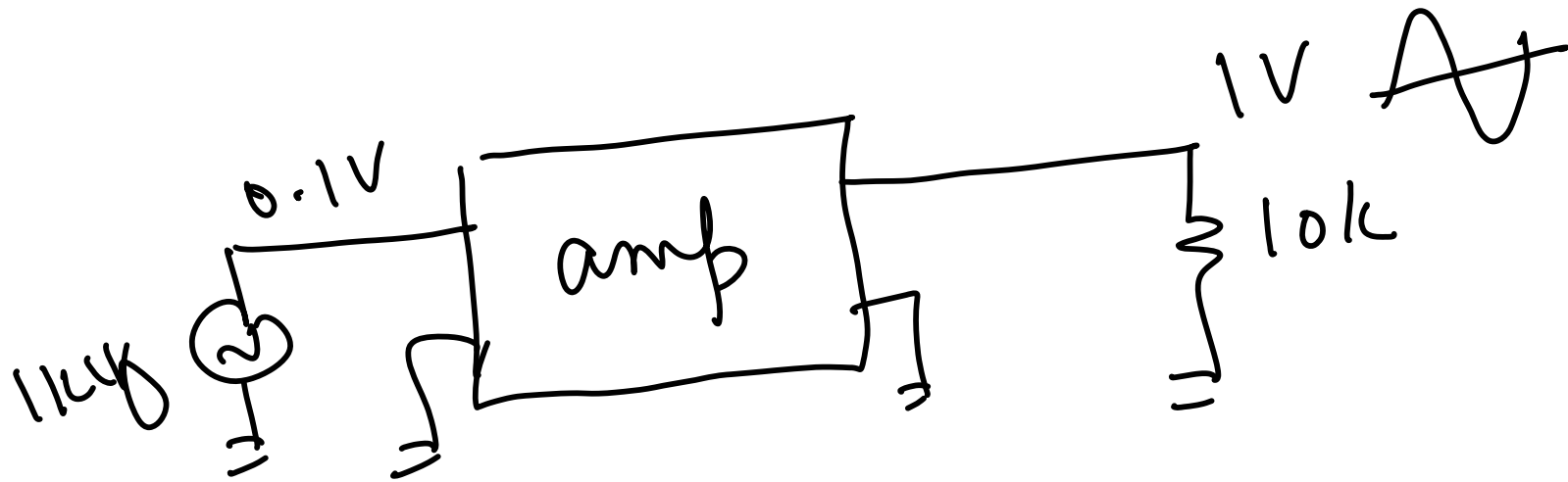
Spec : Input signal 0.1V

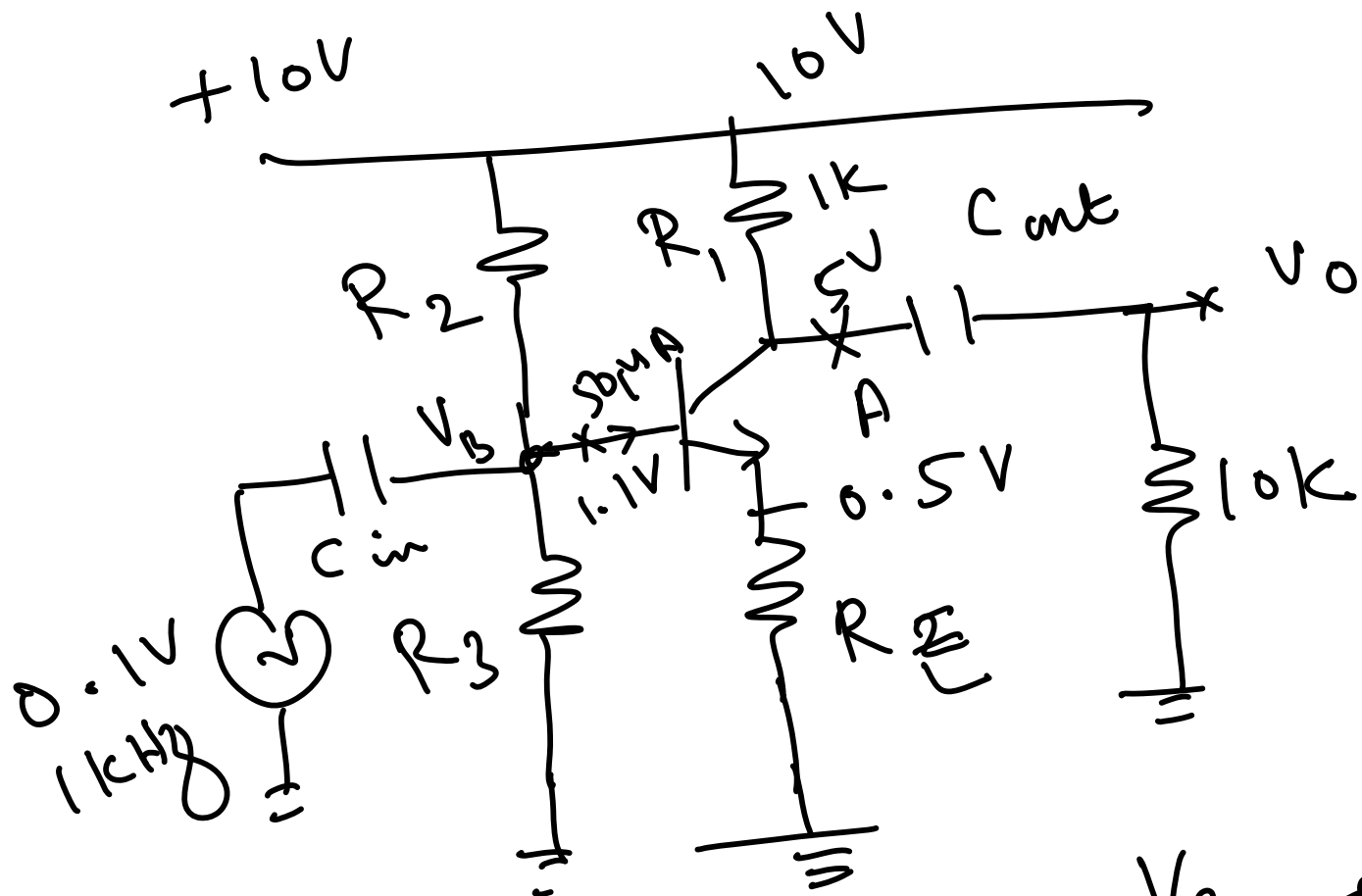
Amplification = 10

Freq = 1 kHz

Supply voltage = 10V

Load Resistance = 10k





Maintain A at $\frac{V_S}{2} = 5V$
 when $V_{in} = 0$

Fix R_1 - 10 times lower
than load which is 10k

$$\bar{e} \quad R_1 = 1k$$

$$\text{Gain} = \frac{R_1}{R_E}$$

$$R_E = 100 \Omega$$

What is the current in R_E ?

$$\text{current in } R_1 = \text{current in } R_E$$

$$\text{Current in } R_1 = \frac{(10-5)}{1k} = 5 \text{ mA}$$

current through $R_E = 5 \text{ mA}$

$$\text{voltage acc } R_E = 100 \times 5 \times 10^{-3} \\ = 0.5 \text{ V}$$

So voltage at the base

$$= 0.5 \text{ V} + 0.6 \text{ V} = 1.1 \text{ V}$$

base current

$$\frac{E \text{mitter current}}{\beta} = \text{base current}$$

$$\text{base current} = \frac{5 \times 10^{-3}}{\beta} = \frac{5 \text{ mA}}{100}$$

$$= 50 \mu\text{A}$$

Current through R_2 and R_3

This is to be kept 10 times
more than the base current
 $= 500 \mu\text{A} = 0.5 \text{ mA}$

voltage acc $R_3 = 1.1 \text{ V}$
current through $R_3 = 0.5 \text{ mA}$

$$\text{So } R_3 = \frac{1.1}{0.5 \text{ mA}} = 2.2 \text{ k}$$

w/ acc $R_2 = 10 - 1.1 = 8.9 \text{ V}$
current through $R_2 = 0.5 \text{ mA}$

$$\text{So } R_2 = \frac{8.9}{0.5 \times 10^{-3}} = 17.8 \text{ k} \\ = 18 \text{ k}$$

$$R_1 = 11k$$

$$R_E = 100\Omega$$

$$R_2 = 18k$$

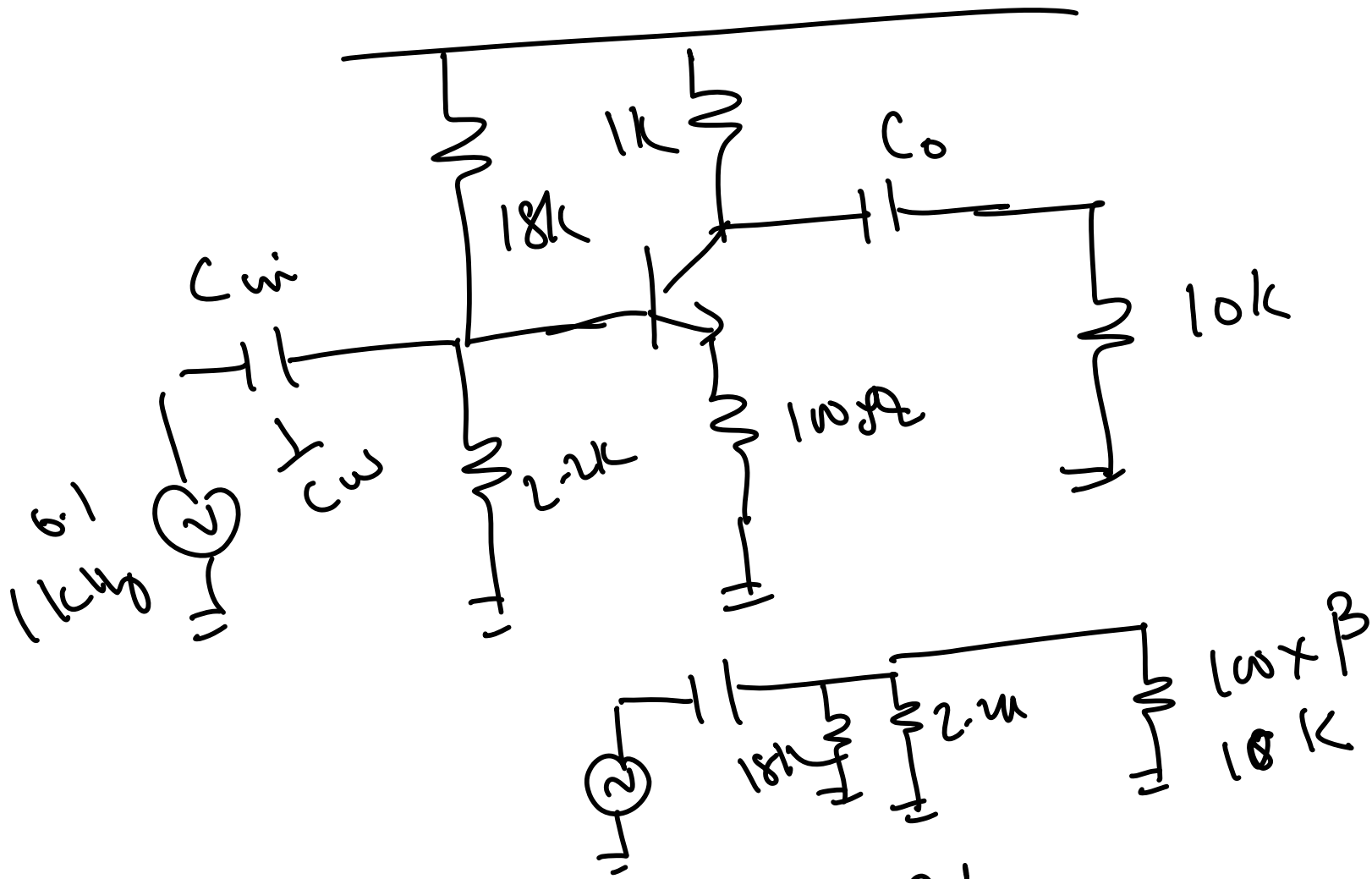
$$R_3 = 2.2k$$

$$C_{in} = ?$$

$$C_{out} = ?$$

INPUT impedance of the amplifier

$$= R_2 \parallel R_3 \parallel 100\Omega \times \beta$$



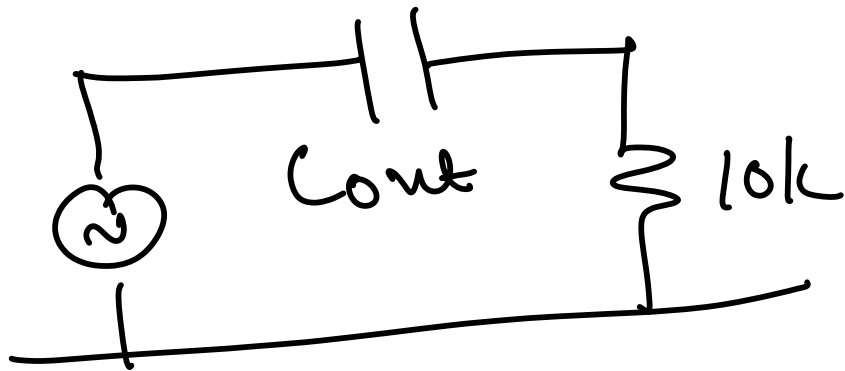
$I_{input} = 2k$
 impedance is $2k$

$$\frac{1}{C\omega} = 200$$
$$\omega = 2\pi \times 10^3$$

$$\frac{1}{200 \times \omega} = C_{in}$$

$$\frac{1}{200 \times 2\pi \times 10^3} = C_{in}$$
$$\frac{10^{-5}}{2 \times 2\pi} = \frac{10^{-5}}{4\pi} = \frac{10^{-6}}{1} = 1 \mu F$$

$C_{in} \approx 1 \mu F$
 Calculation for C_{out}



Impedance of $C_{out} = 1k$

$$\frac{1}{C\omega} = 10^3$$

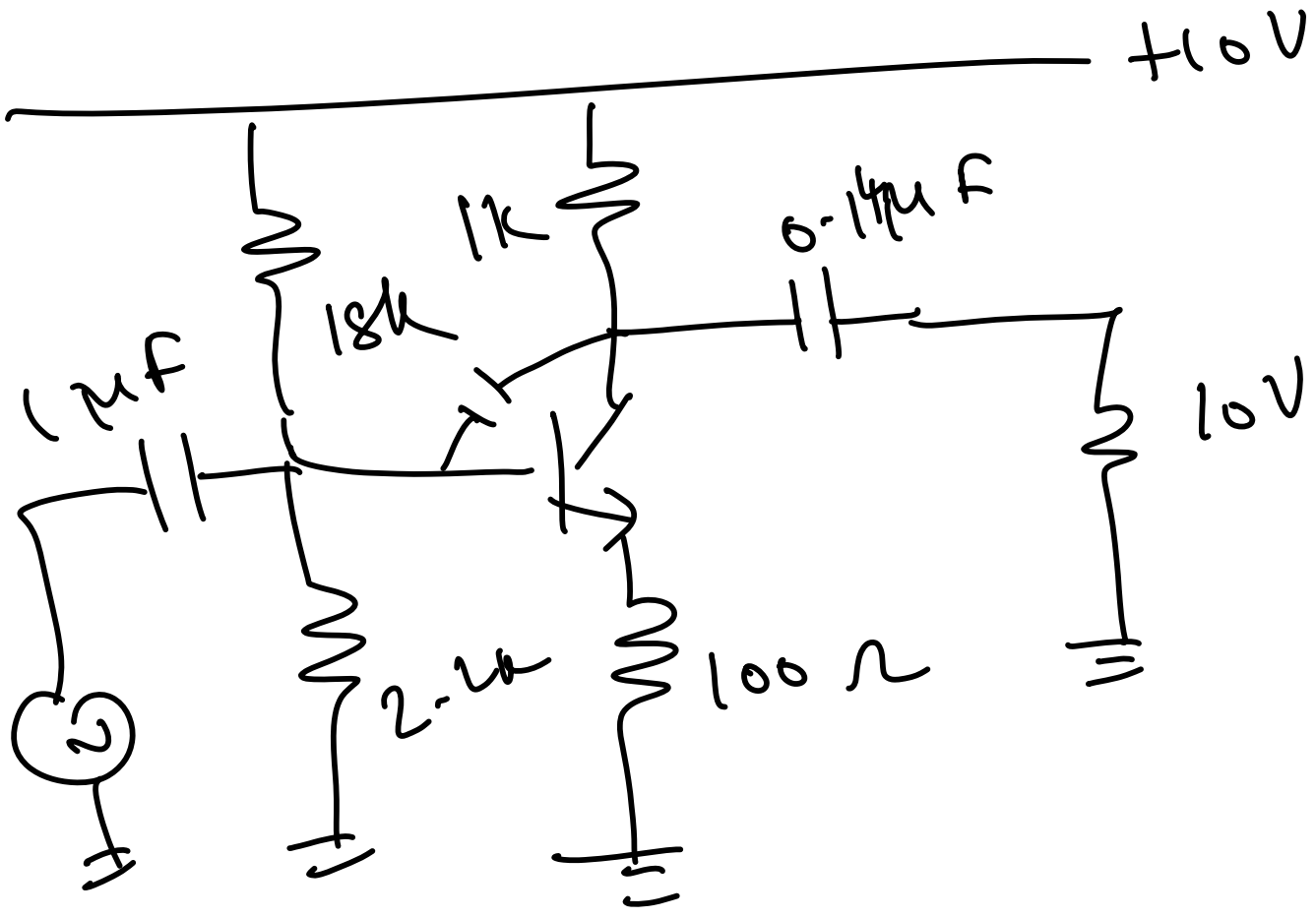
$$\omega = 2\pi \times 10^3$$

$$\frac{1}{C \times 2\pi \times 10^3} = 10^3$$

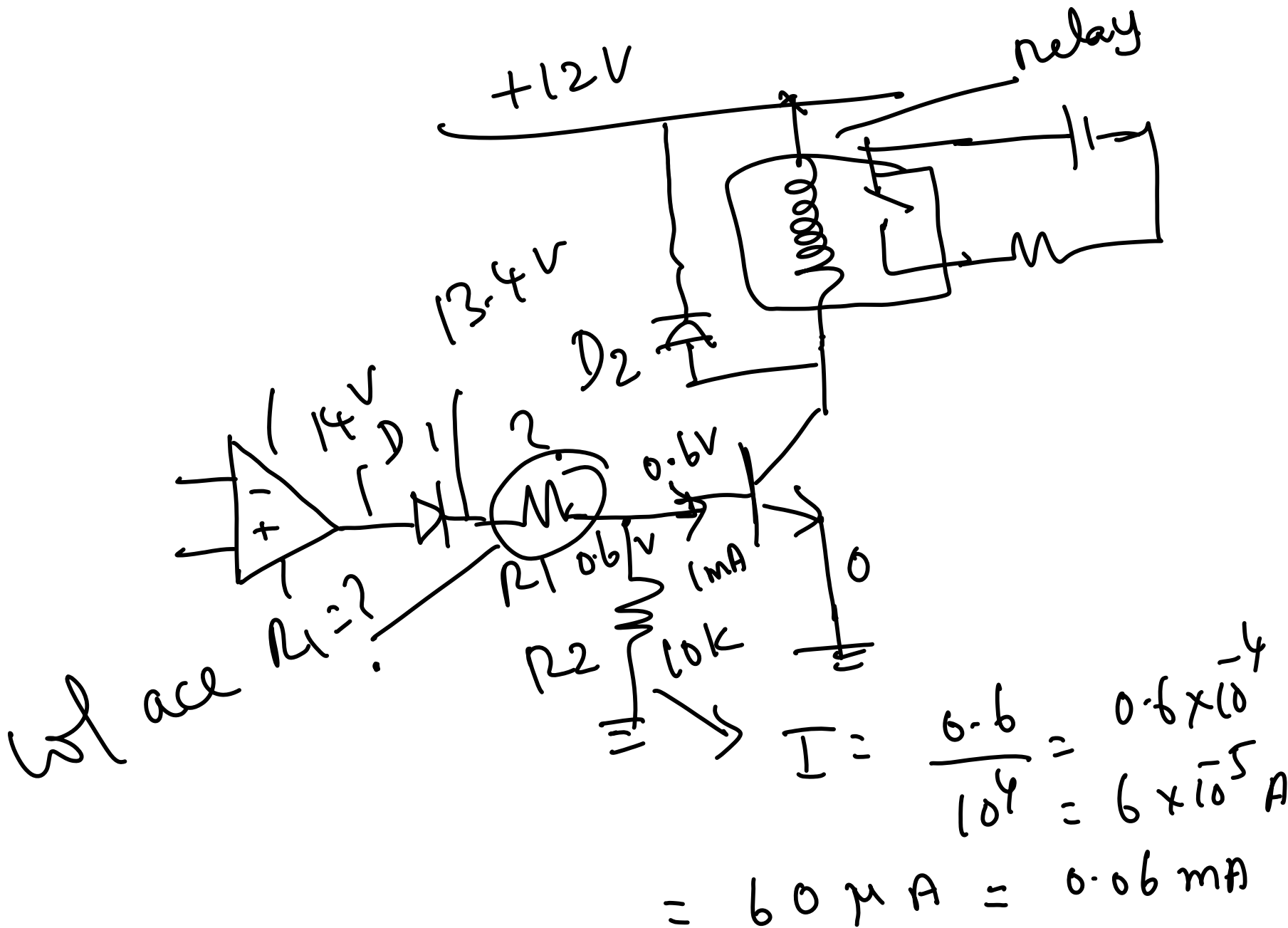
$$\frac{1}{2\pi \times 10^6} = C_{out}$$

$$\frac{10^{-6}}{2 \times 3} = \frac{10^{-7} \times 10}{6} = 1.4 \times 10^{-7}$$

$$C_{out} = 0.14 \mu F$$



How to design a
Relay driver using
transistor



V_o of op amp is +15

Relay should be ON

V_o of op amp is -15

Relay should be OFF

Collector current of the
transistor

Collector current = Relay current

Let relay current
 $I_{be} = 100 \text{ mA}$

$$I_c = 100 \text{ mA}$$

$$I_b = \frac{I_c}{\beta} = \frac{100 \text{ mA}}{100} = 1 \text{ mA}$$

base current = 1 mA

For base emitter cap of
100 pF

For $R_2 = 10k$

Then off time
 $= 10^{-10} \times 10^4 = 10^{-6}$ sec

$$R_2 = 10k$$

Current through R_2

$$= \frac{0.6}{10k} = 0.06 \text{ mA}$$

Total current through R_1

$$= 1 \text{ mA} + 0.06 \text{ mA} \\ = 1.06 \text{ mA}$$

w/ acc $R_1 = (15 - 1.2V - 0.6 - 0.6)$

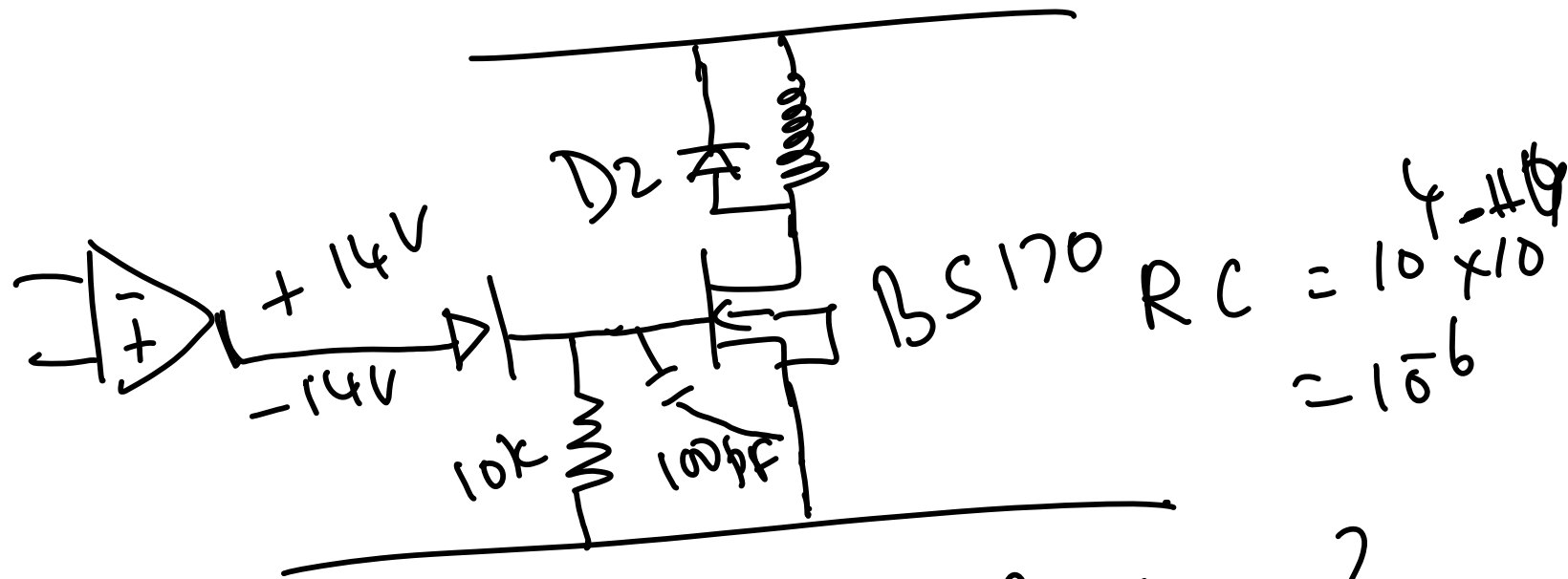
$$= 15 - 2.4 \\ = 12.6 \text{ V}$$

Current through $R_1 = 1.06 \text{ mA}$

$$R_1 = \frac{12.4}{1.06 \text{ mA}} \approx 12 \text{ k}$$

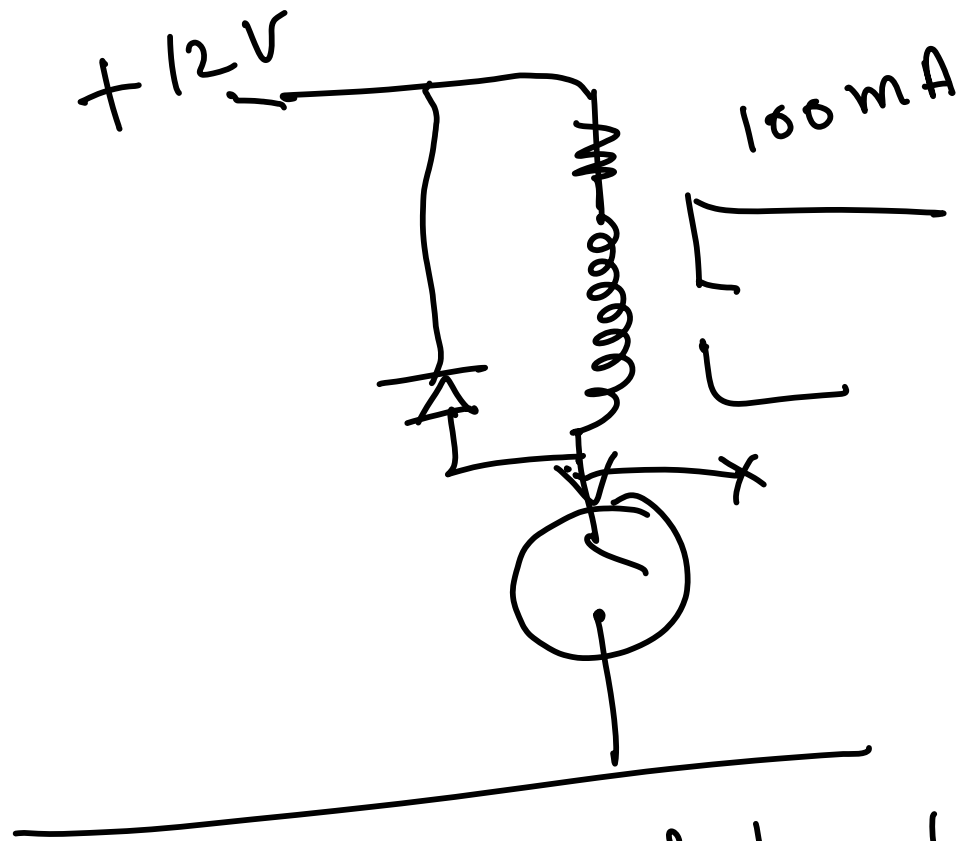
$$R_1 = 10 \text{ k}$$

Relay drive using a MOSFET



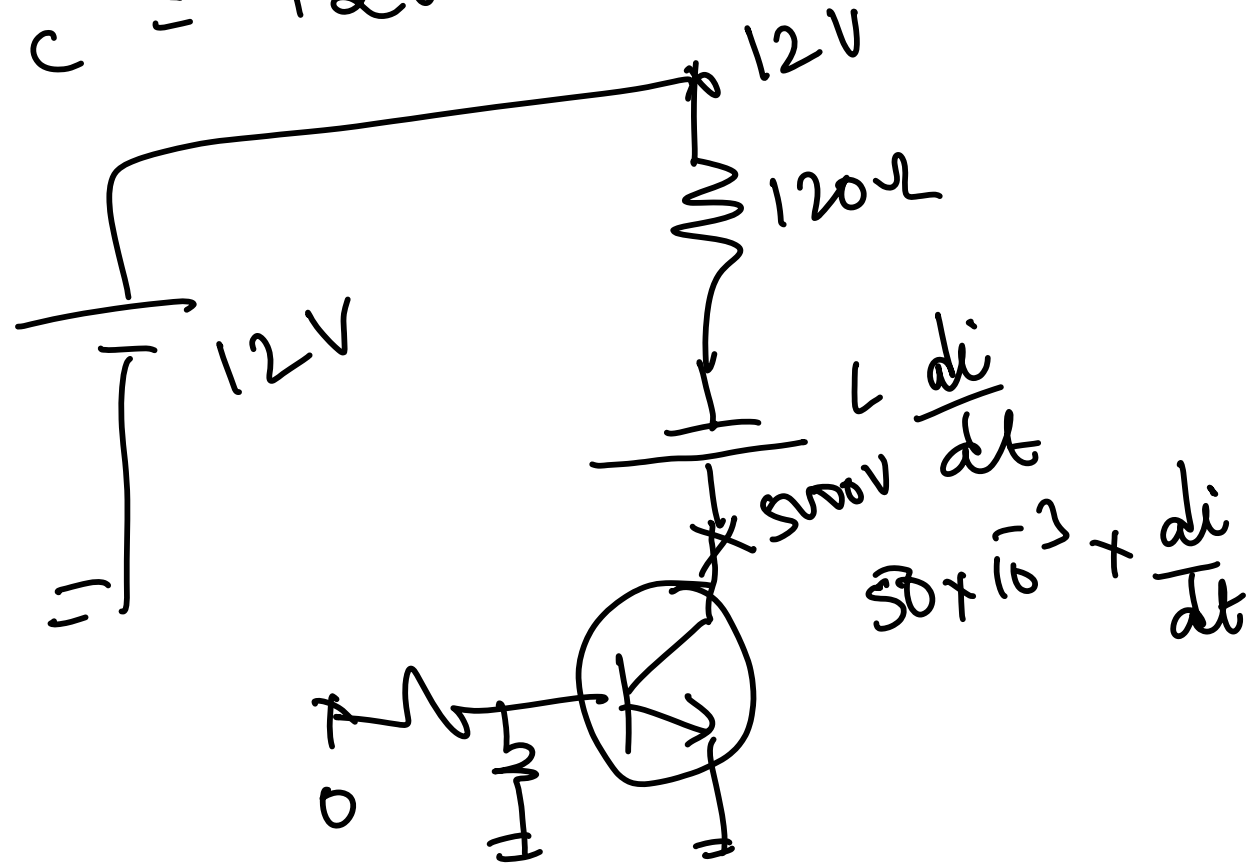
$$RC = 10^4 \times 10^{-10}$$
$$= 10^{-6}$$

What is the use of D2 ?



The resistance of the coil
 $= \frac{12}{100\text{mA}} = 120\Omega$

$$R_c = 120\Omega$$

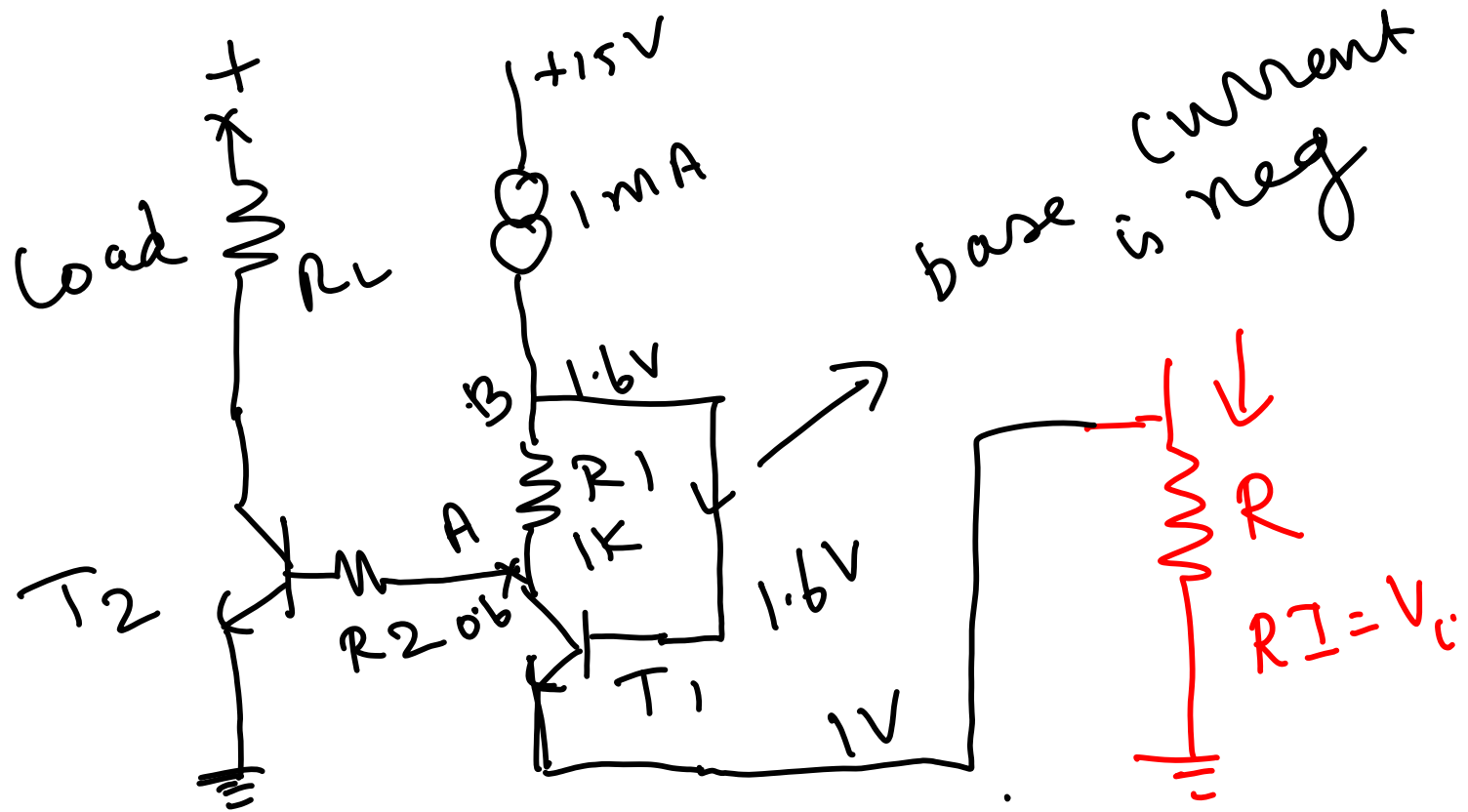


$$dt = 1\text{MS}$$

$$di = 10^{-1}\text{A} = 100\text{mA}$$

$$L \frac{di}{dt} = \frac{50 \times 10^{-3} \times 10^{-1}}{10^{-6}}$$

$$= 50 \times 10^2 = 5000 \text{ V}$$



(1) If the current in R is more than set value the load to be R_L switched off

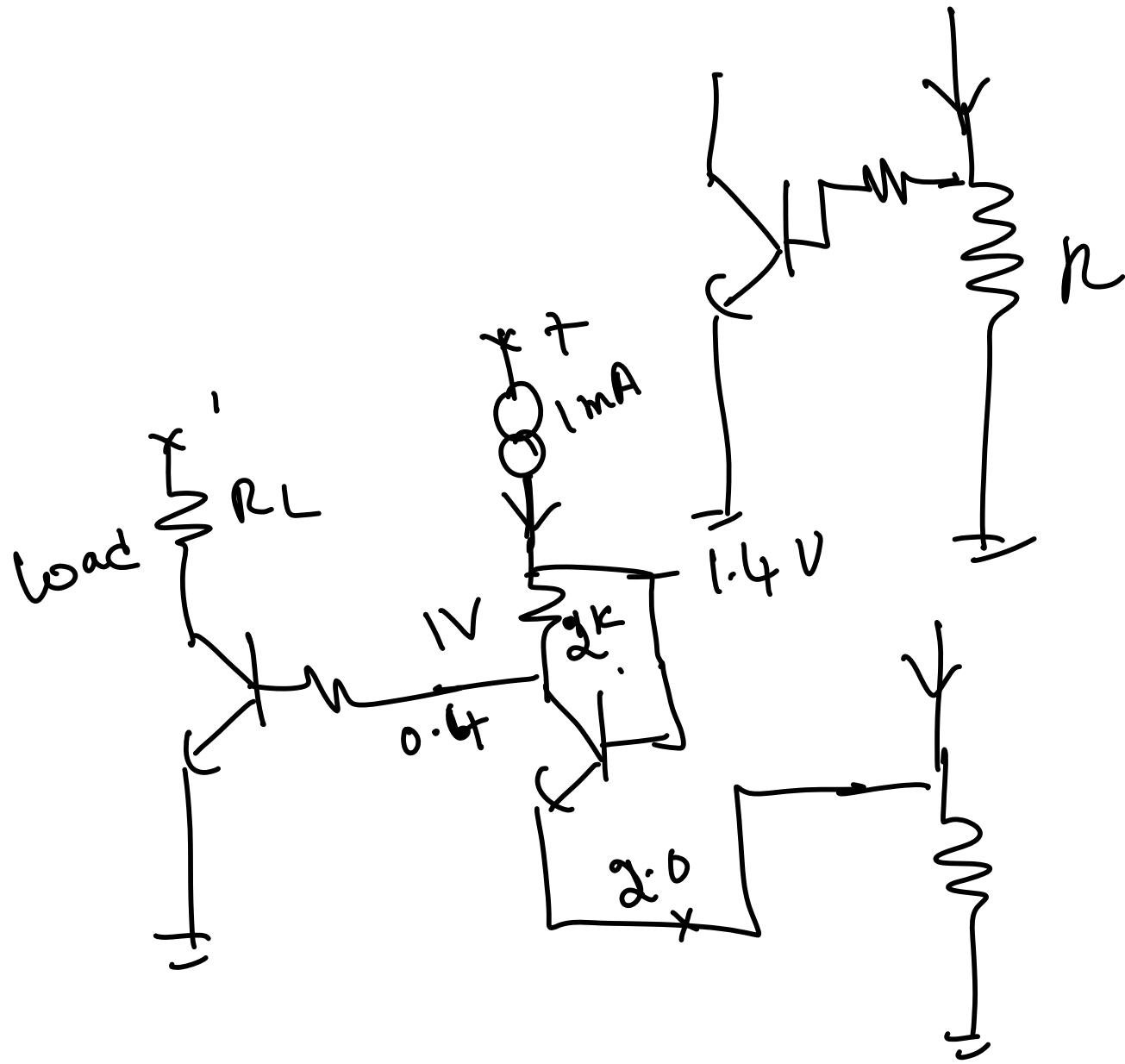
sol acc $R_1 = 1 \times 10^{-3} \times R_1$
 $R_1 = 1K$

$$\text{Wt acc } R_1 = 10^3 \times 10^3$$

voltage at A \rightarrow switch on
transistor $T_2 = 0.6V$

$$\text{Voltage at B} \\ = 1k \times 10^{-3} + 0.6 = 1.6V$$

Then emitter of $T_1 = 1.0V$
ie only when the voltage across
 R is $> 1V$ the transistor T_2
will be ON

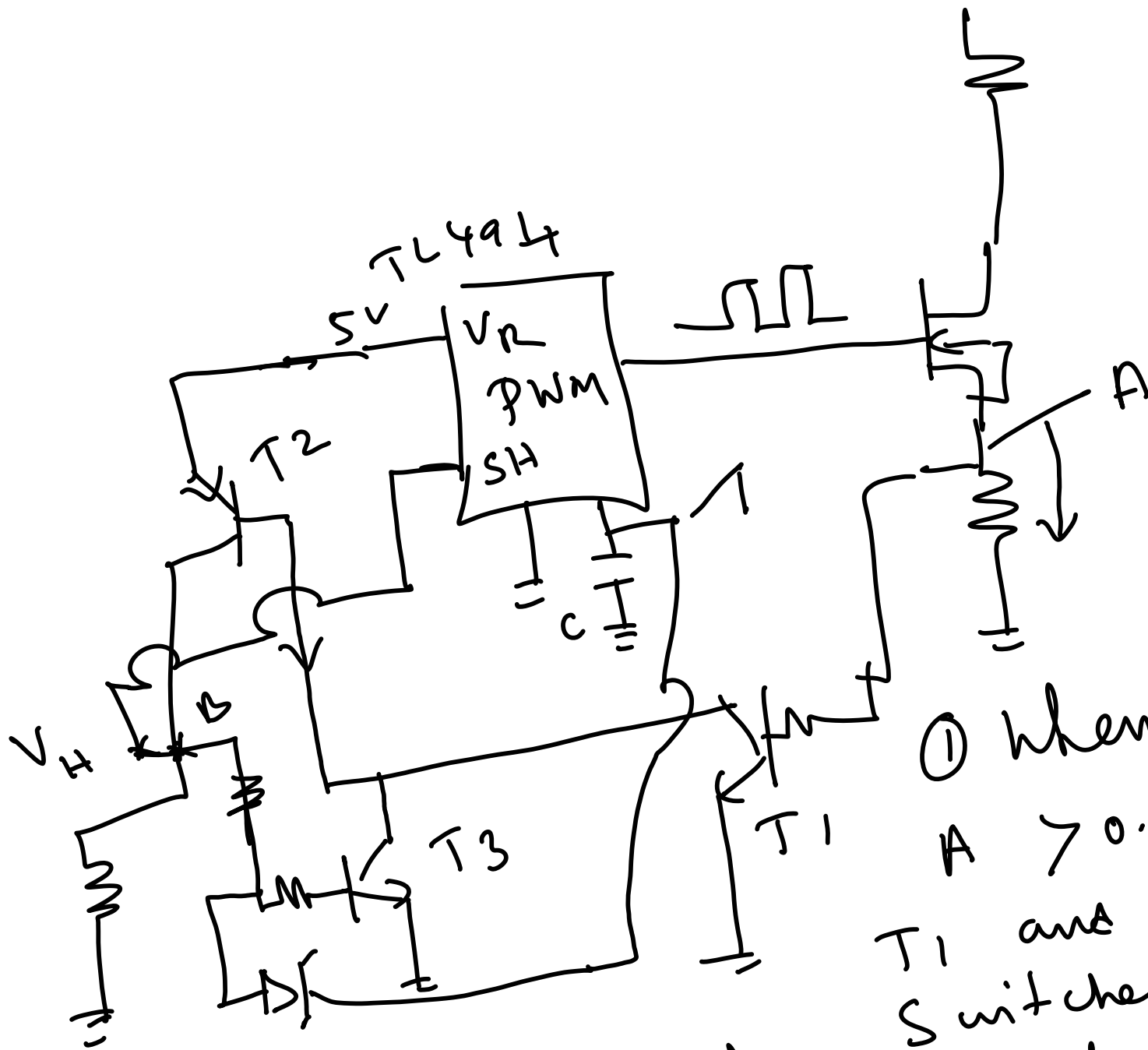


So with temp the
switching vol will not
change.

V_{BE} change in T_2 is
compensated by V_{BE} change in T_1

Switching voltage can be
changed by changing the
Resistance R_1

Transistor as a Latch



① when vol at A $> 0.6V$ then T_1 and T_2 are switched ON

So vol appears at B

③ Then T_3 is switched on
when v_{ω} at A goes more than 0
 T_1, T_2 and T_3 are on
So PWM I_c is switched off

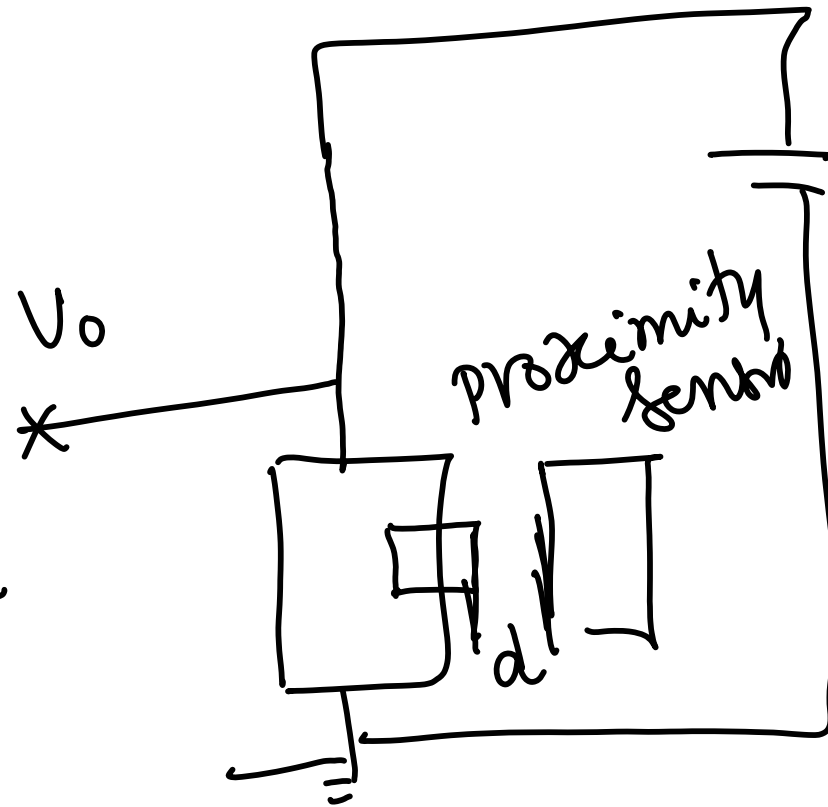
④ So v_{ω} at A = 0
but T_3 will be continuously on.
So v_{ω} at B will be present.

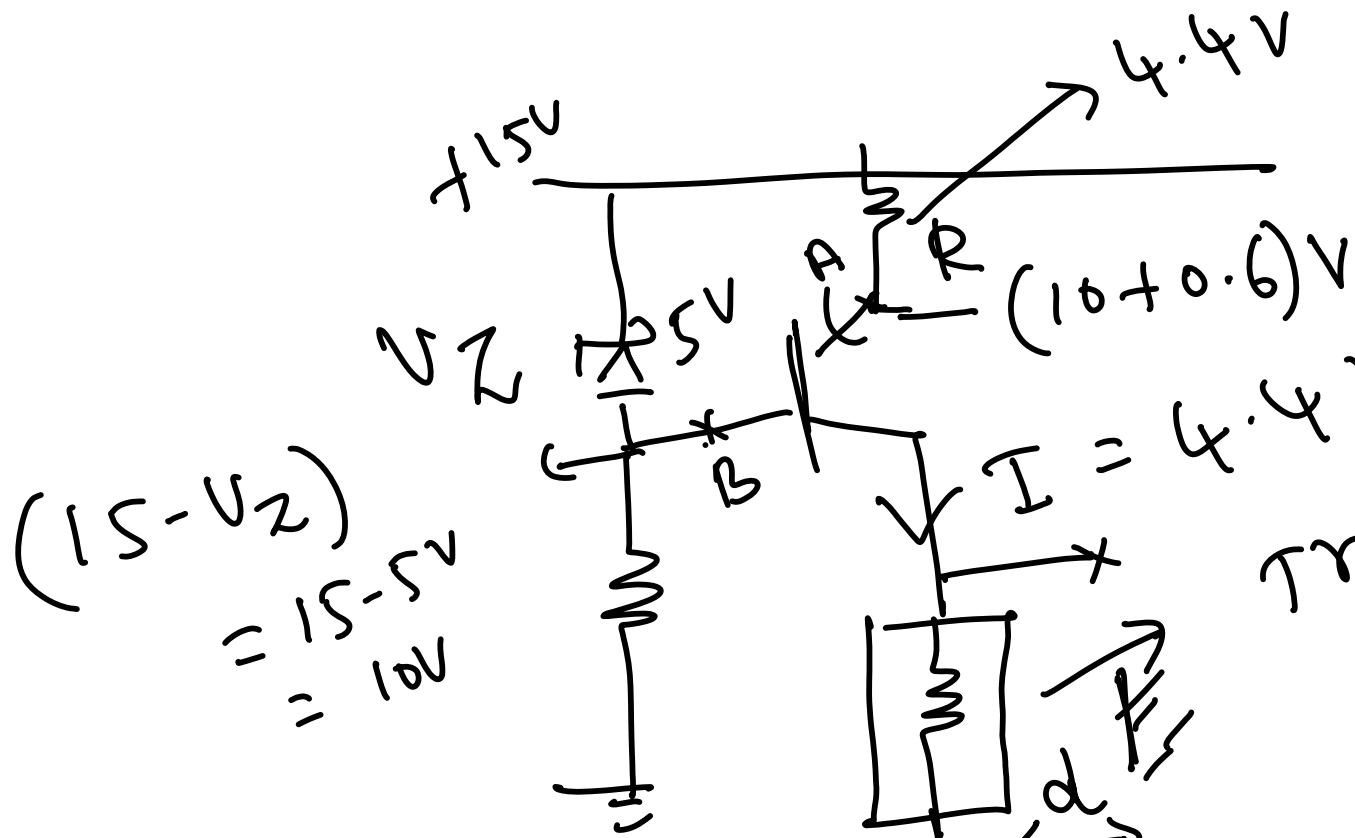
⑤ When the v_{ω} across the
cap C drops to zero, T_3
goes off. And v_{ω} at B = 0

How to use the transistor for temperature in transducers

wt V_o represents
displacement d

However
 V_o changes with
ambient temp





$I_{25} = 4.4 mA$
 $I_{80} = 4.52 mA$

w/ at point A = $10 + 0.6V$
 $= 10.6V$

Because w/ at B = $10V$
 $(15 - 5V) = 10V$

voltage across R

$$= 15 - 10.6 = 4.4 \text{ V}$$

If $R = 1 \text{ k}$

So current through

$$R = \frac{4.4}{1 \text{ k}} = 4.4 \text{ mA}$$

So the current $I = 4.4 \text{ mA}$

at room temperature
I will increase with temp
(ambient)

At 25°C ambient temperature

$$I = 4.4 \text{ mA}$$

What is I at
 80°C ambient?

$$\begin{aligned}
 V_{BE} \text{ at } B &= 10 \text{ V} \\
 V_{BE} \text{ at } 25^{\circ}\text{C} &= 0.6 - 2.2 \text{ mV} \times (25) \\
 &= 0.6 \text{ V} - 2.2 \times 10^{-3} (80 - 25^{\circ}\text{C}) \\
 &= 0.6 - 2.2 \text{ mV} (55^{\circ}\text{C}) \\
 &= 0.6 - 2.2 \times 55 \times 10^{-3} \\
 &= 0.6 - 121 \text{ mV} \\
 &= 0.6 - .12
 \end{aligned}$$

$$\begin{array}{r}
 55 \times 22 \\
 \hline
 110 \\
 110 \\
 \hline
 1210
 \end{array}$$

$$V_{BE} \text{ at } 100^\circ\text{C} = 0.48\text{V}$$

$$\begin{aligned} \text{Voltage at A} &= 10 + 0.48\text{V} \\ &= 10.48\text{V} \end{aligned}$$

$$\begin{aligned} \text{Voltage across R} &= 15 - 10.48 \\ &= 4.52\text{V} \end{aligned}$$

$$I = \frac{4.52}{1\text{k}} = 4.52\text{mA}$$

The current I increases with temp

So if the temp co-eff of the transducer is negative (with increase in ambient temp V_T across the transducer decreases) then this arrangement will compensate.

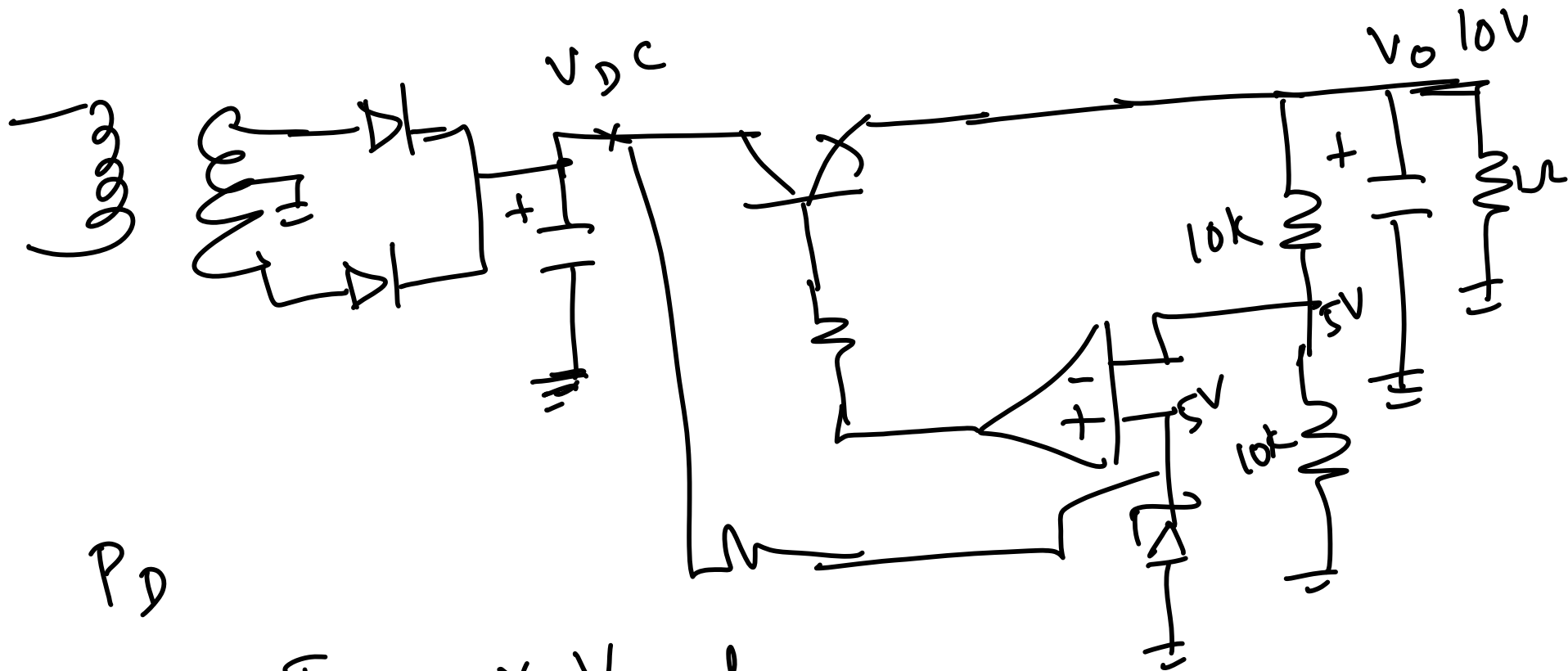
(1) V_{BE} of the transistor changes with temp.

(2) $\Delta V_{BE} = -2.2 \text{ mV}/^\circ\text{C}$

③ ΔV_{DE} is highly reproducible

So it is possible to get
repeatable ~~to~~ result in
the mass production

Transistors in
parallel



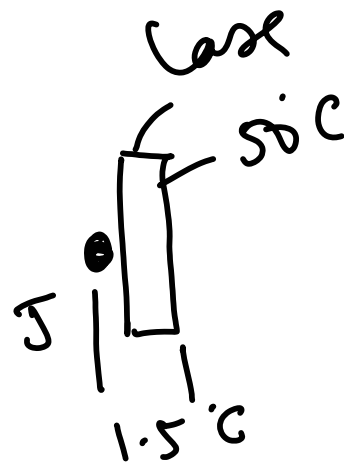
P_D

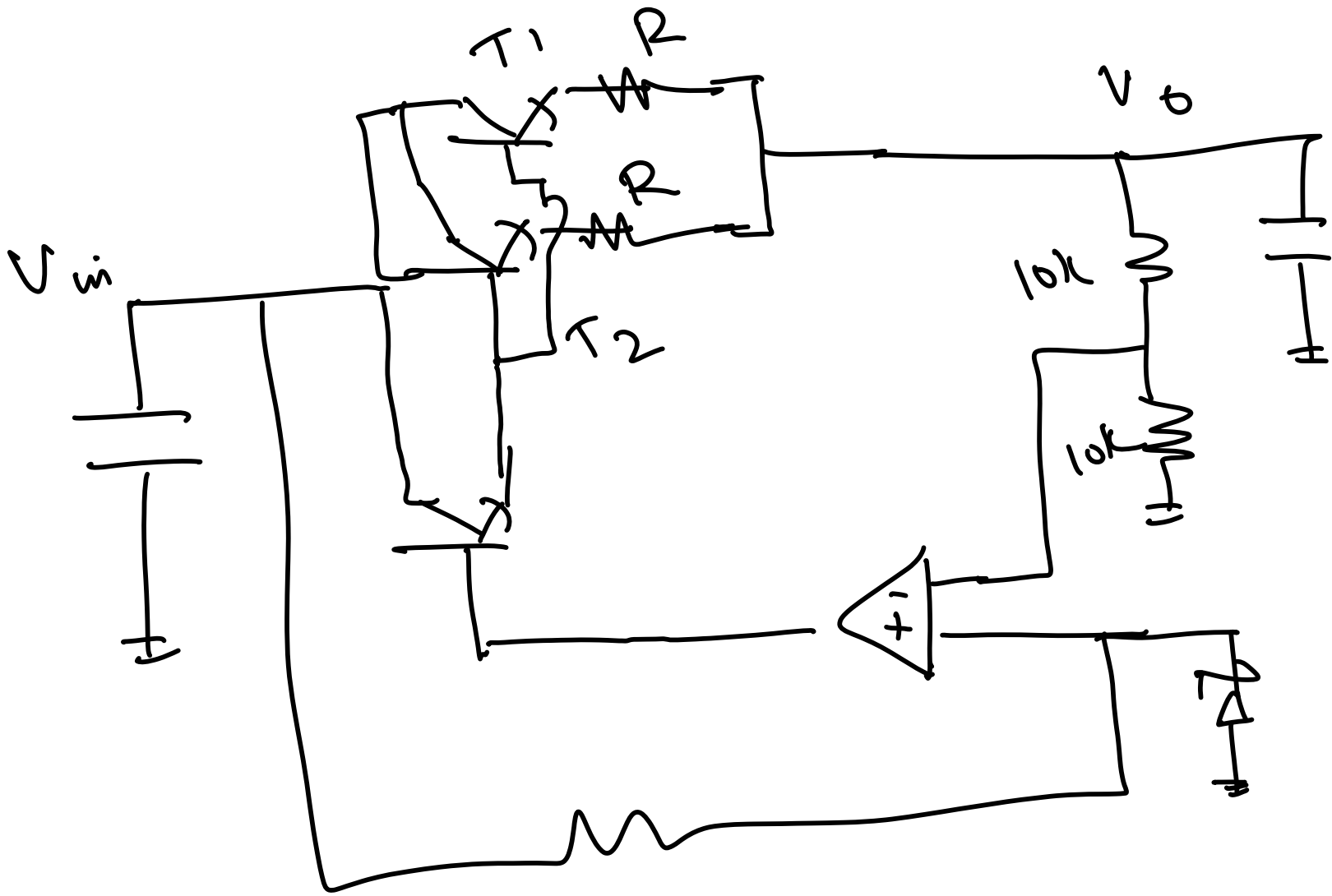
$$= I_{out} \times V_{drop}$$

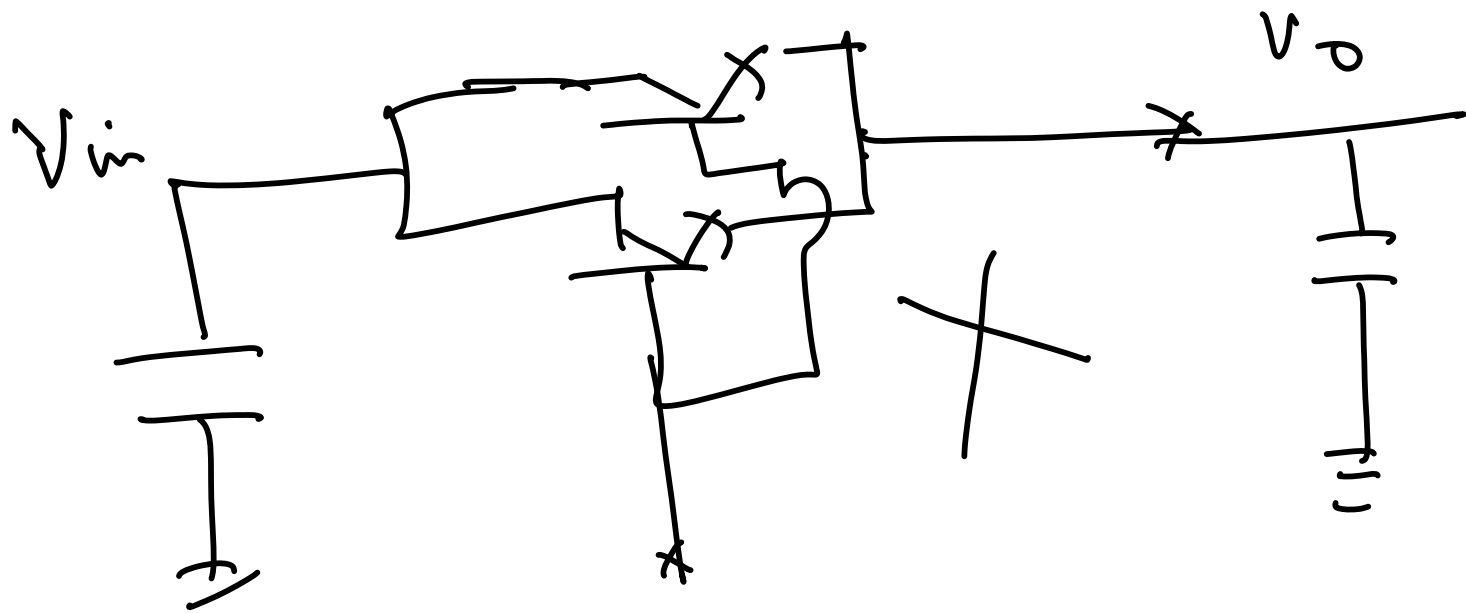
$$= 10 \times 5 = 50 \text{ W}$$

For 3055 Transistor

$$\theta_{JC} = 1.5^\circ \text{C/W}$$



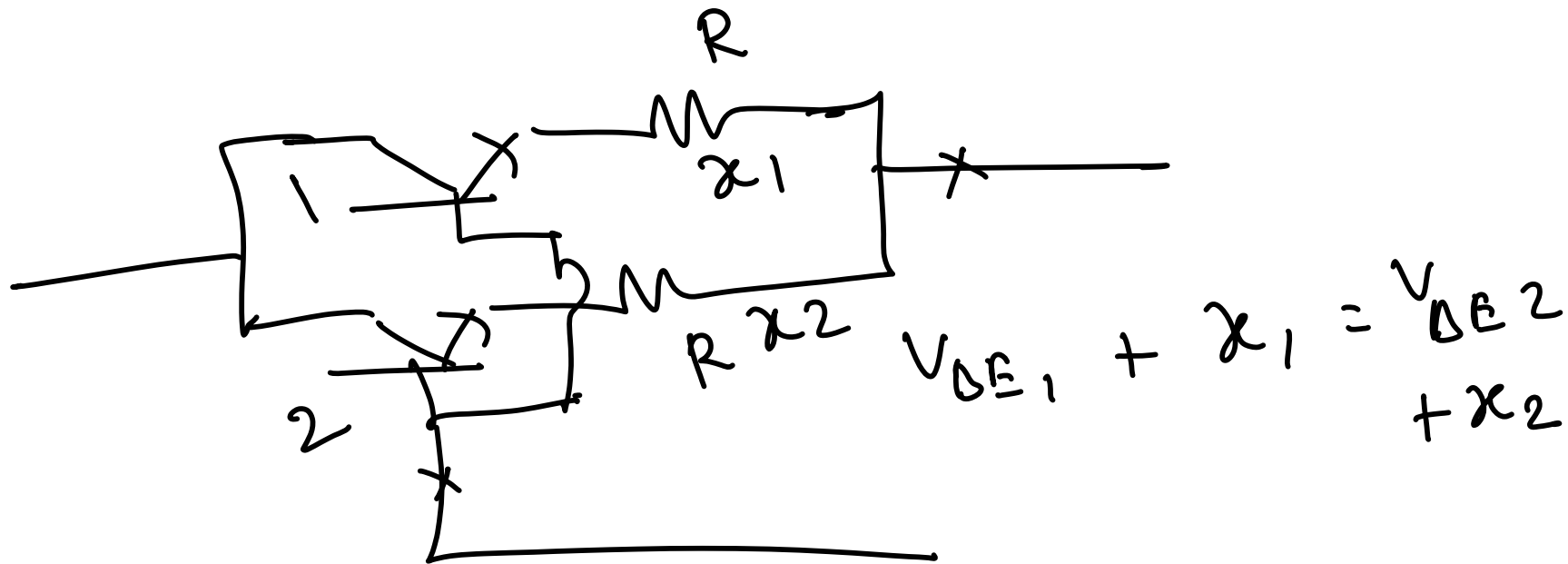




For the same I_c

V_{BE} requirement is different for different transistors.

This difference is ~ 50mV max



If V_{BE1} and V_{BE2} are
different by 50mV

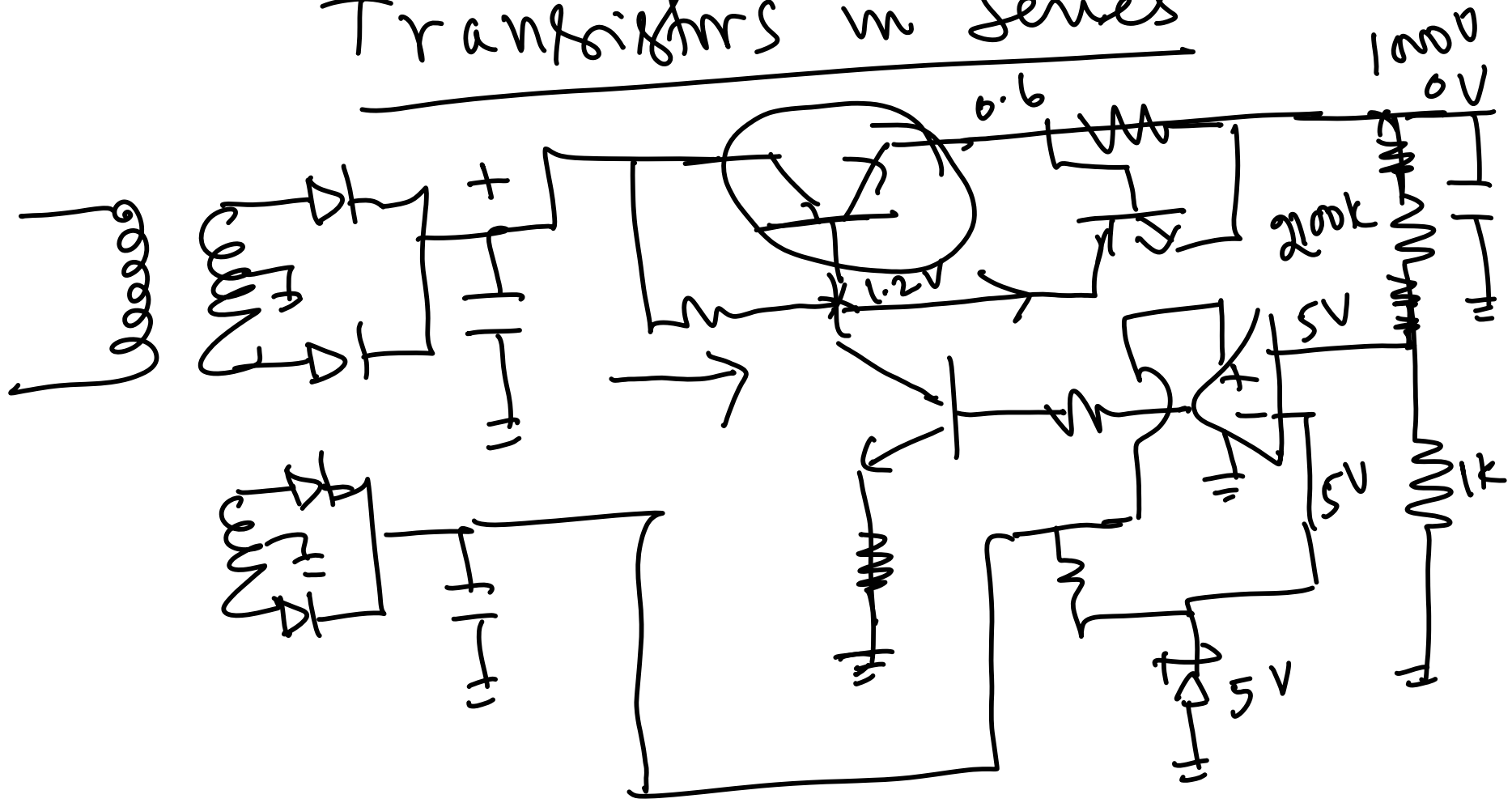
then $\alpha_1 \approx \alpha_2 = 50\text{mV}$

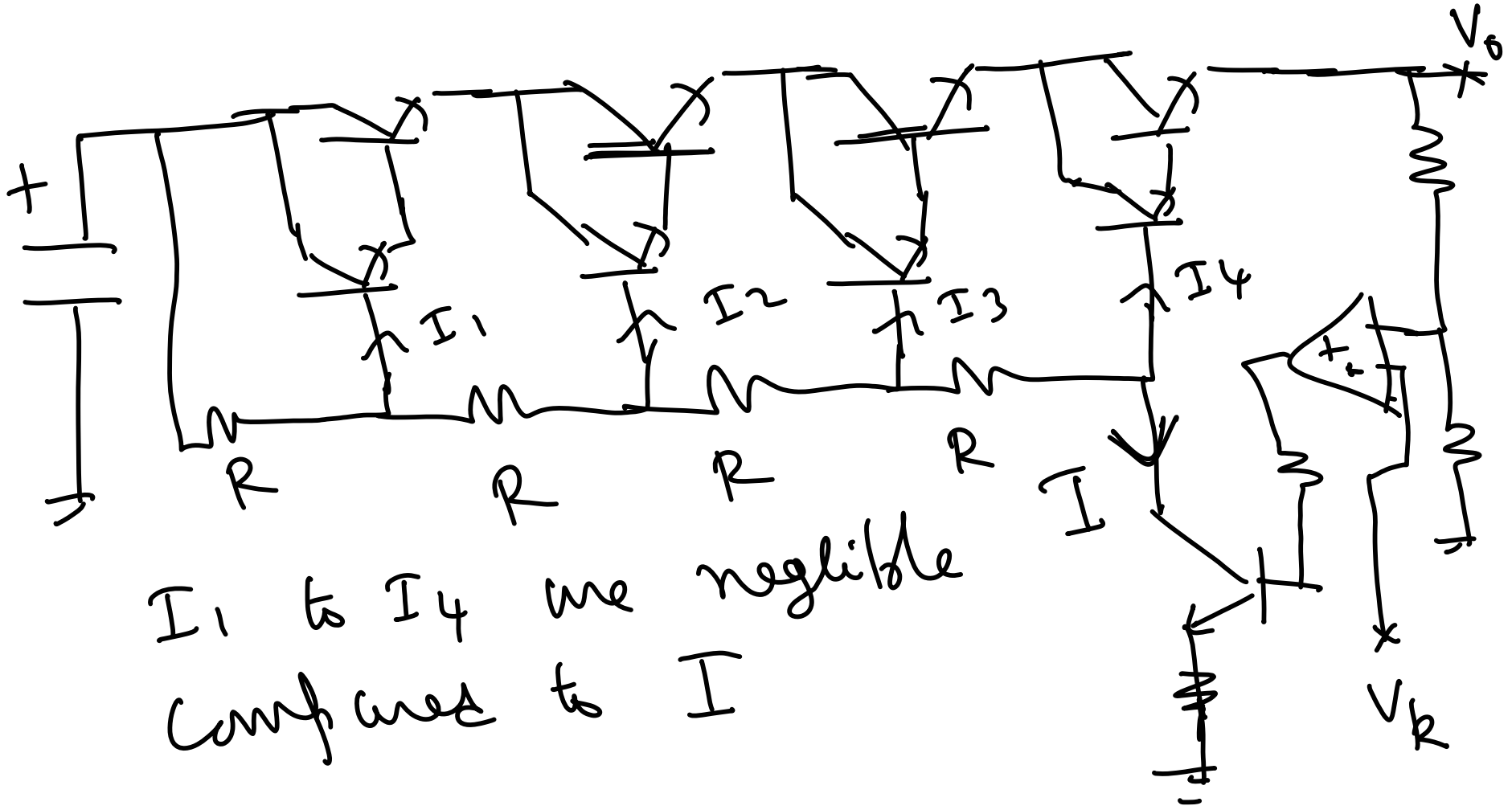
If $R = 1\Omega$

$R I_1 \approx R I_2 = 50\text{mV}$

$I_1 \approx I_2 = 50\text{mA}$

Transistors in Series





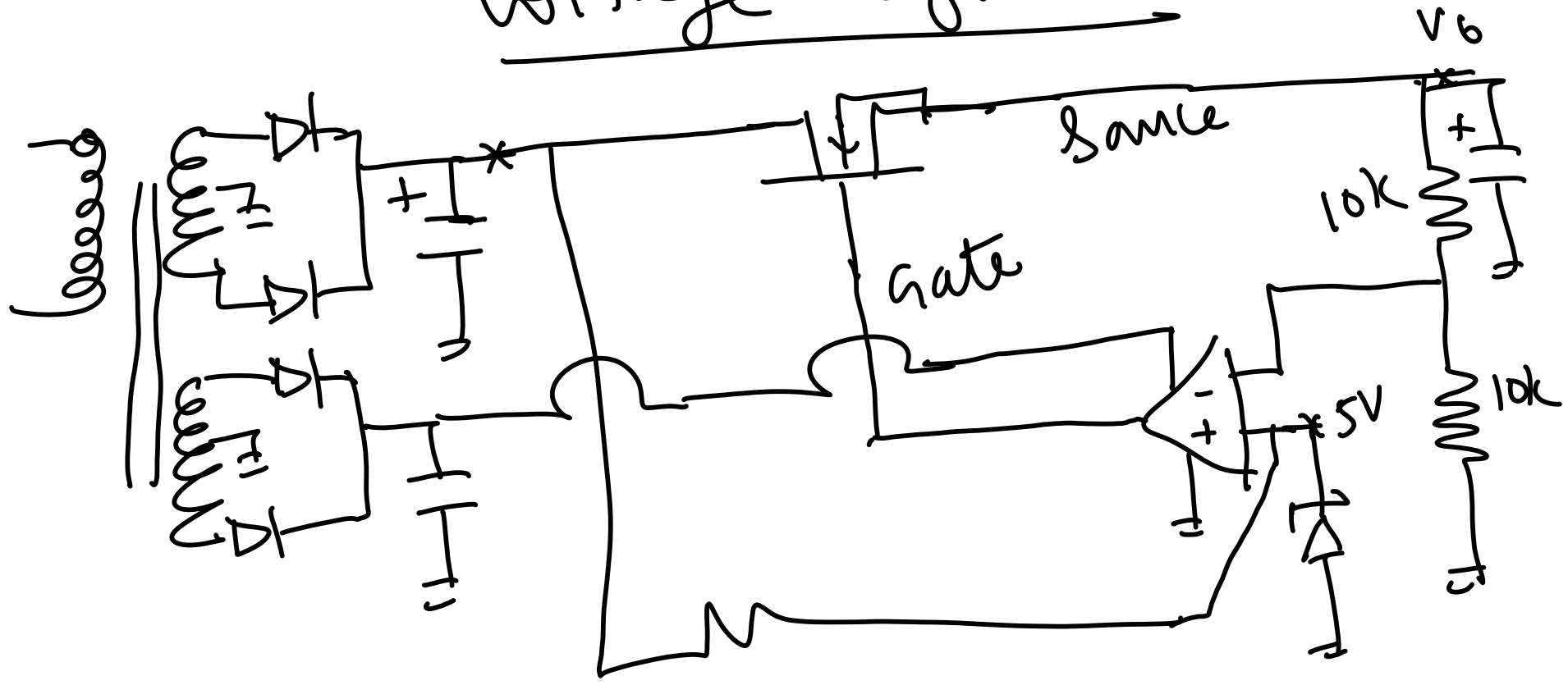
I_1 to I_4 are negligible
 compared to I

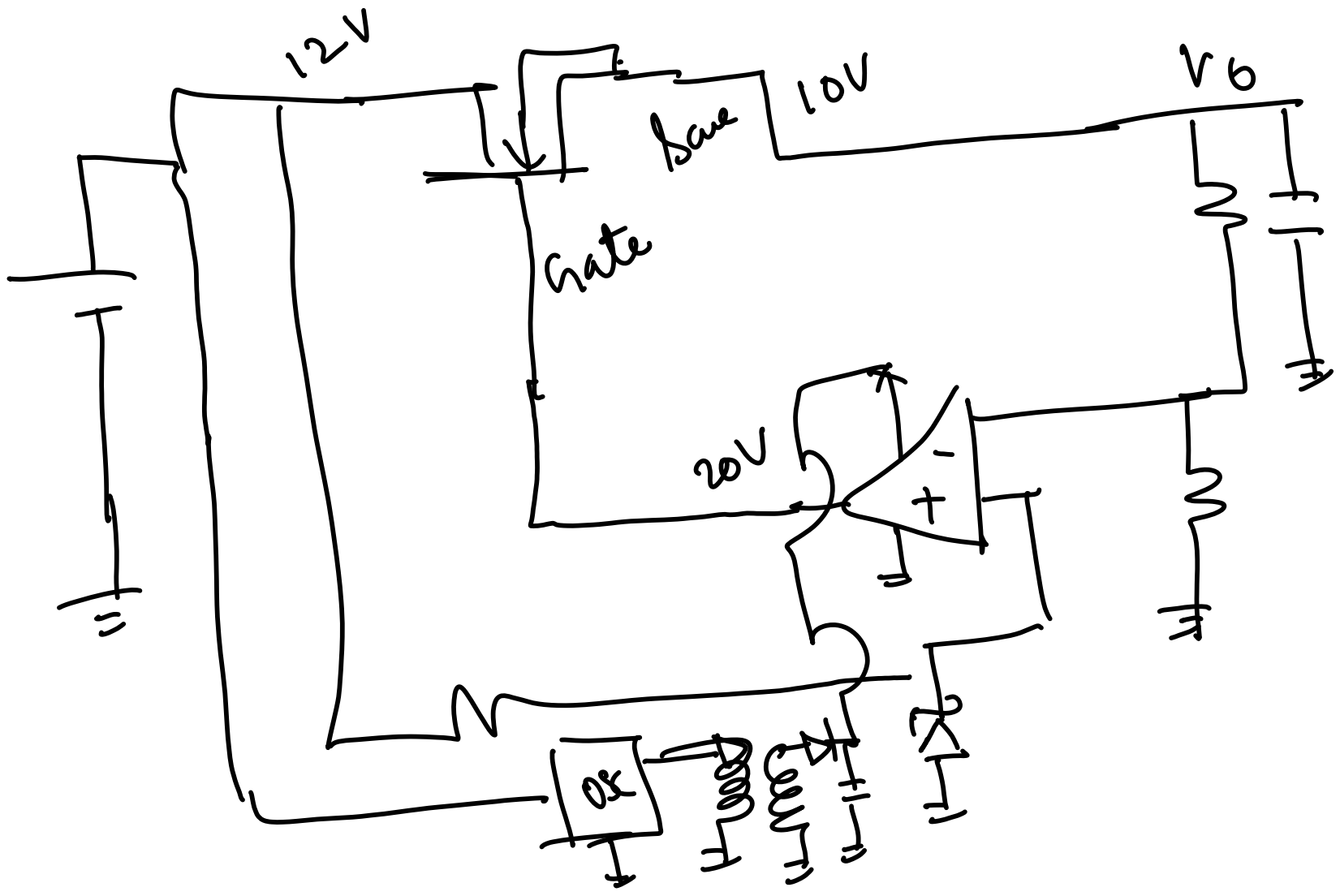
① Connect the transistors in series to boost the capacity of the circuit.

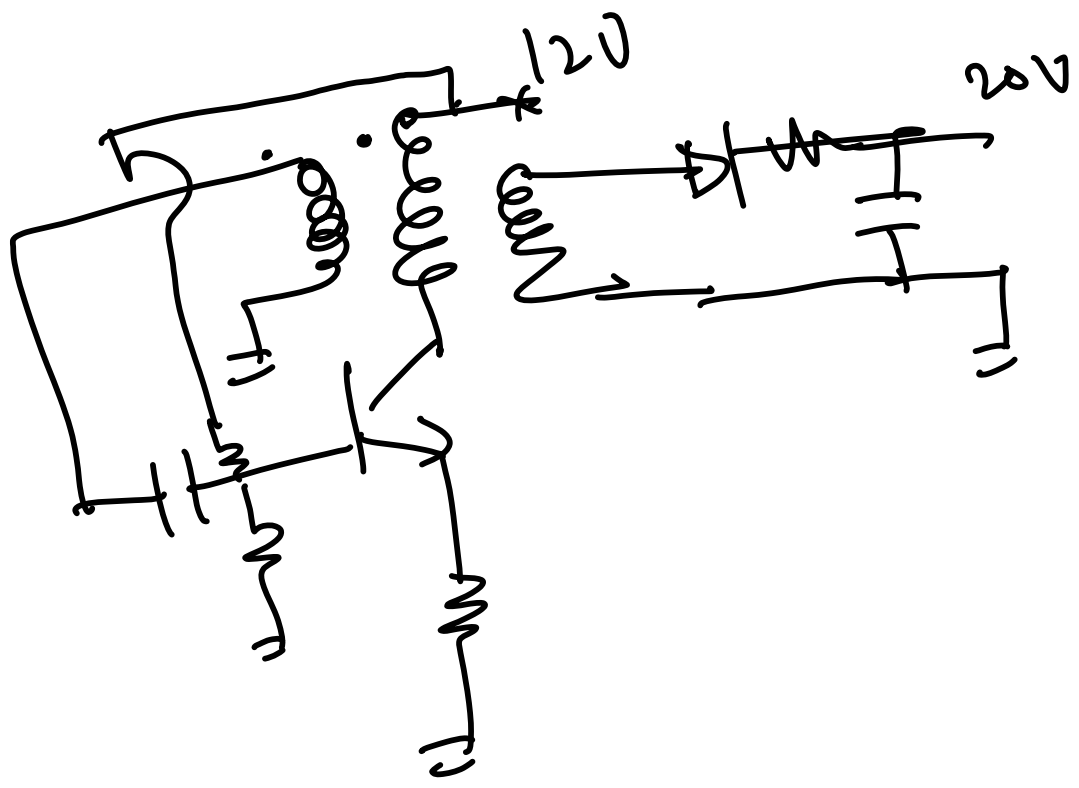
② Connect the transistors in parallel to boost the current handling capacity of the transistors.

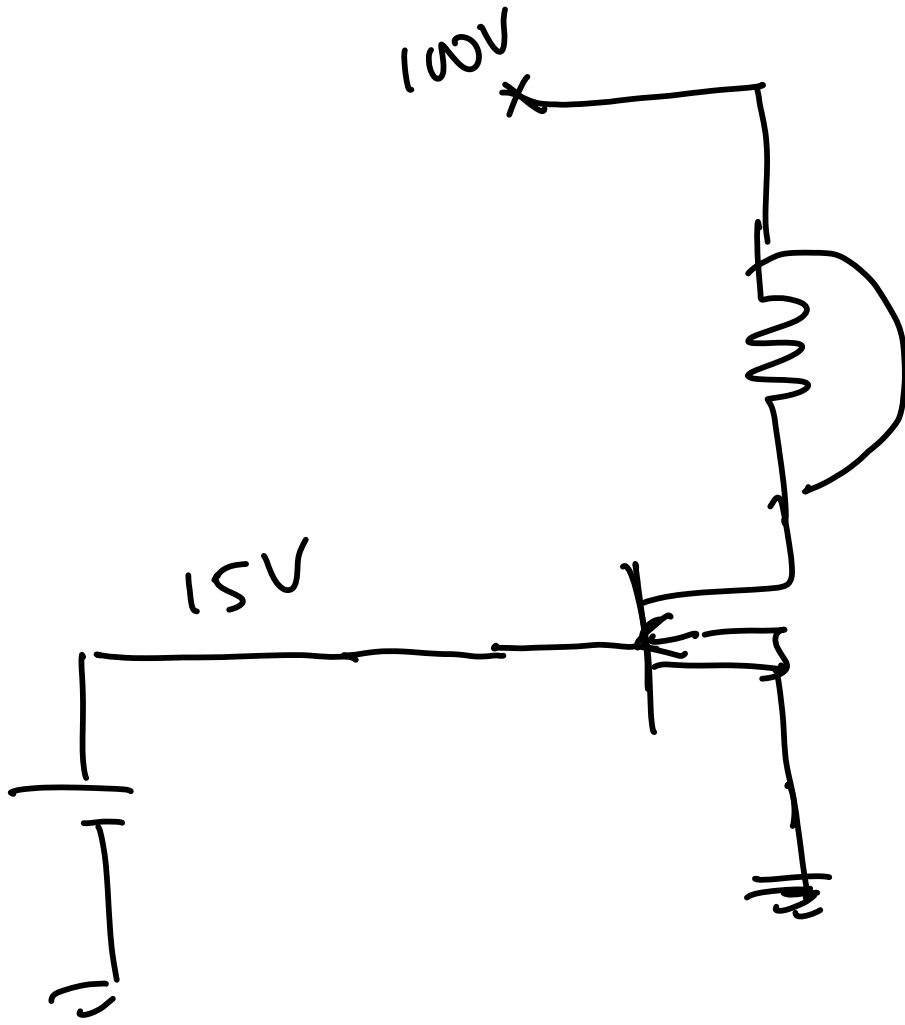
③ Connect the transistors in parallel to reduce the heat dissipation in one single transistor.

Low Drop out voltage regulators

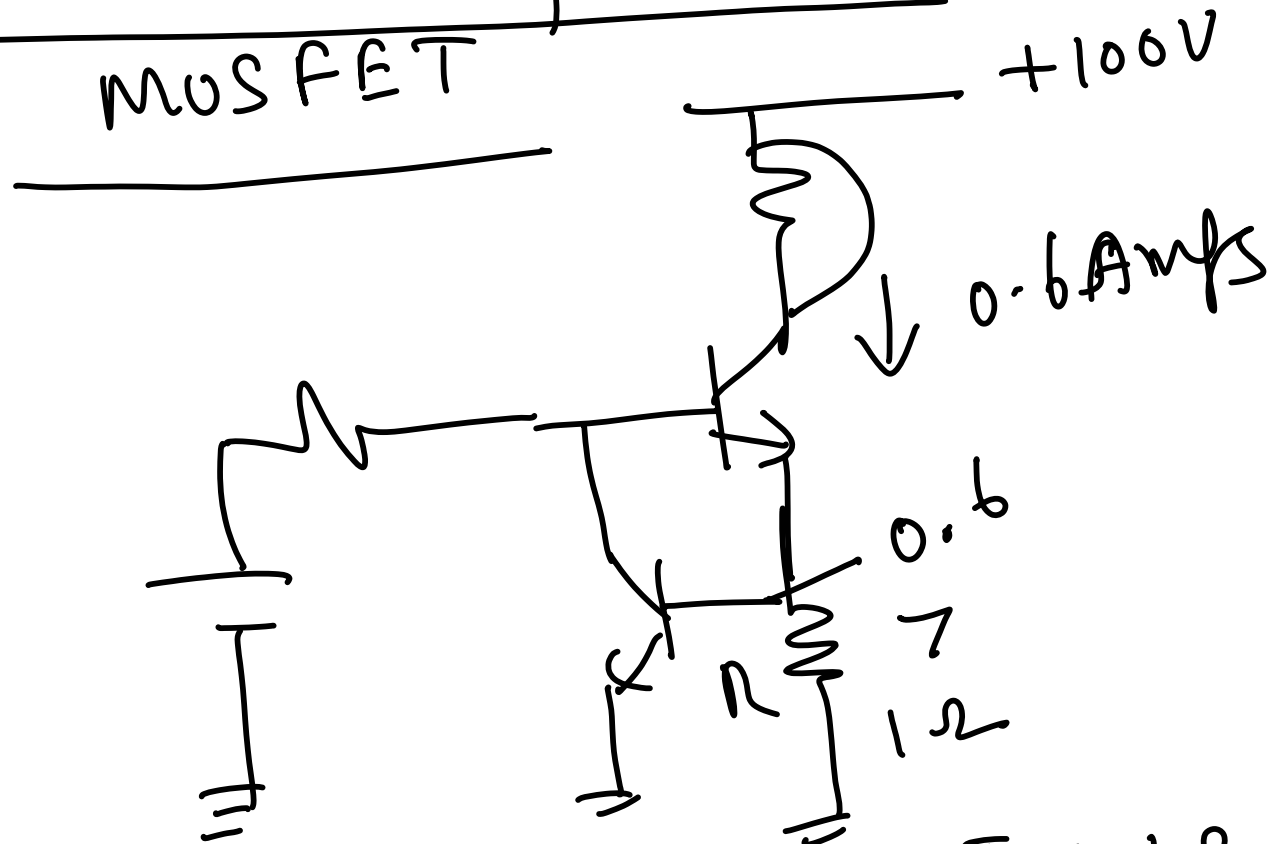








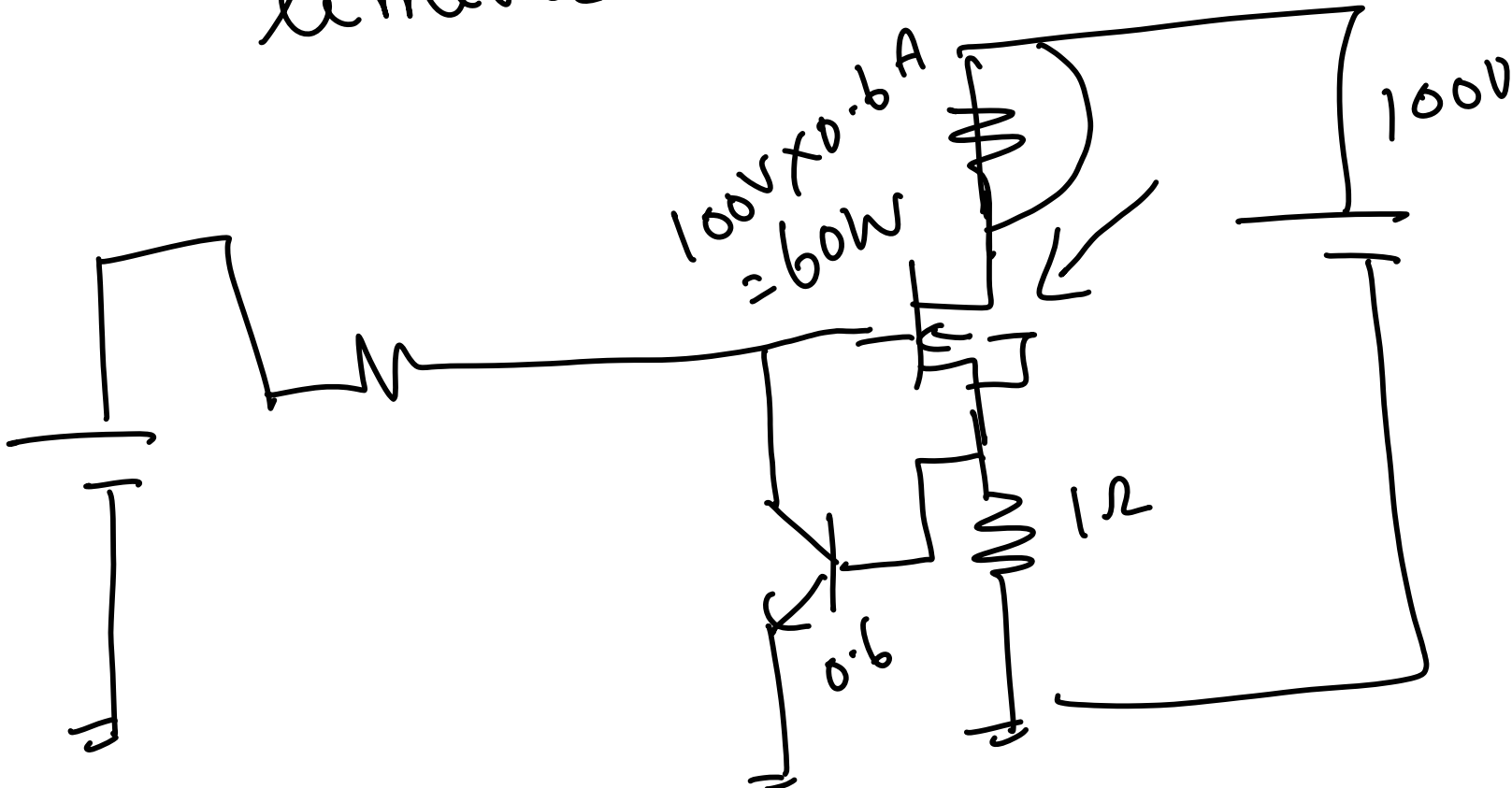
Short circuit protection to MOSFET

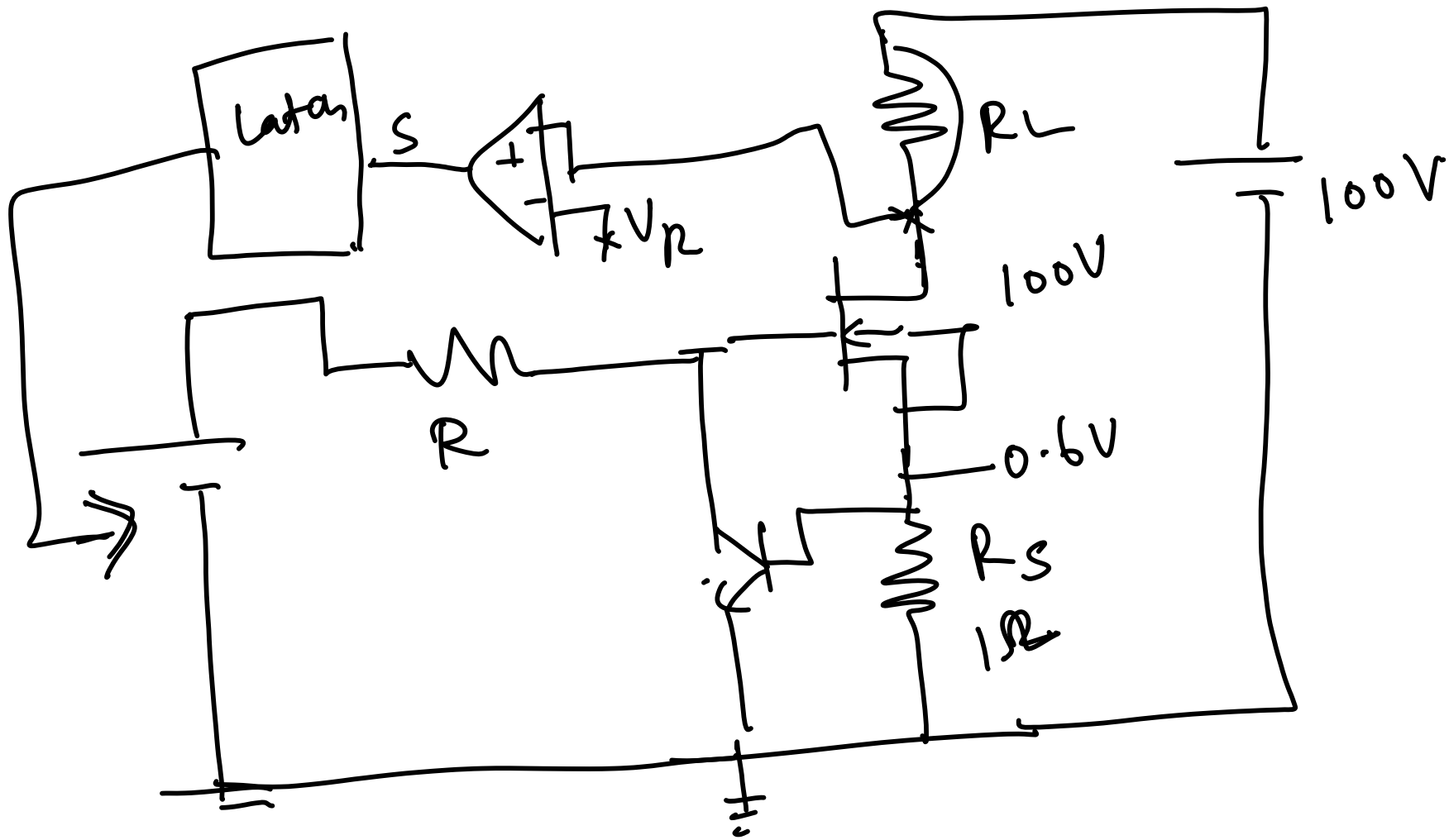


$$V_{BE} = 0.6V = IR = I \times 1\Omega$$

$$0.6 = 1 \times I$$

$I = 0.6 \text{ A}$
Short circuit current is
limited to 0.6 Amps





Resistance measurement

- ① Temperature sensor
 - ↳ PRT
 - ↳ Thermistors
- ② position measurement
- ③ weight measurement
strain gauges

① Very low resistance
measurement
few $m\Omega$ to $\mu\Omega$



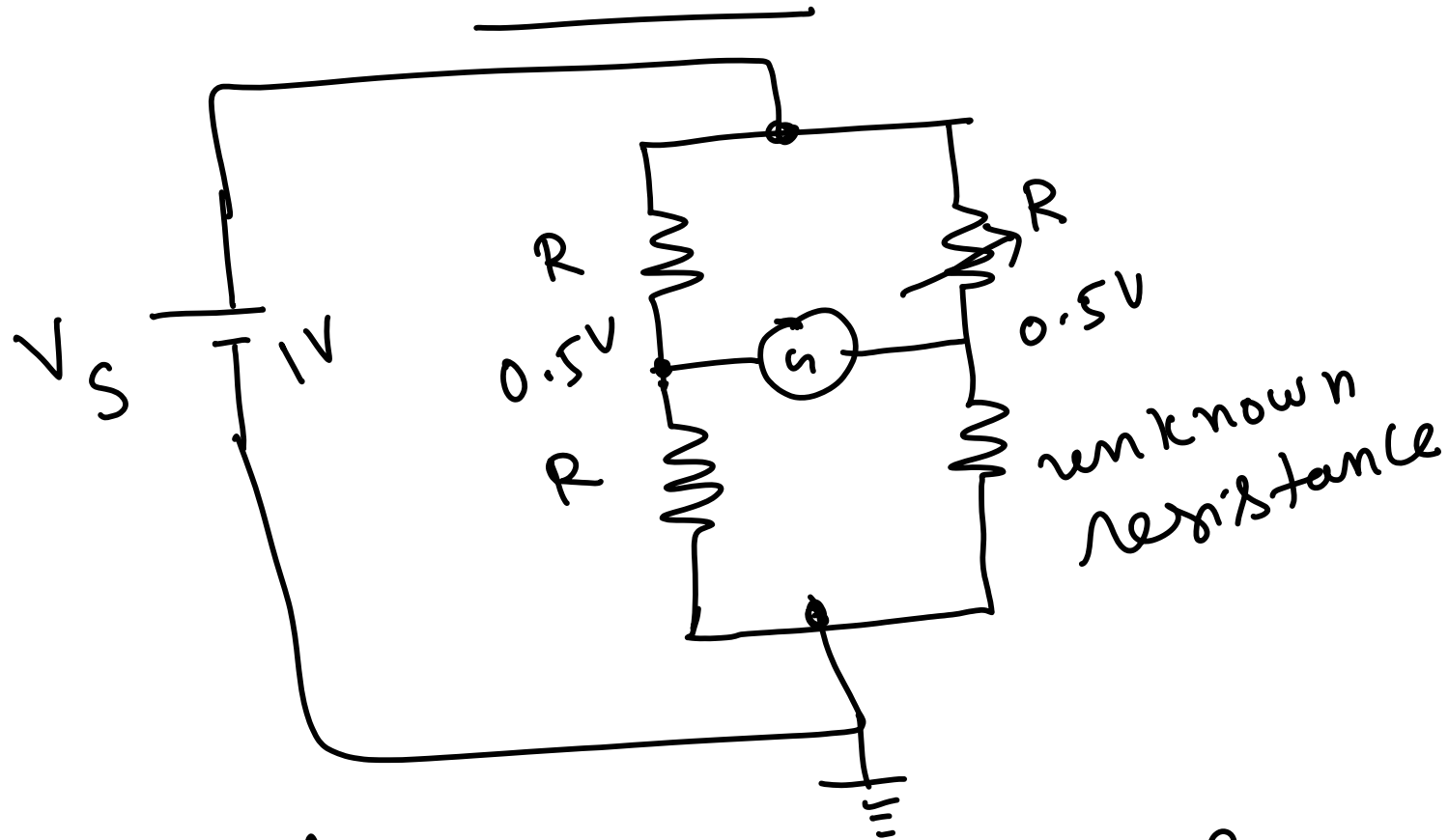
Sample resistance
measurement



② Medium range resistance
measurement
 1Ω - $100k$

③ Very high resistance
measurement
100 k Ω - 100 m Ω

Bridge based resistance measurement



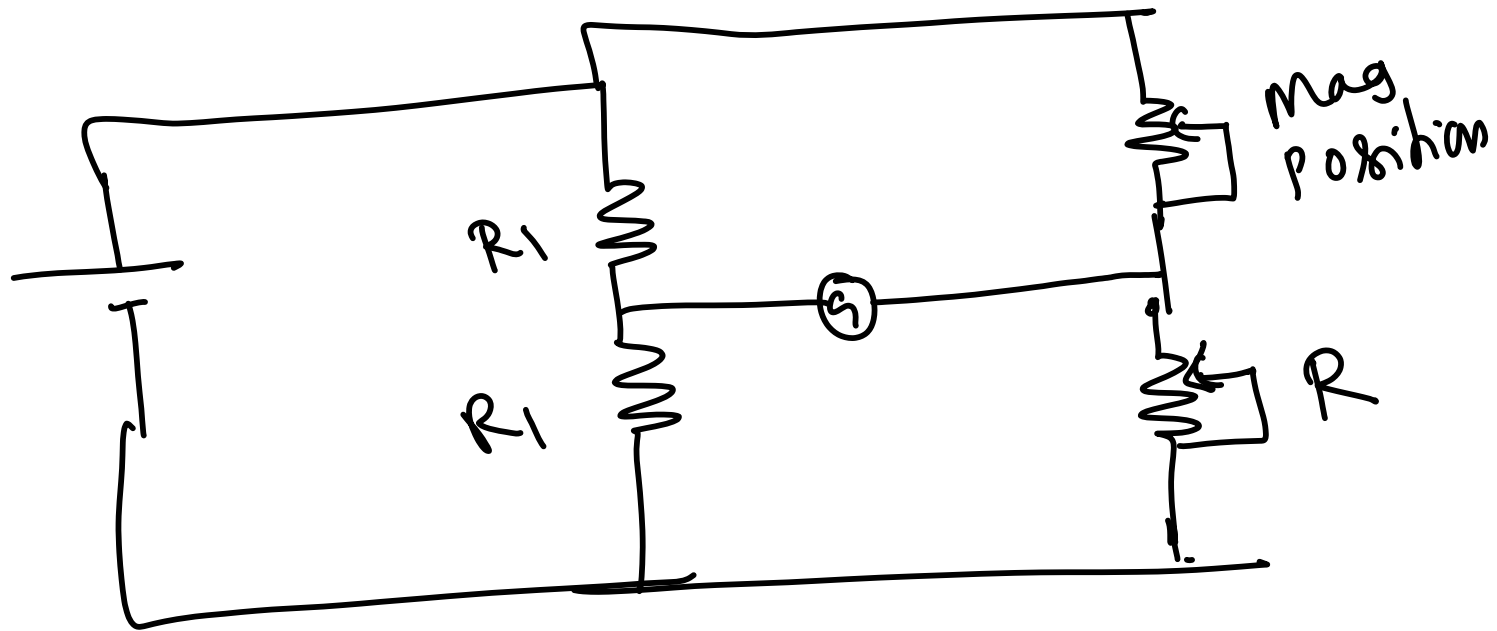
At balance
unknown resistance = R
Temp co-eff of the fixed

Resistors = $10 \text{ ppm}/^\circ\text{C}$

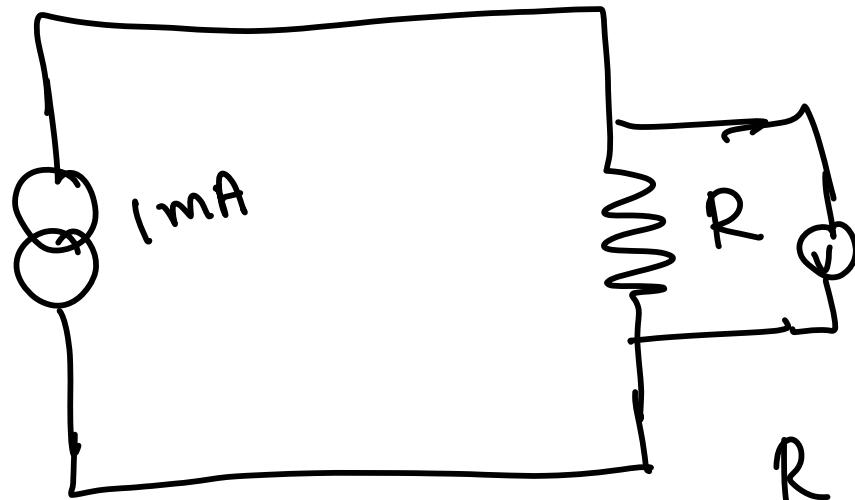
Bridge method gives high accuracy.

- ① All resistors are having same temp co-eff
- ② Bridge excitation voltage will not affect the balancing point

For example for position measurement if potentiometer is used then



Constant current source
based resistance measurement



$$V = RI$$
$$= R \times 1mA$$

$$R = 100 \Omega$$

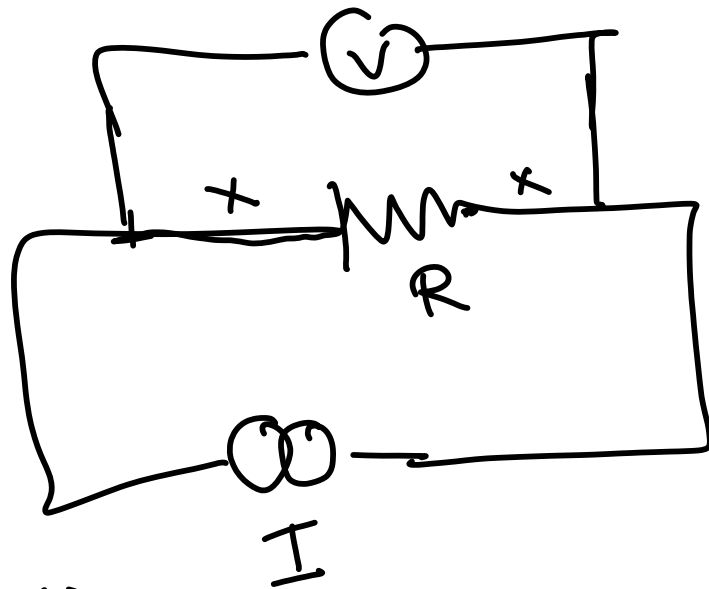
$$V = 100 mV$$

① The error in current
drift or in constant current
source due to ambient
temperature variation makes
the measurement less
accurate

② Error in voltage measurement
also responsible for in accuracy

Low resistance measurement

Range : few $m\Omega$ to few $\mu\Omega$



In very low
resistance

(i)

low

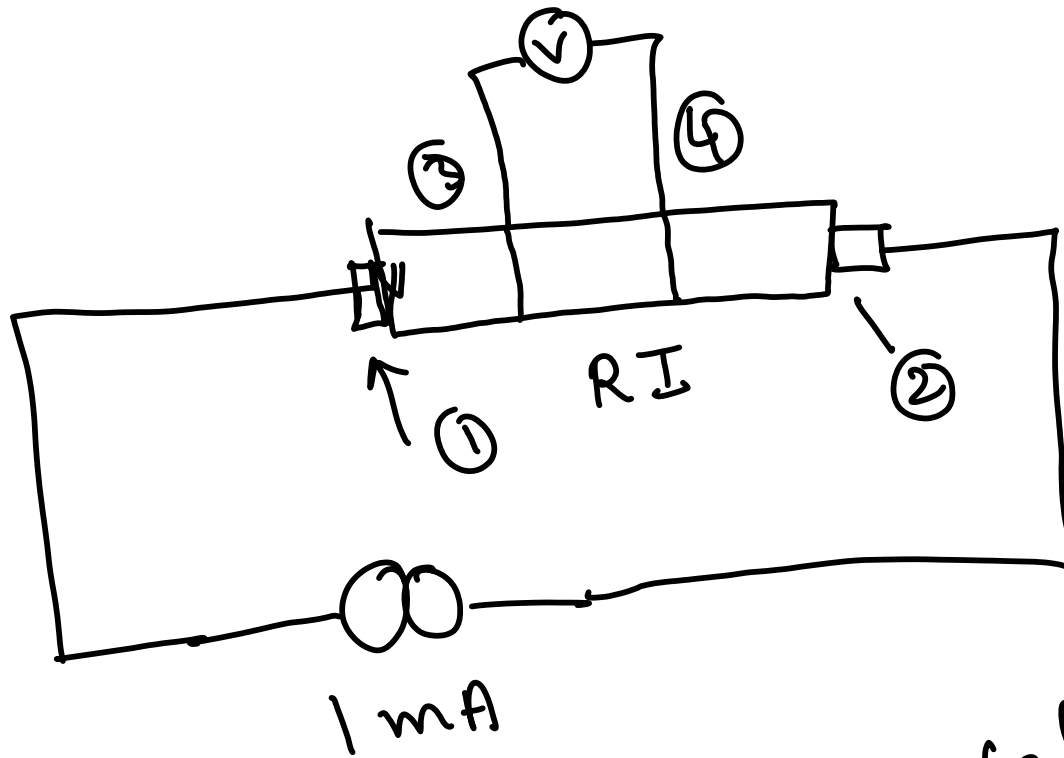
measurement

Contact resistance is added
to the real value

② For very low R
the contact resistance can
give large error

4 - Probe Resistance measurement

① This avoids contact resistance
problem. So it is highly
suited for very low
resistance measurement



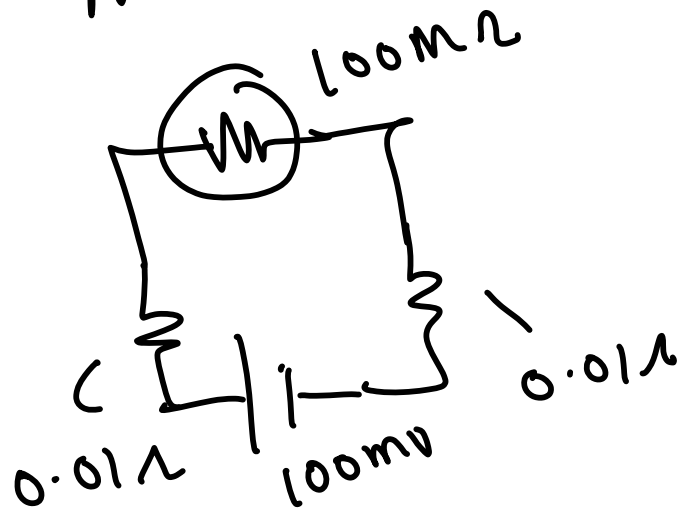
Probes (1) and (2) are called current points
 Probes (3) and (4) can be called voltage points

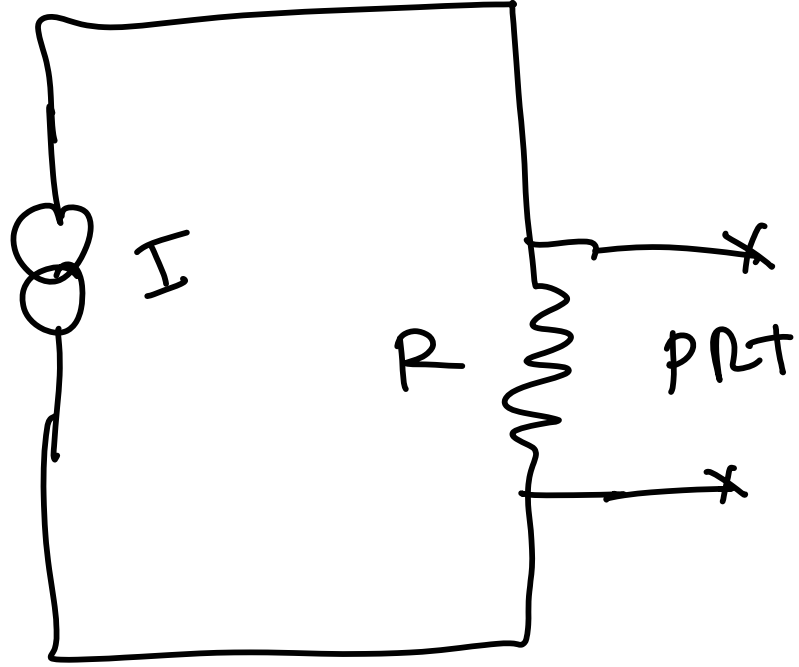
Wattmeter reading = $V = RI$

I is known

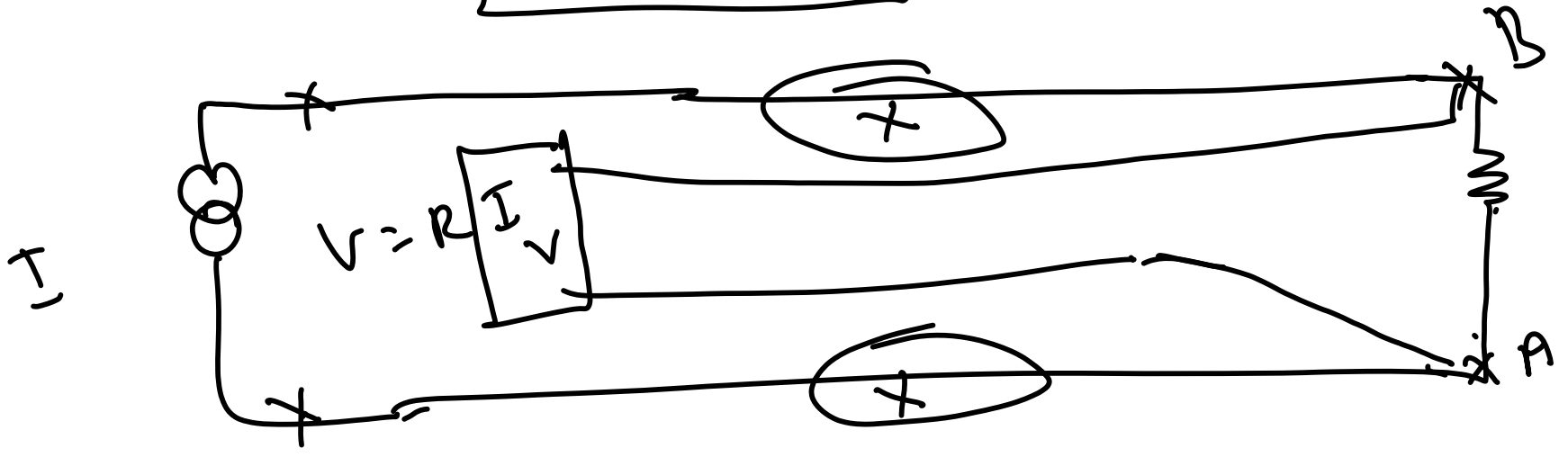
R can be computed

The contact resistance at the
 voltage points (3) and (4)
 will not affect the accuracy



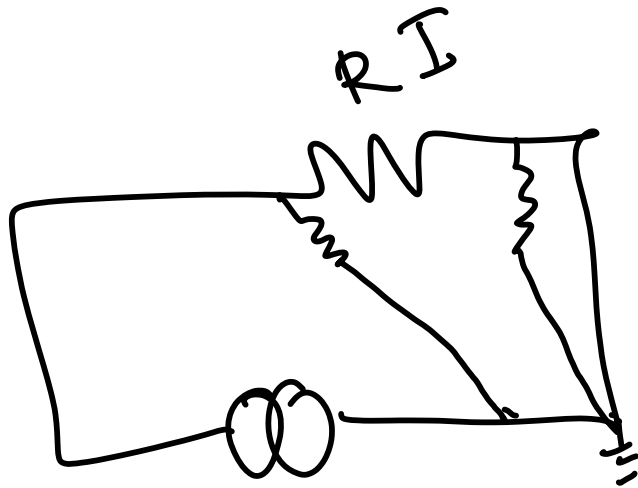


$$RI = V_0$$

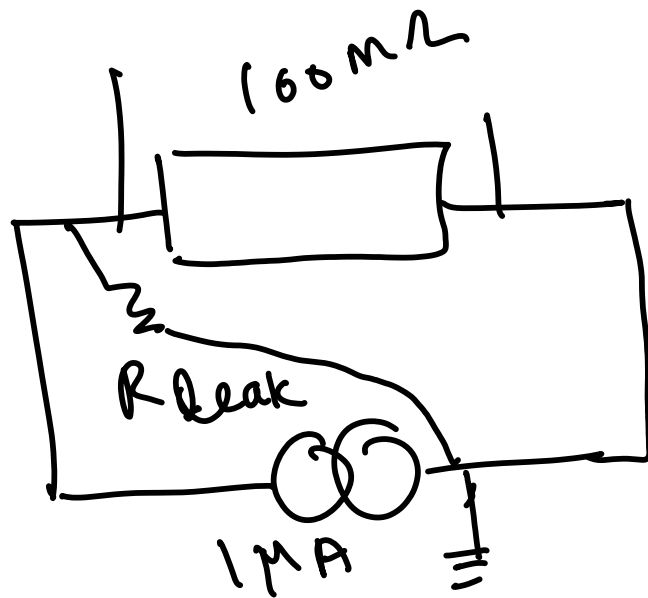


High resistance measurement

Constant current source method is not suitable



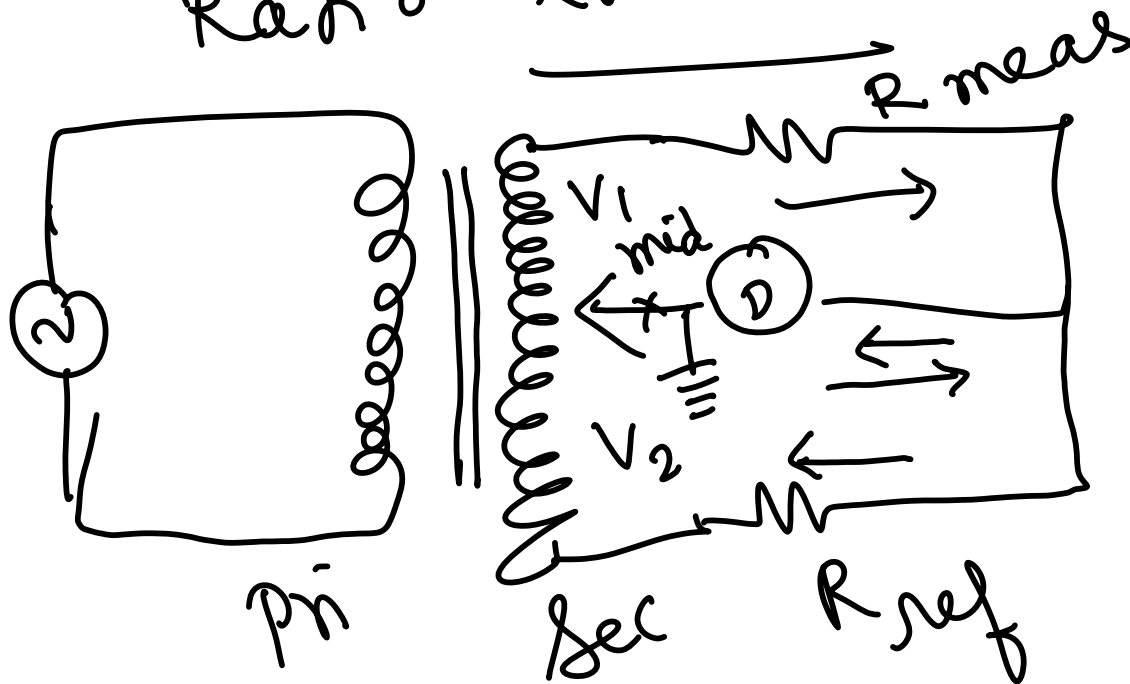
$$10^6 \times 10^{-6} = 1V$$



In high resistance the leakage
 resistance R_{leak} diverts the
 current that is coming from
 the constant current source

This makes system less accurate

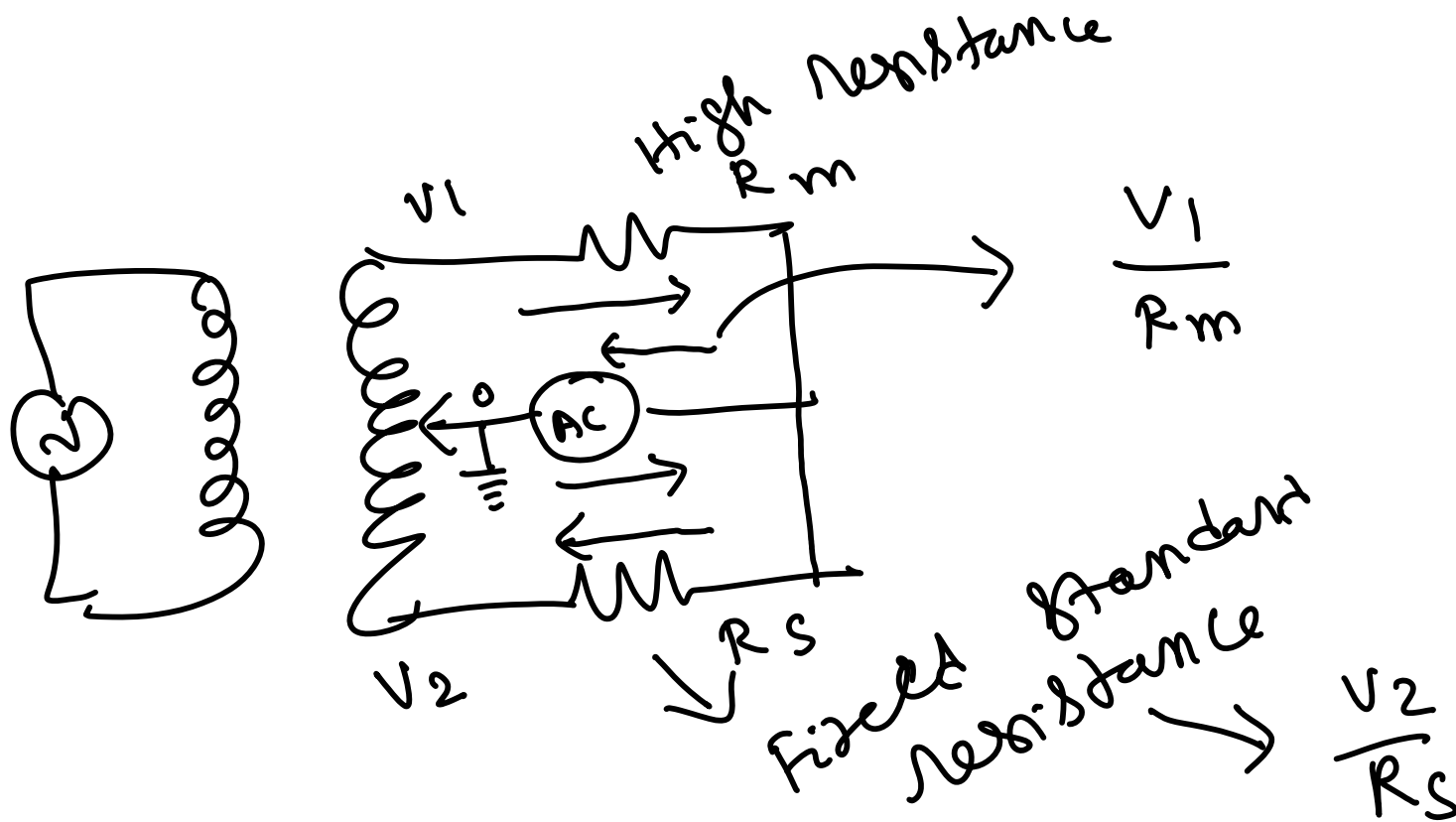
For high Resistance measurement use
Ratio transformer bridge



If the secondary centre tap
is at mid point

Then $V_1 = V_2$

Ratio transformer bridge
for high resistance
measurement



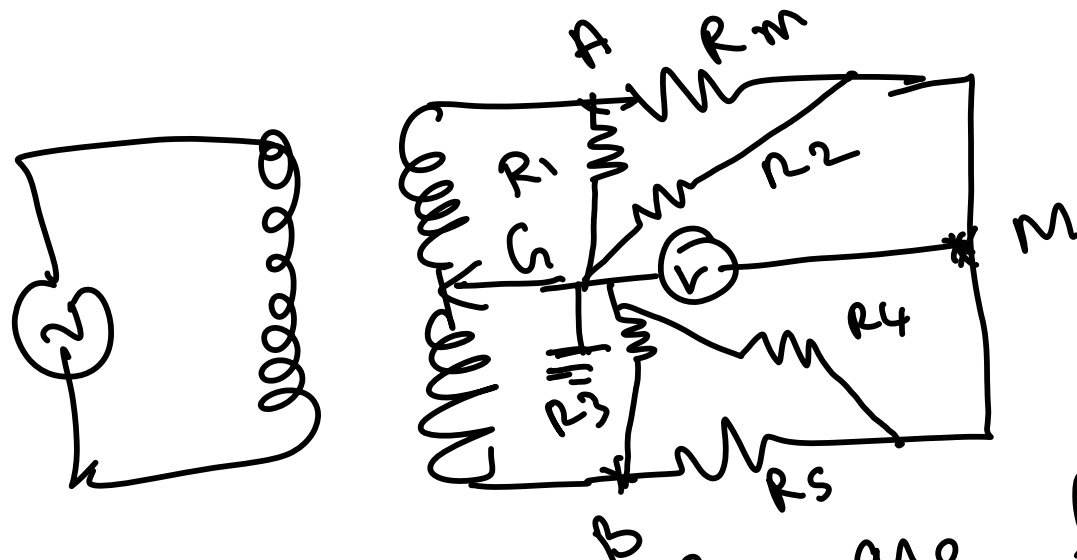
V_1 and V_2 are
 180° out of phase

$$\frac{V_1}{R_m} = \frac{V_2}{R_s}$$

$$\frac{V_1}{V_2} = \frac{R_m}{R_s}$$

R_s is known
 \therefore V_1 and V_2 ratio is

$\frac{V_1}{V_2}$ is known then unknown resistance can be calculated



R_1, R_2, R_3, R_4 are leakage resistances
These resistances are not

contributing for the balance
why?

Wt acc $R_2, R_4 = 0$
at balance

So no current is flowing
through R_2, R_4 at balance
so it is not affecting the
bridge balance

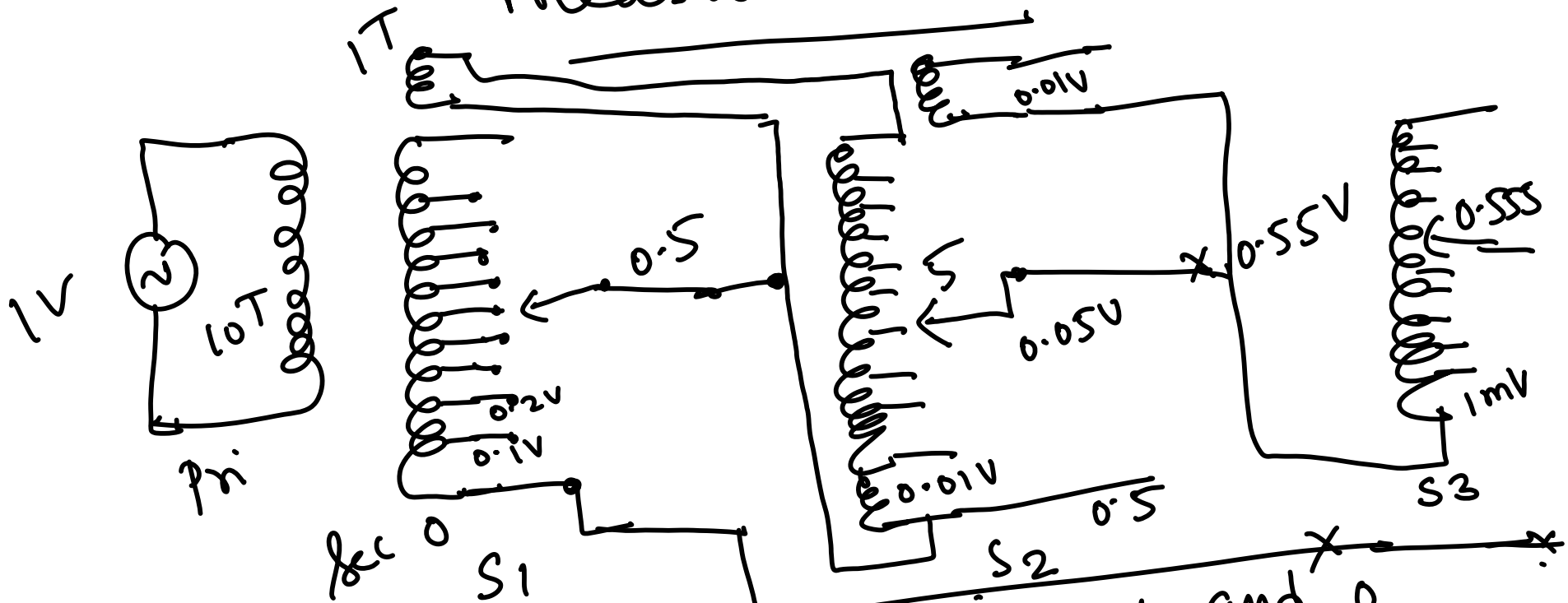
R_1, R_3 are just loading
the secondary of the transformer
but output impedance of the
transformer is way low

So the loading of R_1, R_2
will not change V_1, V_2 .
So no effect on the balance
of the bridge.

$$\frac{V_1}{V_2} = \frac{R_m}{R_s}$$

If V_1 and V_2 are measured
using a meter, then meter error
involved in this measurement
also to be considered.

How to avoid V_1, V_2 measurement?

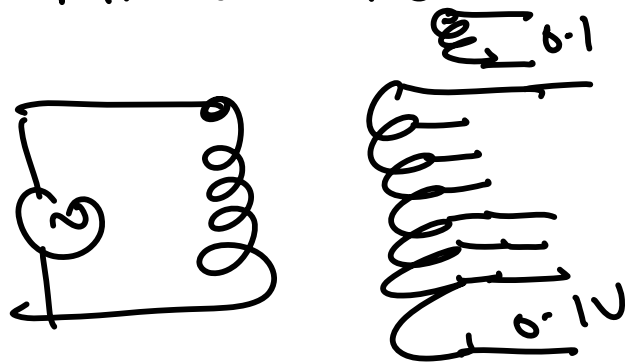


There are 10 T in the primary and 100 in the secondary.

So for 1V primary the vol acc each turn of secondary = 0.1V

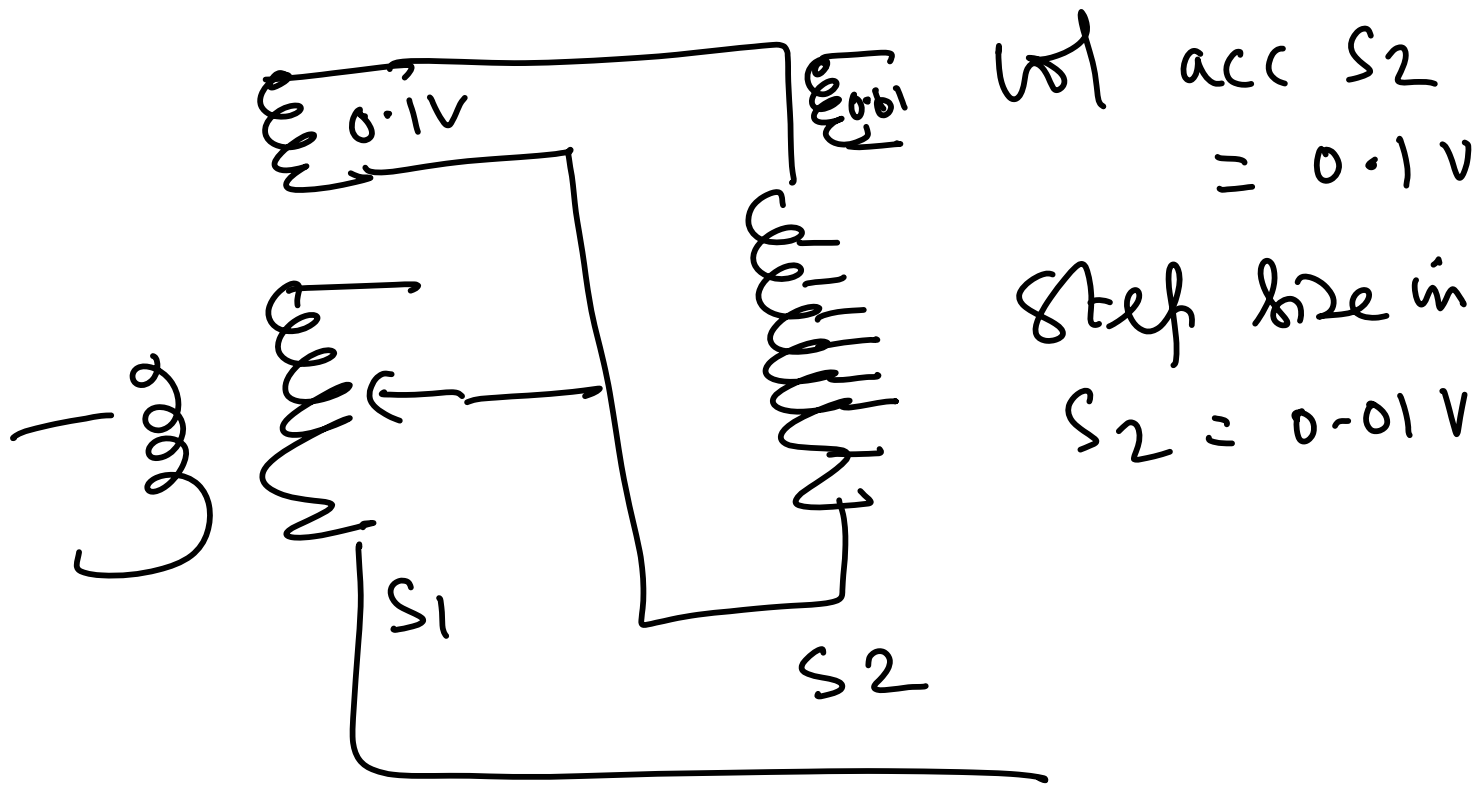
① For 3 digit accuracy
use 3 secondaries in the
ratio transformer

First secondary V is 1V

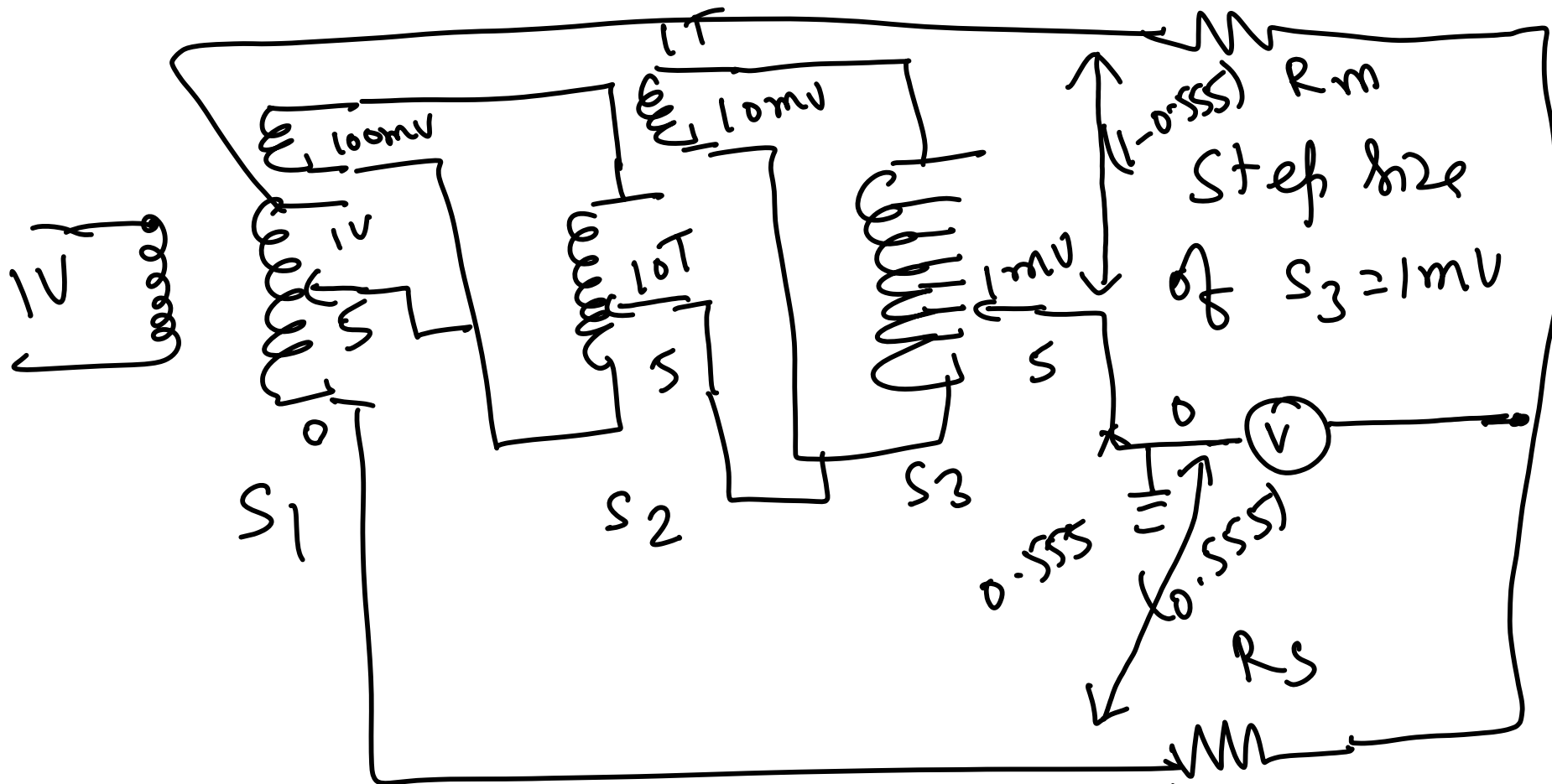


The step size
is 0.1V

The S_1 auxiliary winding is
having 0.1V



The auxiliary winding of S_2 is having vol of ~~10~~ 10 mV
 This winding of 10 mV is connected to the 3rd winding S_3



① The excitation voltage is not applied to the primary changes then also the measurement is accurate

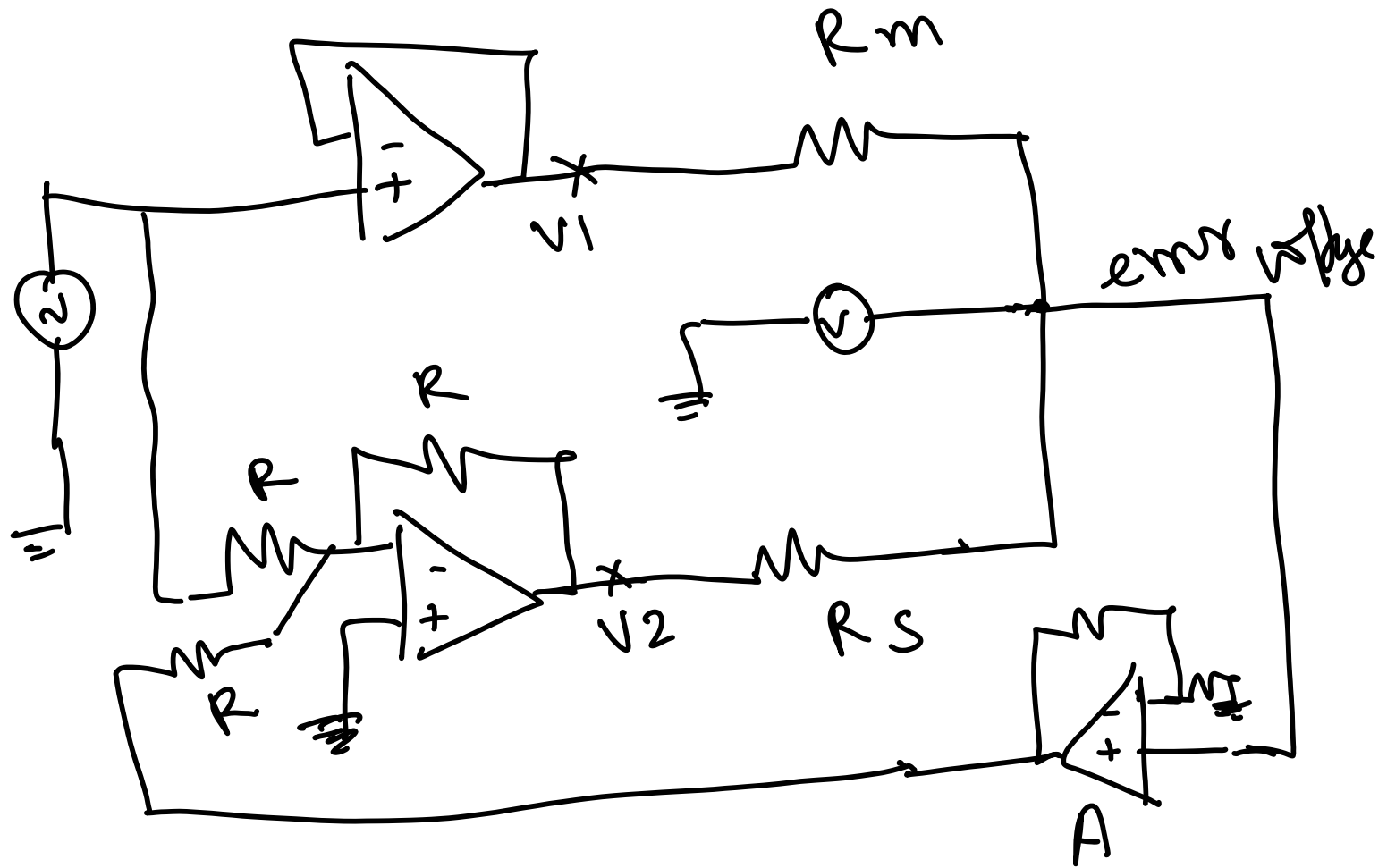
Because the vol charge
in the primary affects
proportionally all the secondaries
So the ratio $\frac{V_1}{V_2}$ is not
changing.

② The voltmeter used for
balancing will not affect
the measurement, even if it is
not calibrated.
This is because it is a null
method.

① This method is good for high resistance measurement $> 10\text{ k}$ up to several $100\text{ m}\Omega$

② This is not good for low resistance measurement, because the current drawn from the transformer secondary will produce w/ errors.

This - advantage : Manual balancing is required



If the gain of the amplifier A is high then bridge will get balanced automatically.

This is because

V_2 is changing in a
opposite way to the
error voltage

So V_1 and V_2 ratio is
adjusted automatically to
balance the bridge

$$\frac{V_1}{V_2} = \frac{r_m}{r_s}$$

But V_1 and V_2 must be
measured.

The error in the measurement
of V_1 and V_2 affects the

Resistance measurement.

So it is not as accurate as ratio transformer bridge

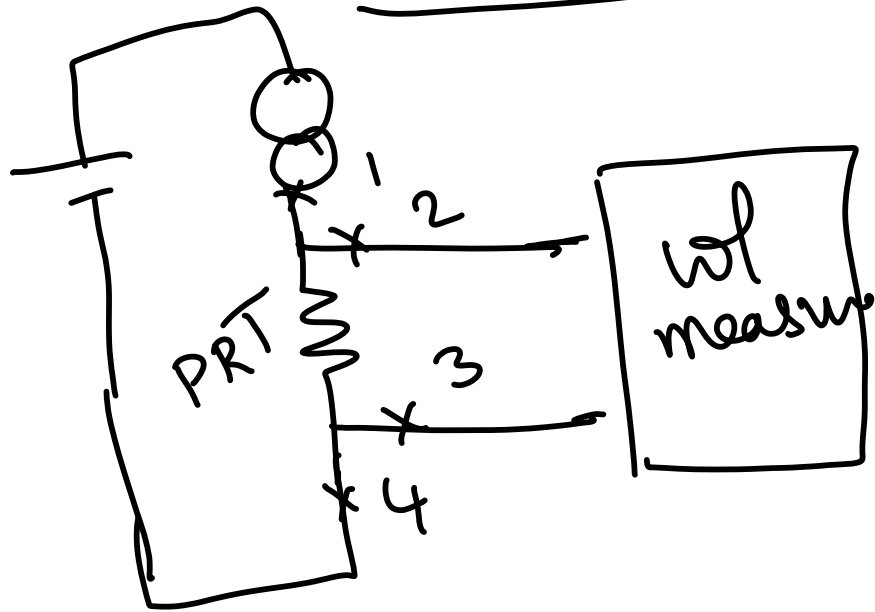
Drawback: If the θ of amp introduce phase shift error then measurement will not be accurate

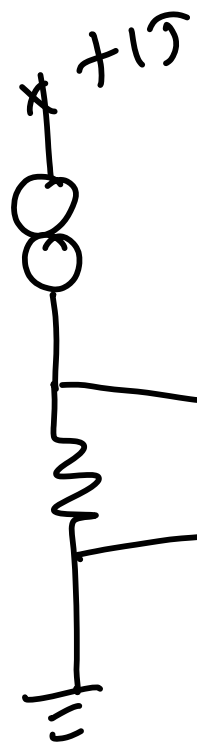
The phase shift introduced by the θ of amps must be very small

So high band width of amp stage is required. or use several of amps with low gain from each stage

For low frequency
measurement say few Hz
then phase shift is not
a problem.

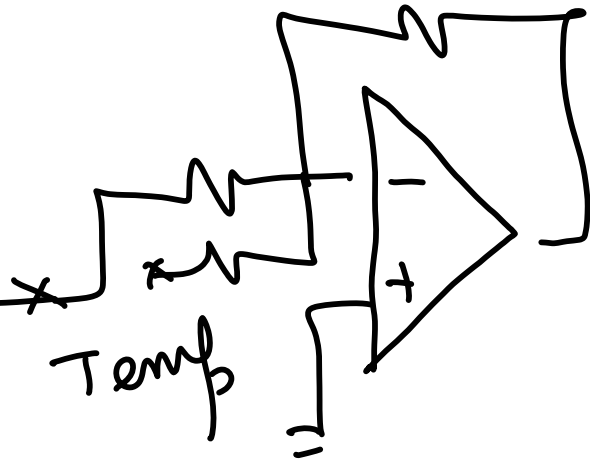
Platinum Resistance Thermometer





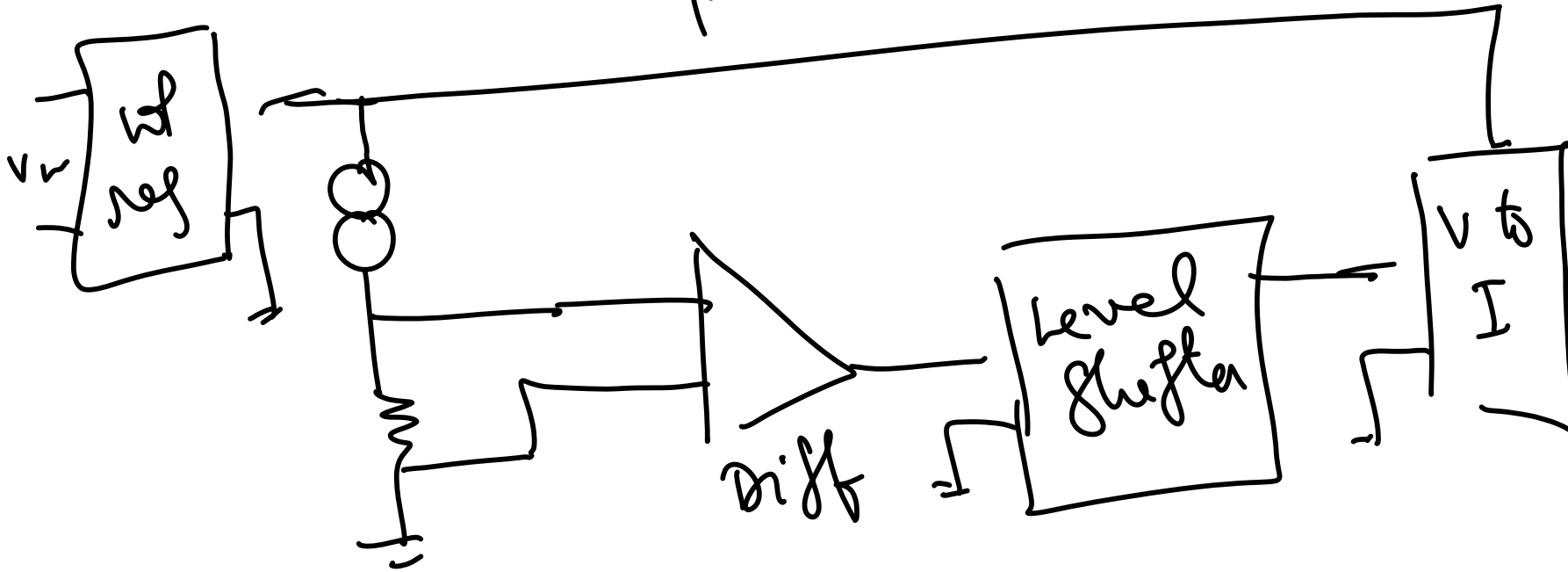
Case - 1

voltage based measurement



Case - 2

4-20 mA current based
Temperature measurement



4-20 mA Temperature Transmitter using PRT

INPUT : $\pm 24V$ DC

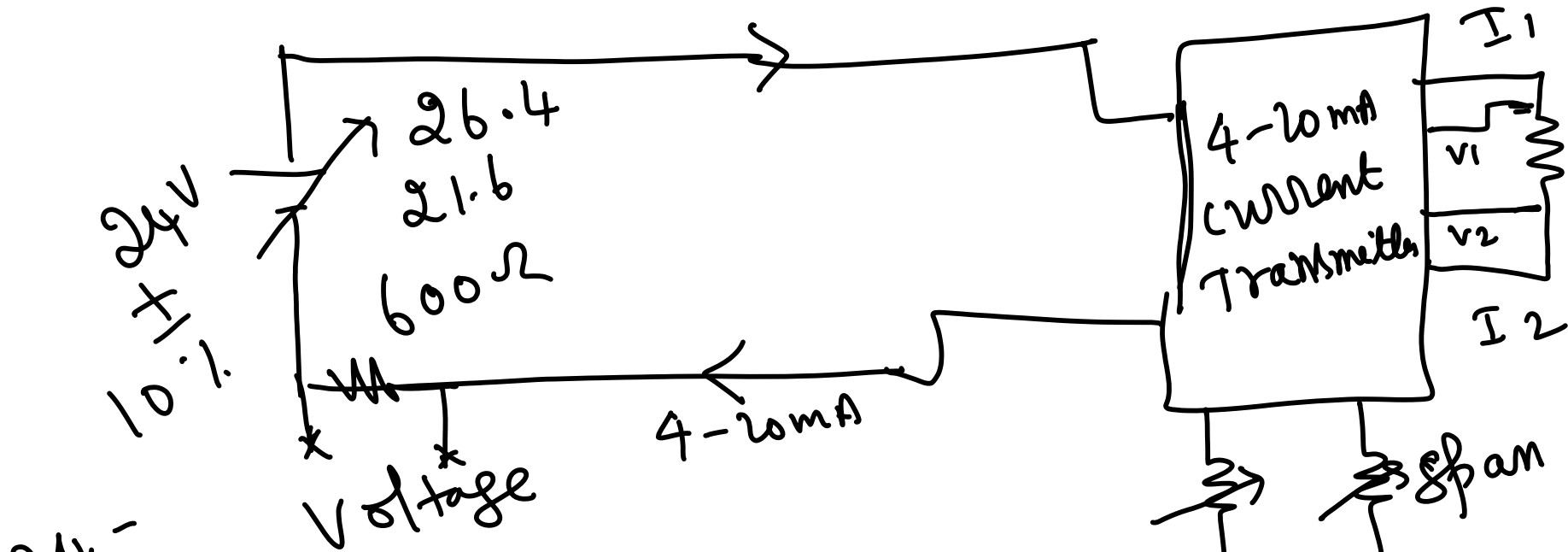
OUTPUT : 4-20 mA current

Transducer = PRT

Temp range : 0 to $400^{\circ}C$

Ambient temp range : $-20^{\circ}C$ to $80^{\circ}C$

Accuracy : $\pm 1\%$



$$\frac{24 - 2.4}{21.6}$$

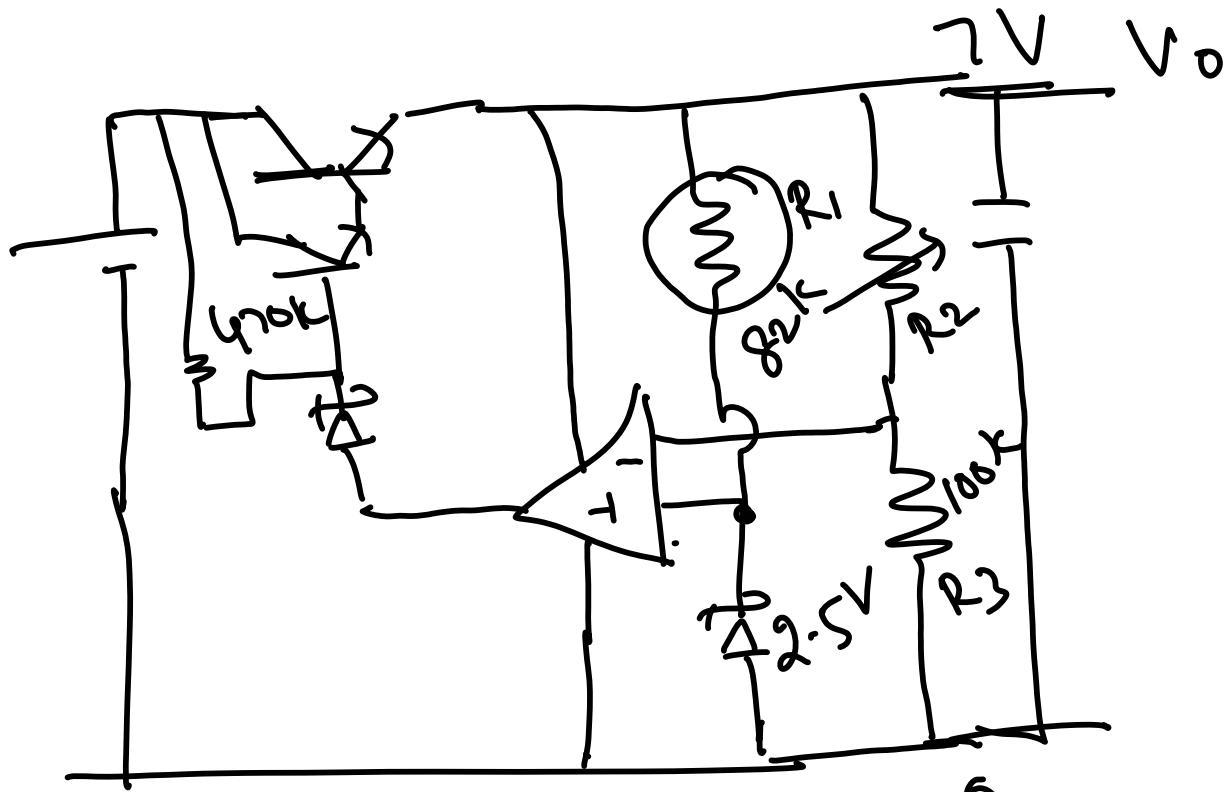
At 0V → I → 4 mA
 At 4V → I → 20 mA

At 0V → $600 \times 4 = 2.4V$
 At 4V → $600 \times 20 = 12V$

① Supply voltage variation
21.6 to 26.4 v

② Load variation
0 to 600 Ω

So the variation of the load
and the variation in the 24v
supply varies to available
voltage to the
transmitter current



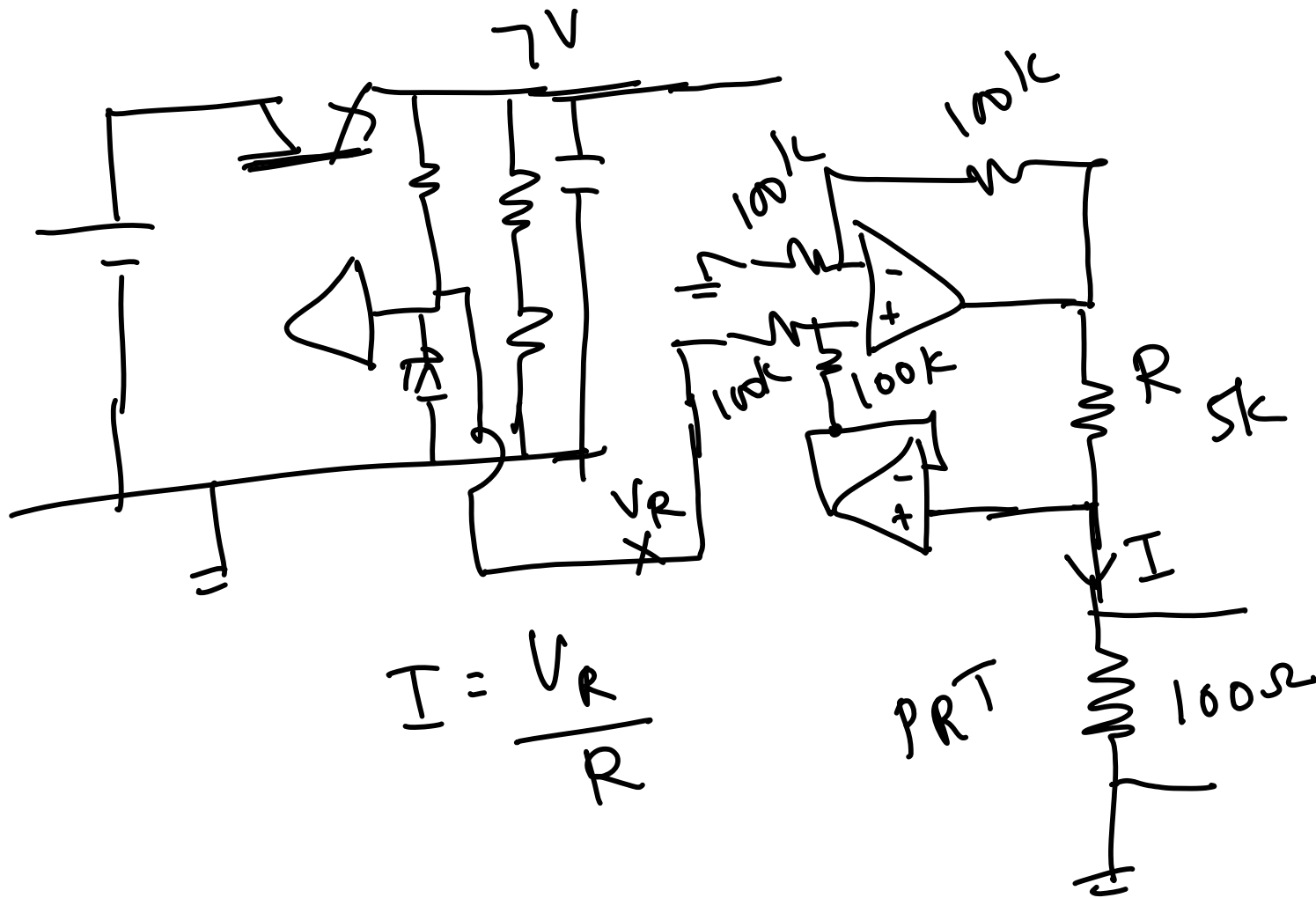
$$R_1 = \frac{(7 - 2.5) \times 50 \times 10^6}{82 \times 10^3} = \frac{4.5 \times 10^6}{82} \approx 55 \text{ k}$$

W/ acc $R_3 = 2.5 \text{ V}$

$$I = \frac{2.5}{R_3}$$

$$V_o = \frac{2.5}{100k} (100k + R_2)$$

R_2 can be calculated

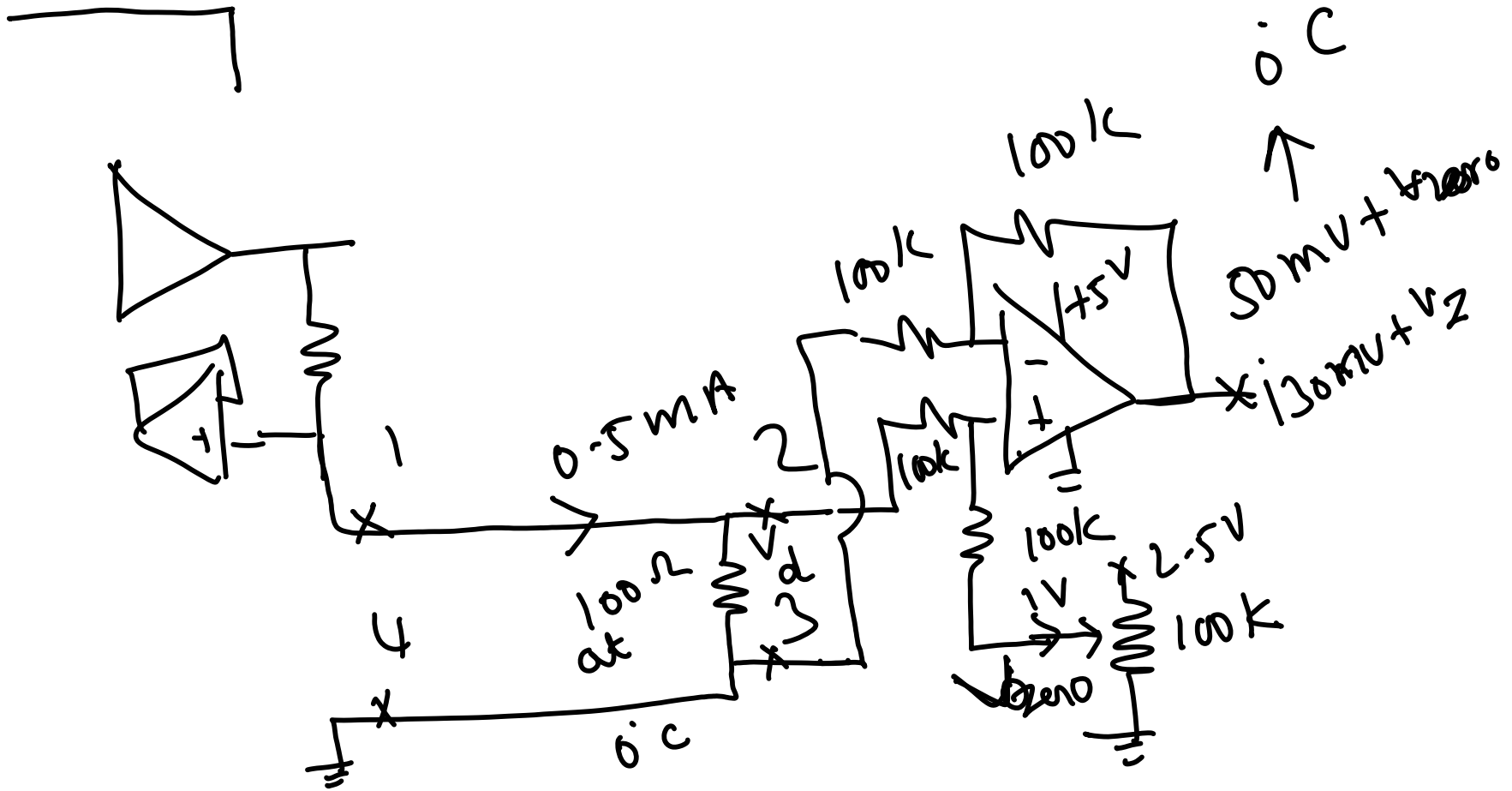


$$I = \frac{V_R}{R}$$

$$I = 0.5 \text{ mA}$$

$$I = \frac{2.5 \text{ V}}{R} = 0.5 \times 10^{-3}$$

$$R = \frac{2.5 \times 10^3}{0.5} = 5 \text{ K}$$



$$\begin{aligned}
 V_o &= V_d + V_{\text{zero}} \\
 &= 50\text{mV} + 1\text{V} \\
 &= 1.05\text{V}
 \end{aligned}$$

So by adjusting the zero pot we can vary the output voltage

PRT resistance value
at i_c = $100\ \Omega$

PRT resistance at
 4mA = $100\ \Omega + \frac{0.4 \times 400}{100} \times 100$
= $260\ \Omega$

At 0°C PRT Res

$$= 100 \Omega$$

W/ acc PRT = $100 \times 0.5 \text{ mA}$
= 50 mV

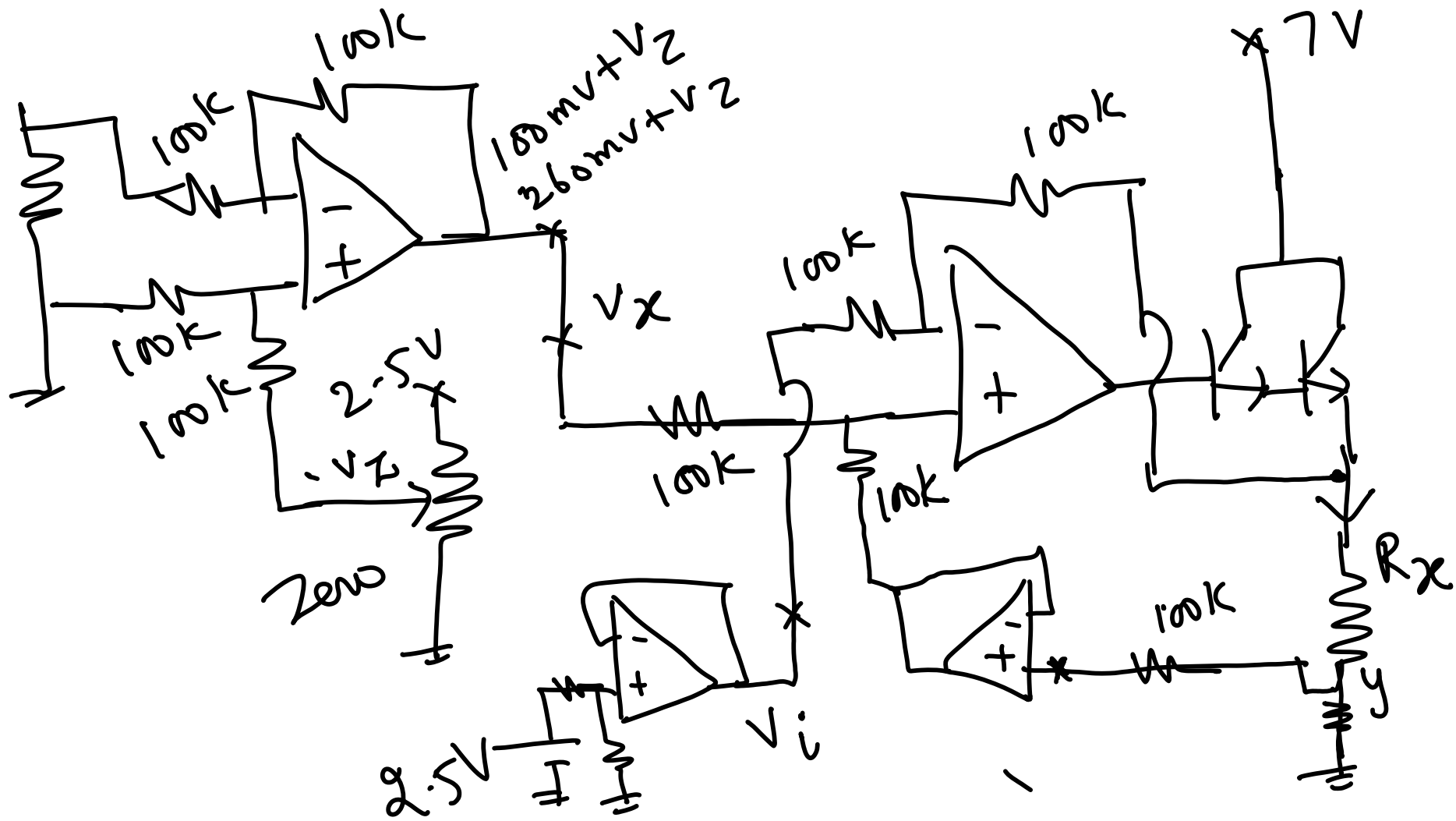
At 400°C PRT Resistance
= 260 Ω

W/ temp acc PRT = $260 \times 0.5 \times 10^{-3}$
= 130 mV

For PRT excitation of

$$\text{Then } V_0 = 100 \text{ mV} + V_{\text{zero}} \quad (\text{at } 0 \text{ c})$$

$$V_0 = 260 \text{ mV} + V_{\text{zero}} \quad (\text{at } 40 \text{ c})$$



Assuming 3 mA current is drawn by the rest of the circuit we have to fix

$$I = 1 \text{ mA} \quad \text{at} \quad 100 \text{ mV} + V_Z$$

$$I = 17 \text{ mA} \quad \text{at} \quad 260 \text{ mV} + V_Z$$

$$\frac{(V_x - V_i)}{R} = I$$

$$V_x = \begin{array}{l} 100 \text{ mV} + V_Z \quad \text{at } 0 \text{ C} \\ 260 \text{ mV} + V_Z \quad \text{at } 40 \text{ C} \end{array}$$

$$V_{\pi} = 200 \text{ mV at } 0^{\circ} \text{C}$$

$$V_{\pi} = 360 \text{ mV at } 40^{\circ} \text{C}$$

$$\text{At } V_{\pi} = 200 \text{ mV} \quad \frac{200 \text{ mV} - V_{i}^{\circ}}{100} = 1 \text{ mA} \Rightarrow$$

$$\text{For } V_{i} = 100 \text{ mV then}$$

$$\hat{I} = 1 \text{ mA}$$

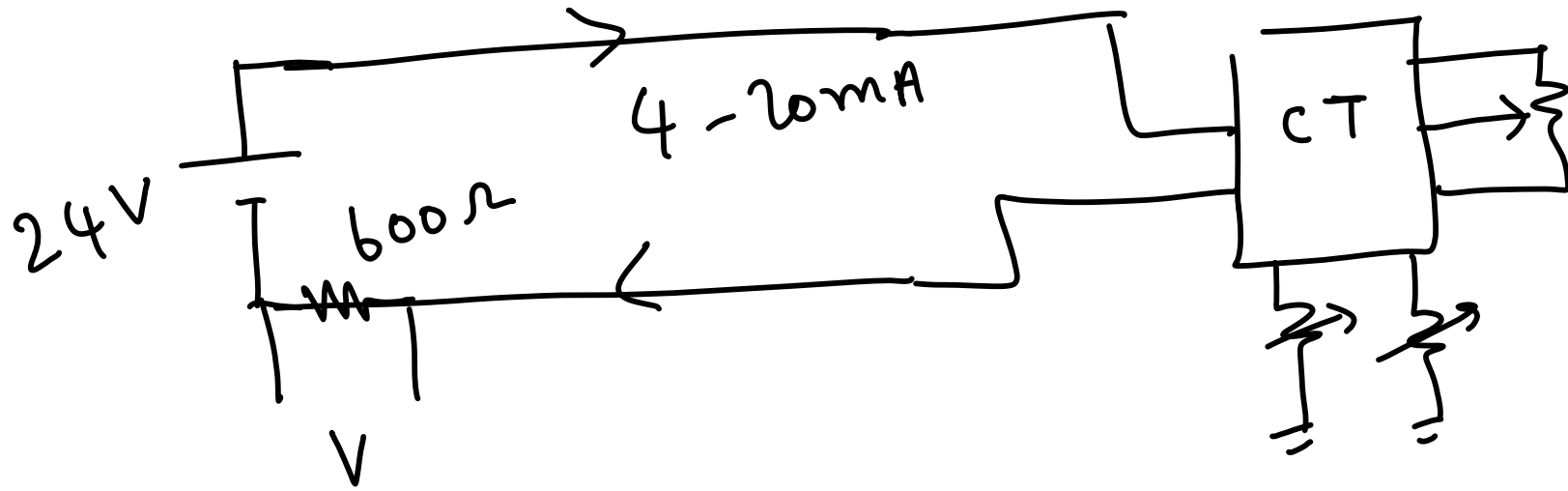
$$\text{For } V_{\pi} = 360 \text{ mV}$$

$$\text{For } V_{i} = 100 \text{ mV}$$

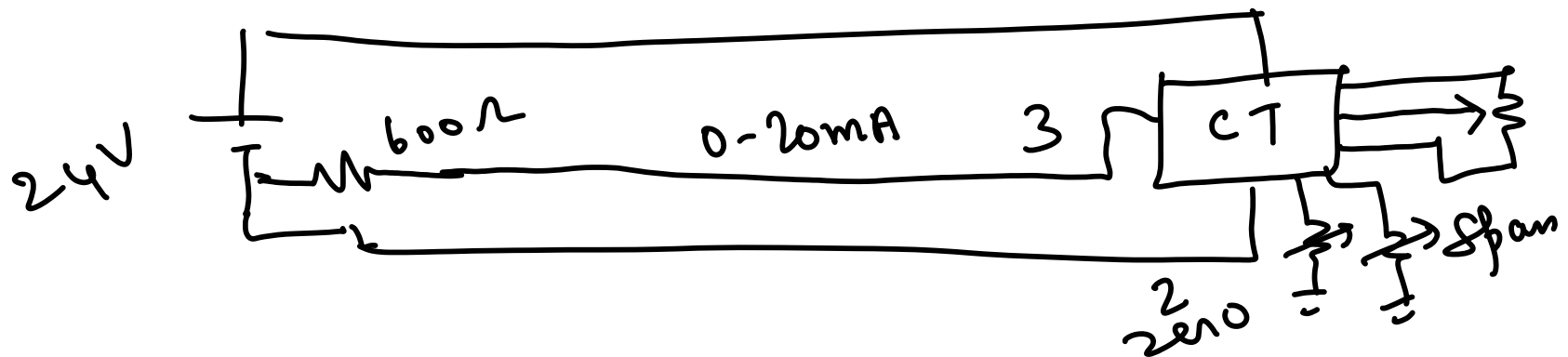
$$I = \frac{260}{100} = 2.6 \text{ mA} - 1 \text{ mA}$$

Adj V_i , R_x , V_L one can
Get 1 mA at 0° C
ans 17 mA at 40° C

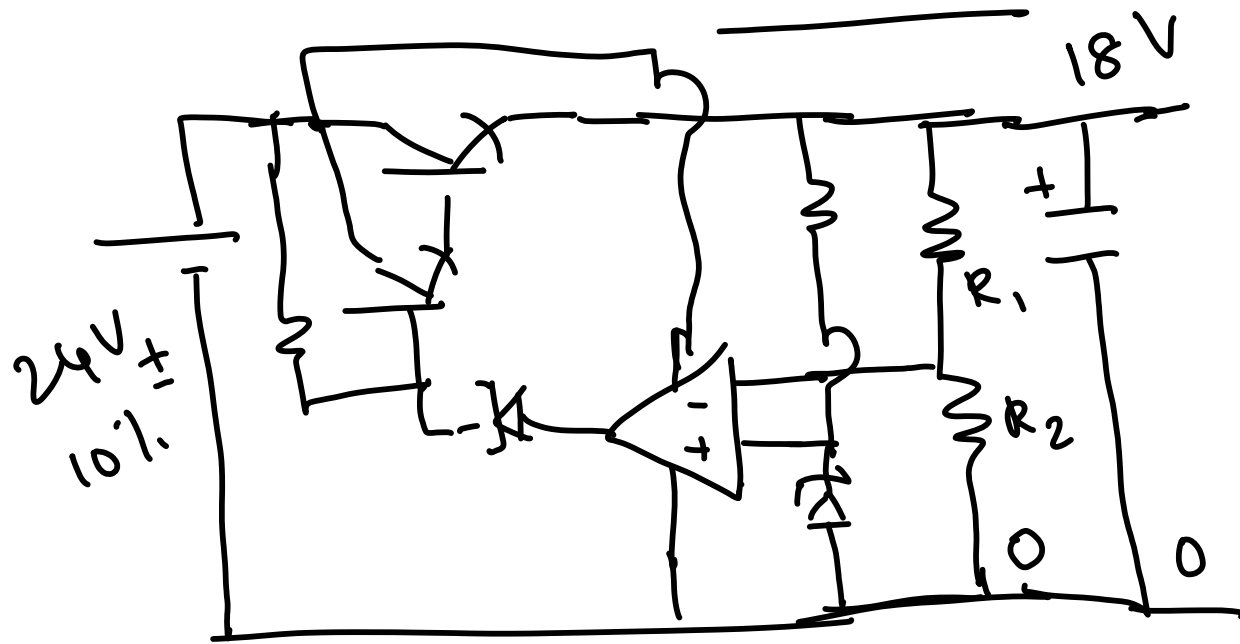
3-wire current transmitters



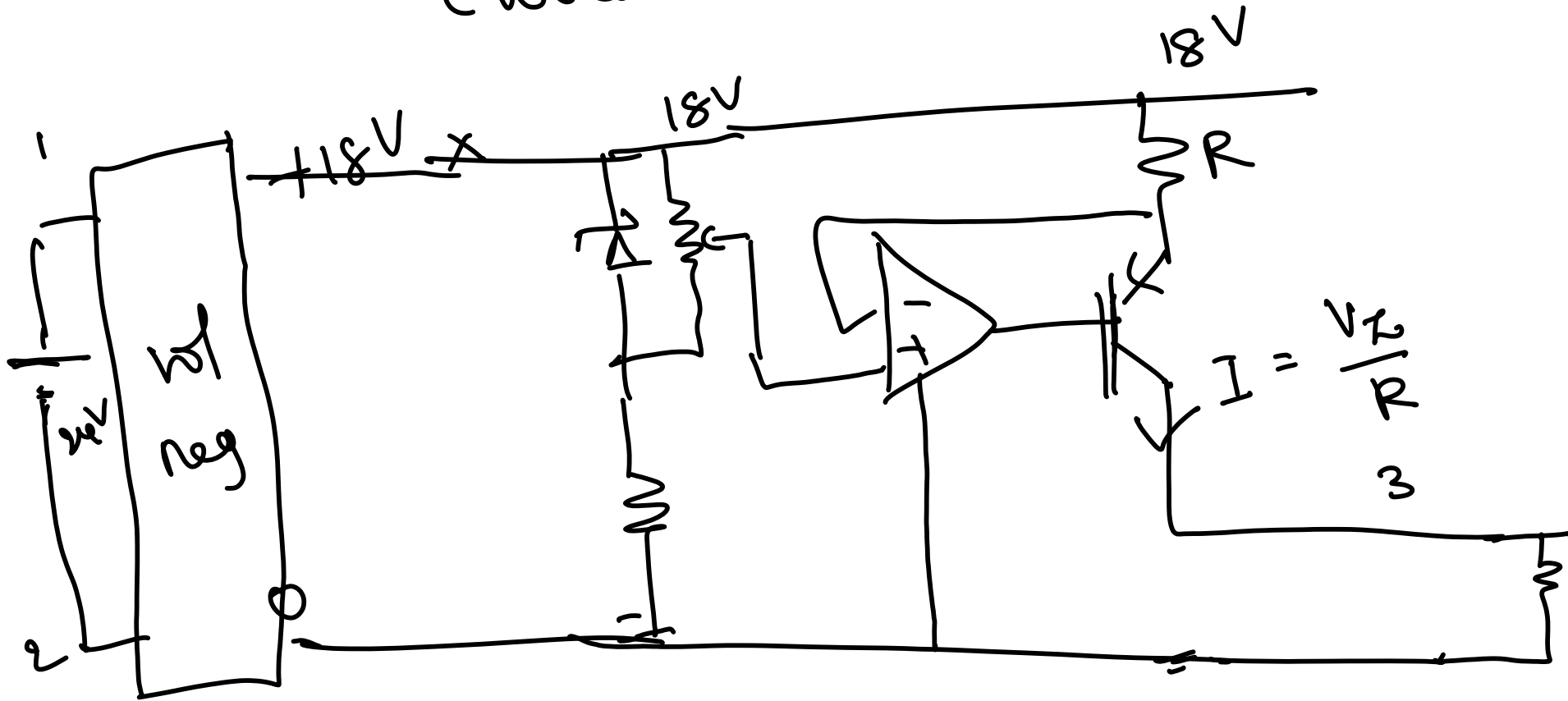
3-wire current transmitters

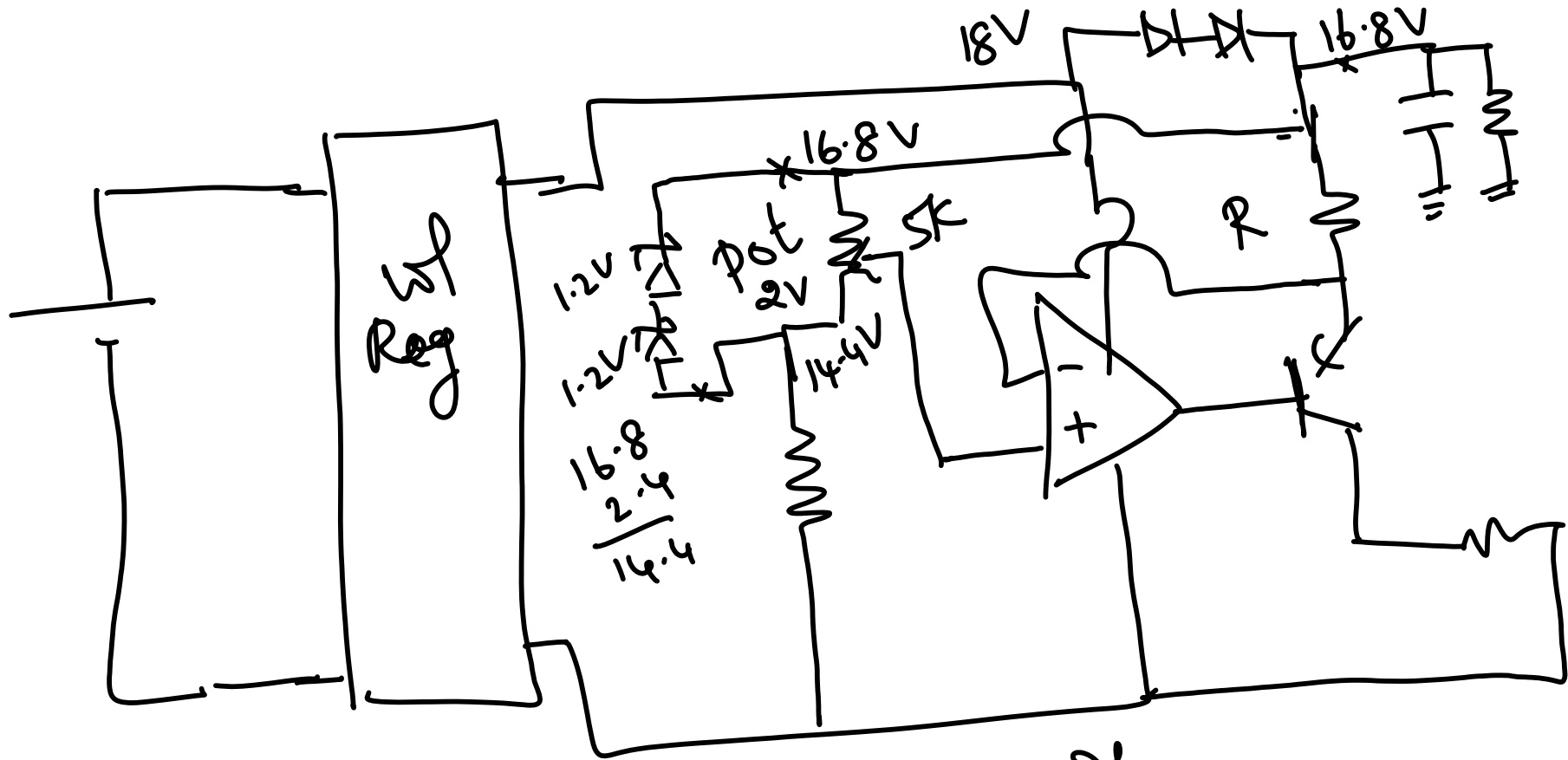


0 - 20mA current transmitter



Current transmitter





Total expected w/ charge = 2.4V

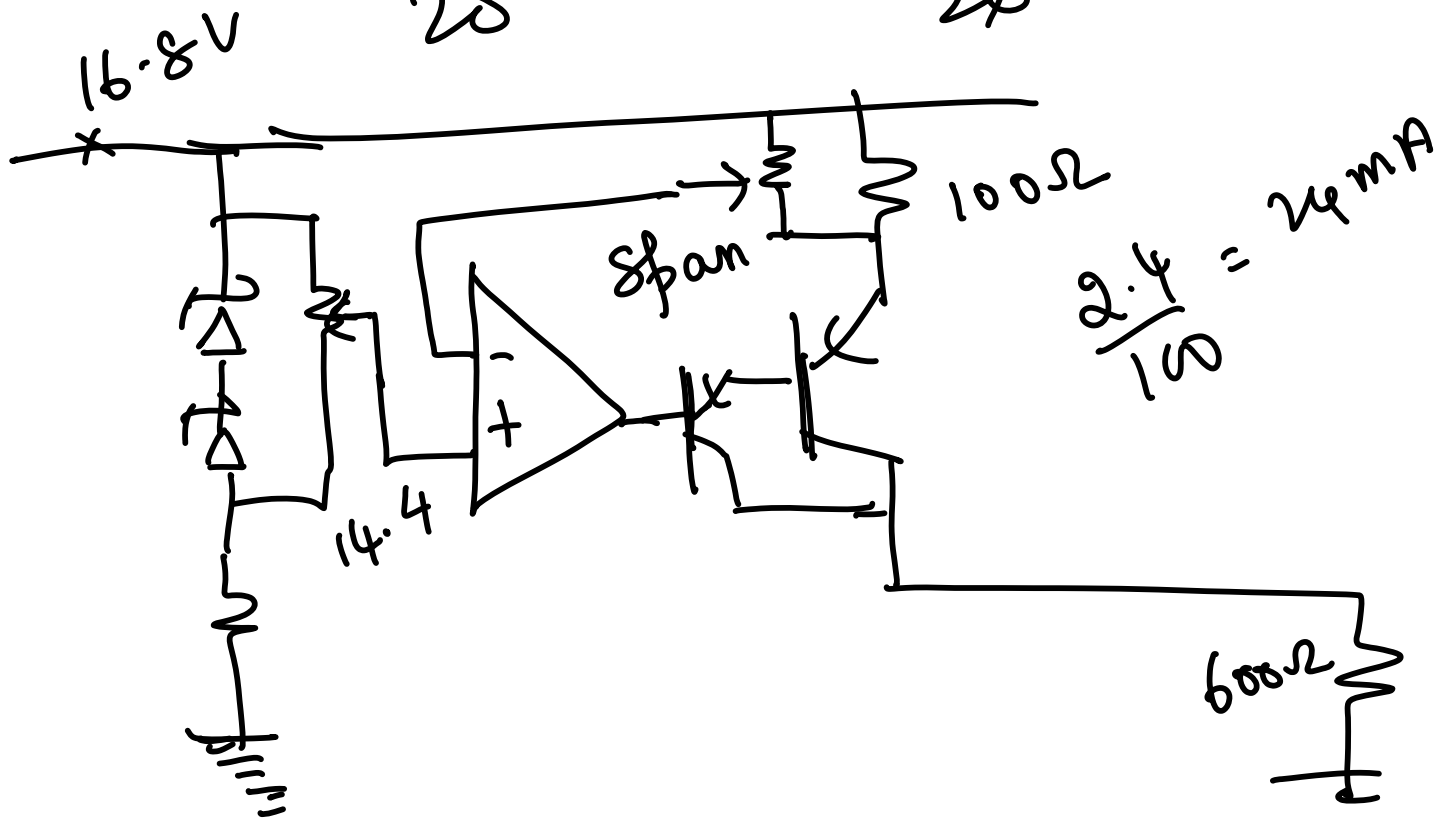
Real expected w/ charge = 1.6V

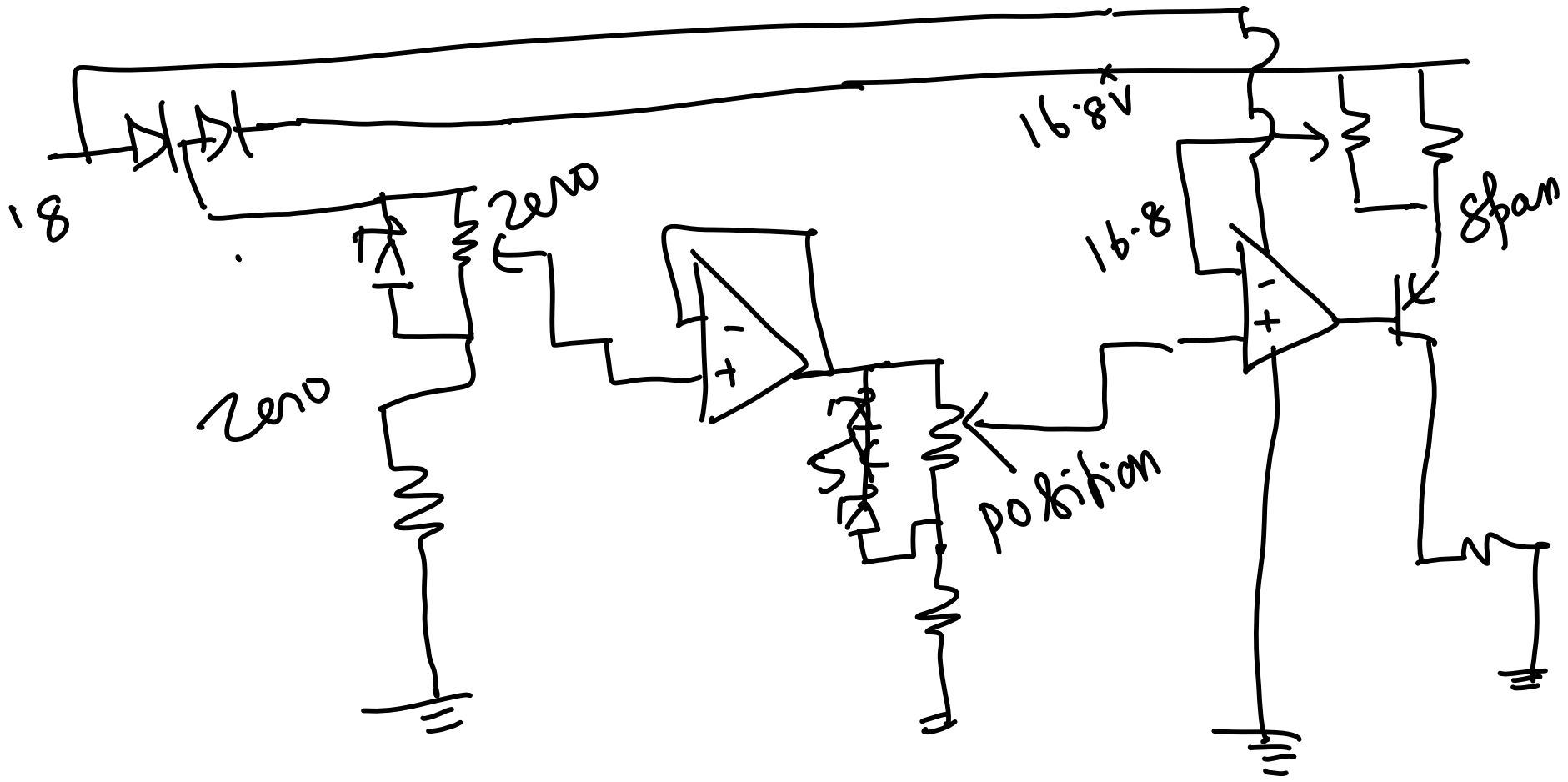
For 20mA expected current charge

required resistance

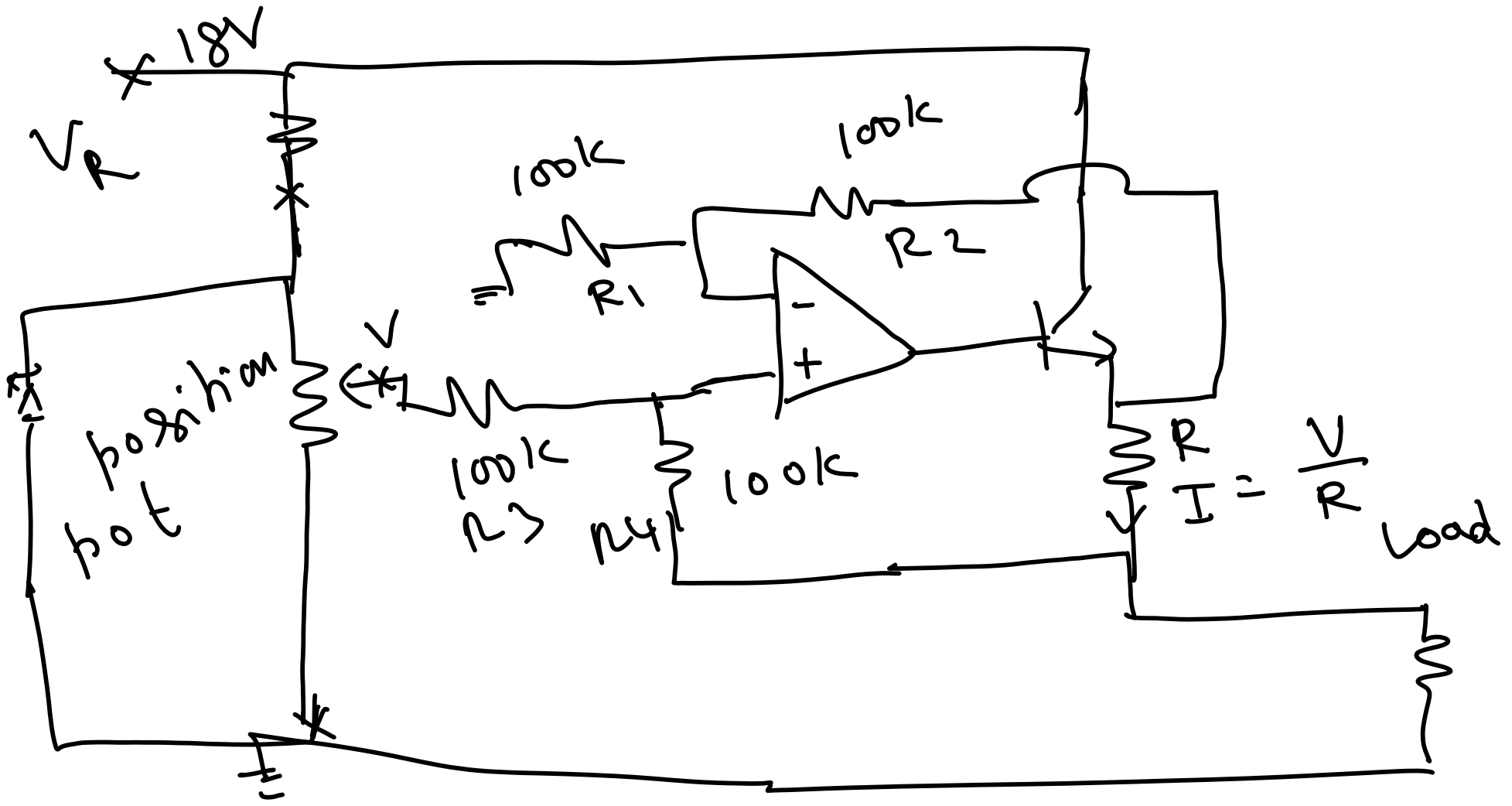
$$= \frac{1.6}{R} = 20 \times 10^{-3}$$

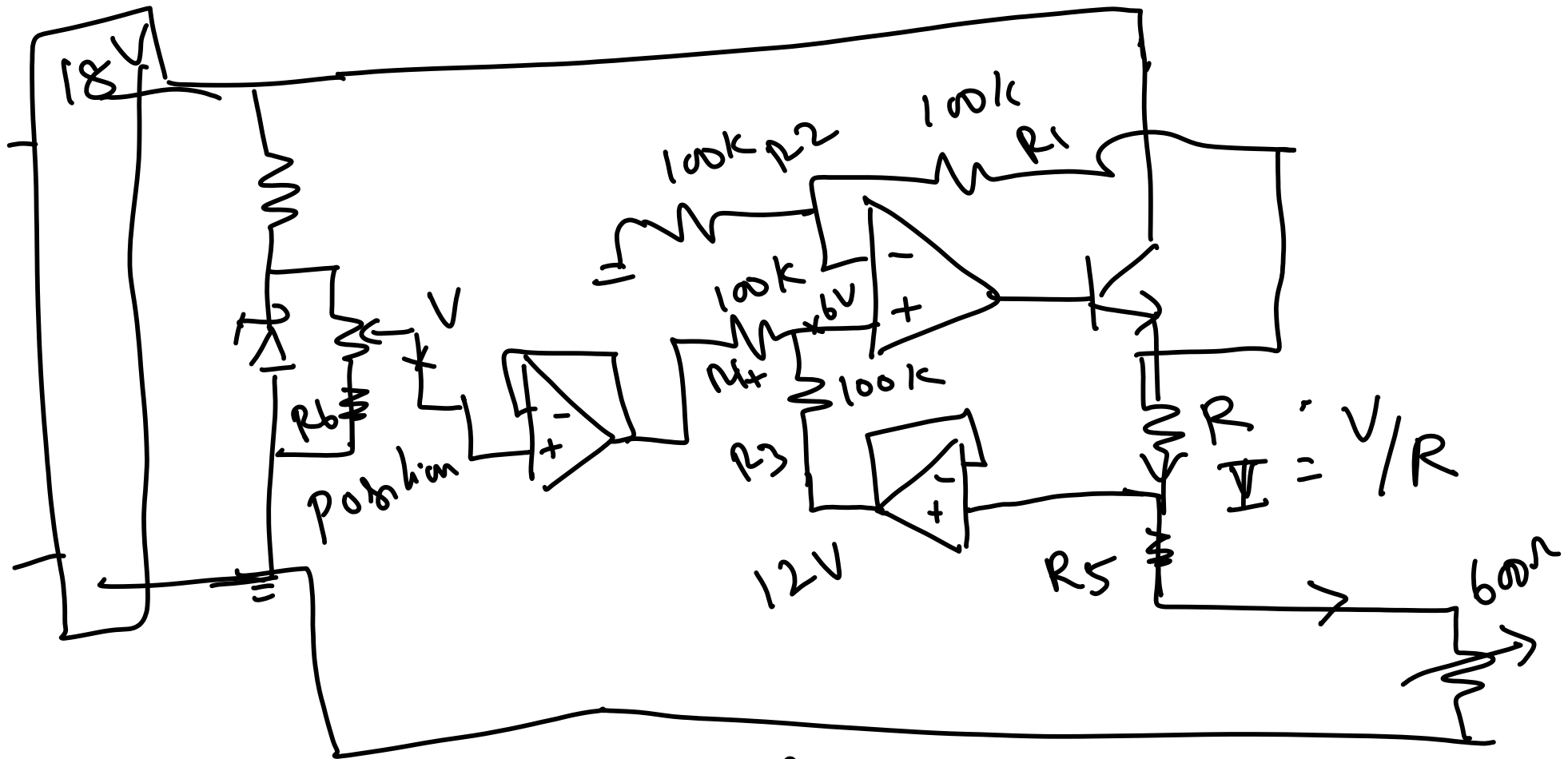
$$R = \frac{1.6 \times 10^3}{20} = \frac{1600}{20} = 80 \Omega$$





Current transmitter with 4th side reference





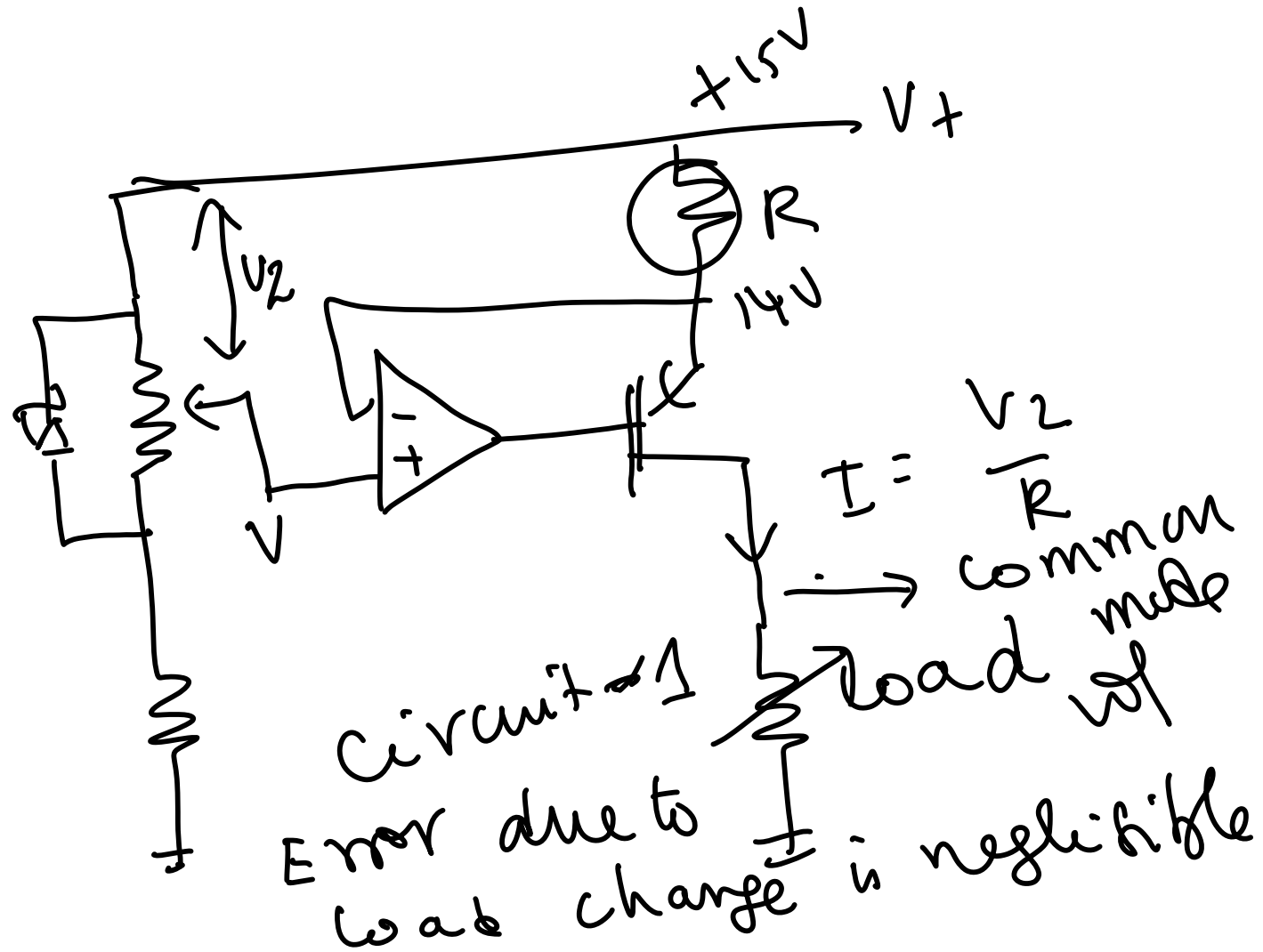
$$\frac{R_1}{R_2} = \frac{R_3}{R_4}$$

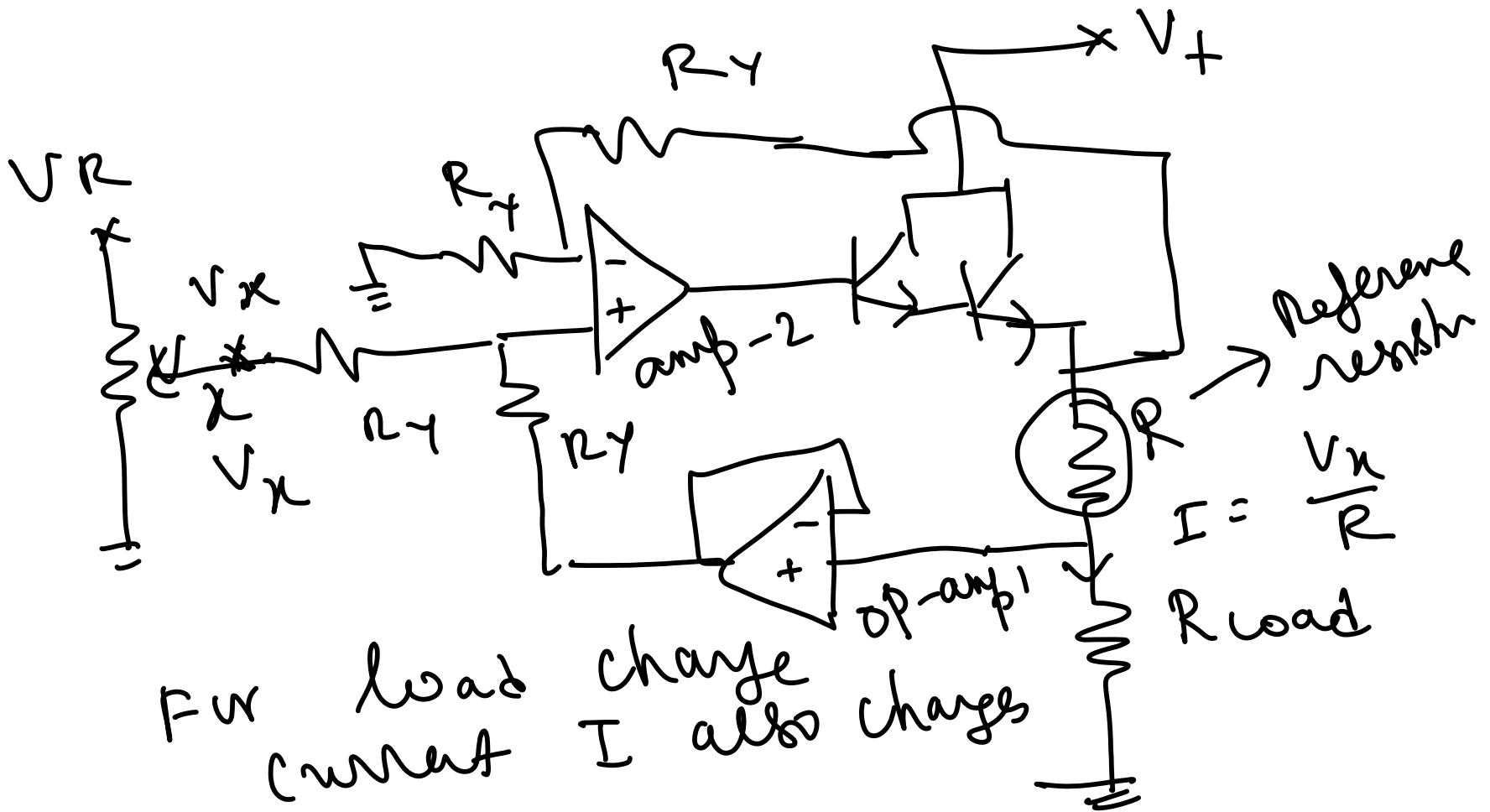
① The input voltage to the op amp is not at the supply potential. At the

maximum of amp if not
terminals see only half
the supply voltage

problem

At gnd end the of amps
may see zero potential
at zero current.
by adding resistors R_5, R_6
the problem is not solved.





by a small amount

① Due to finite CMRR
OF THE OP AMP-1

② The four resistors
(R_y) may not equal

For 1% tolerance resistance
then about 2% error in
current is expected due to

So CMV
to current I is expected
change with load

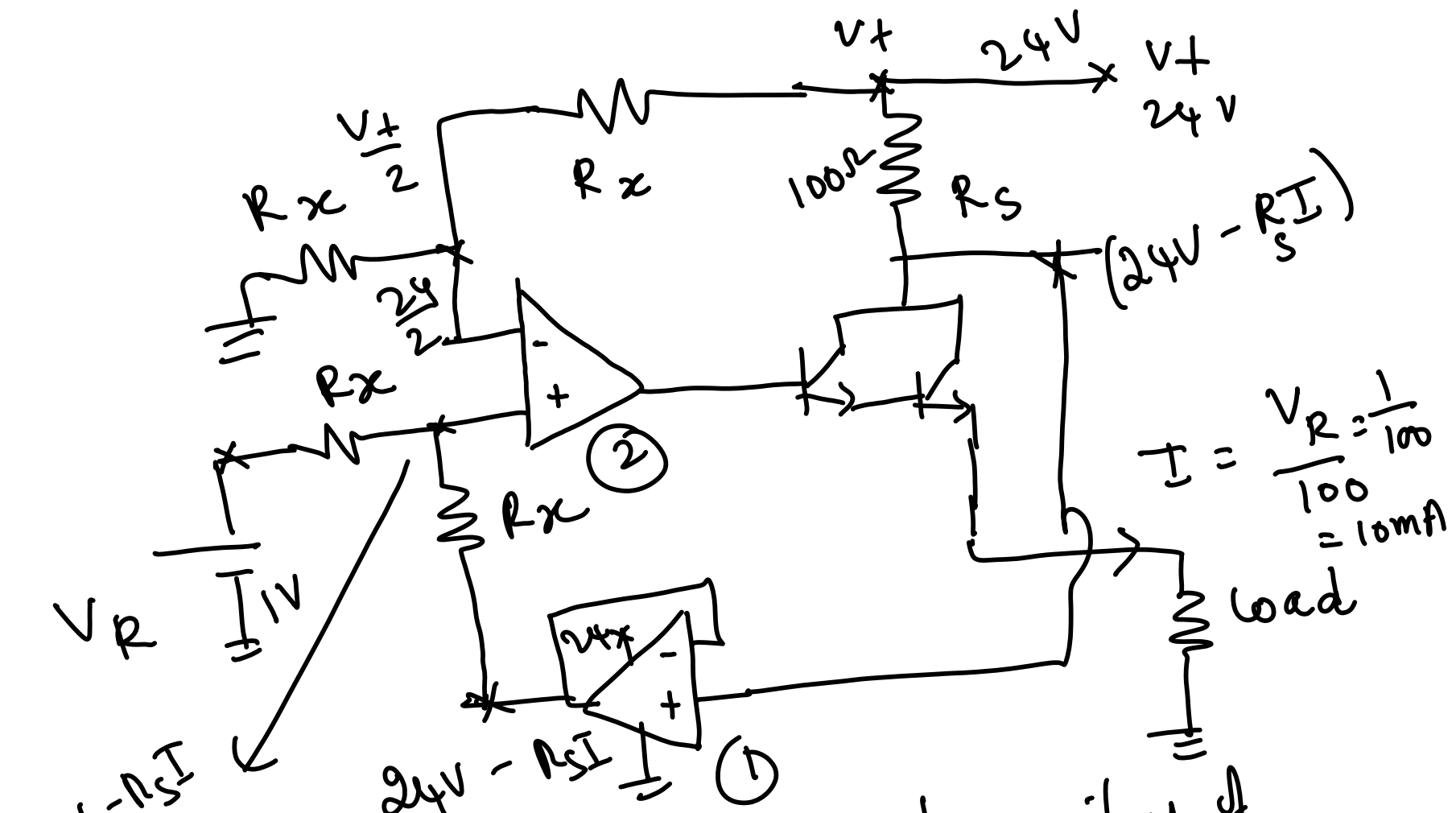
For 12V charge across
load resistance then

The voltage error at
of amp 2 = i_{∞} =

$$\frac{12 \times 2}{100}$$

$$= \frac{24}{100} = 240 \text{ mV}$$

$$\Delta I = \frac{240 \text{ mV}}{R}$$



Wt at non-inverting input of op amp-2 = $\frac{24}{2} - \frac{R_s I}{2} + \frac{V}{2}$

$$V_+ = V_-$$

$$R_s I = V_R$$

$$I = \frac{V_R}{R_s}$$

Advantage

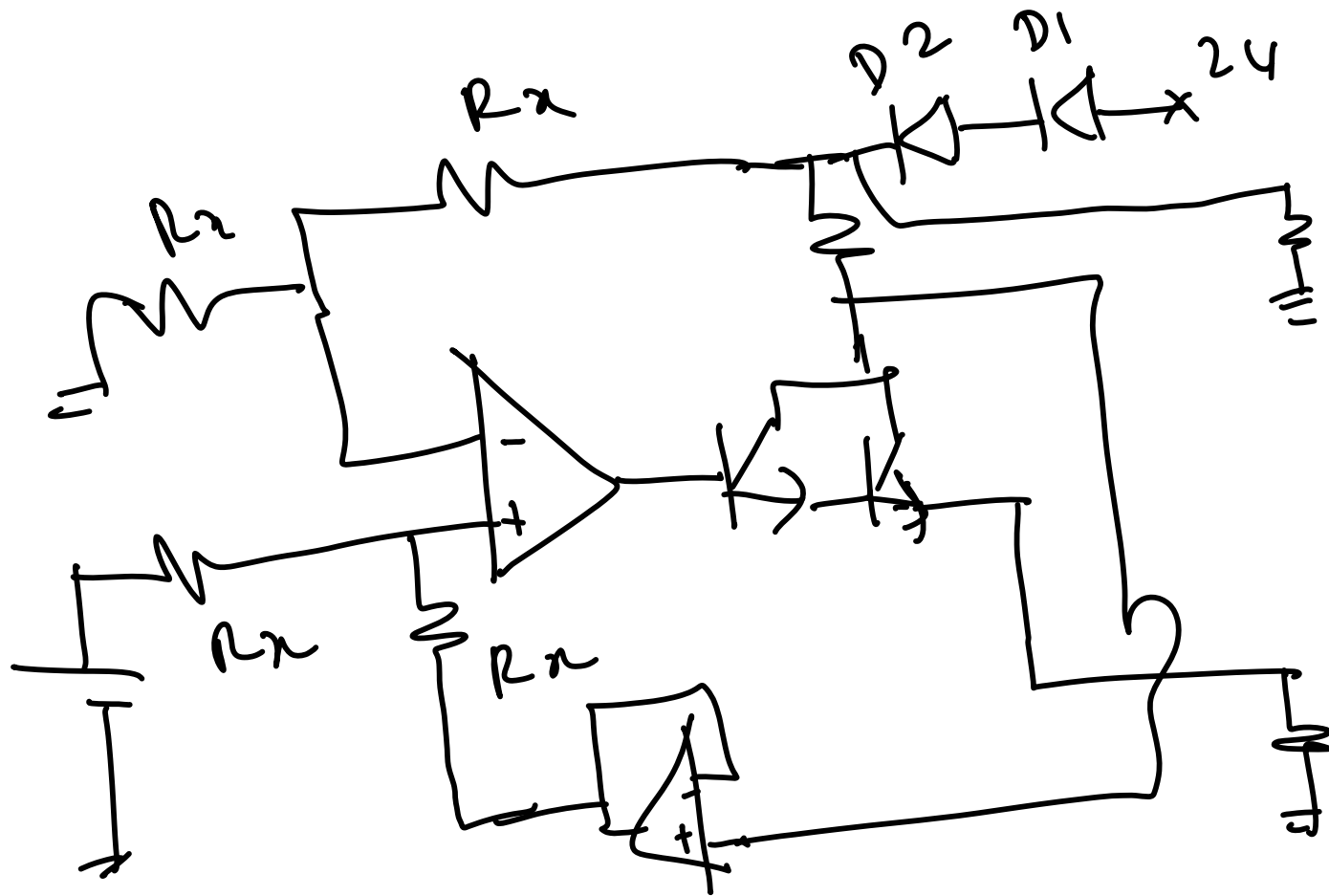
When load resistance changes, the voltage seen by the op-amp is not changing. That is no common mode voltage problem.

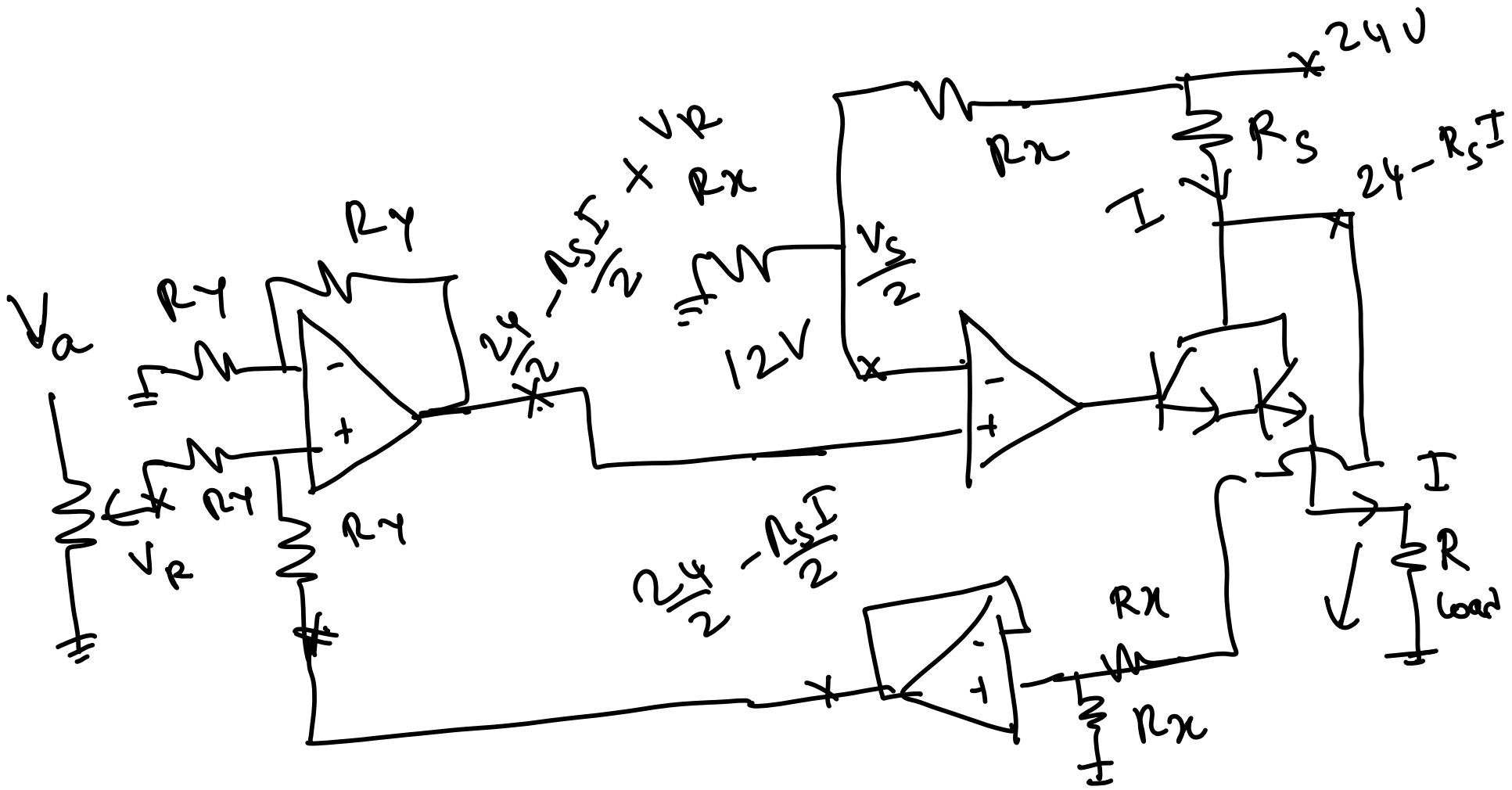
The resistors R_x need not be matched. The mismatch

Gives error only for a
small amount if input
Supply voltage changes.

This advantage

OP-amp-1 sees input
voltage very close to its
Supply voltage. This calls
for slightly higher
Supply voltage to the op-amps





$$I = \frac{2 V_R}{R_S}$$

$$V_+ = \frac{24}{2} - \frac{R_S I}{2} + V_R = V_-$$

$$V_- = \frac{24}{2}$$

$$\frac{24}{2} = \frac{24}{2} - \frac{R_s I}{2} + V_R$$

$$\frac{R_s I}{2} = V_R$$

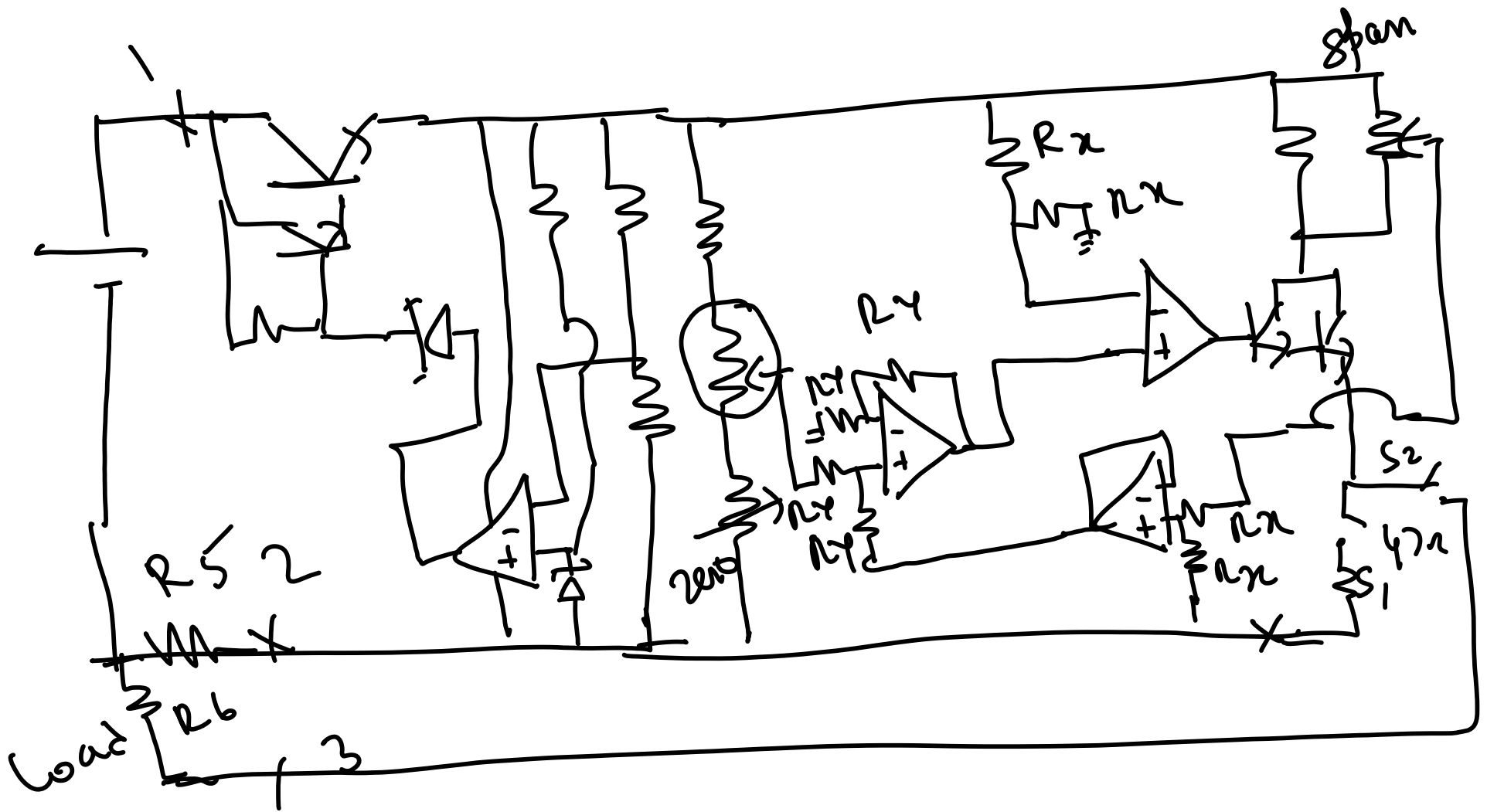
$$I = 2 \frac{V_R}{R_s}$$

Errors

- ① R_s drift will introduce a current error
- ② All the resistors R_x, R_y drift will introduce errors

③ offset voltage drift
and offset current
drift of all three
of amps introduce
current drift error

④ Reference voltage
drift will also introduce
error.



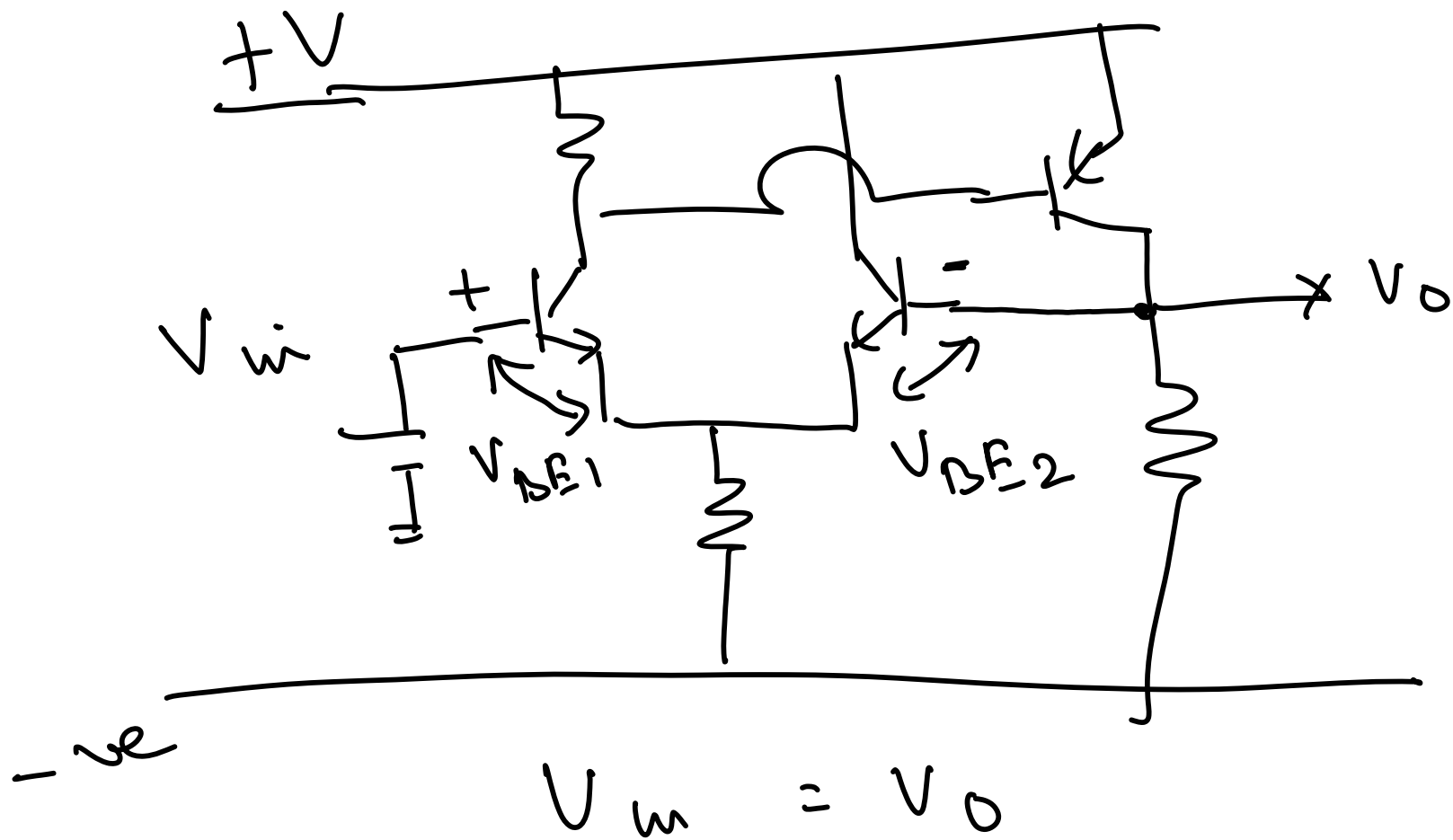
For 2 wire System
 S_1 is ON S_2 is OFF
 R_6 is open and R_5 is
connected

For 3 wire System
 S_1 is OFF S_2 is ON
 R_6 is connected and R_5 is
shorted.

This resistance based/potentiometer
based current transmitters
are used for displacement
measurement in the process
control industry.

op amp errors and error budgeting

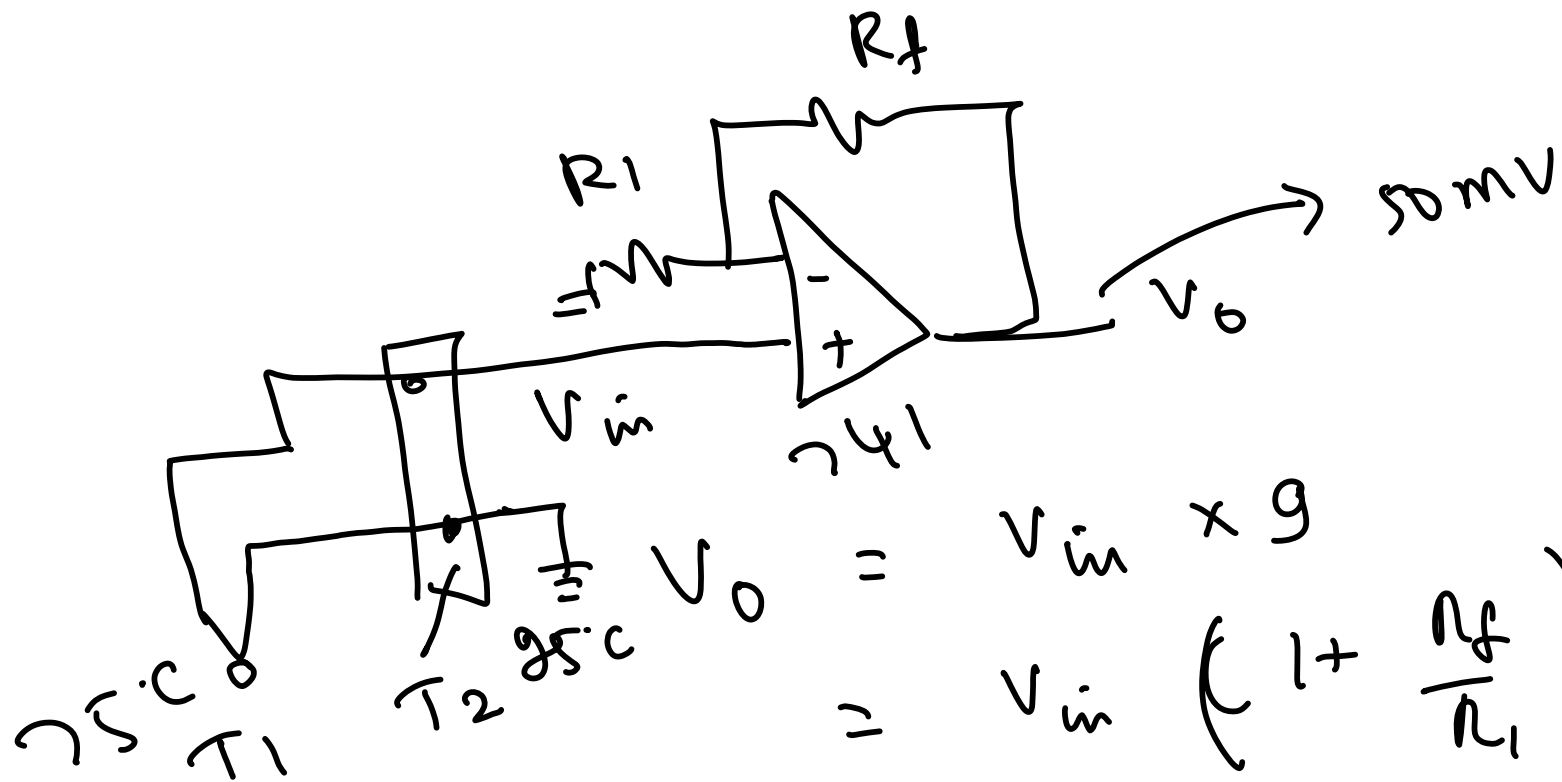
- ① Offset voltage drift
- ② Bias current drift -
Offset current drift
- ③ Gain drift error
- ④ Input resistance
- ⑤ Output resistance of the op
amp
- ⑥ CMRR introduces error



Base - emitter voltage
of the input transistors are
~~iden~~ same over a
working temp range

ΔV_{BE} = offset voltage

ΔV_{BE} change with temp is
called offset voltage drift



$$V_0 = V_{in} \times g$$

$$= V_{in} \left(1 + \frac{R_f}{R_1} \right)$$

Sensitivity of the thermocouple
 $= 40\text{mV}/^{\circ}\text{C}$

Thermocouple output voltage
 $(T_1 - T_2)$ Sensitivity $= V_0$

$$T_1 - T_2 = 50^\circ\text{C}$$

$$\text{Sensitivity} = 40 \mu\text{V}/^\circ\text{C}$$

$$V_0 = 50 \times 40 \mu\text{V} = 2 \text{mV}$$

$$\text{gain} = 25 = \left(1 + \frac{R_f}{R_1}\right)$$

$$R_f = 24 \text{k}$$

$$R_1 = 1 \text{k}$$

Output of the op amp

$$= 25 \times 2 \text{mV} = 50 \text{mV}$$

For 741 of amp

$$\text{Offset w/ drift} = \pm 15 \mu\text{V}/^\circ\text{C} \\ \text{max}$$

For ambient temp

variation of -20°C to $+80^\circ\text{C}$

Total offset w/ drift

$$= 15 \times 100 = \pm 1.5 \text{ mV}$$

Total output w/

$$= (2 \text{ mV} \pm 1.5 \text{ mV}) \times 25$$

error due to offset w/

$$\text{drift} = \pm 25 \times 1.5 \text{ mV} = \pm 37.5 \text{ mV}$$

The expected error
at the output = $\pm 37.5^\circ\text{C}$

This error is large for this
 $40\text{ mV}/^\circ\text{C}$ signal provided
by the thermocouple

What is to be done

① Go for low drift
op amps \rightarrow LM714
LM07

offset vol drift $\rightarrow 0.5\text{ mV}/^\circ\text{C}$

For $\pm 0.5 \mu\text{V}/^\circ\text{C}$ of amp
the thermocouple amp error

$$= 100 \times 0.5 \mu\text{V}$$

$$= 50 \mu\text{V}$$

Total error = $50 \mu\text{V}$ at the input

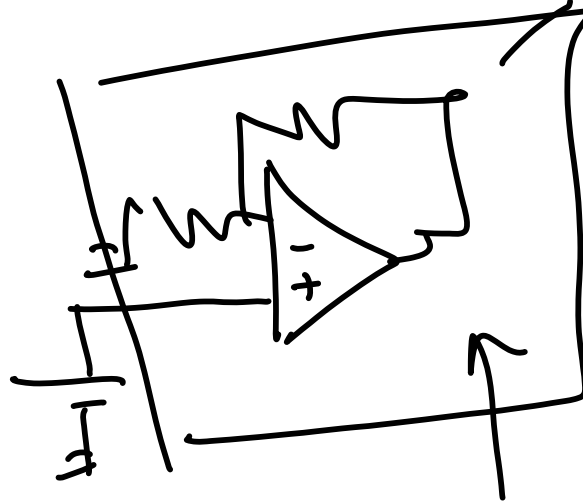
At the input Insul Sensitivity

$$= 40 \mu\text{V}/^\circ\text{C}$$

$$\text{Total error in } ^\circ\text{C} = \frac{50}{40} = 1.25^\circ\text{C}$$

Very low DC signals

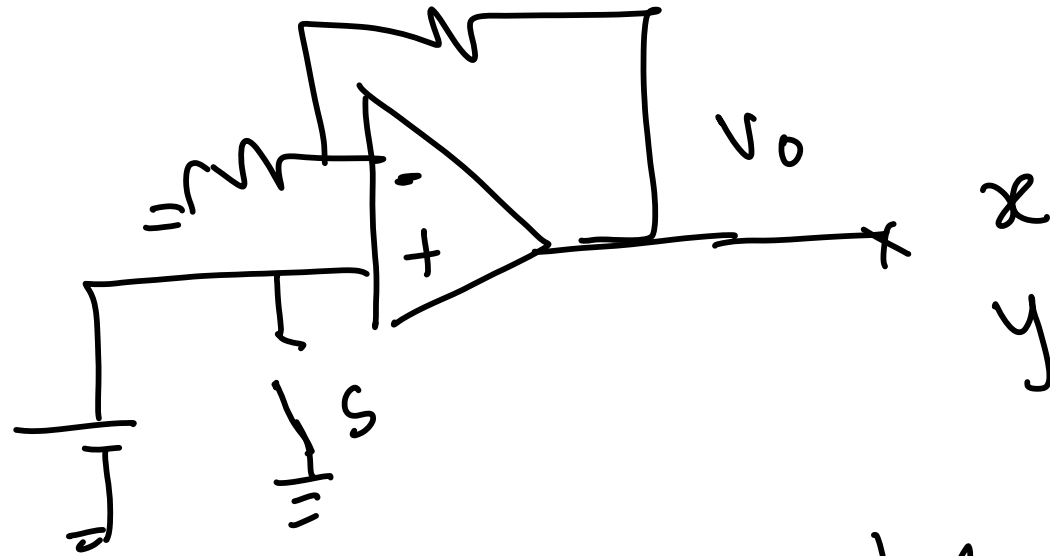
① Use over



②

Chopper Stabilized of amp
 $0.01 \mu\text{V}/^\circ\text{C}$

③ Go for Auto zero method



When the input is grounded

$$V_o = V_{OFF} \times g$$

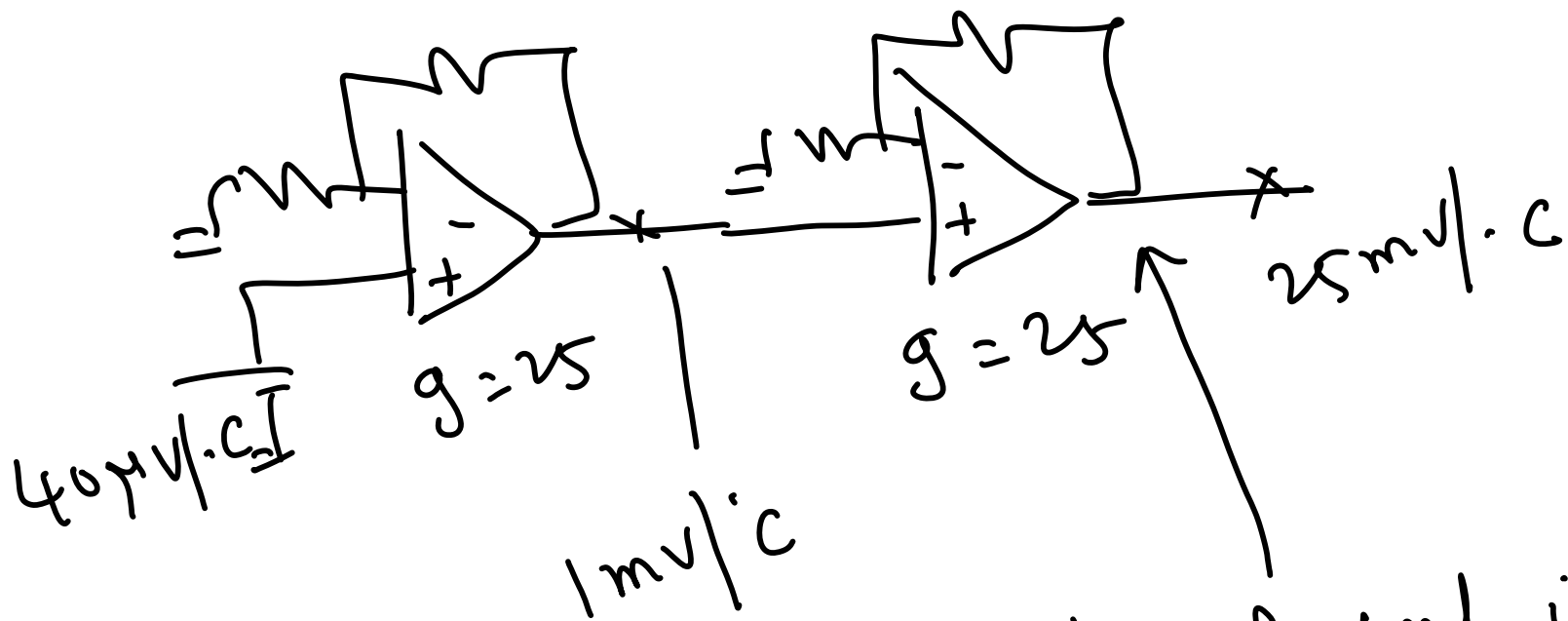
V_{OFF} changes with ambient temp.

① Measure the output
by grounding the input
let it be x

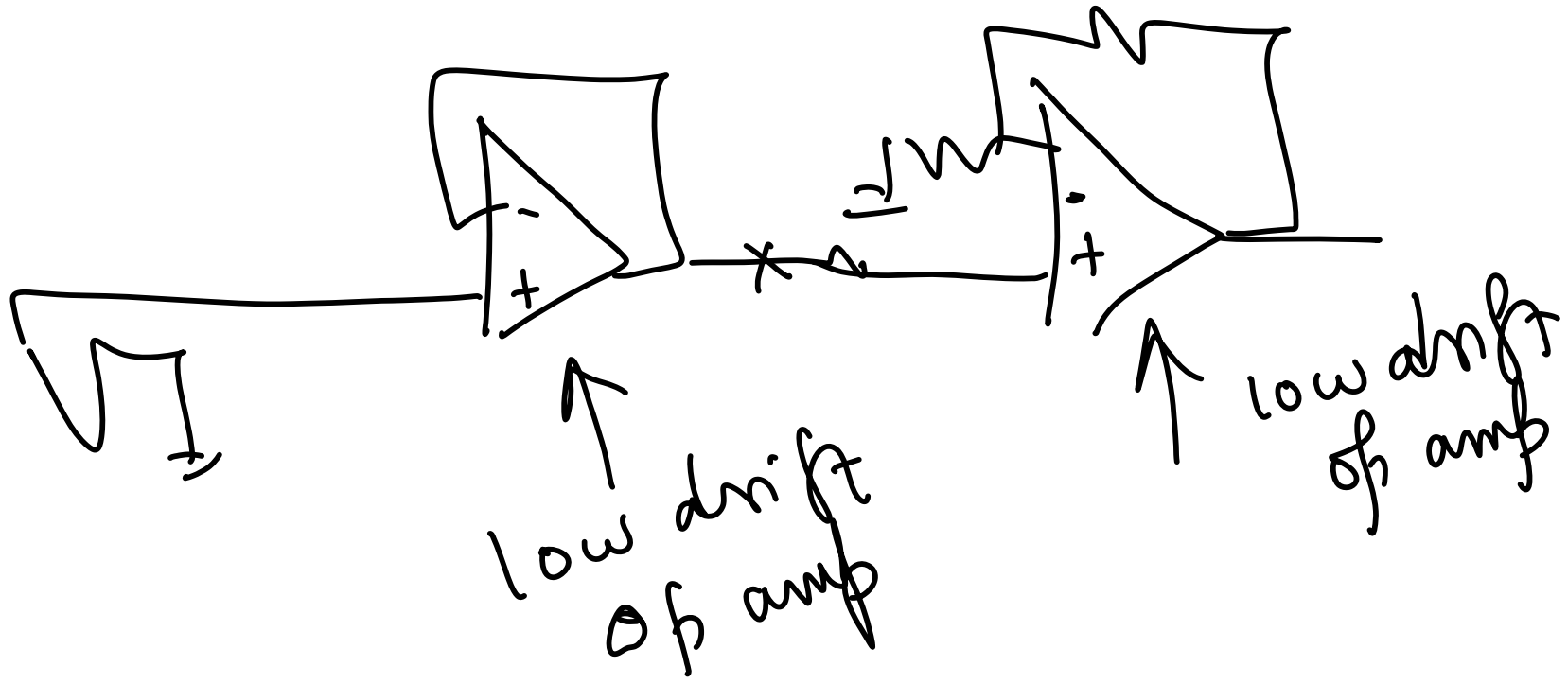
② Measure the output
by applying the input vol

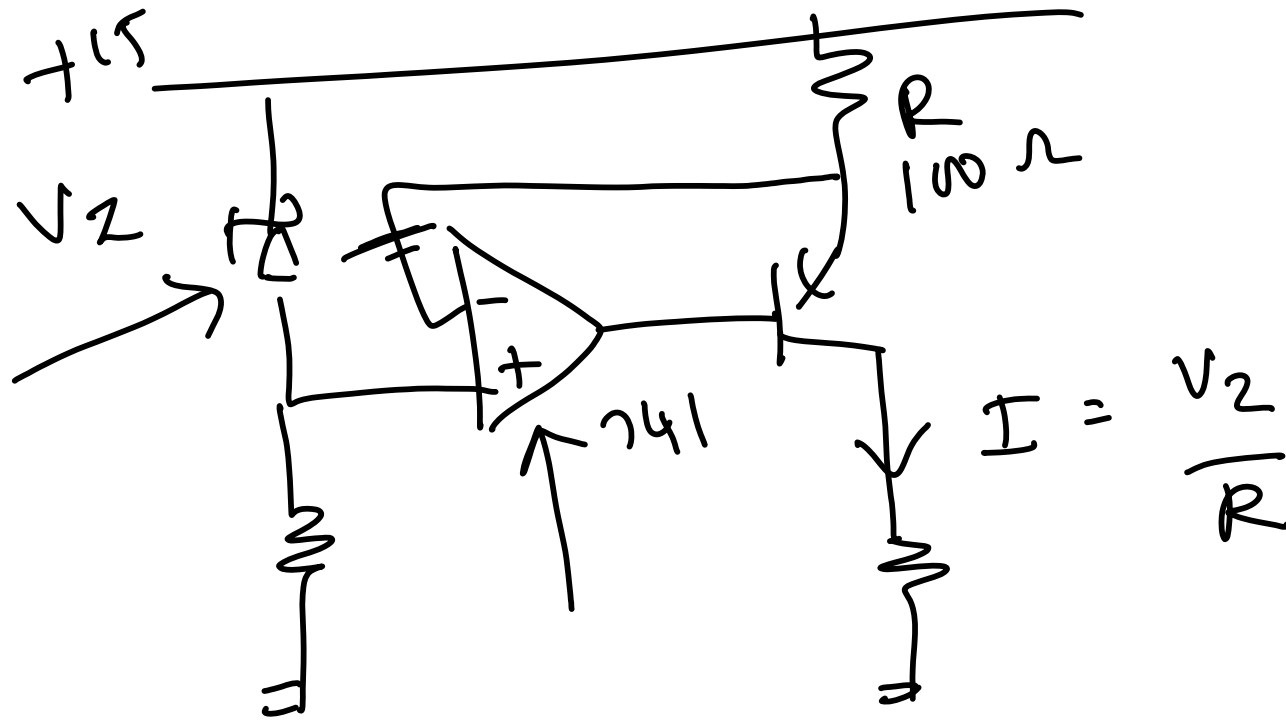
let it be y

$$x - y = \text{signal}$$



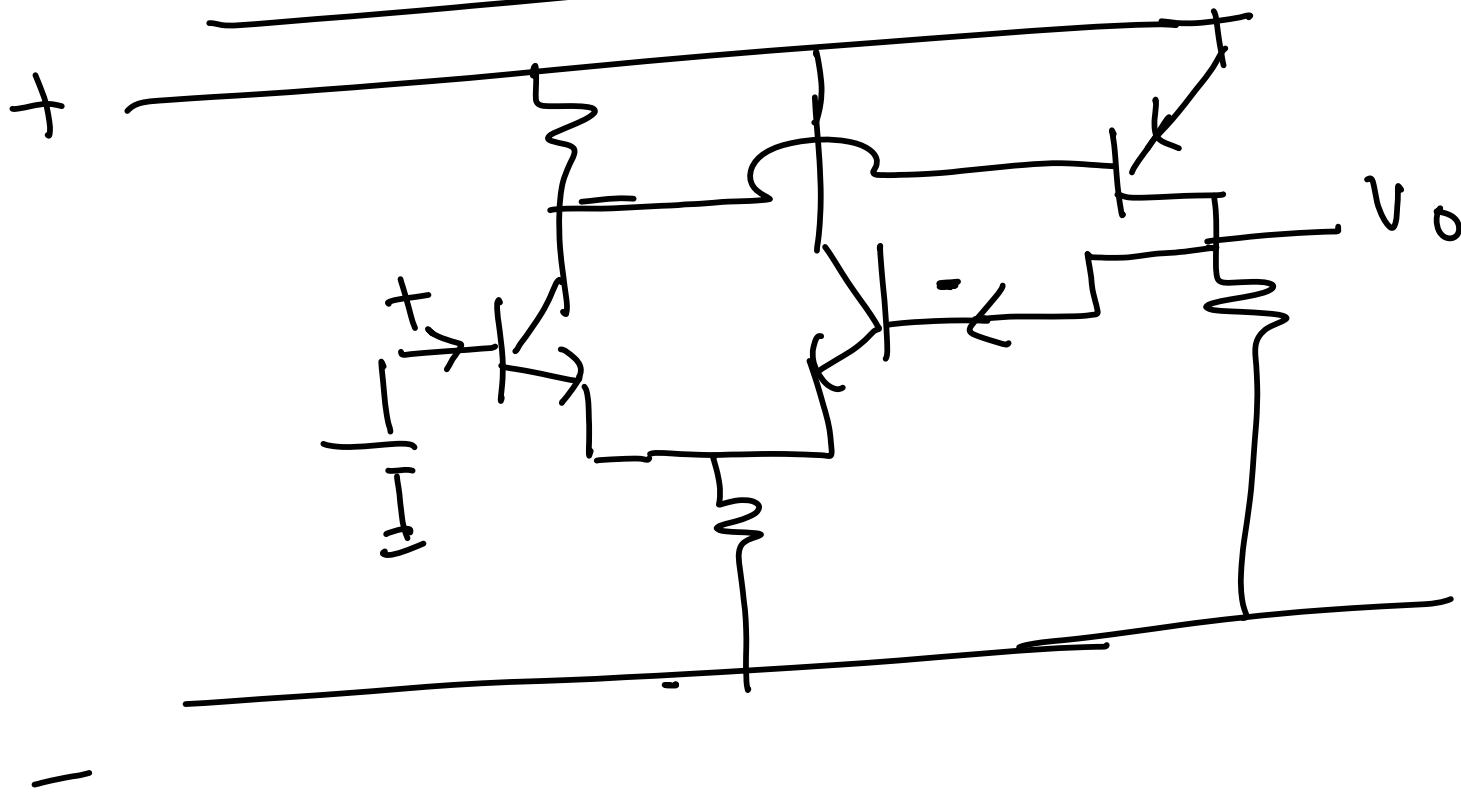
Drift of the $IS+$ of amp is
 very important and not the
 second of amp drift



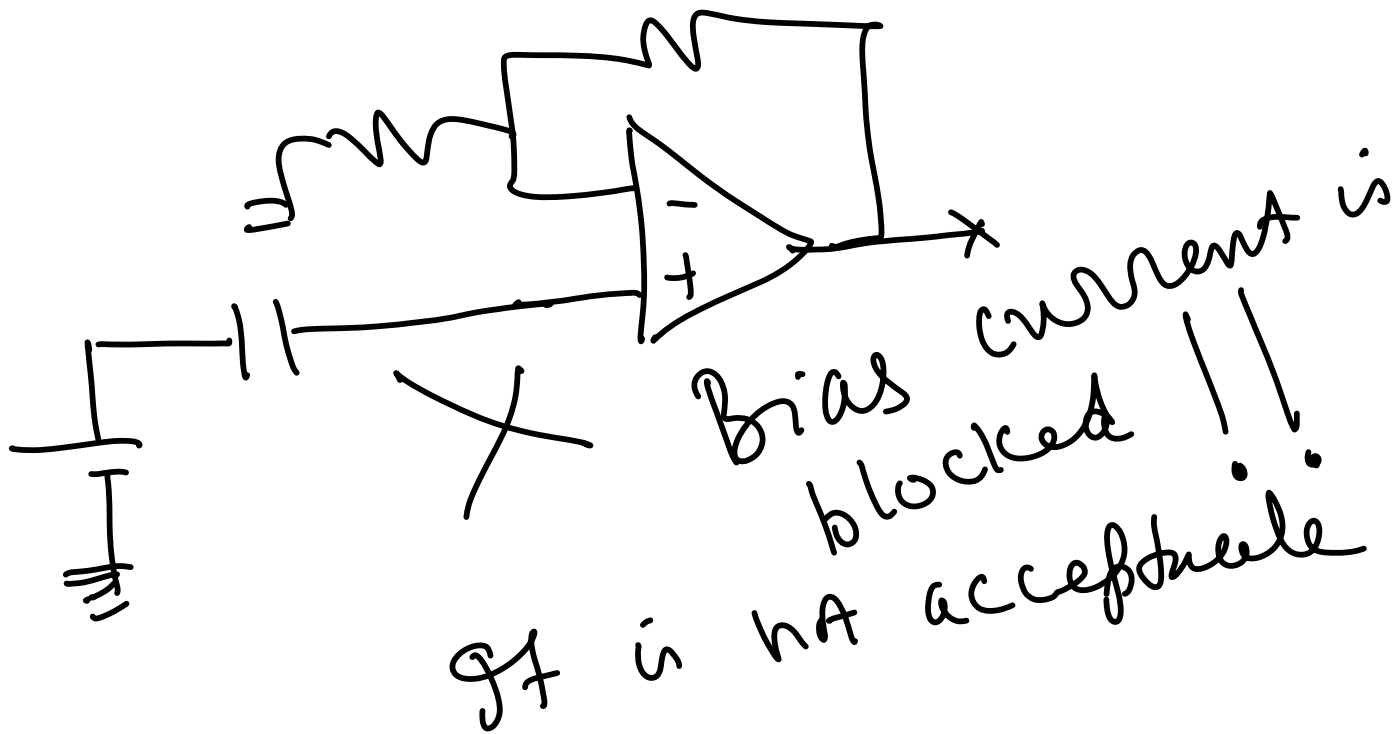


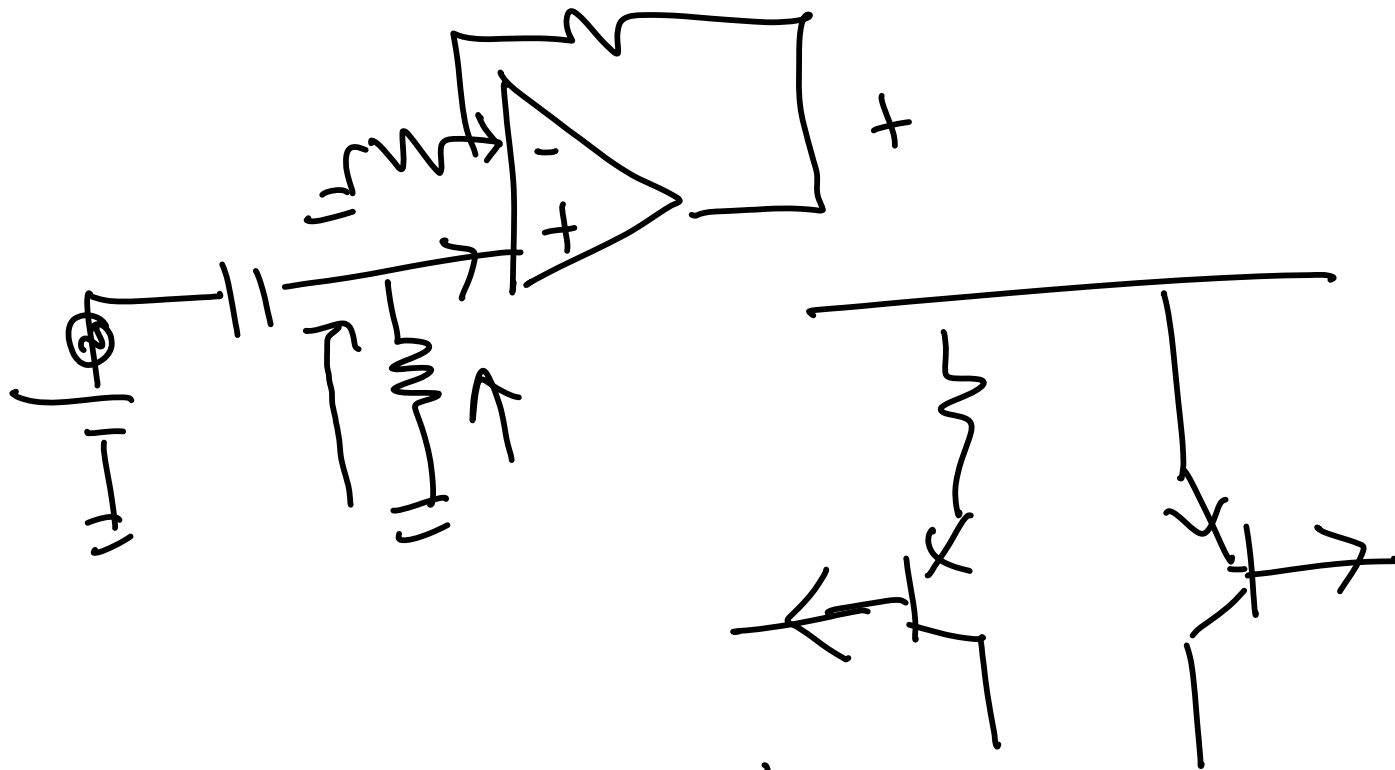
worst case current drift
 $= \frac{1.5 \text{ mV}}{R} = \frac{1.5}{100}$
 $= \frac{1500}{100} = 15 \text{ mA}$

Bias current error



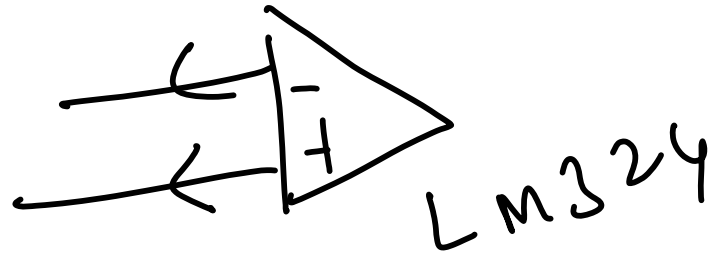
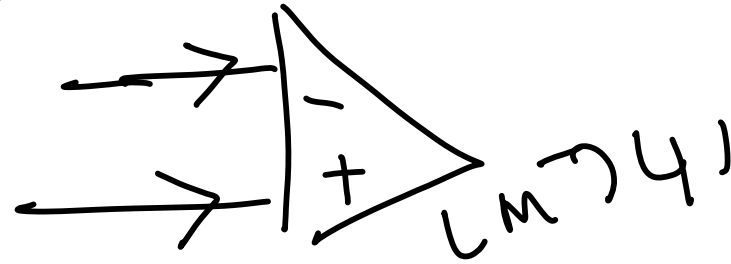
Base current of the
input transistors are called
bias current
bias current = 50 nA

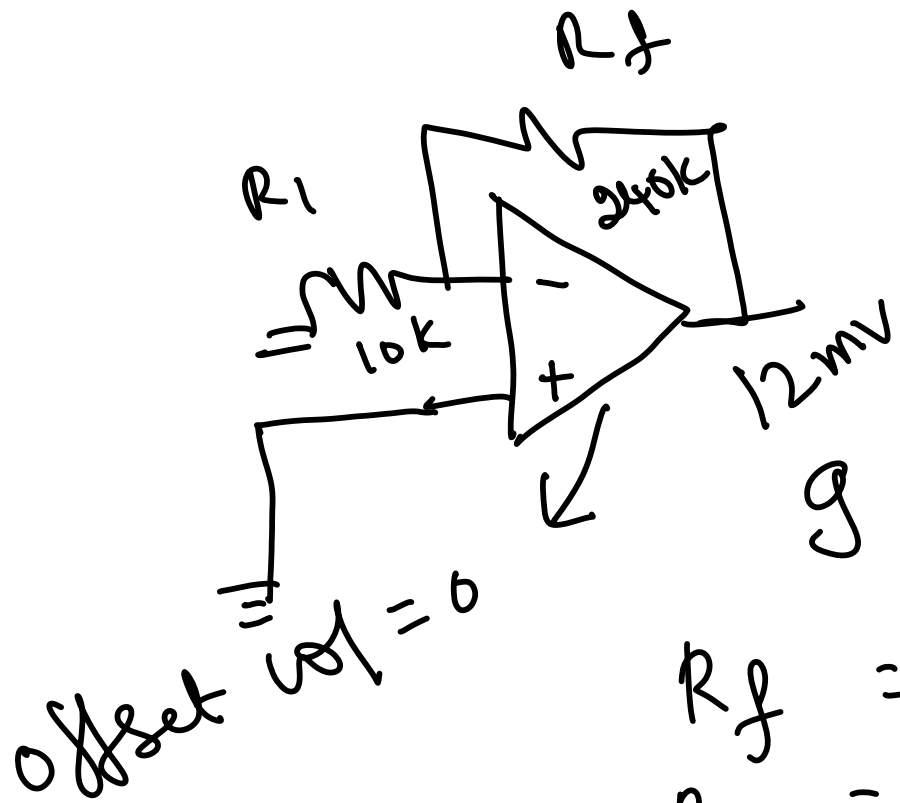




I_n NPN transistor of amp's input flows into the input of amp
 I_n PNP transistor of amp's input bias current (ex 241)

bias current flows out
from the of amp
(LM324)





$$V_{in} = 0$$

$$V_o = 0$$

$$g = 25$$

$$R_f = 24k$$

$$R_1 = 1k$$

The expected $V_o = 0$
 but in real life $V_o \neq 0$

For $I_{B-} = 50 \text{ nA}$

Then current through $R_f = 50 \text{ nA}$

So w/ acc $R_f = 50 \times 10^{-9} \times 240 \times 10^3$

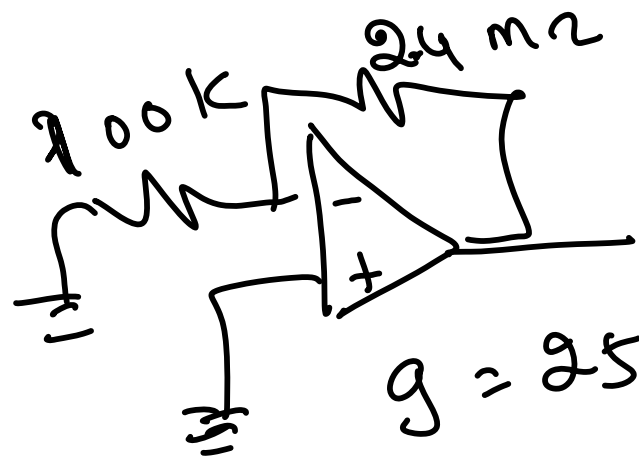
$$= 50 \times 240 \times 10^{-6} \text{ V}$$

$$= 5 \times 24 \times 10^{-4} \text{ V}$$

$$= 120 \times 10^{-4} \text{ V}$$

$$= 12 \text{ mV}$$

The error due to bias current
is 12 mV



The bias current error

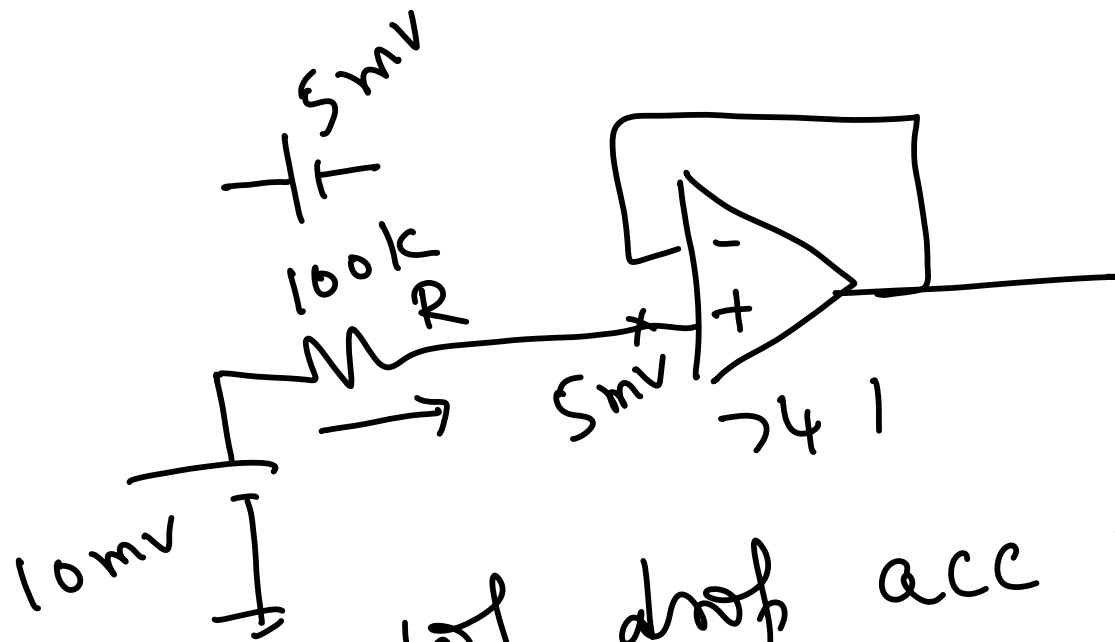
$$= 2.4 \times 10^6 \times 50 \times 10^{-9}$$

$$= 24 \times 5 \times 10^{-3}$$

$$= 120 \text{ mV}$$

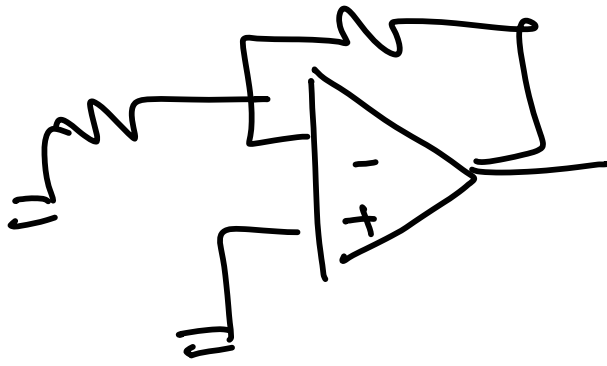
For $R_f = 24 \text{ k}$ } $g = 25$
 $R_1 = 1 \text{ k}$

bias current error = $24 \times 10^3 \times 50 \times 10^{-9}$
 $= 1.2 \text{ mV}$

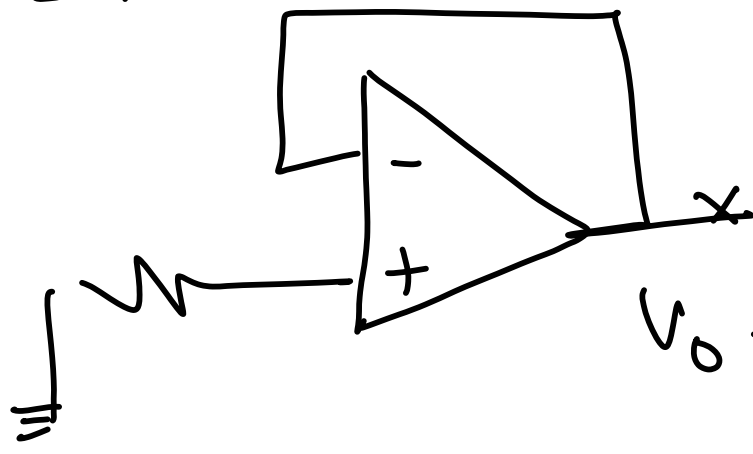


$$\begin{aligned} \text{vol drop acc } R_{-9} &= 10^5 \times 50 \times 10^{-9} \\ &= 50 \times 10^{-4} \\ &= 5 \text{ mV} \end{aligned}$$

The output of amp actually amplifies 5mV and not 10mV

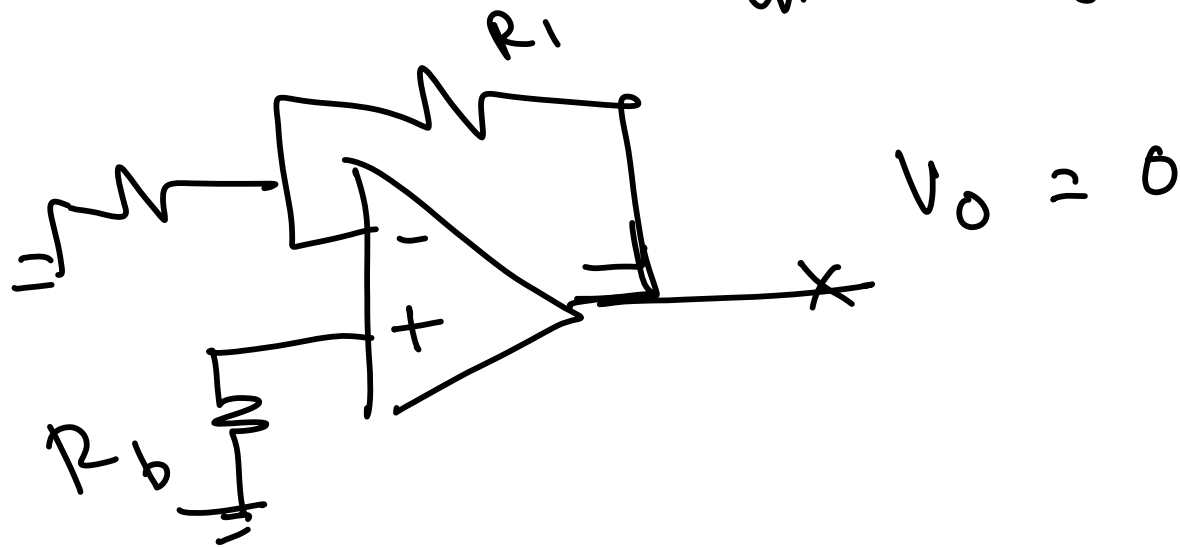


$$v_o = +v_e$$



$$v_o = -v_e$$

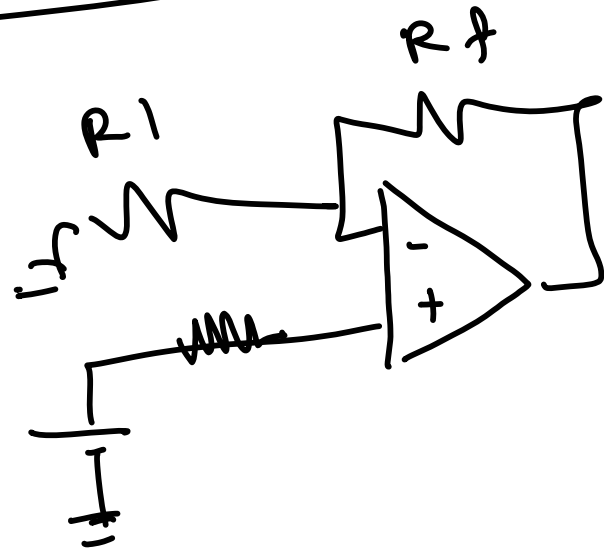
How to combine bias
current error at non-inverting
terminal with bias
current error in
inverting terminal

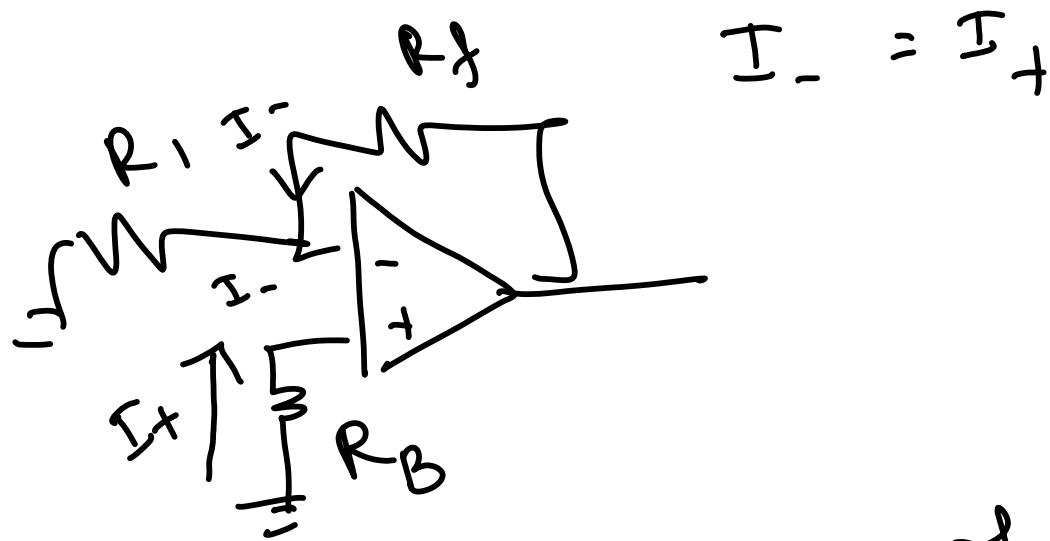


by assuming $I_{B+} = I_{B-}$
we can make error due to
bias current to zero by
selecting the resistor values
- x - x - x -

no: 26

Bias current error





By adding R_B , -ve w/ is introduced at the non-inverting input

$$R_f I_- = R_B I_+ (1 + g)$$

$$= R_B I_+ \left(1 + \frac{R_f}{R_1} \right)$$

$$R_f = R_B \left(1 + \frac{R_f}{R_1} \right)$$

$$R_B = \frac{R_f}{1 + \frac{R_f}{R_1}} = \frac{R_f R_1}{R_1 + R_f}$$

parallel combination of
 R_f and R_1

The assumption is

$$I_- = I_+$$

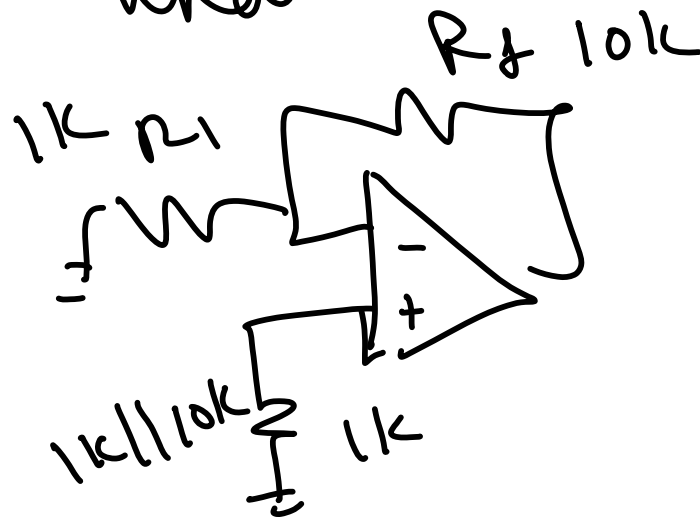
∴ I_- is not equal to I_+
In fact this is the real

life situation.

So how to reduce the error?

Assume $(I_+ - I_-) = I_{\text{offset}}$ (current)

If offset current is known
then what is the error?



Then V_o error

$$= (I_{\text{offset}} \times R_b) g$$

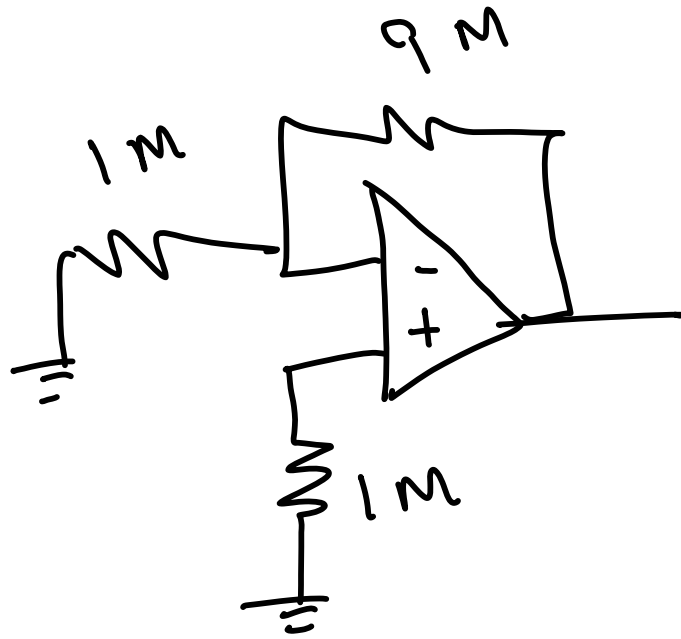
The error voltage at the output

~~to~~ $I_{\text{offset current}} \times R_b \times g_{\text{in}}$

For 741 op amp

$$I_{\text{offset current}} = 10 \text{ nA}$$

$$V_o \text{ error} = 10 \times 10^{-9} \times 10^3 \times 10$$
$$= 10^{-4} \text{ V}$$



$$\begin{aligned}
 V_o &= 1\text{M} \times 10 \times 10^{-8} \\
 &= 10^6 \times 10^{-8} \times 10 \\
 &= 0.1\text{V}
 \end{aligned}$$

The error voltage due to bias current increases with the resistance that is used to set the gain.

The offset current is not constant. It is changing with

temperature.

This is called offset current drift.

Offset current drift is a

major problem and not the
offset current by itself

① Offset voltage drift is a
major problem and it doesn't
depend up on gain setting
resistors

② The offset current drift is also a serious problem and it depends on the gain setting resistors.

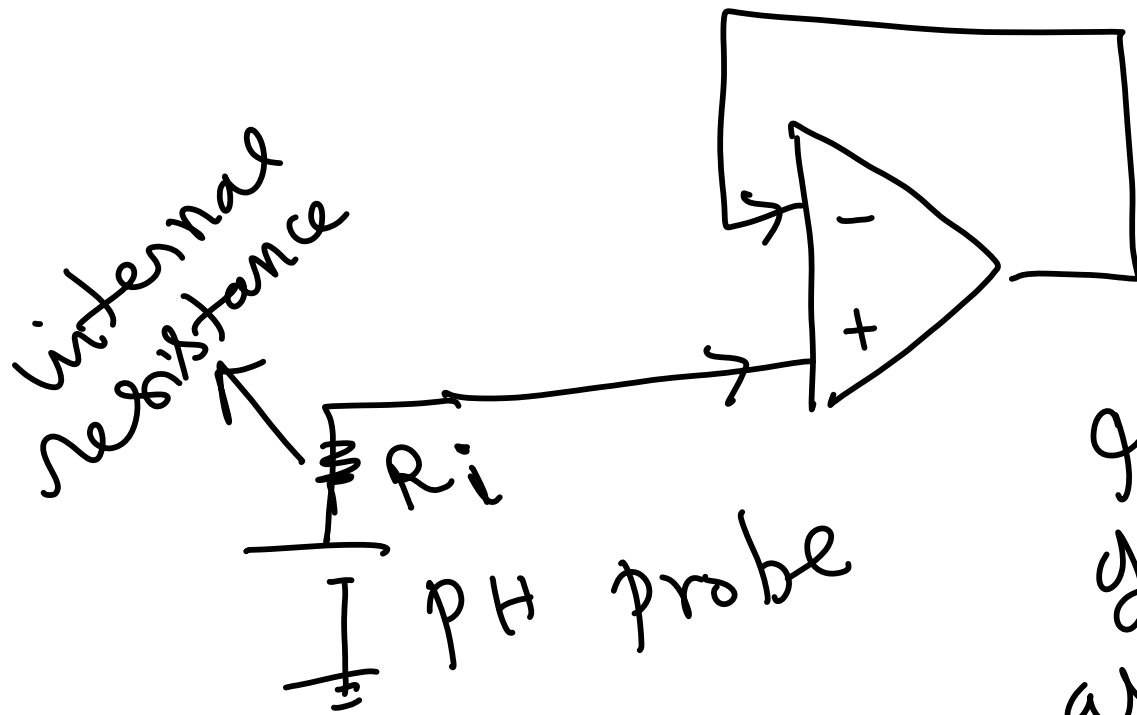
What is that we can do
to reduce the offset current
drift? (other than reducing
the resistor values)

① Go for low bias current
or low offset current
op-amps. Like Fet input
op amps.

For 741
offset current is 10 nA
[3741] which is FET input of amp
the offset current is 10 pA

Design of pH meter amplifier

- ① Select FET input of amp
- ② Use the op amp in voltage follower mode



Internal resistance
of the pH probe is
about $100\text{ M}\Omega$

The bias current I_+ must
flow through R_i

Vol drop across $R_i = R_i I_+$

Assume that
pH probe $v_i = 50 \text{ mV}$

Then v_i acc R_i

$$= 100 \text{ m}\Omega \times I_+$$

$$= 10^8 \times 10 \times 10^{-12}$$

$$= 10^{-3} \text{ V}$$

Here $I_+ = 10 \text{ pA}$

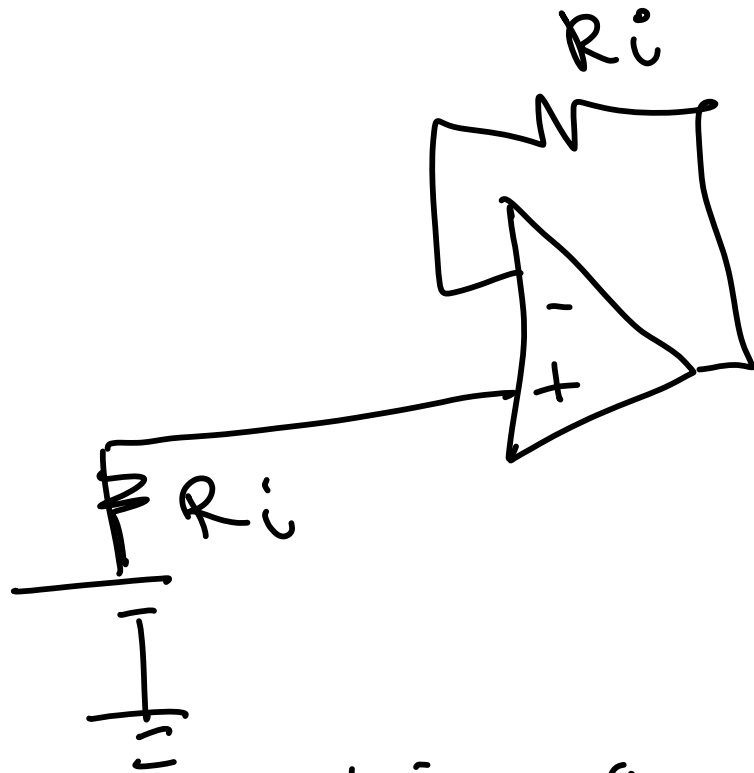
The actual voltage that is
appearing at the input

$$= 50 \text{ mV} - 1 \text{ mV} = 49 \text{ mV}$$

of the bias current of
the op amp is 1 nA

Then the voltage drop on R_i
 $= 10^8 \times 10^{-9} = 100 \text{ mV}$

Then net voltage at the
non-inverting terminal
 $= 50 \text{ mV} - 100 \text{ mV} = -50 \text{ mV}$

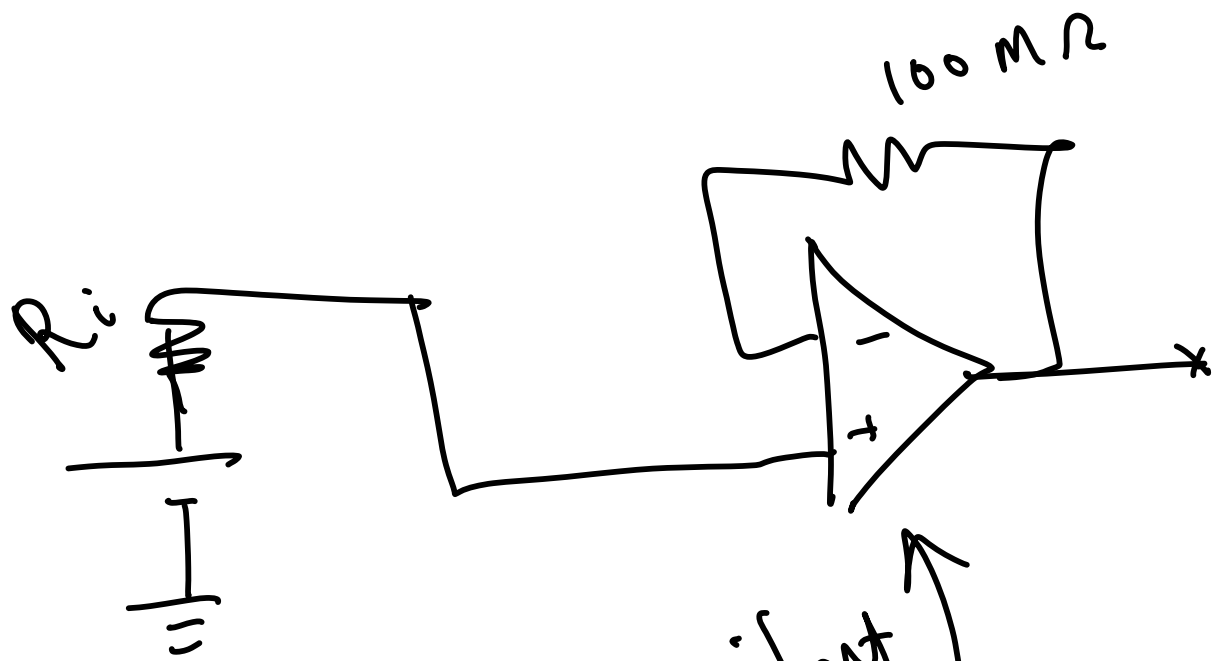


① By adding a resistance equal to R_i in the feedback path one can reduce the bias current error

② Even if we manage to connect R_i exactly in the feed back path due to offset current there will be an error voltage at the

output
The error voltage = $R_i I_{\text{offset current}}$

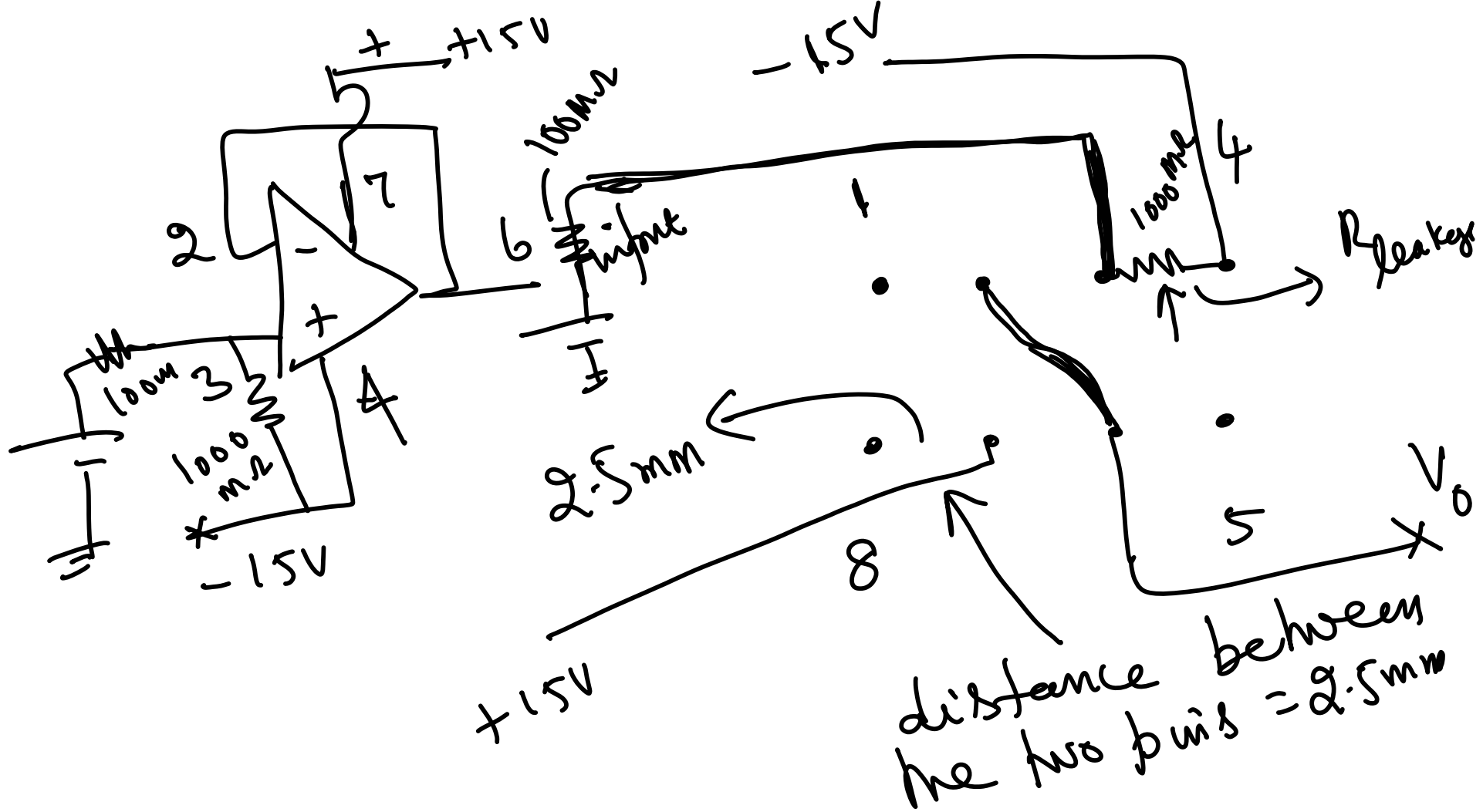
Since offset current is normally less by a factor of 10, adding resistance in the feed back path reduces the error



Fet input
op amp

I issues in the low bias current
op amp

① The leakage current in the PCB will introduce large error



Assume that

$$V_{in} = 0$$

$$R_{in} = 100 \text{ M}\Omega$$

$$R_{leak} = 1000 \text{ M}\Omega$$

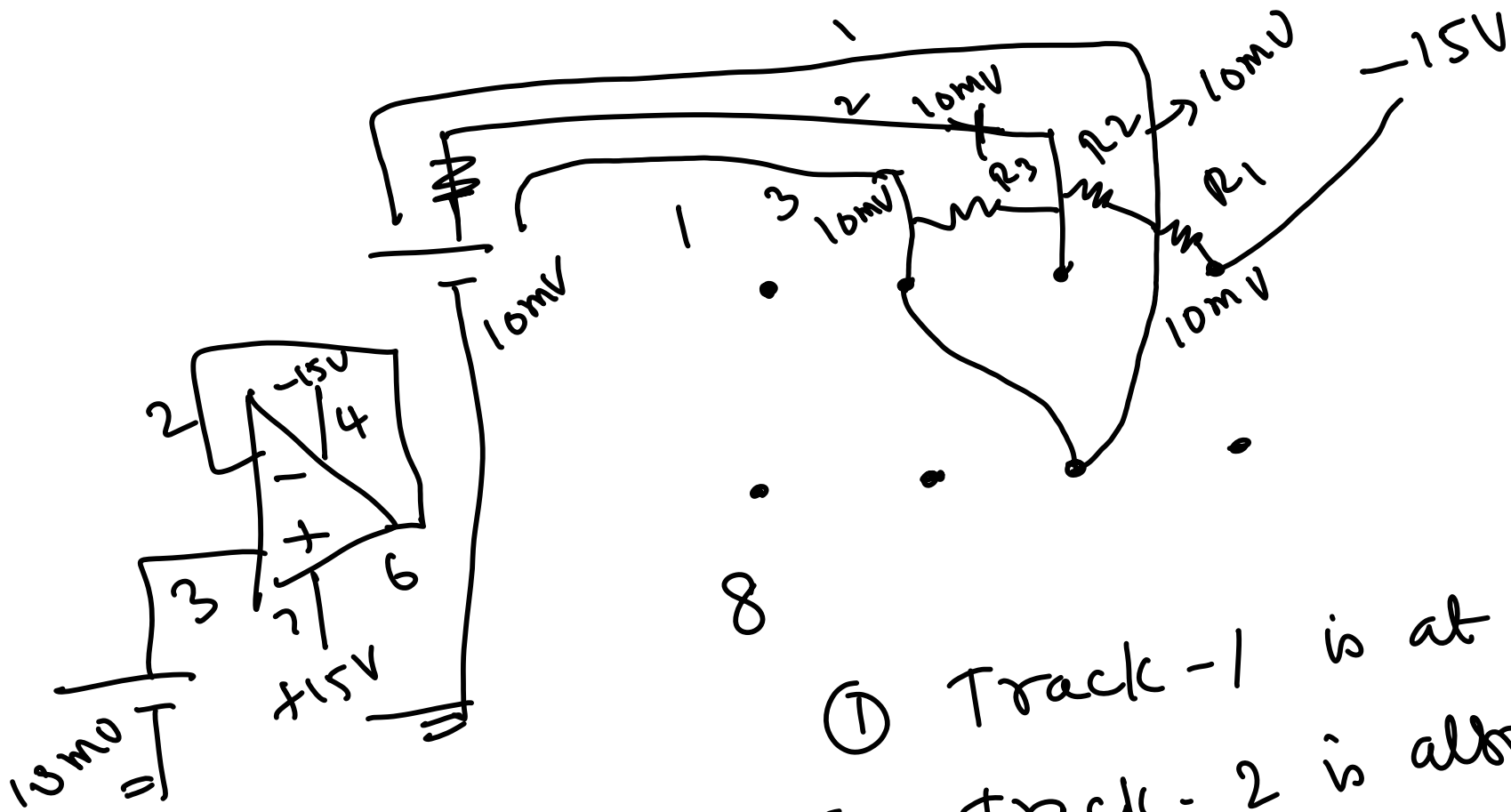
Because of the $R_{leakage}$
Vol at the non-inverting input

$$= -15V \times \frac{100}{1100}$$

$$= \frac{15}{11} = \frac{150}{11} = \underline{1.4V}$$

How to reduce this error?

We use Guarding technique to reduce the error due to leakage resistance.



- ① Track-1 is at 10mV
- ② Track-2 is also 10mV
- ③ Track-3 is also 10mV

So current through R_2 and R_3 are zero

However the leakage resistance R_1 sees one side $-15V$ and at the other side it sees $-10mV$

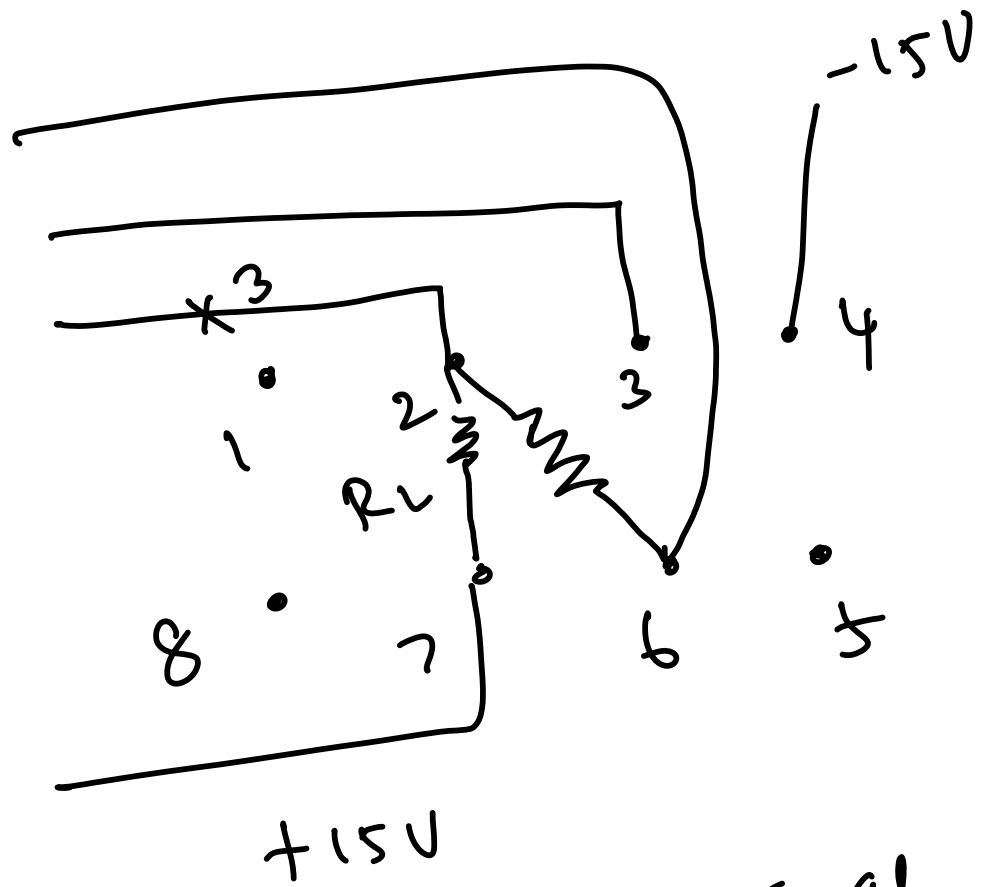
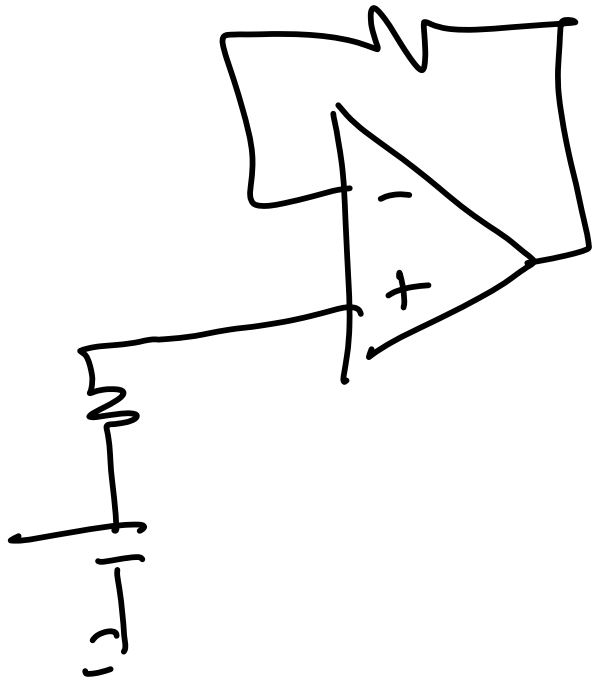
So there will be current through R_1

This current R_1 flows through the output terminal of the op amp. However this will not introduce any error at the output why?

Because the output
resistance of the op amp is
nearly zero.

So current flowing through the
output will not introduce any
error

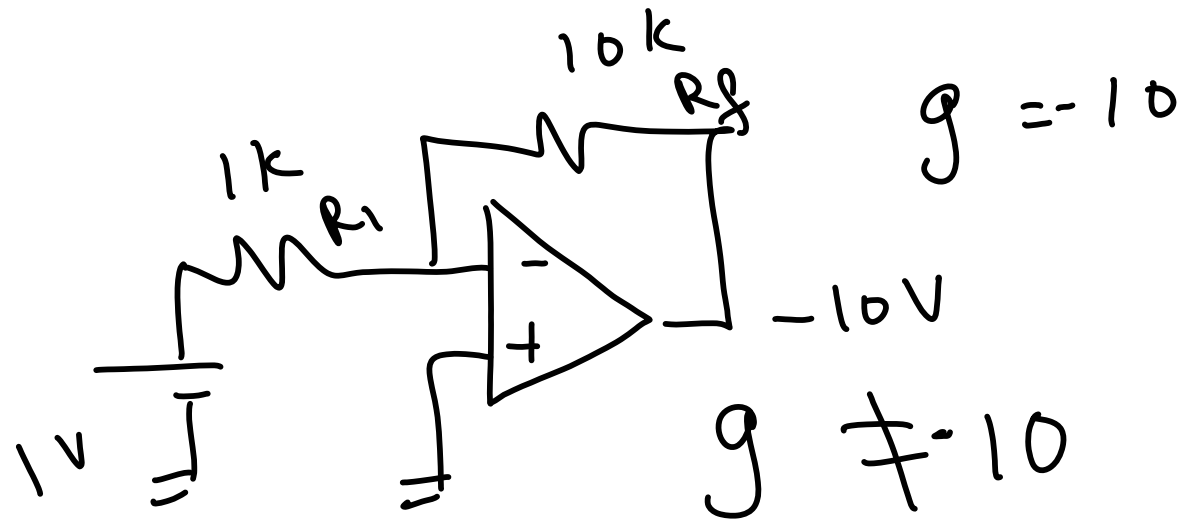
What happens if we introduce
compensating resistance in the
feedback path?



R_L will introduce an error at
 pin 2. The guarding point 3
 is of no use.

Lec no: 27

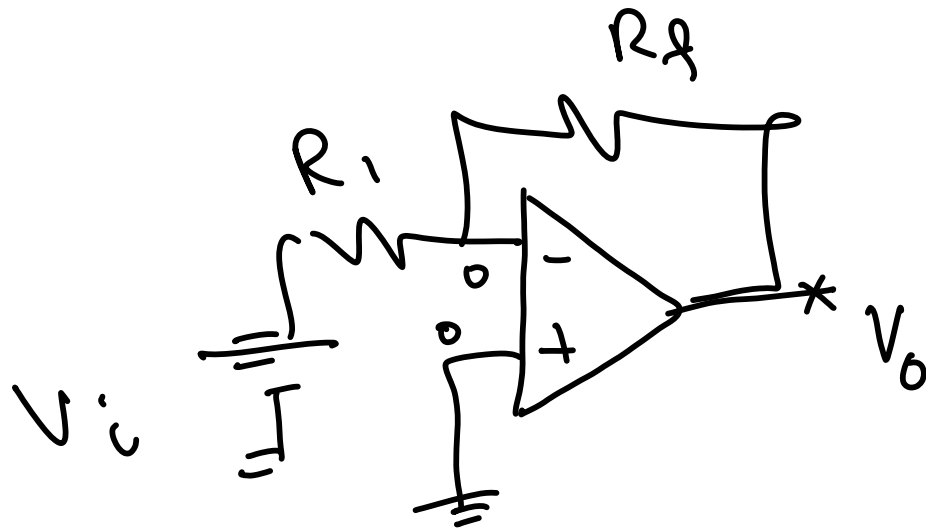
GAIN error in op amp



Actual gain = ?

$$\text{Set gain} = -\frac{R_f}{R_1}$$

Set gain \neq actual gain



inverting terminal

+ = non inverting terminal
wt

In actual case

wtage difference between

non inverting and inverting
terminal is amplified by
open loop gain

$$V_o = (V_+ - V_-) \text{ open loop gain}$$

non zero

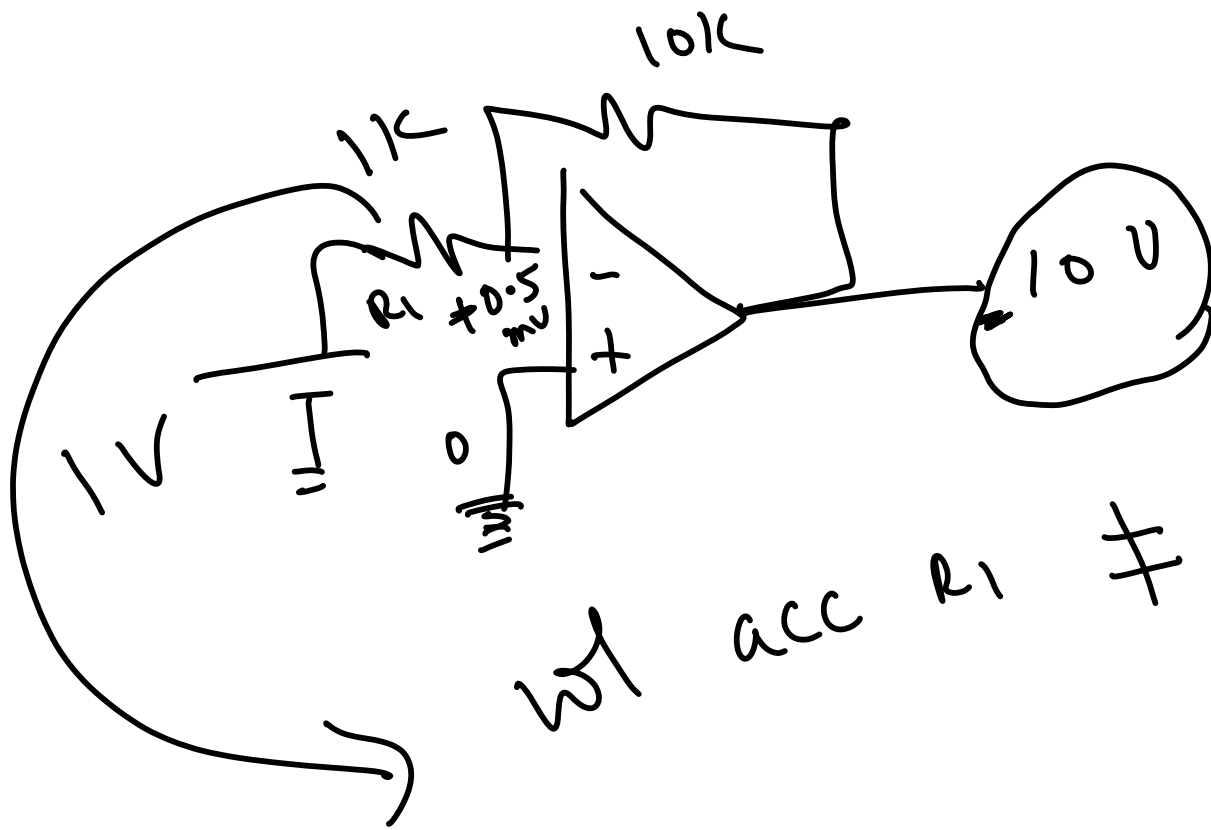
$$(V_+ - V_-) = \frac{V_o}{A}$$

For example

$$\text{For } V_o = 10\text{V}$$
$$A = 20000$$

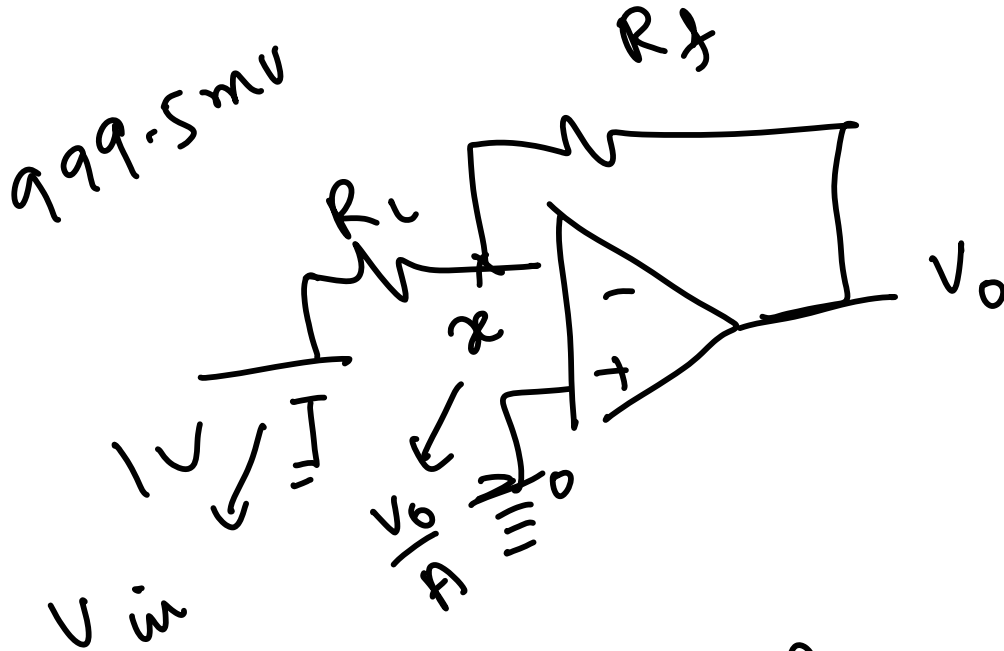
$$(V_+ - V_-) = \frac{10}{20000}$$

$$= \frac{1}{2000} = 0.5 \text{ mV}$$



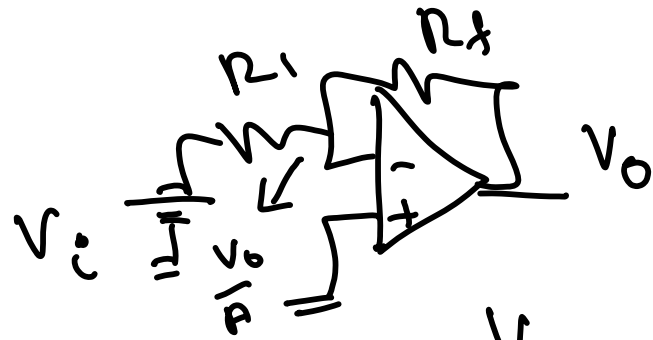
→ This will be less than 10

Actual gain is always less than set gain



$$\text{Set gain} = \frac{R_f}{R_1}$$

$$\text{actual gain} = \frac{V_o}{V_{in}}$$



$$\left(V_i - \frac{V_o}{A} \right) \frac{R_f}{R_1} = V_o \quad \frac{V_o}{A} = x$$

The input diff = $\frac{V_o}{A}$

The effective input vol = $V_i - \frac{V_o}{A}$

$$\left(V_i - \frac{V_o}{A} \right) g_s = V_o$$

$$\frac{(V_i A - V_o)}{A} g_s = V_o$$

$$\frac{V_o}{V_i} = \text{actual gain} = G_a$$

$$\left(V_i - \frac{V_o}{A} \right) g_s = V_o$$
$$\left(A V_i - V_o \right) g_s = V_o \times A \rightarrow \text{div by } V_i$$

$$\left(A - \frac{V_o}{V_i} \right) g_s = \frac{V_o}{V_i} \times A$$

$$\left(A - G_a \right) g_s = G_a \times A$$

$$G_s = \frac{G_a \times A}{A - G_a}$$

$$G_s = \frac{G_a}{1 - \frac{G_a}{A}}$$

$$G_S = \frac{G_A}{\left(1 - \frac{G_A}{A}\right)}$$

$$G_S = 100$$

What is G_A ?

Assume $A = 10000$

$$100 = \frac{G_A}{1 - \frac{G_A}{10000}}$$

$$100 \left(1 - \frac{G_A}{10000}\right) = G_A$$

$$100 - \frac{G_A}{100} = G_A$$

$$10000 - G_A = 100 G_A$$

$$10000 = 101 G_A$$

$$G_A = \frac{10000}{101}$$

$$\text{Actual} = 99$$

If the set gain and actual gain are to be close

then open loop gain must be very large

(1) open loop gain must be large compared to set gain

② The open loop gain A
Changes with temp

∴ So the gain obtained from
the op amp changes with the
temperature

↓
because open loop gain A
changes with temperature

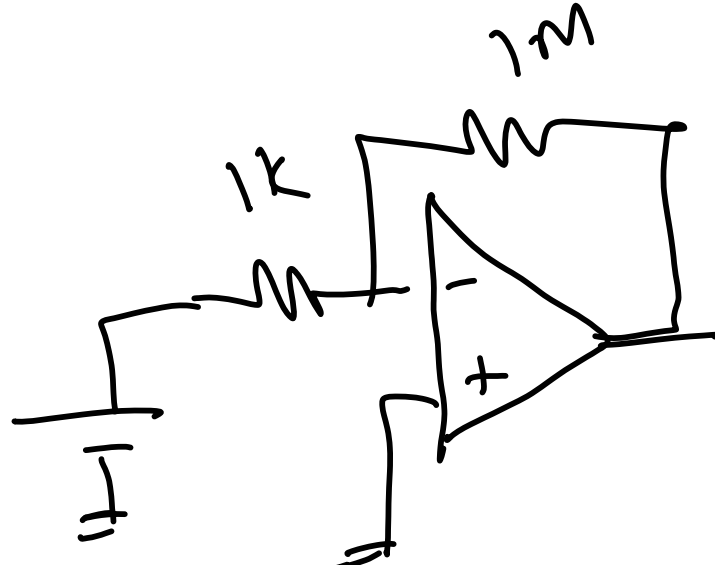
To keep the gain change to
a minimum we have to
make sure $\frac{h_s}{A}$ is small

Example - 1

Required

gain = 1000 = G_s
of amp 741

$A = 20,000$



$$1000 = \left(\frac{G_A}{1 - \frac{G_A}{20000}} \right)$$

$$G_A = \frac{G_s}{1 + \frac{G_s}{A}}$$

$$G_A = \frac{1000}{1 + \frac{1000}{20000}} \rightarrow \text{Set gain}$$

open loop gain

$$G_A = \frac{1000}{1 + \frac{1}{20}} = \frac{1000}{1.05}$$

SSO

$$G_A = \frac{955}{1}$$

SS it Stable again?
Kemp ??

The open loop gain of the op amp changes with temp

Assume that gain increases

from 20000 \rightarrow 30000

Then the new actual gain is given by

$$G_A = \frac{G_s}{1 + \frac{G_s}{A}}$$
$$= \frac{1000}{1 + \frac{1000}{30000}}$$

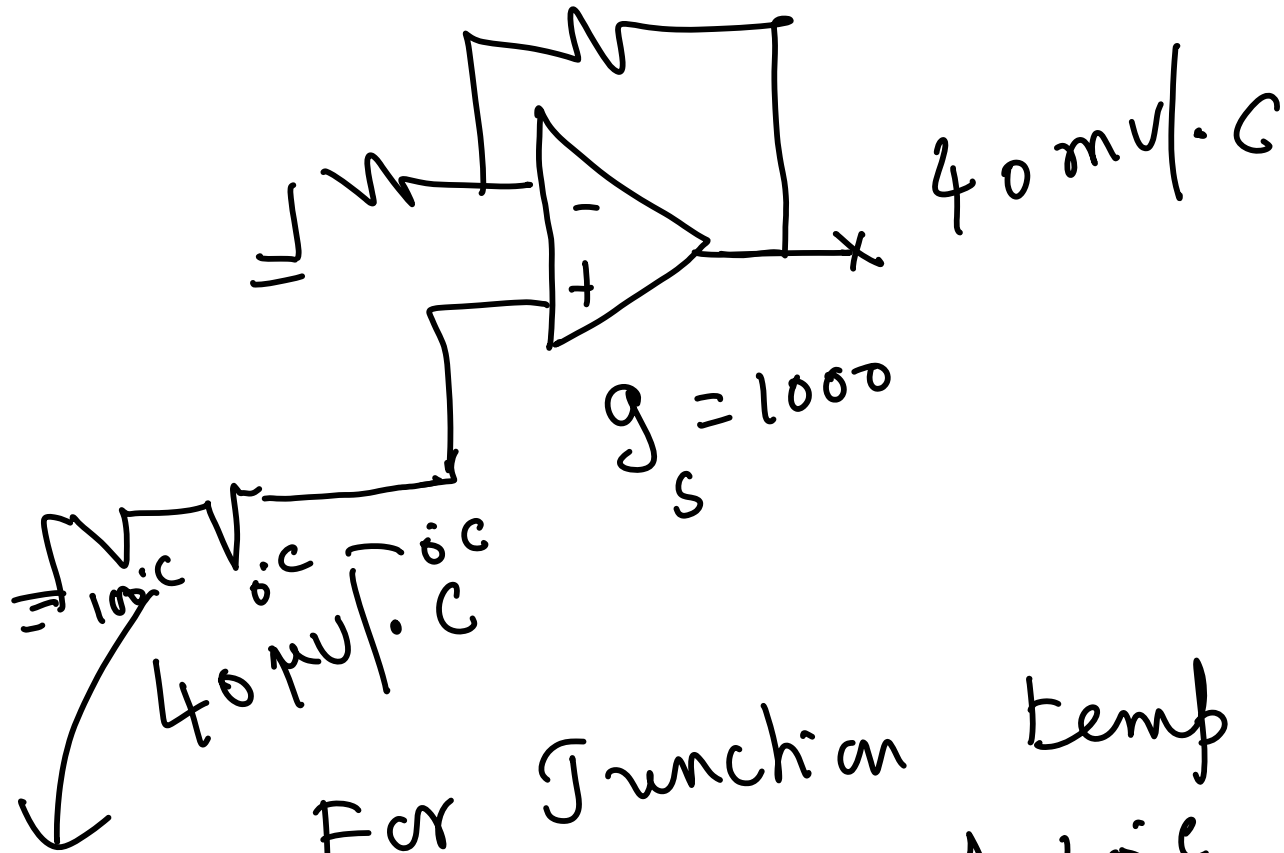
$$G_A = \frac{1000}{1 + \frac{1}{30}} = \frac{1000}{1.03}$$

$$G_A \approx 970$$

The gain which is supposed to
be 1000 is
at 25°C ambient → 955
85°C ambient → 970

Example 2

Thermo Couple amp



For Junction temp
difference of 10°C
the expected thermo couple
vol = $40 \times 100 = 4 \text{ mV}$

For gain of 100 (Set gain)
the expected output is

$$= 4 \text{ mV} \times 100 = 4 \text{ V}$$

In real case you will never get
4 V output even though
thermocouple voltage is correctly at
4 mV

We know at 25°C ambient

the $A = 2000$

At 50°C ambient

$A = 3000$

Actual gain at
25°C ambient = 955

Actual gain at
50°C ambient = 970

V_o at 25°C ambient = 4×955 mV

V_o at 50°C ambient = 4×970 mV

at 25°C = 3.820 V

at 50°C = 3.880 V

Difference in output = 60 mV

At the output of the
of amp Sensitivity = $40 \times 1000 \mu\text{V}$
= 40 mV

The expected error = 1.5°C
at the output

The absolute error at 25°C

$$= (4 - 3.820) \text{ V}$$

$$= 180 \text{ mV}$$

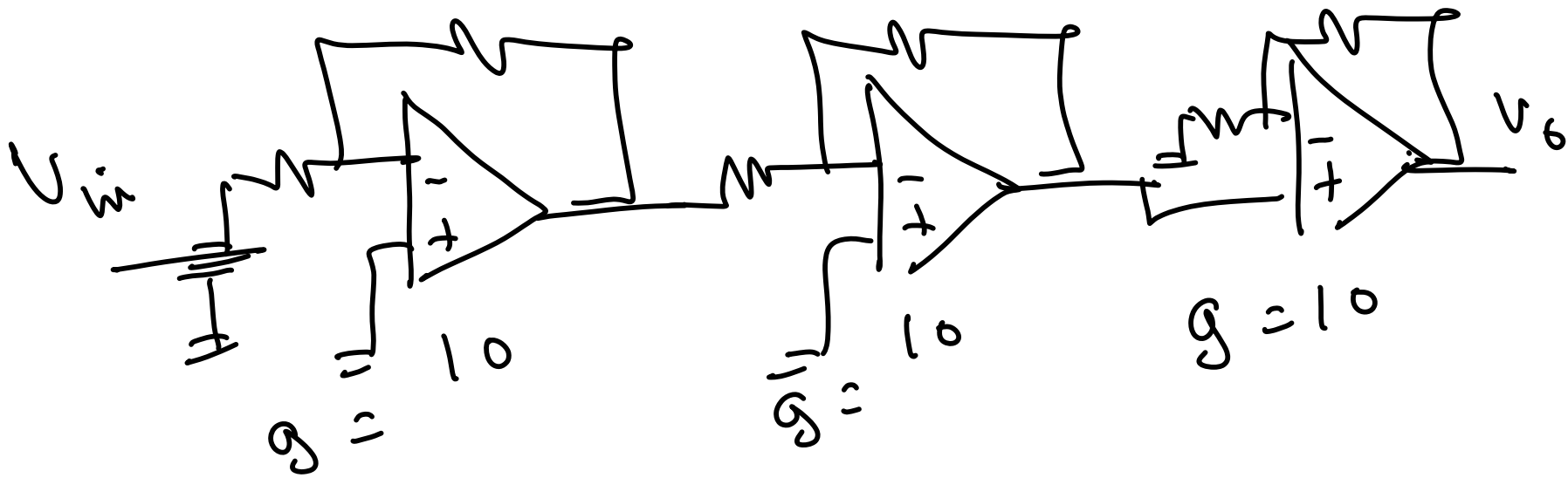
$$= \frac{180}{40} = 4.5^\circ\text{C}$$

At room temp 100°C temp
will be read as $= 96.5^{\circ}\text{C}$

At 80°C room temp 100°C temp
will be read as $= 98^{\circ}\text{C}$

What is to be done?

Obtain the required gain of
1000 in 3 stages.



Total gain = 1000

Single Stage gain

$$G_A = \frac{10}{1 + \frac{10}{20000}} = \frac{10}{1 + \frac{1}{2000}}$$

$$= \frac{10}{1 + 0.0005} = \frac{10}{1.0005} = 9.995$$

For 3 Stages

$$\text{total gain} = \frac{10}{1.0005} \times \frac{10}{1.0005} \times \frac{10}{1.0005}$$

$$\approx 999$$

- check this

total gain at

80c ambient

$$= \frac{10}{1 + \frac{10}{3000}} \times \frac{10}{1 + \frac{10}{3000}} \times \frac{10}{1 + \frac{10}{3000}}$$

$$= 999.5$$

check this

To get larger gain use
many stages

to get the required gain
from multiple stages.
This reduces the gain error
and also gain drift.

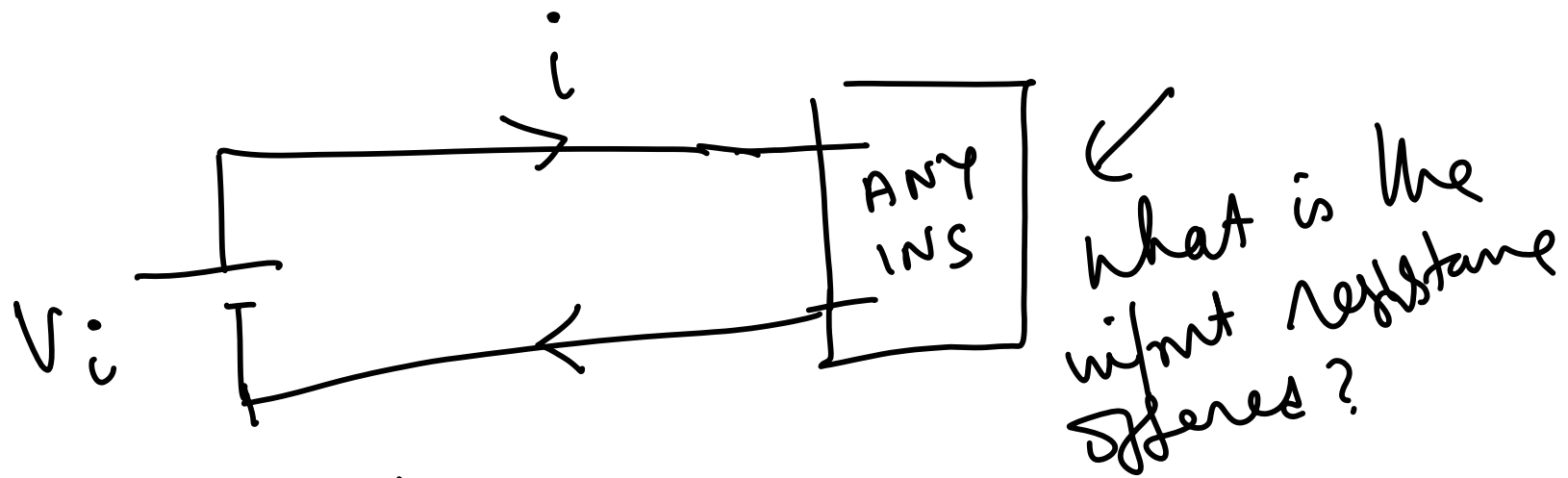
Do not set large gain
for one single stage

Lec no: 28

② INPUT RESISTANCE

③ output resistance

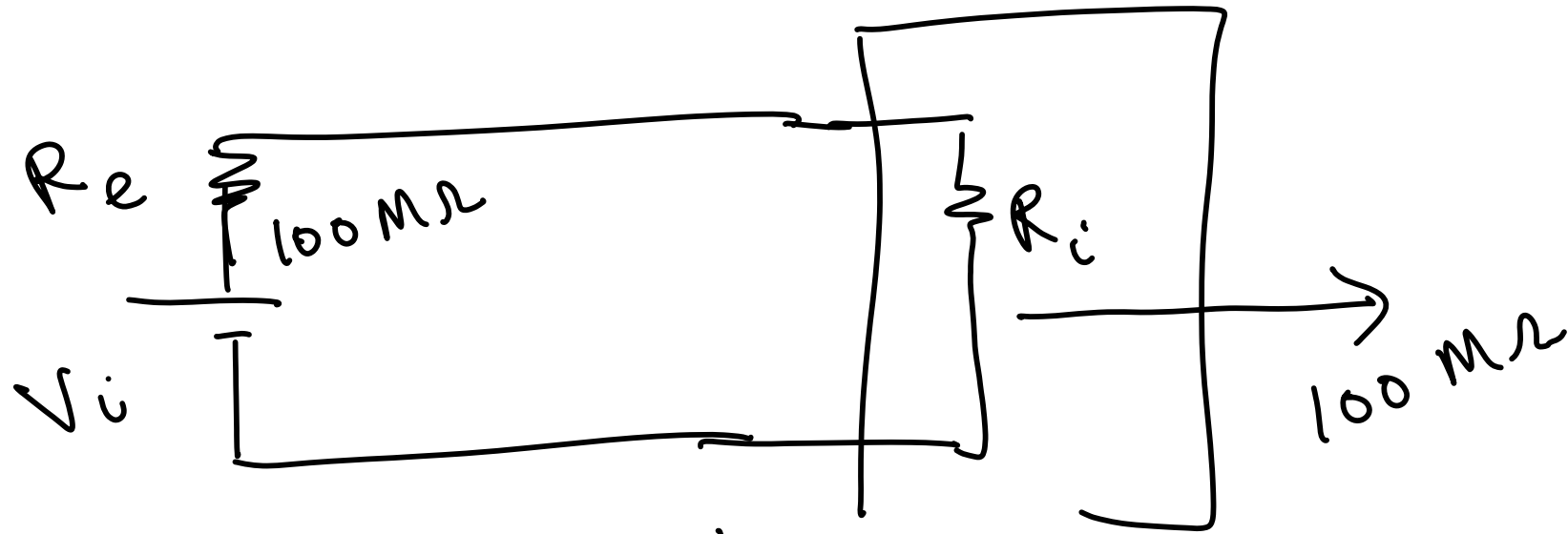
INPUT RESISTANCE



The effective input resistance

$$= \frac{V_i}{i} = \frac{1V}{1\mu A} = 1M\Omega$$

As long as source impedance is zero the input resistance offered by the instrument is of no importance



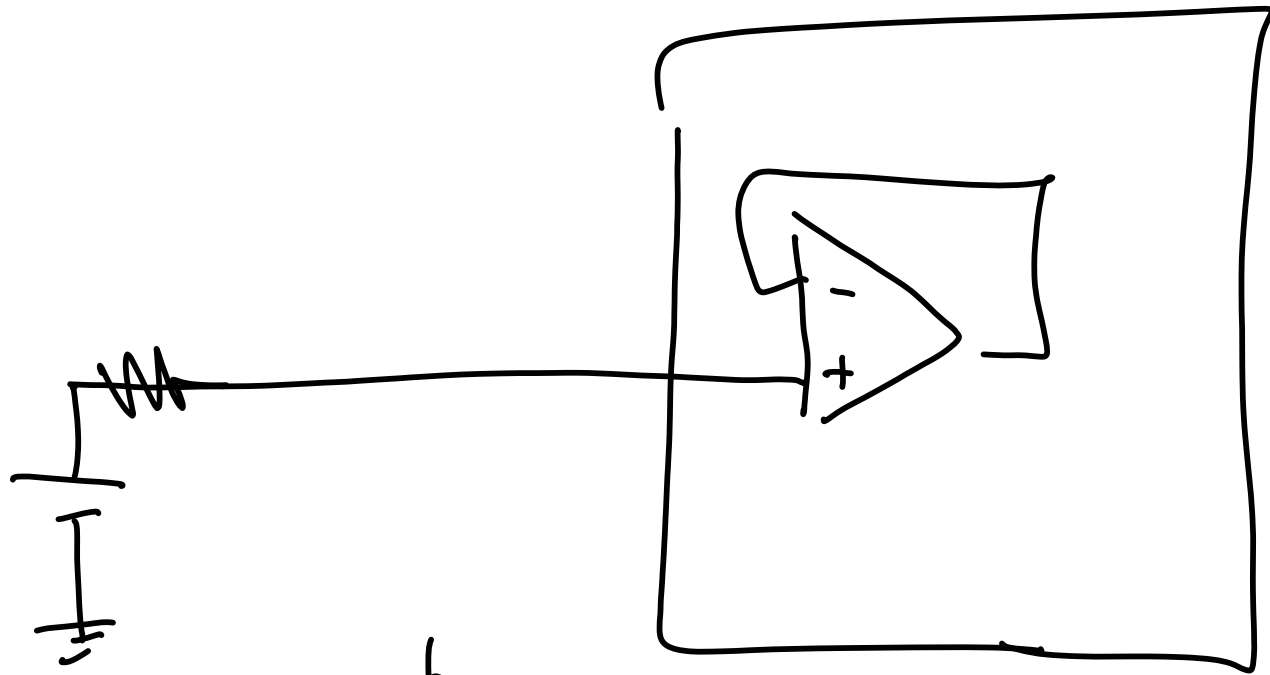
For PA Probe

internal resistance = $100\text{ M}\Omega$

Even if $R_i = 100\text{ M}\Omega$

Then half of V_i alone
appear as input at the
instrument

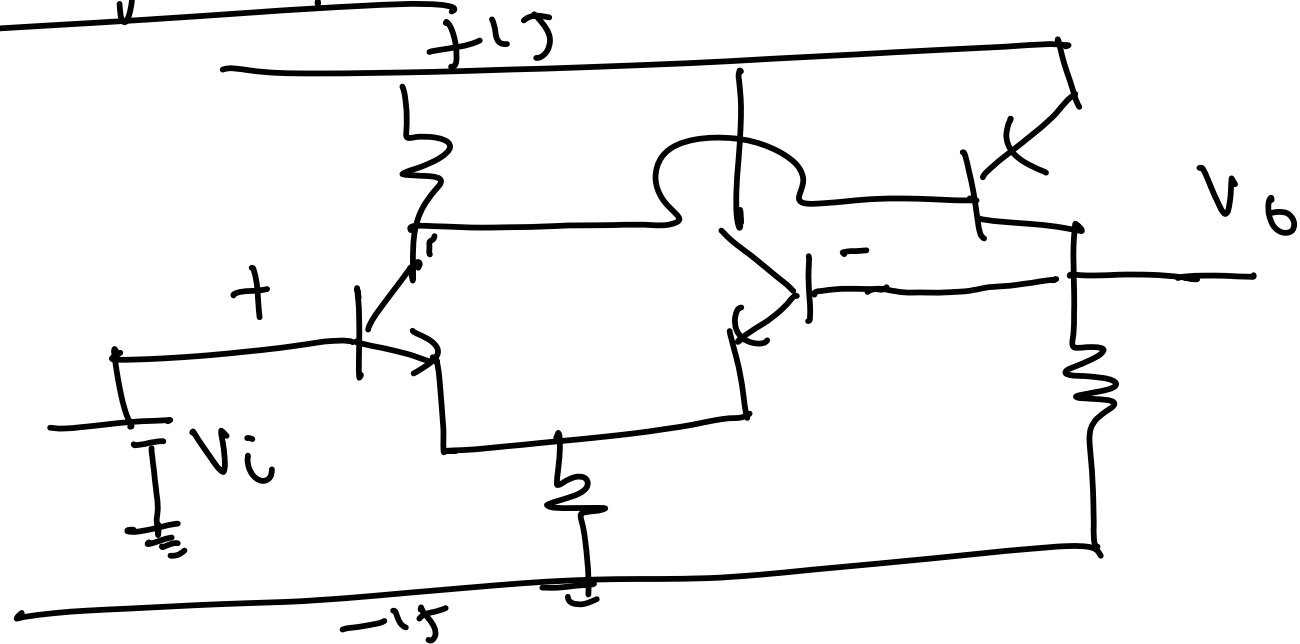
So ideally speaking
input resistance must be
infinite for voltage measurement



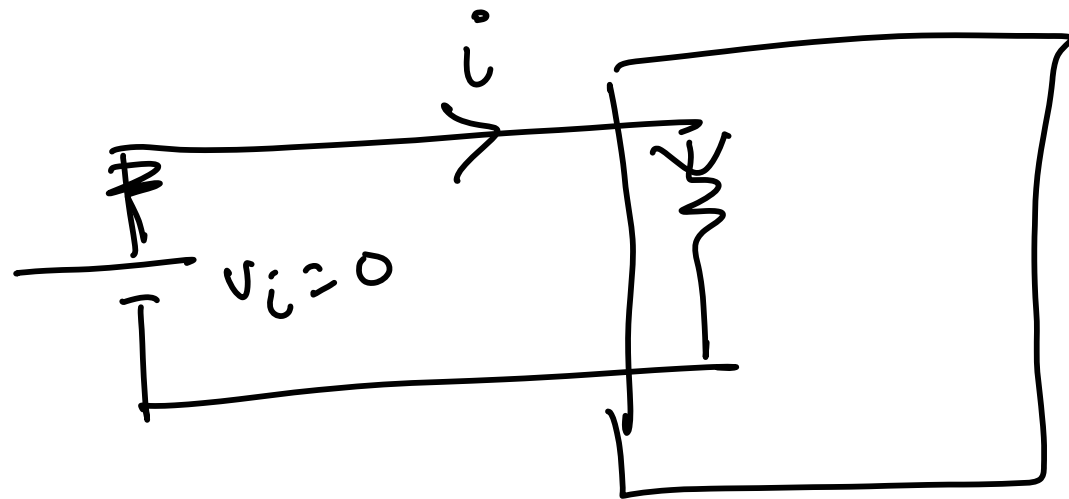
① what is the
input resistance offered by the
op amp

- ② For ideal op amp it is infinite
- ③ But for real op amp it is not infinite.
It also varies with gain

Real op amp



In case of op amp
even for $V_i = 0$ there is a
current

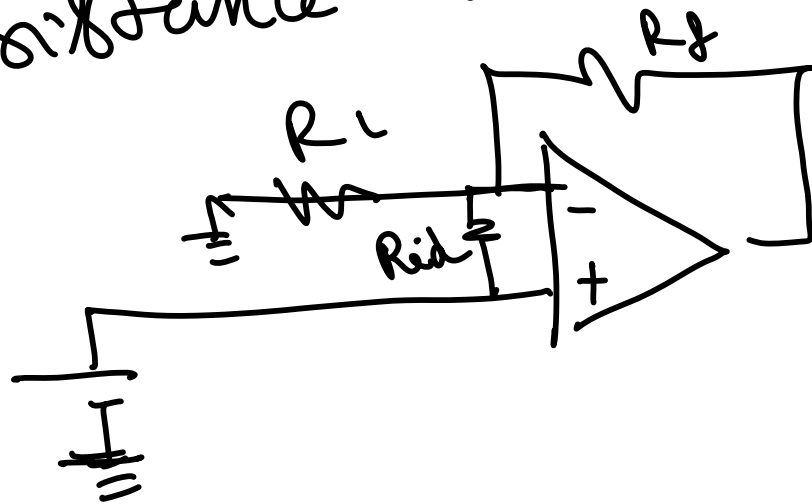


Here even for
 $V_i = 0$ there is a current to
the input. This is taken as
bias current.
Bias current is not considered
directly for input resistance

Calculation.

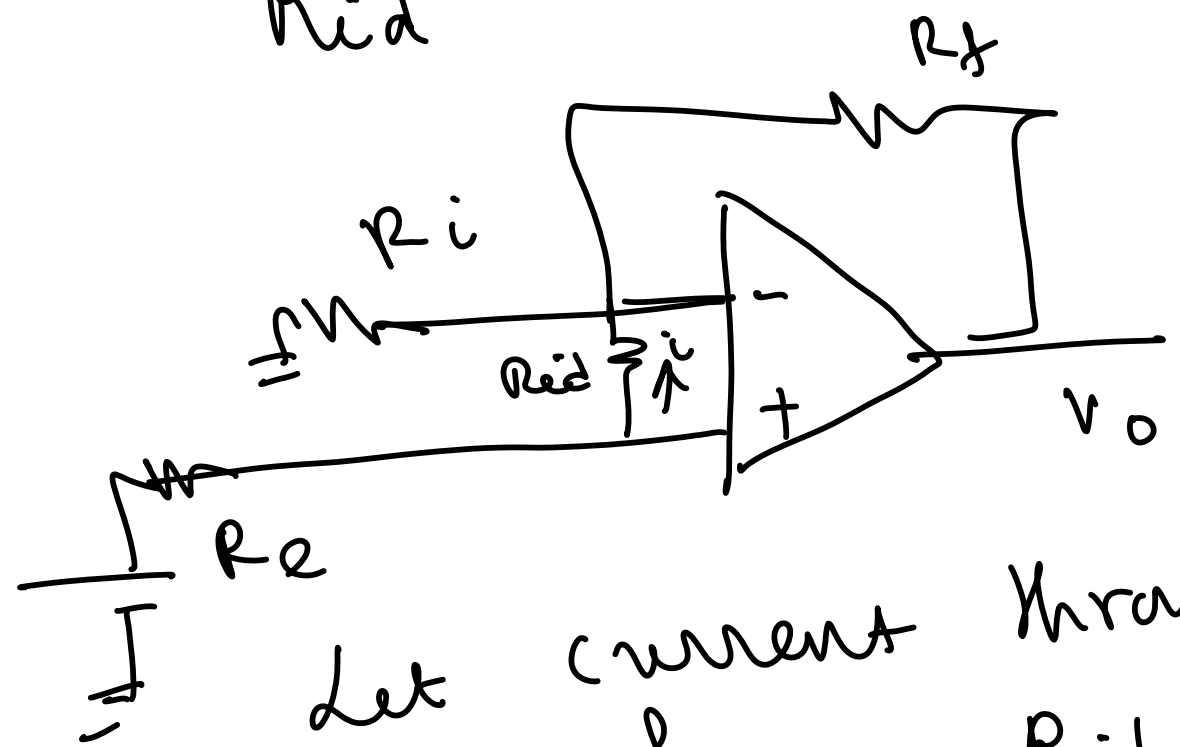
However when the input voltage goes up bias current increases. This increase in current is due to input resistance

How to represent the input resistance ~~is~~ with the of amp



R_{id} is called differential
input resistance of the
 op amp

R_{id} is not input resistance



Let current through $R_{id} = i$
 Then w/ acc $R_{id} = R_{id} \times i$

$(R_{id} \times i) =$ differential vol
at the input

$$(R_{id} \times i) A = V_o \quad \text{--- (1)}$$

When A is open loop gain

$V_o =$ output voltage

$$i = \frac{V_i}{R}$$

where V_i is the
input voltage
 R is the input
resistance

$$\left(R_{id} \times \frac{V_i}{R} \right) A = V_o$$

$$\frac{R_{id} \times A}{R} = \frac{V_o}{V_i}$$

but $\frac{V_o}{V_i} = \text{gain}$

$$\frac{R_{id} \times A}{R} = g$$

g is a
closed loop
gain

$$g = \frac{R_{id} \times A}{R}$$

$$R = \frac{R_{id} \times A}{g}$$

① The input resistance offered by the op amp varies with gain g . Higher the closed loop gain lower the input resistance

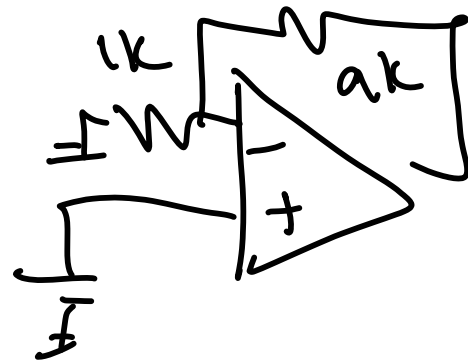
For example

for 741 op amp

$$R_{id} = 200k$$

$$A = 20000 \text{ (min)}$$

$$\text{For } g = 10$$



What is the input resistance offered by this circuit?

$$\begin{aligned} R &= \frac{R_{id} \times A}{g} = \frac{200 \times 10^3 \times 20000}{10^{-3}} \\ &= 200 \times 10^3 \times 2 \times 10^3 \\ &= 2000 \times 10^6 \\ &= 2000 \text{ M}\Omega \end{aligned}$$

For $g = 1000$

$$\begin{aligned} R &= \frac{200 \times 10^3 \times 20000}{1000} \\ &= 200 \times 10^3 \times 20 \end{aligned}$$

$$= 4 \times 10^6 = 4 \text{ M}\Omega$$

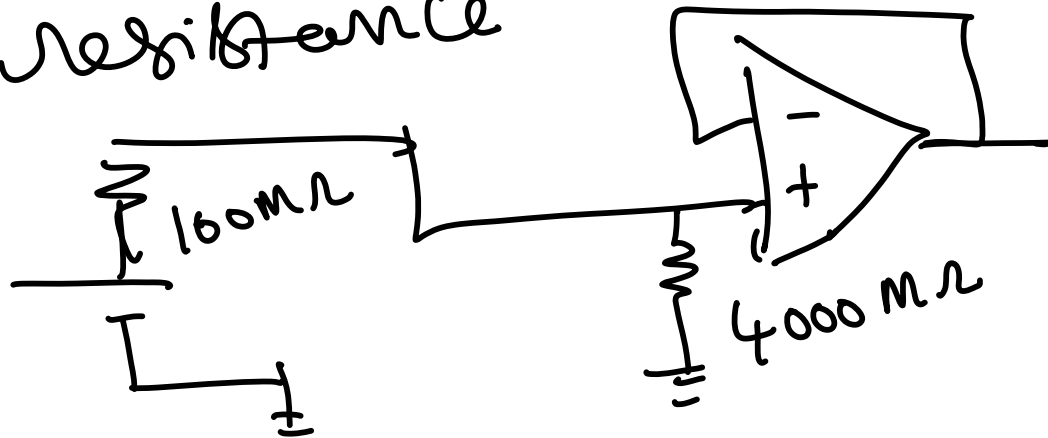
For voltage follower.

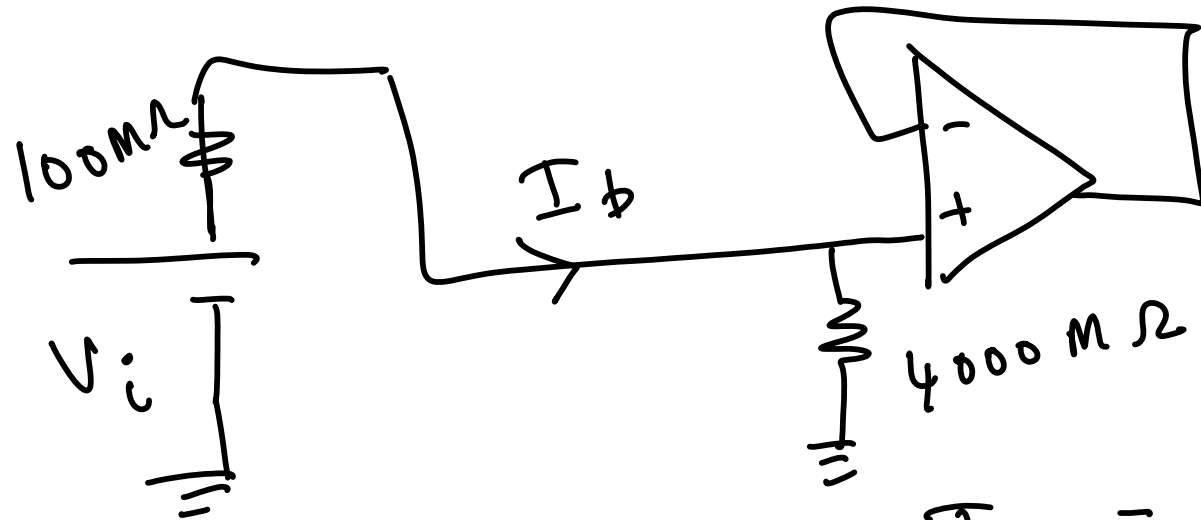
$$R = \frac{R_{id} \times A}{g} = \frac{200 \times 10^3 \times 20000}{1}$$

$$= 4 \times 10^9$$

$$= 4000 \text{ M}\Omega$$

voltage follower gives highest input resistance





For example if $I_b = 10\text{ pA}$
 For R_{in} input of amp
 w/ drop on the internal resistance

$$= 10^8 \times 10 \times 10^{-12}$$

$$= 10^9 \times 10^{-12} = 1\text{ mV}$$

voltage loss due to bias current
 $= 1\text{ mV}$

Voltage loss due to input
resistance of the amp

$$= V_i \times \frac{100}{4000+100}$$

$$= V_i \times \frac{100}{4100} = V_i \times \frac{1}{41}$$

If $V_i = 100 \text{ mV}$

Then voltage loss = $\frac{100}{41} = 2.5 \text{ mV}$

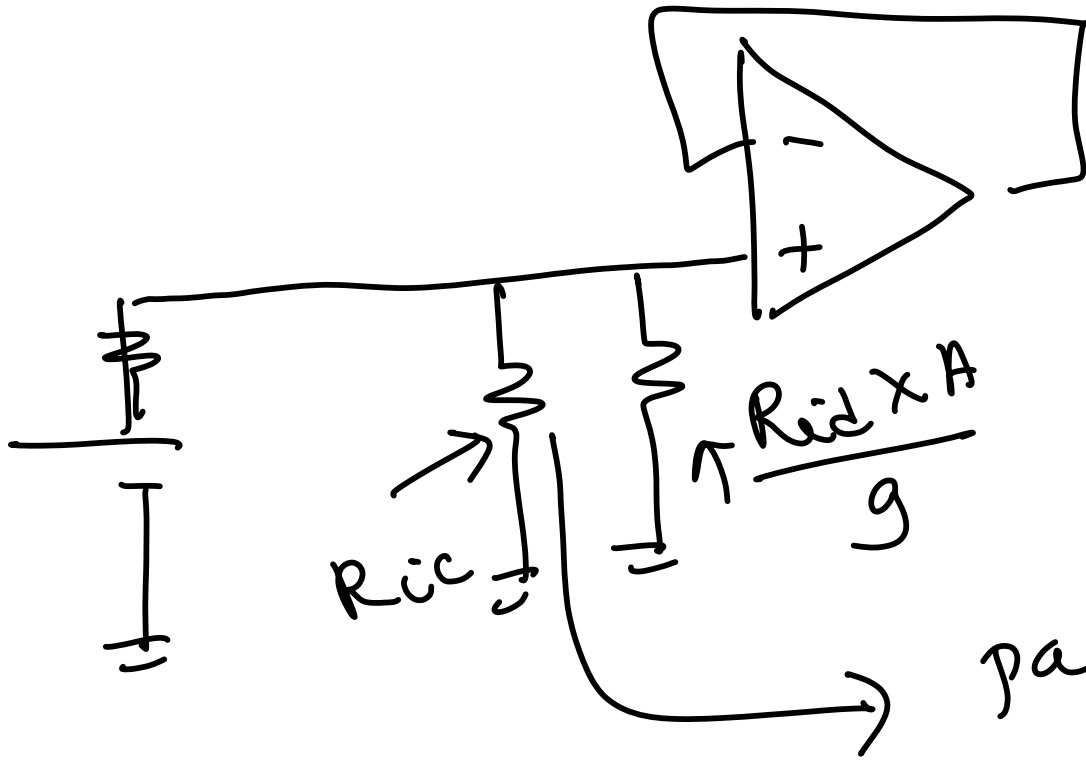
So for 100 mV pH probe output
1 mV is lost due to bias current
and 2.5 mV is lost due to input

Resistance

Total loss in WJ

$$= \text{bias current loss} + \text{input resistance loss}$$

Input resistance is also affected by package resistance



Package resistance is constant.
 It is not changing with gain etc.

The effective input resistance
of the op amp = $R_{ic} \parallel R$

where $R = \frac{R_{id} \times A}{g}$

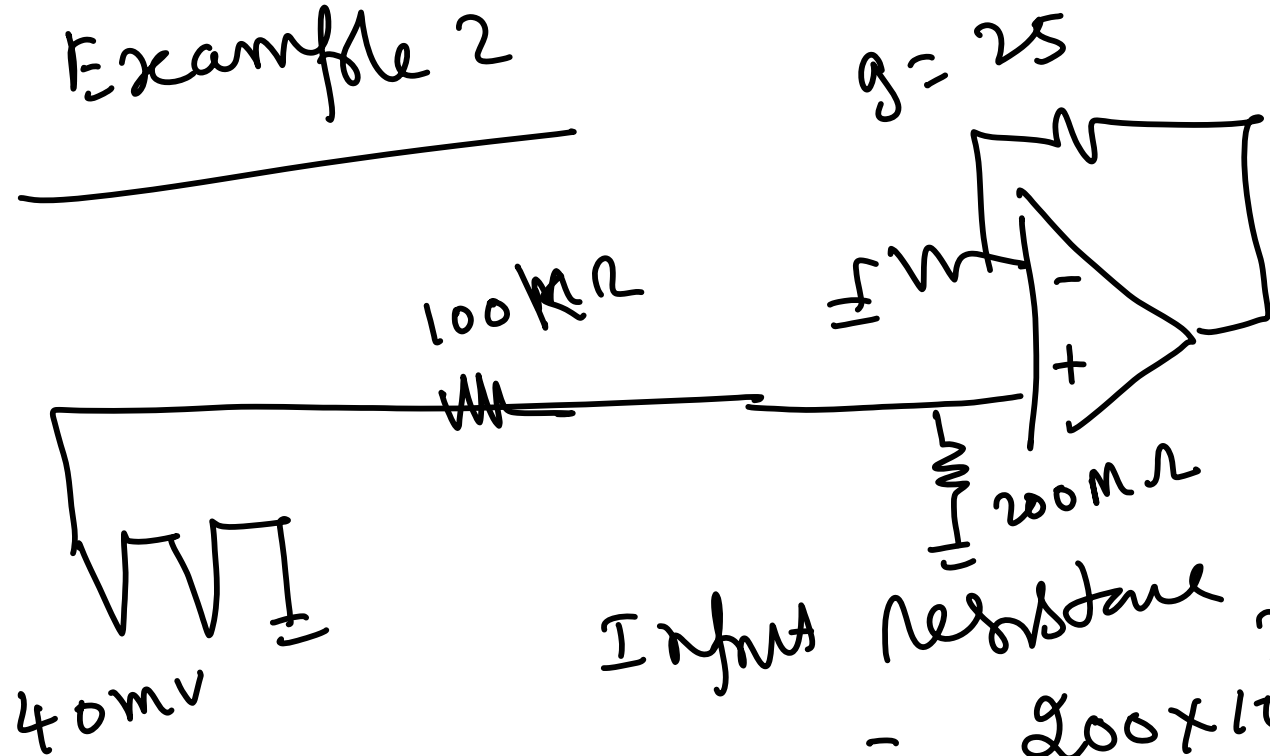
For 741 or $g = 1$

$$R = 4000 \text{ m}\Omega$$

$$R_{ic} = 4000 \text{ m}\Omega$$

So for 741 op amp the highest
input resistance = $4000 / 4000 \text{ m}\Omega$
= $2000 \text{ m}\Omega$

Example 2



Input Resistance

$$= 200 \times 10^3 \times \frac{25000}{25}$$

$$= 200 \text{ m}\Omega$$

The internal resistance = 100 k Ω

Voltage loss due to input resistance

$$= \frac{40 \times 10^{-3} \times 100 \times 10^3}{200 \times 10^6}$$

$$= \frac{40 \times 10^6}{200 \times 10^6} = \frac{40 \times 10^{-6}}{2}$$

$$= 20 \mu V$$

loss due to bias

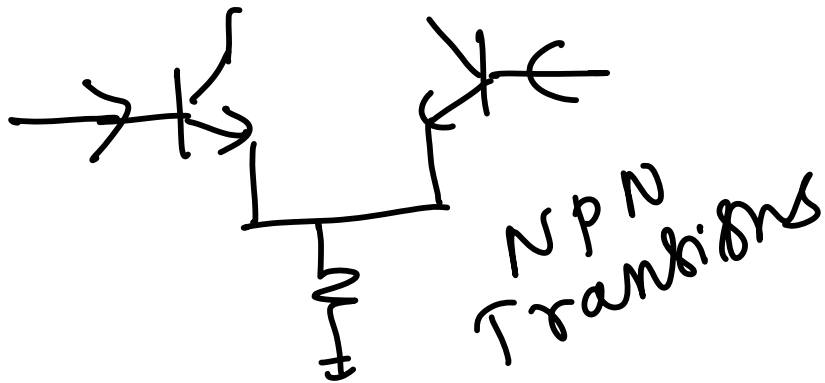
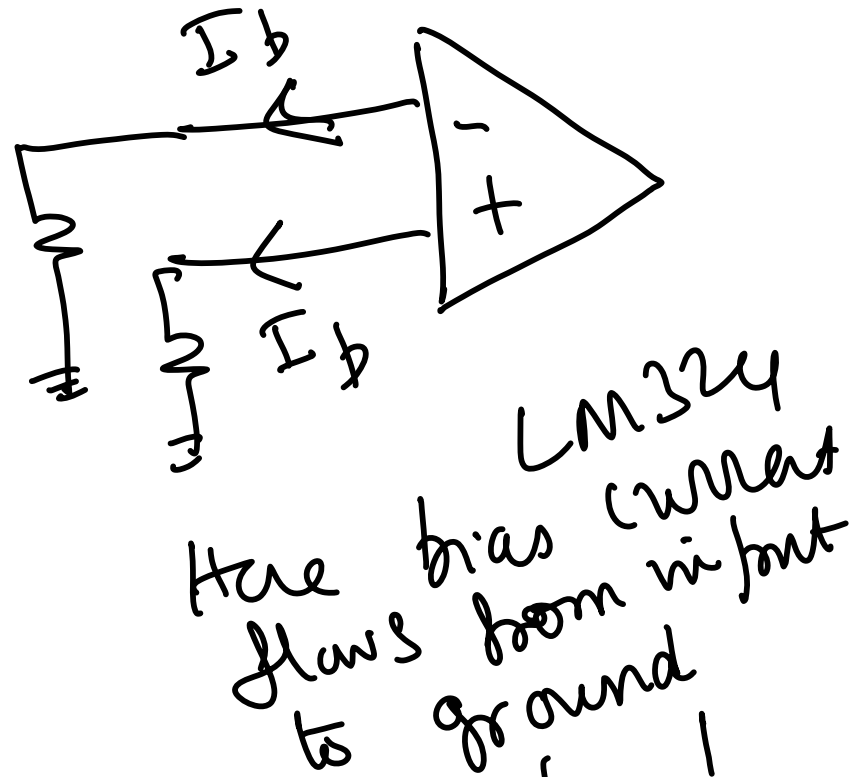
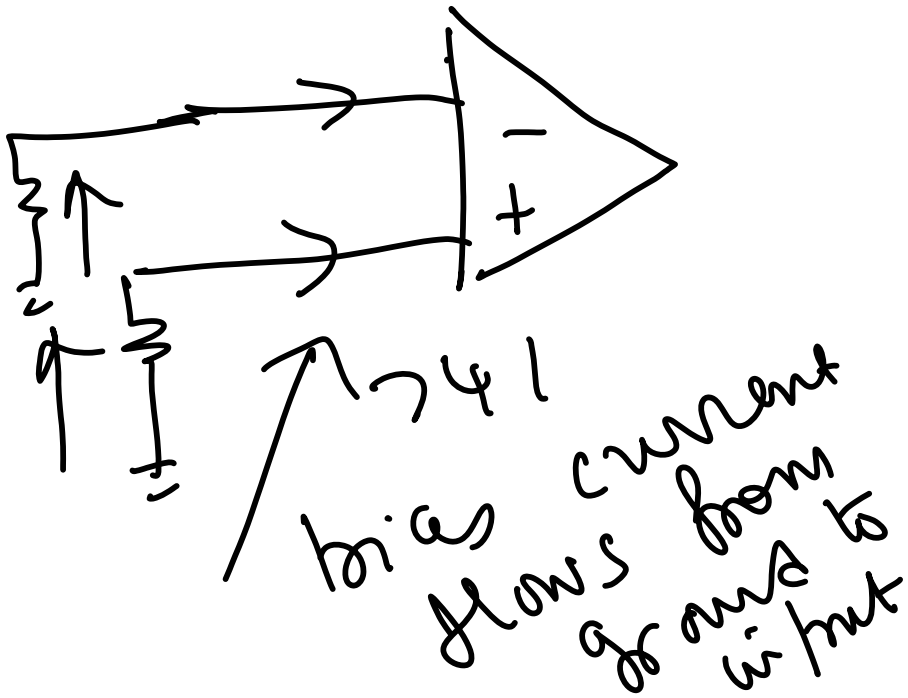
$$\text{Current} = R_{\text{wit}} \times I_b \rightarrow 10 \text{ nA}$$

$$= 100 \times 10^3 \times 10^{-8}$$

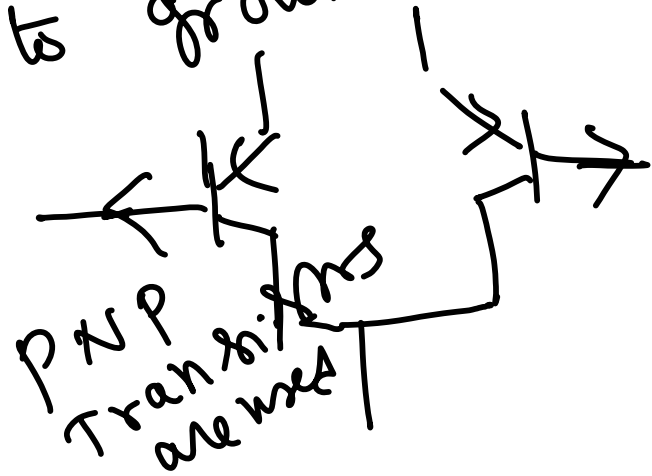
$$= 100 \times 10^{-5} = 1 \text{ mV}$$

In this loss due to bias
current is more than wit
resistance loss

Bias current direction depends on the op amp !!



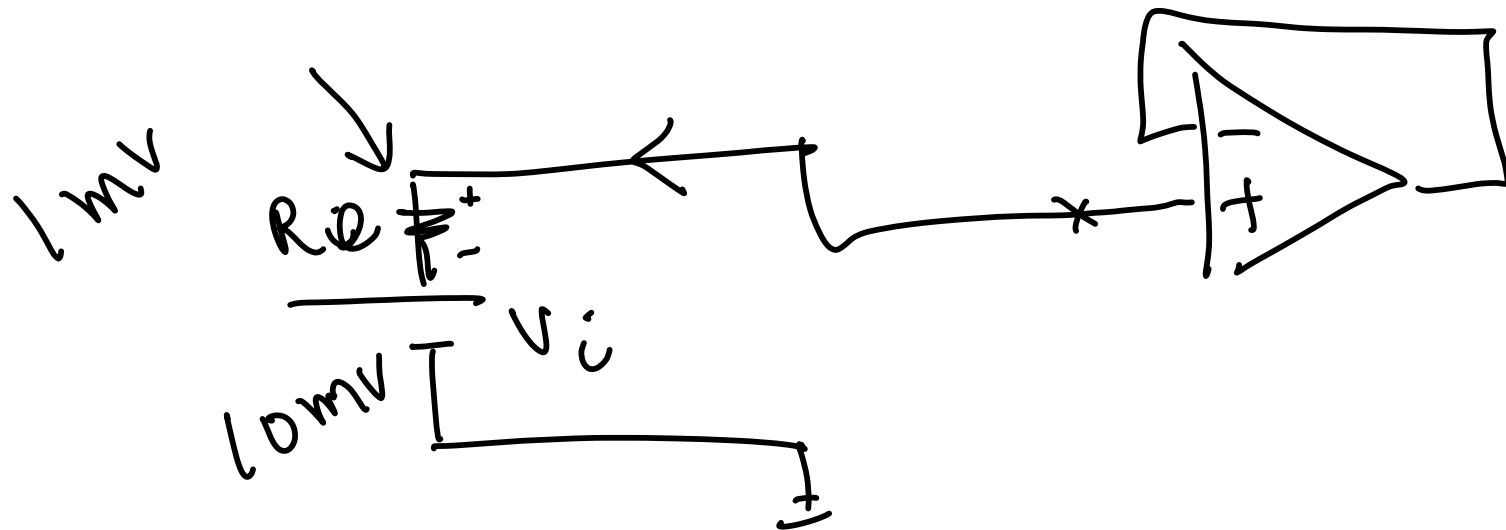
NPN Transistors



PNP Transistors are used

① Most of the op amps are NPN type. So bias current flows into the terminals

② Only single supply op amps use PNP transistors. (rail to rail op amp)



Voltage drop across the
internal resistance R_e

$$= R_e \times I_b$$

$$= 10^5 \times 10^{-8} = 10^{-3} \text{ V} = 1 \text{ mV}$$

This voltage is added to the
input source.

So the net effective voltage

$$\text{seen by the op amp} = 10 \text{ mV} + 1 \text{ mV}$$

$$= 11 \text{ mV} \quad (\text{For } 324 \text{ op amp})$$

In case of 741 op amp

The effective voltage
at the input of the op amp
 $= 10 \text{ mV} - 1 \text{ mV} = 9 \text{ mV}$

In addition to this voltage
loss due to input resistance
must be calculated as before.

This error is same for both
the types of op amp. There
is no difference.

- x - x -

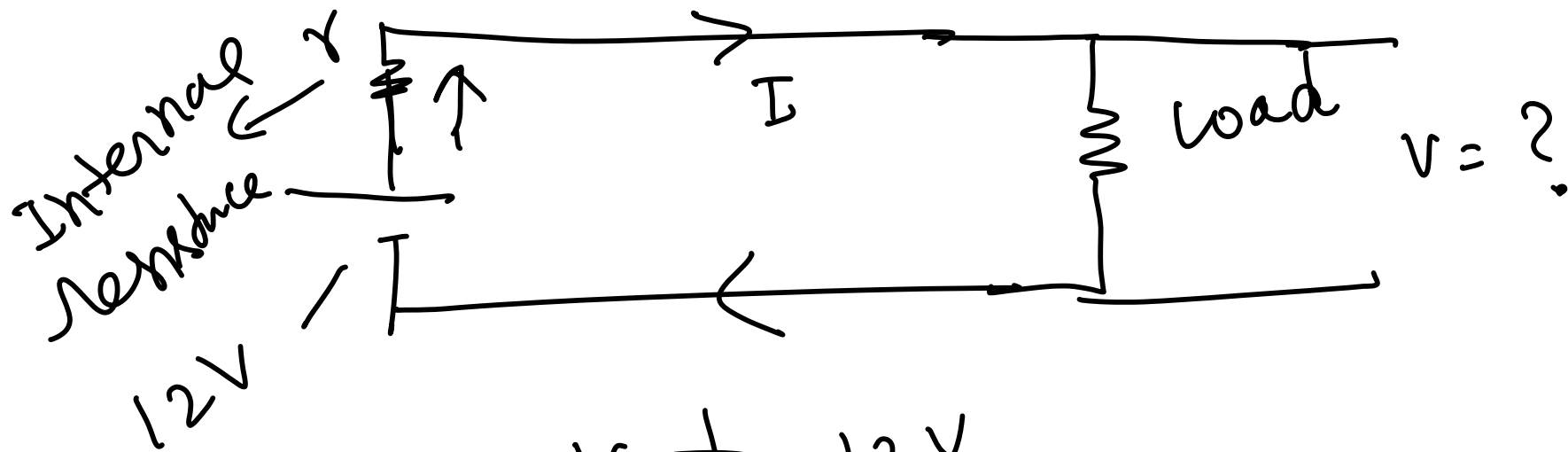
L. no. 29

Output resistance
of the op amp

$R_o = \text{output resistance}$
 $\neq 0$

- ① Output resistance of the op amp is not zero
- ② It varies with the gain

Output resistance?



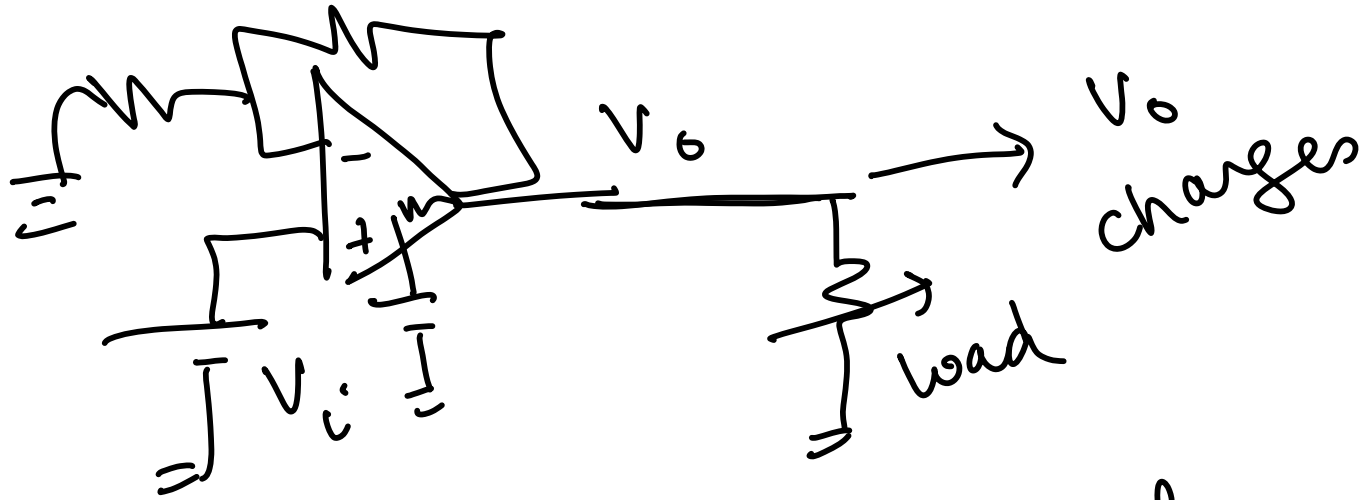
$$V \neq 12V$$

Voltage drop on the internal
resistance $V = rI$

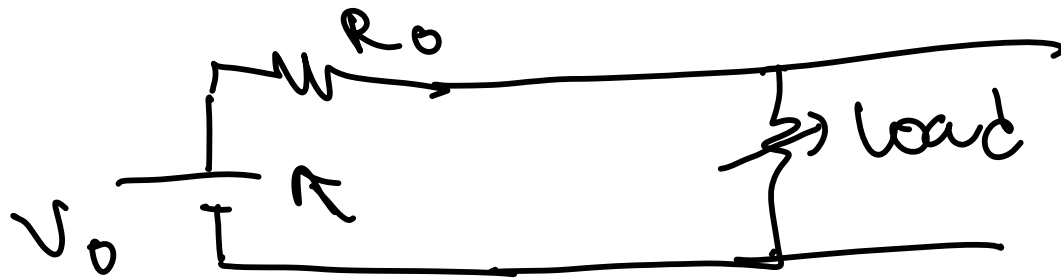
$$\text{Load } V = 12 - rI \quad \text{where } I \text{ is } I_{\text{chass}}$$

$$\text{So } V_L = 12 - rI$$

So with load current
load voltage changes

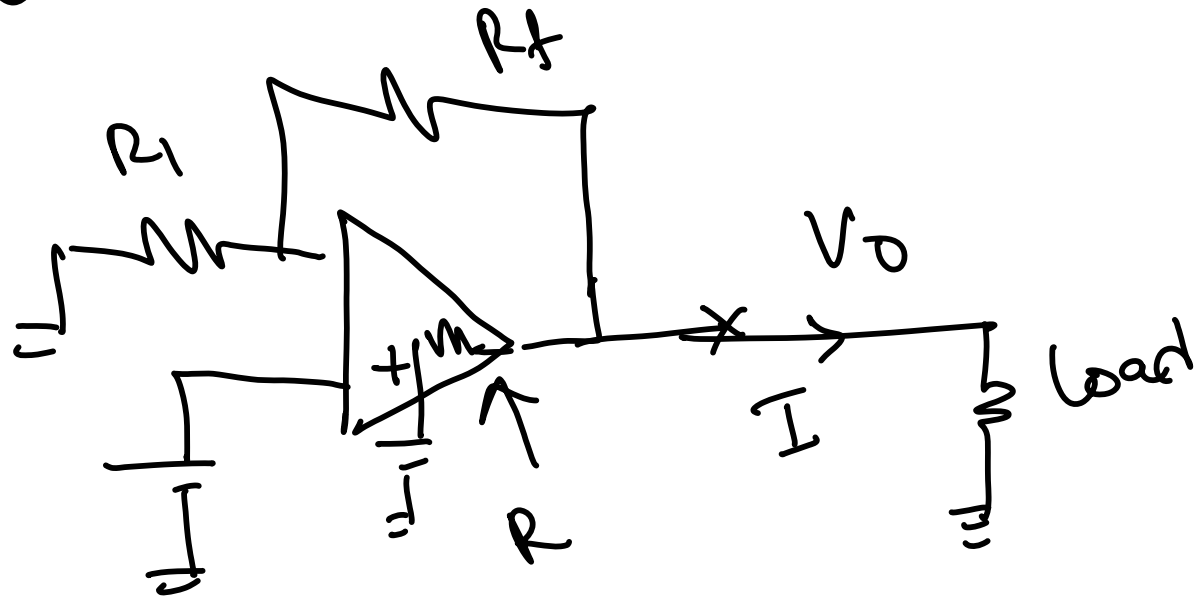


i.e. output voltage of the op amp
changes with the load resistance



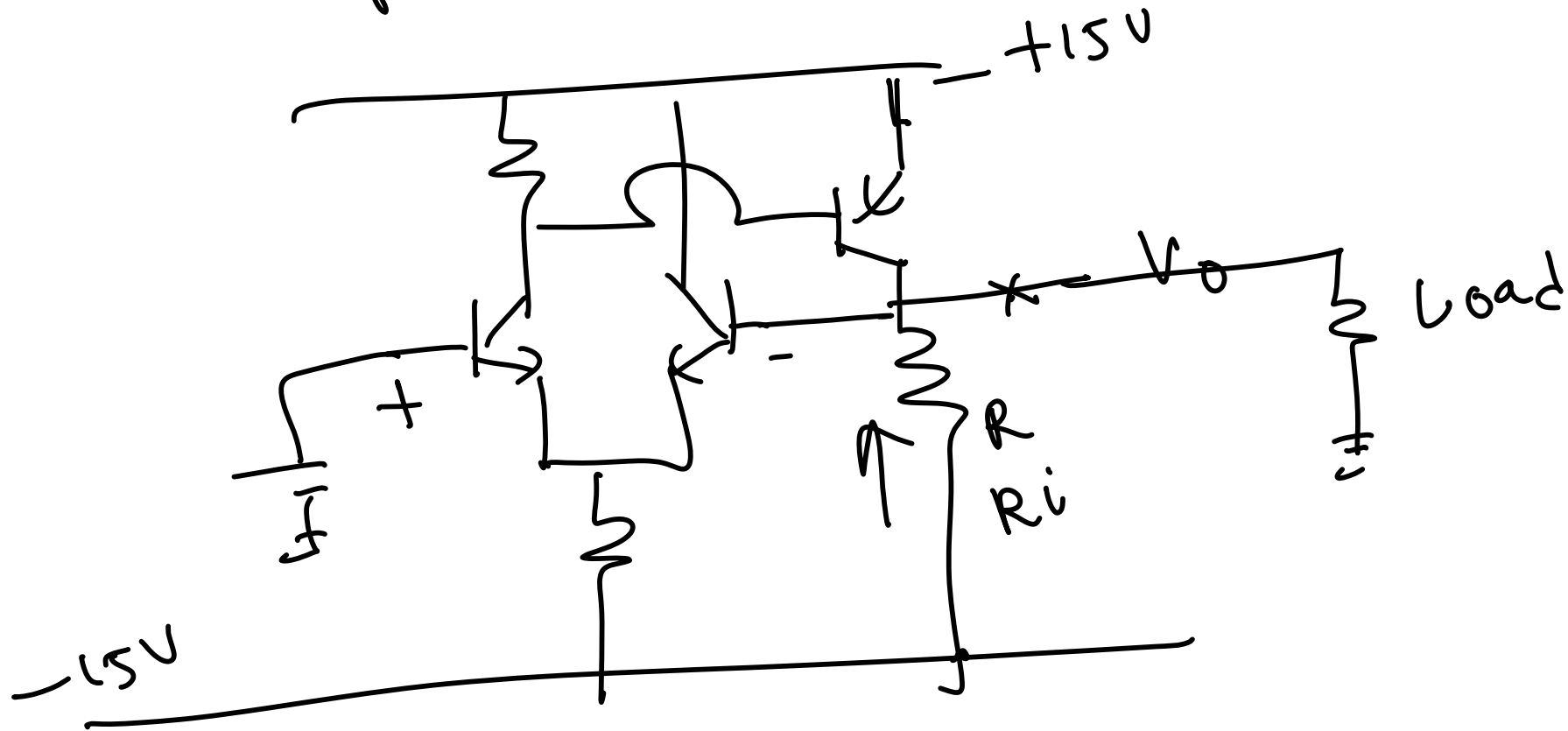
For any voltage source there is a finite internal resistance. So output voltage will change with the load.

In the case of op amp what is R_o ?



Assuming R_f and R_i are
very large

We can take I as the
full current of op amp.

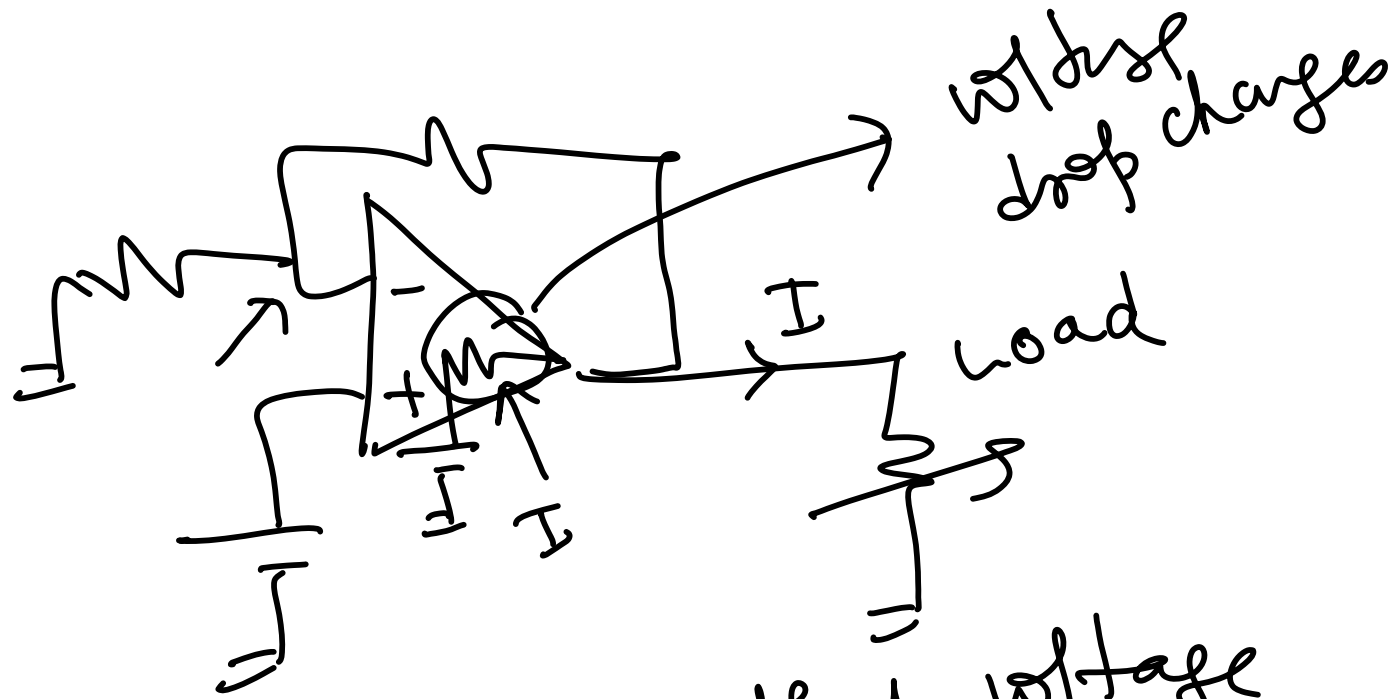


In this case the resistance R is acting as an internal resistance.

But the effective output resistance is not R

because of the closed loop feedback most of the voltage that is lost is compensated

So the effective output resistance is much smaller than R .



The effective output voltage
 charge is much smaller

$$= R_o I$$

where R_o is effective output
 resistance of the amp

In a typical op amp

$$\text{circuit} = R = 100 \Omega$$

but R_o is few milli ohms

In real life

when load resistance is decreased the voltage at

the inverting terminal decreases so that output vol is put back.

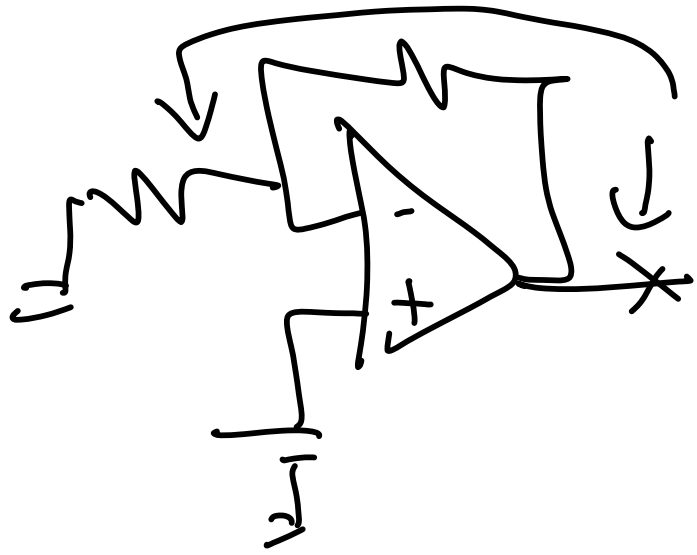
But output vol will not be equal to original.

Voltage drop on the internal
resistance of the op amp = $R I$

Assume the effective output
resistance is R_o

i.e. $R_o I =$ output voltage
change

So what is the voltage change
at the inverting ter. of the
op amp ??



The voltage change at -ve input is

$$= \frac{R_o I}{g}$$

where g is the closed loop gain

what is the relation between

charge in vol at -ve ter.
and output terminals

(charge at inverting
terminal) $\times A =$
output vol
change

$$R I = \left(\frac{R_o I}{g} \right) A$$

$$R = \frac{R_o A}{g}$$

$$R_o = \frac{R \times g}{A}$$

Output Resistance

$$R_o = R \times \frac{g}{A}$$

For example for most of the
of amp $R = 100 \Omega$

$$R_o = 100 \times \frac{100}{20,000}$$

closed loop gain

open loop gain

internal loss

$$R_o = \frac{10^4}{2 \times 10^4} = 0.5 \Omega$$

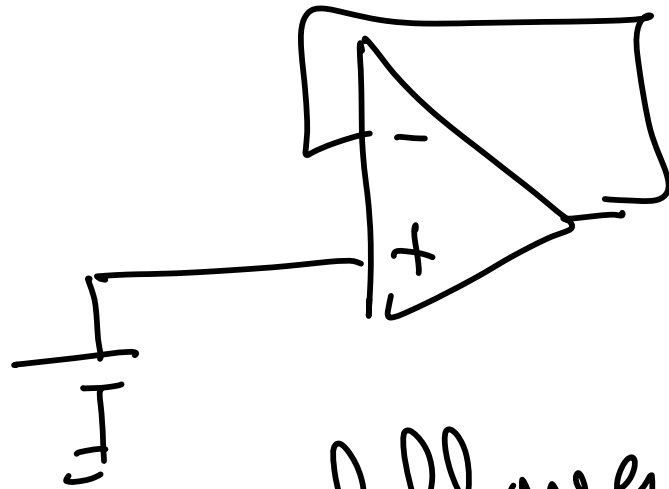
For 741 for voltage follower

$$R_o = 100 \times \frac{1}{20000}$$

$$= \frac{1}{200} = 5 \text{ m}\Omega$$

When the closed loop gain is less than the output resistance also less

So voltage follower gives
lowest output resistance



(1)

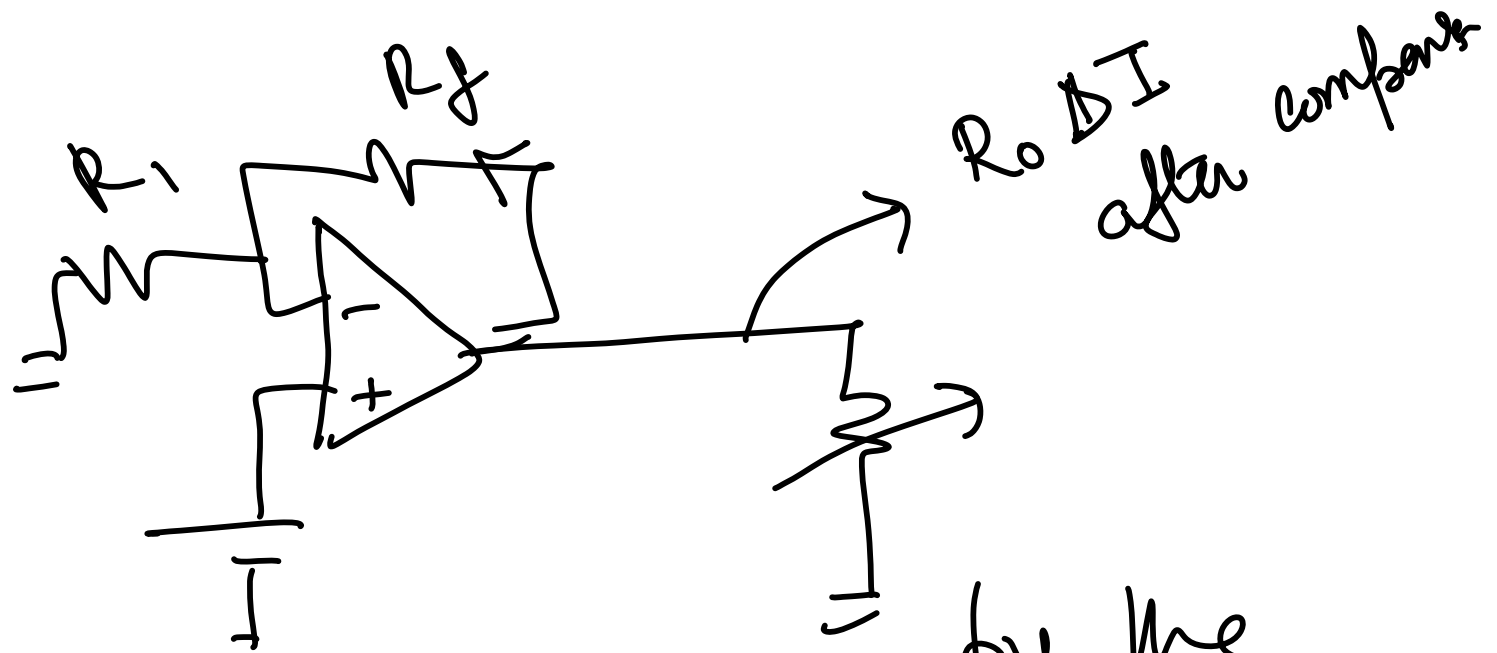
voltage follower gives
highest input resistance

② voltage follower gives
lowest output resistance

$$R_o = 100 \times \frac{1000}{20000}$$

$$\approx 5 \Omega$$

For $\beta = 100$ then output
resistance goes up to 5Ω !!



R value is given by the manufacturer in the data sheet

In real case R_f also acts as a load

If R_F is small then
output voltage will decrease

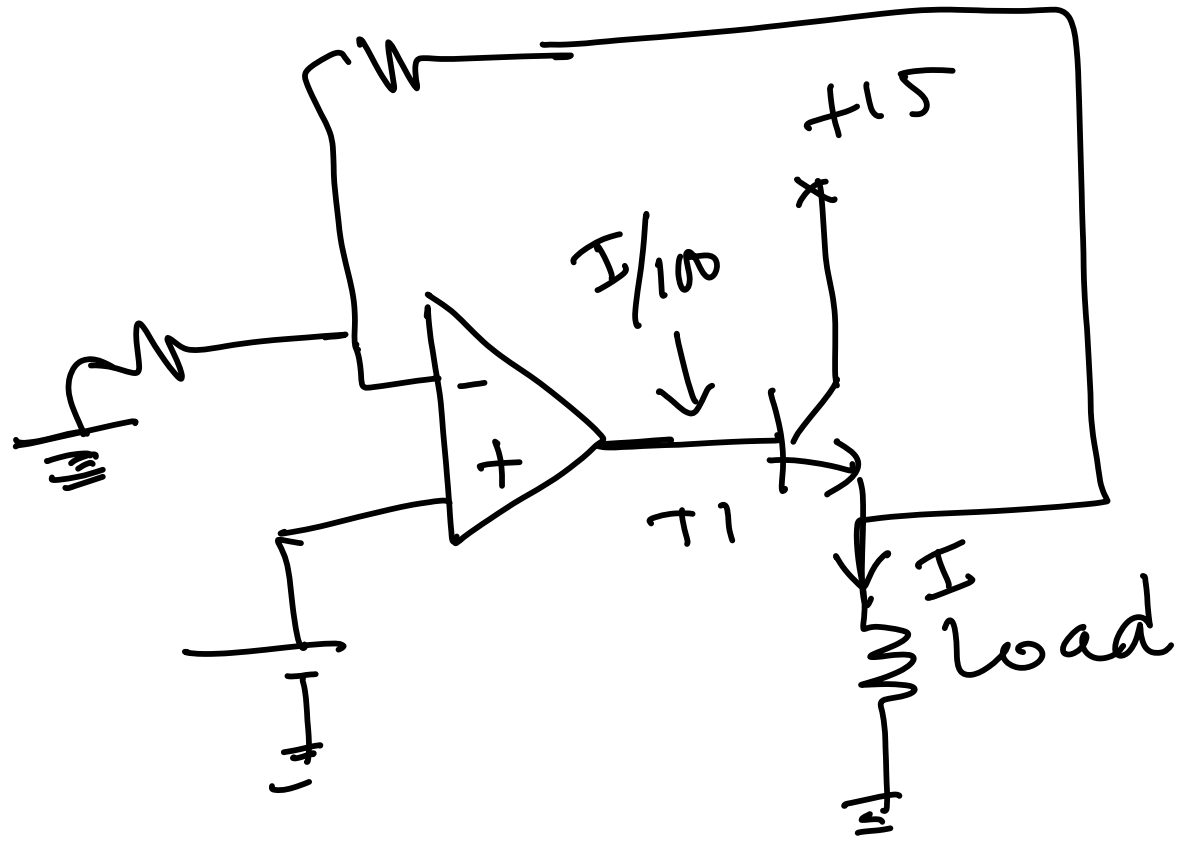
So one should not use low
value of R_F .

Low value of R_F reduces
the bias current error, but
it will increase the output
resistance related error

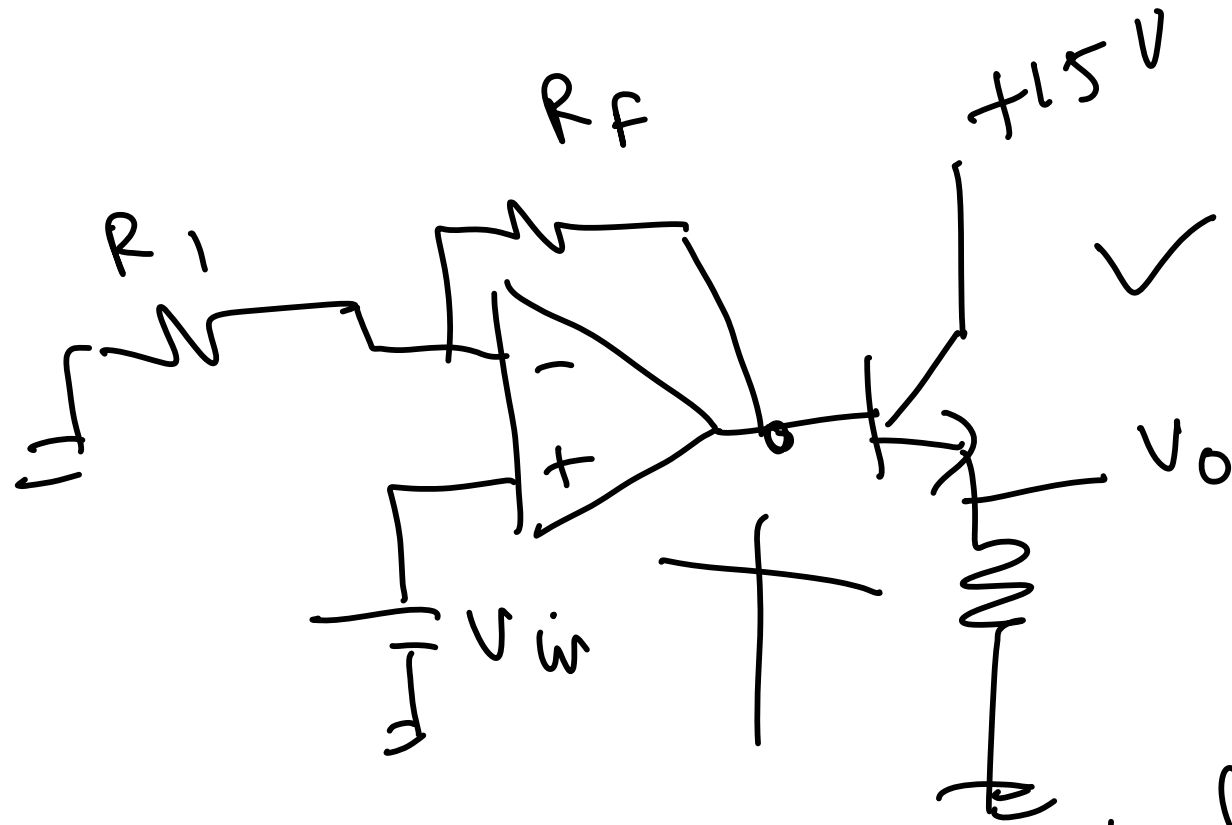
It should be noted that
normally there is a internal
current limit or way of-amp.

For most of the op amps
~~and~~ I is limited to 10mA

So normally bias current
related error is much larger than
output resistance related error



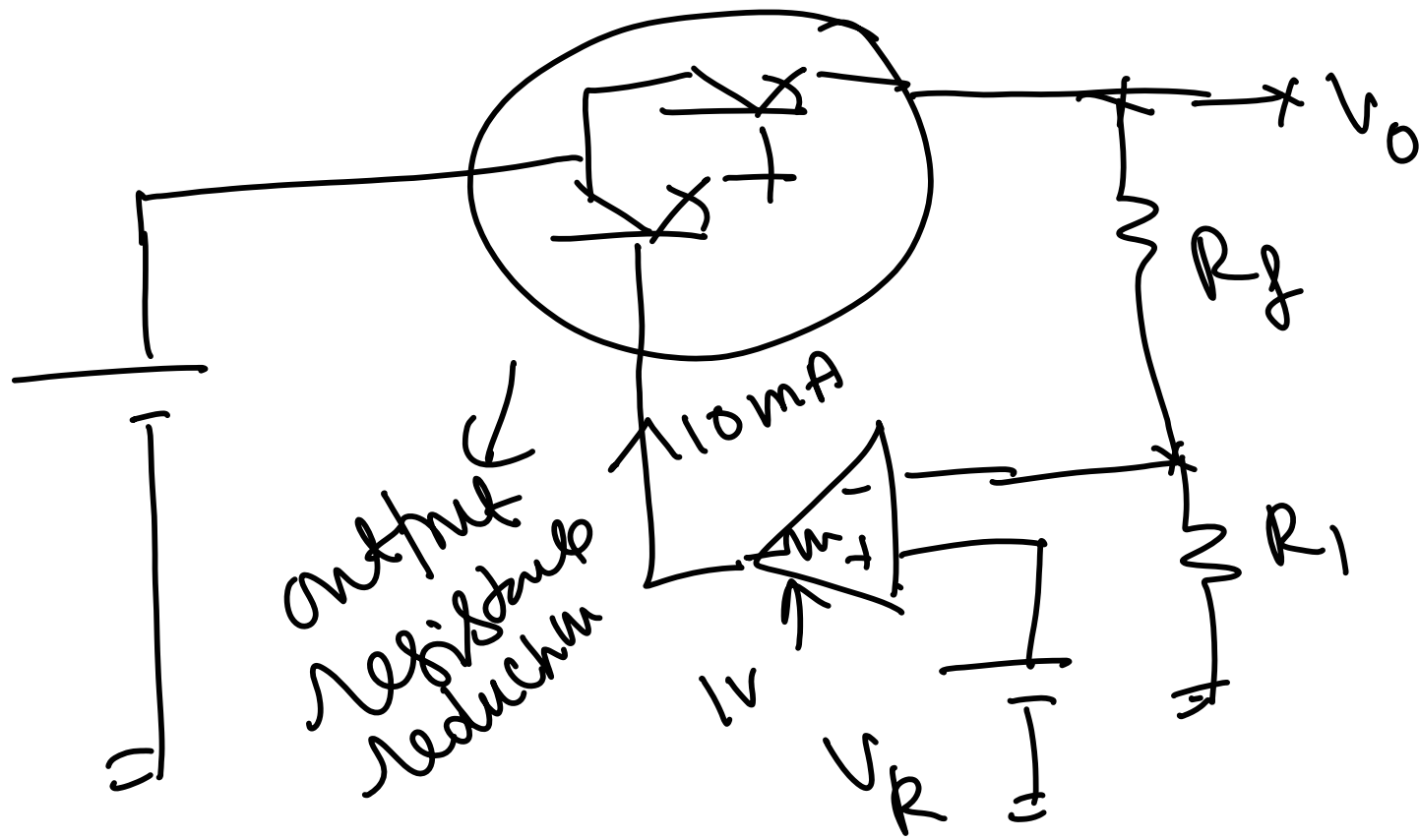
For $\beta = 100$



This is not acceptable

V_{BE} is a loss !!

R_{in} V_{BE} changes w/m temp



Voltage regulator
 It can also be considered
 as non-inverting amp.

$$V_o = V_R \left(1 + \frac{R_f}{R_1} \right)$$

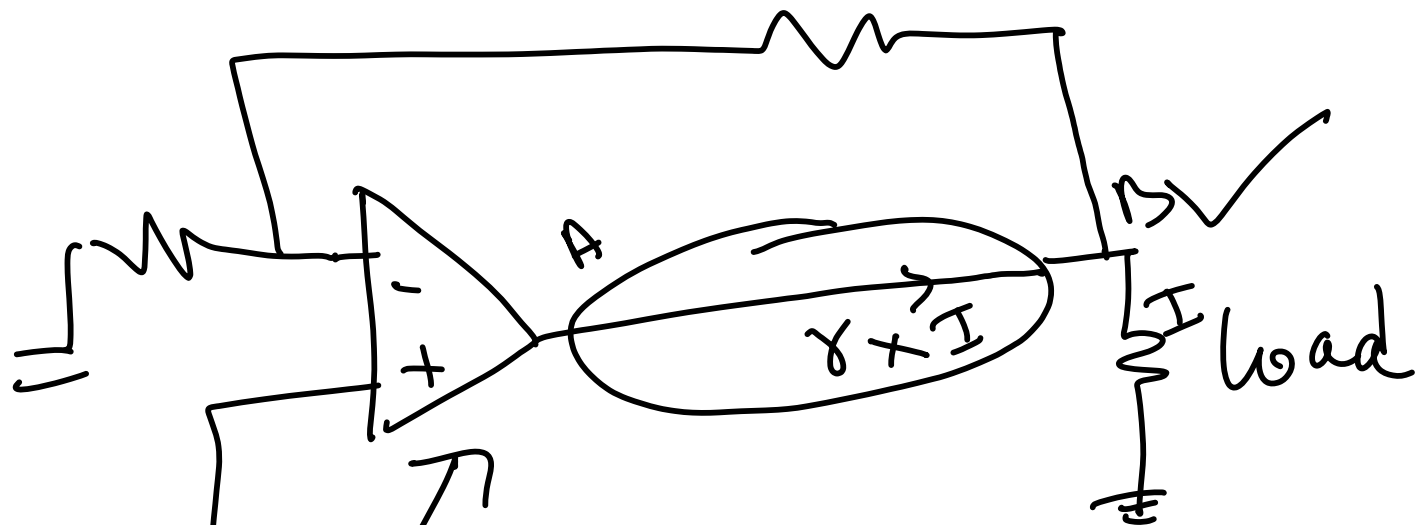
It is a non-inverting amp with low output resistance

gain

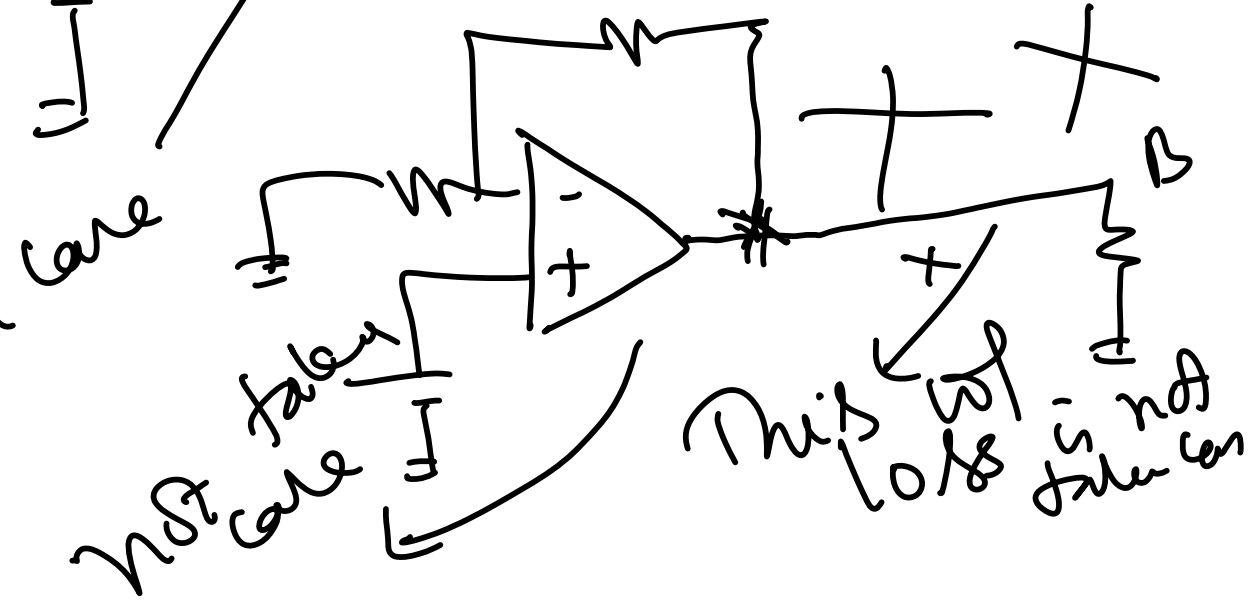
At the output of the op amp

$R_o \times 10 \text{ mA} =$ is the expected charge

$$R_o = 100 \times \frac{2}{20000} = \frac{200}{20000} = 10 \text{ m}\Omega$$



Vol drop
between
A and B
is taken care

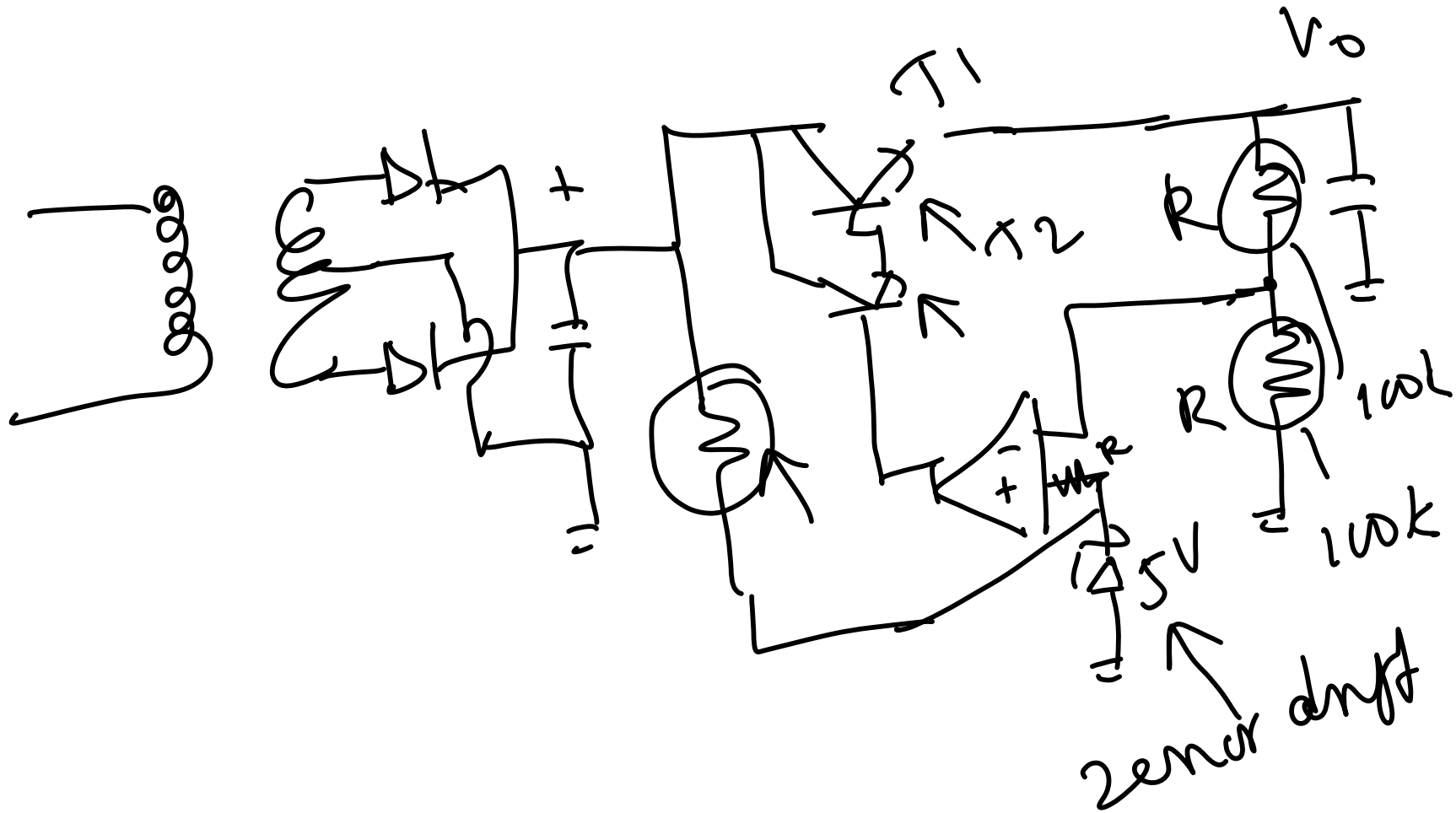


Not taken
care

This Vol
drop is not
taken

Lecture-36

calculations of op-amp errors



$$V_O = 5V \times 2 = 10V$$

V_{BE} drift of T_1 and T_2
is actually compensated
by the loop gain

① V_{offset} drift of op amp
directly affects the output

For 741

$$\text{drift} = 15 \mu V/^\circ C$$

$$\text{For } I_{IC} = 1.5 \text{ mA}$$

So total drift is 3 mV

Zener drift error

LM336 \rightarrow drift
 $f_{zcc} = 30 \text{ ppm}/^\circ\text{C}$

For 10°C drift

$$= \frac{30 \times 100 \times 5}{10^6} = \frac{150 \times 10^2}{10^6}$$

$$= 150 \times 10^{-4} = 15 \text{ mV}$$

The expected output
drift = 30 mV

③ Resistance drift error $\propto R_1 \text{ and } R_2$

④ Bias current
drift error $\rightarrow R_1 \text{ and } R_2$

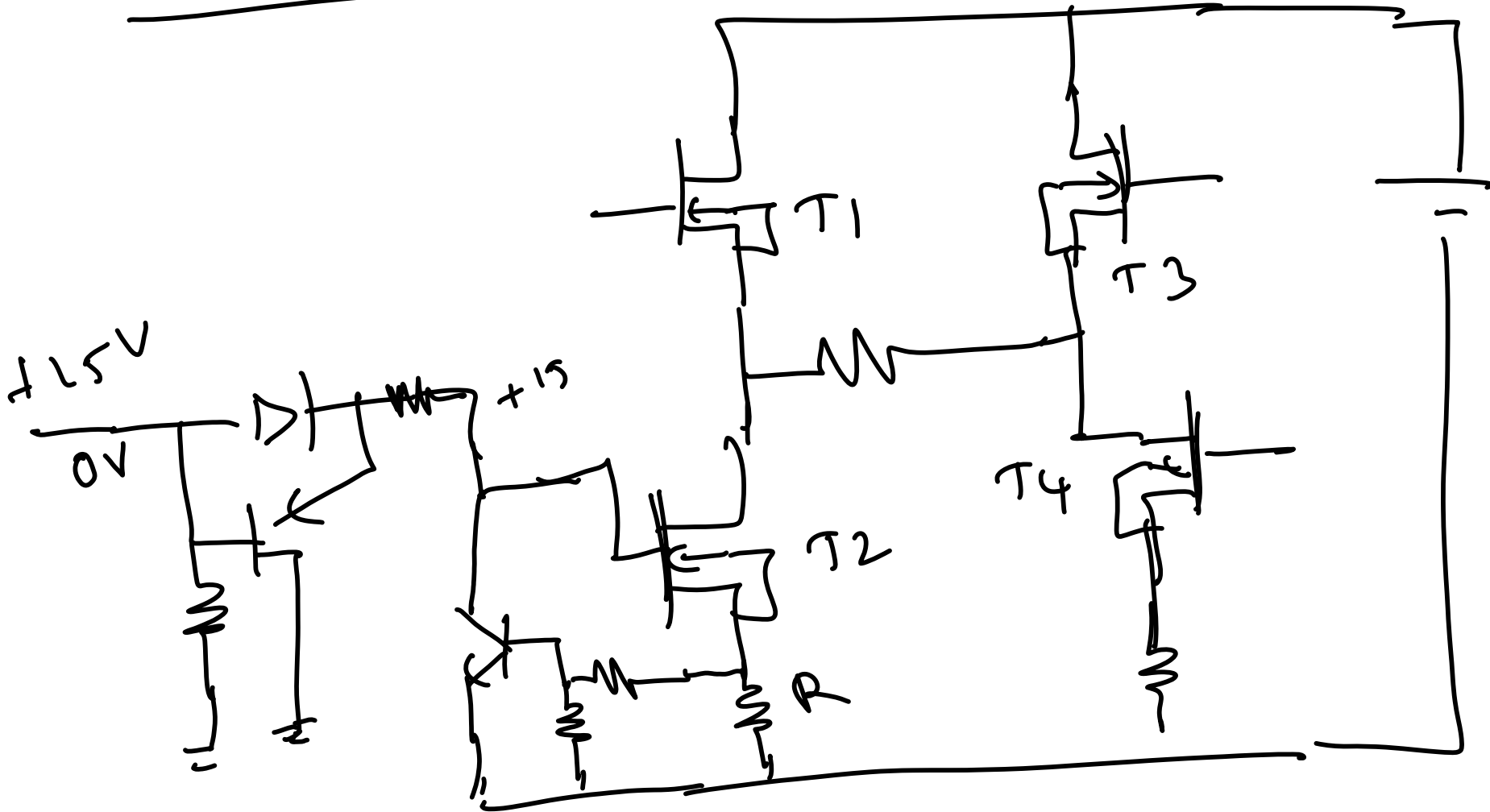
Reduce the bias current
error by reducing the R_1
and R_2

or
Add Resistance in the
non inverting input.

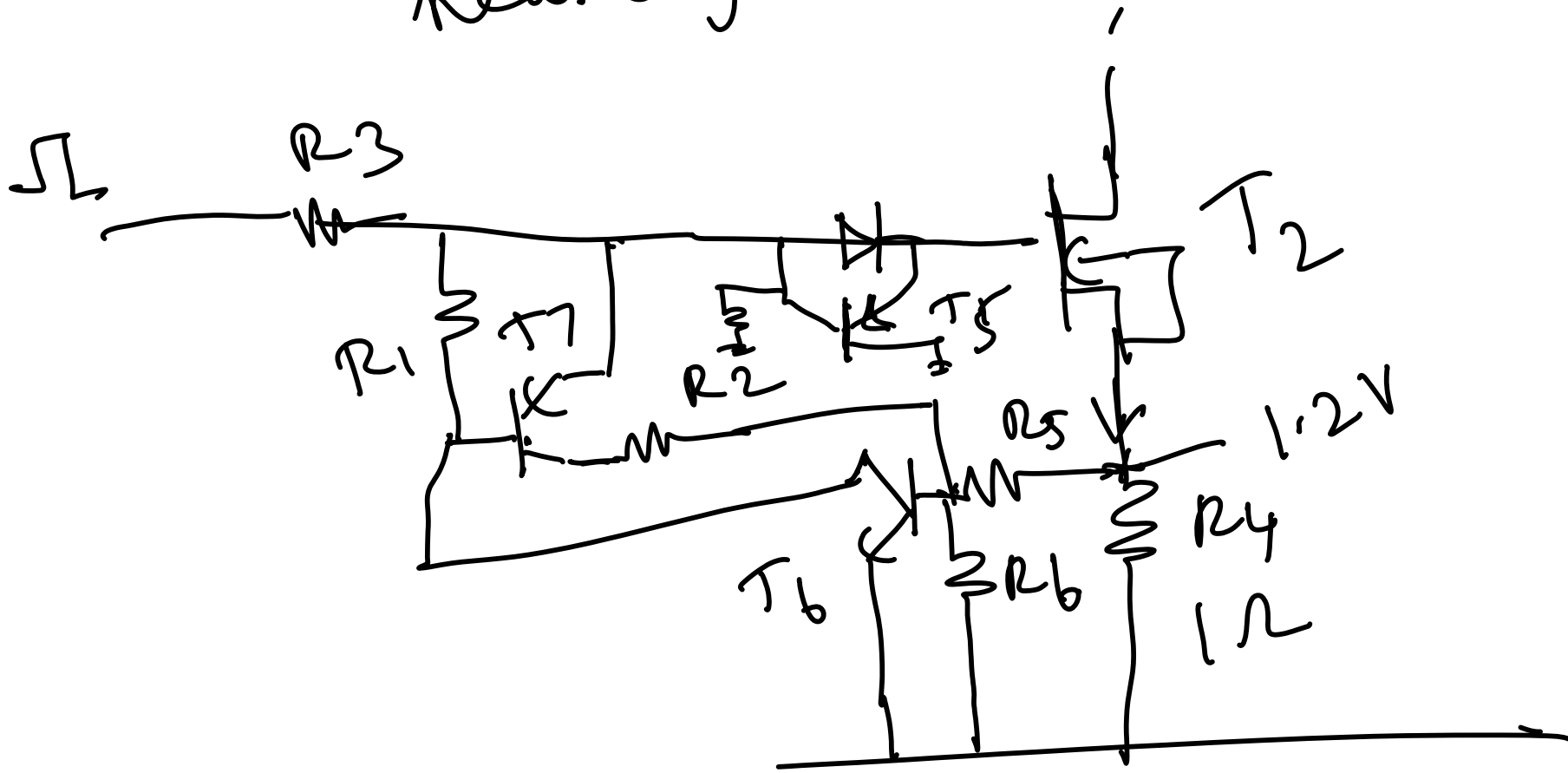
Circuit - 2

H-bridge drive

Current sensing error



This circuit will limit the current but it will damage the T_2 because of heating



Wol all R_4 is applied to T_6

When T_6 $V_{BE} > 0.6V$

T_6 is turned ON

This makes T_7 to turn ON

This makes Wol at the base

of T_6 to be present even
with out the current

i.e. T_6 is latched

This makes T_2 to go OFF.

So T_2 will be OFF for the remaining period of the pulse. The latch will be reset at the next zero pulse input.

If $R_E = 1\Omega$

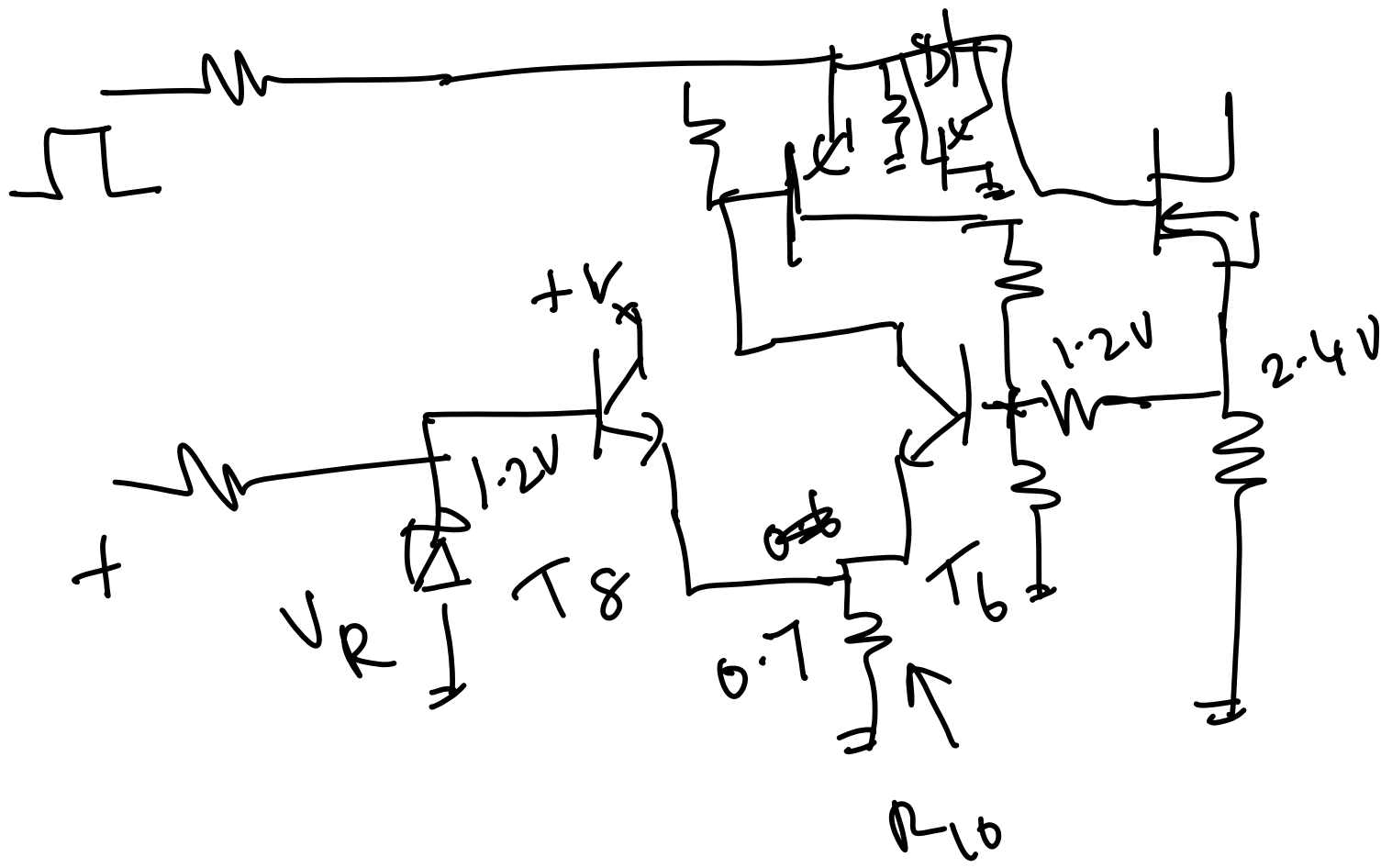
Then at $1.2A$ current
 $0.6V$ will appear at the
base of T_6

So current limiting is taking
place at $1.2A \rightarrow$ This is
at $25^\circ C$
ambient

At $75^\circ C$ ambient

Then T_6 needs only $0.5V$

So current limiting will
take place at $1A$



Base emitter

V_{BE} drift of T_b is
eliminated by using T_{gms}

V_R
This is because when V_{BE} changes
the voltage across R_{10} also
changes

For example at $25^\circ C$
w/ $R_{10} \rightarrow 0.6V$
At $75^\circ C \rightarrow 0.5V$

T_b conducts at 25°C ambient

when V_{BE} is 0.6V i.e.

voltage at the base is $0.6 + 0.6$
 $\approx 1.2\text{V}$

~~T_b~~ T_b conducts at 75°C ambient

when V_{BE} is 0.5V i.e.

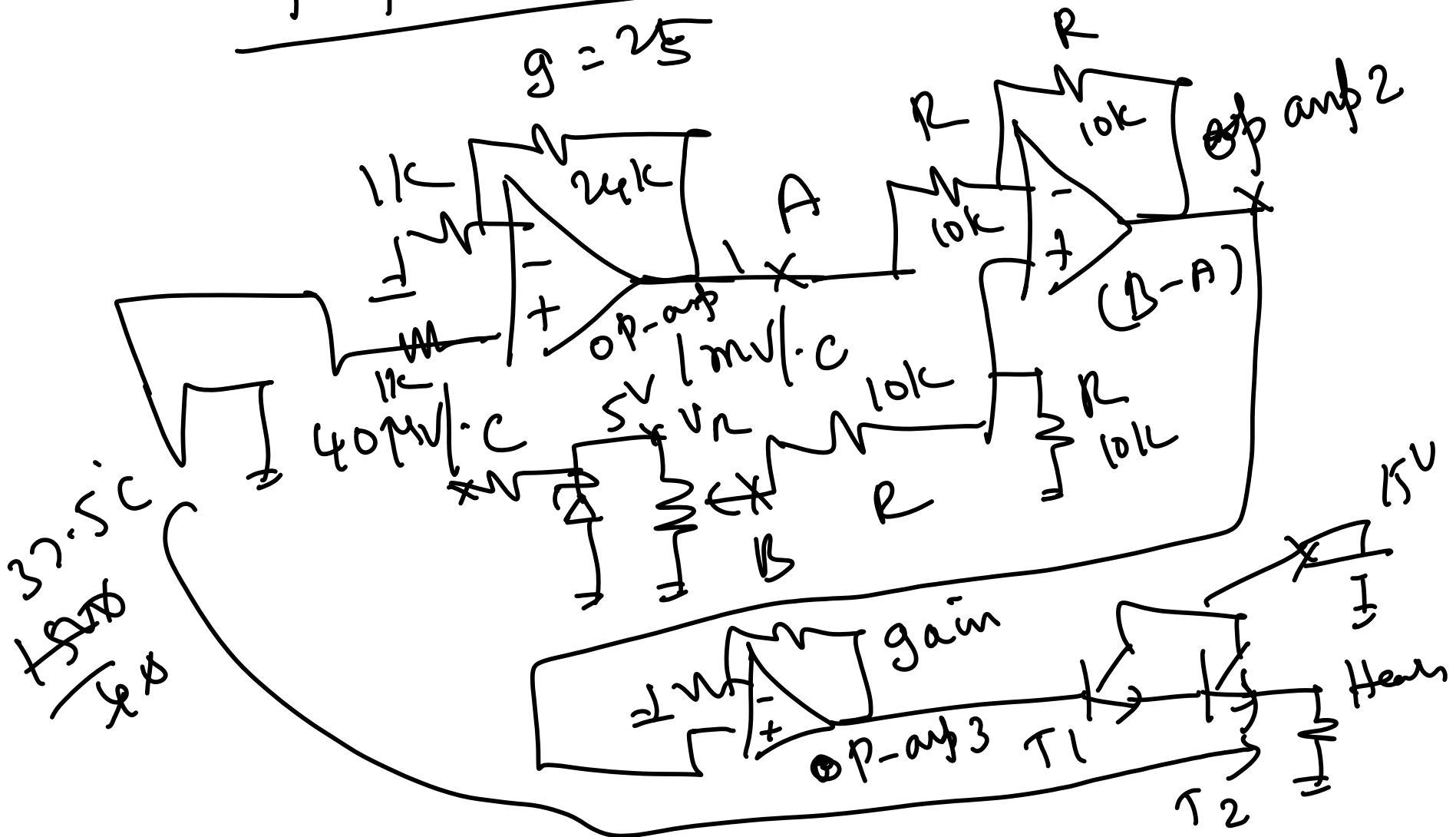
voltage at the base is $0.5 + 0.70$
 $\approx 1.2\text{V}$

i.e. at all temperatures current limiting is taking place when

T_b base vol is at 1.2V

Circuit 3 — Drift Calculation

Thermo couple based proportional temp controller



Point A gives actual temp.

point B gives set temp

$(B - A) \rightarrow$ error vol

op amp \rightarrow amplifies the error voltage and the amplified vol is applied to the heater through the Transistors

Calculation of errors

① op amp - 1 handles the low level signal

So offset voltage drift of

op amp - 1 is a concern

So use low offset voltage drift op amp.

LM-07 \rightarrow V_{offset} drift is

0.5 μ V/C. For 10°C ambient temp change 50 μ V drift is

expected. This is equal to

$$\frac{50}{40} = 1.25^\circ\text{C}$$

Total error due of offset
voltage drift

Op amp 1 \rightarrow $\frac{50 \mu\text{V}}{40 \mu\text{V}} = 1.25^\circ\text{C}$

Op amp 2 \rightarrow offset v_t \rightarrow 1.5 mV
drift

error \rightarrow $\frac{1.5 \text{ mV}}{1 \text{ mV}} = 1.5^\circ\text{C}$

signal \leftarrow 1 mV

of amp 3 $\rightarrow \frac{1.5 \text{ mV}}{1.0 \text{ mV}} = 1.5^\circ \text{C}$

Total error = $\begin{array}{r} 1.25 + \\ 1.50 \\ 1.50 \\ \hline 4.25^\circ \text{C} \end{array}$

If gain in of amp 1 is kept as 50

Then the error comes down
of amp 1 — 1.25°C

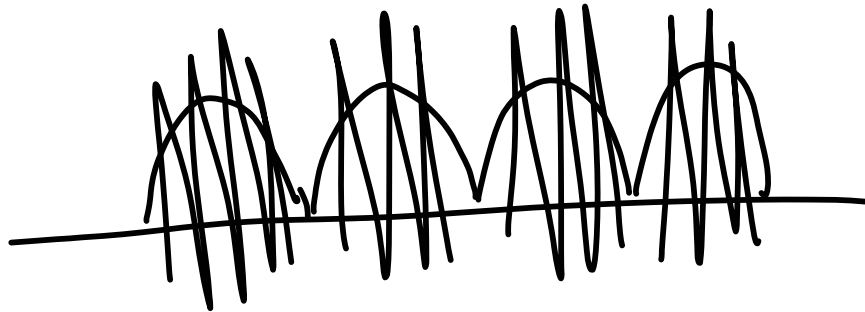
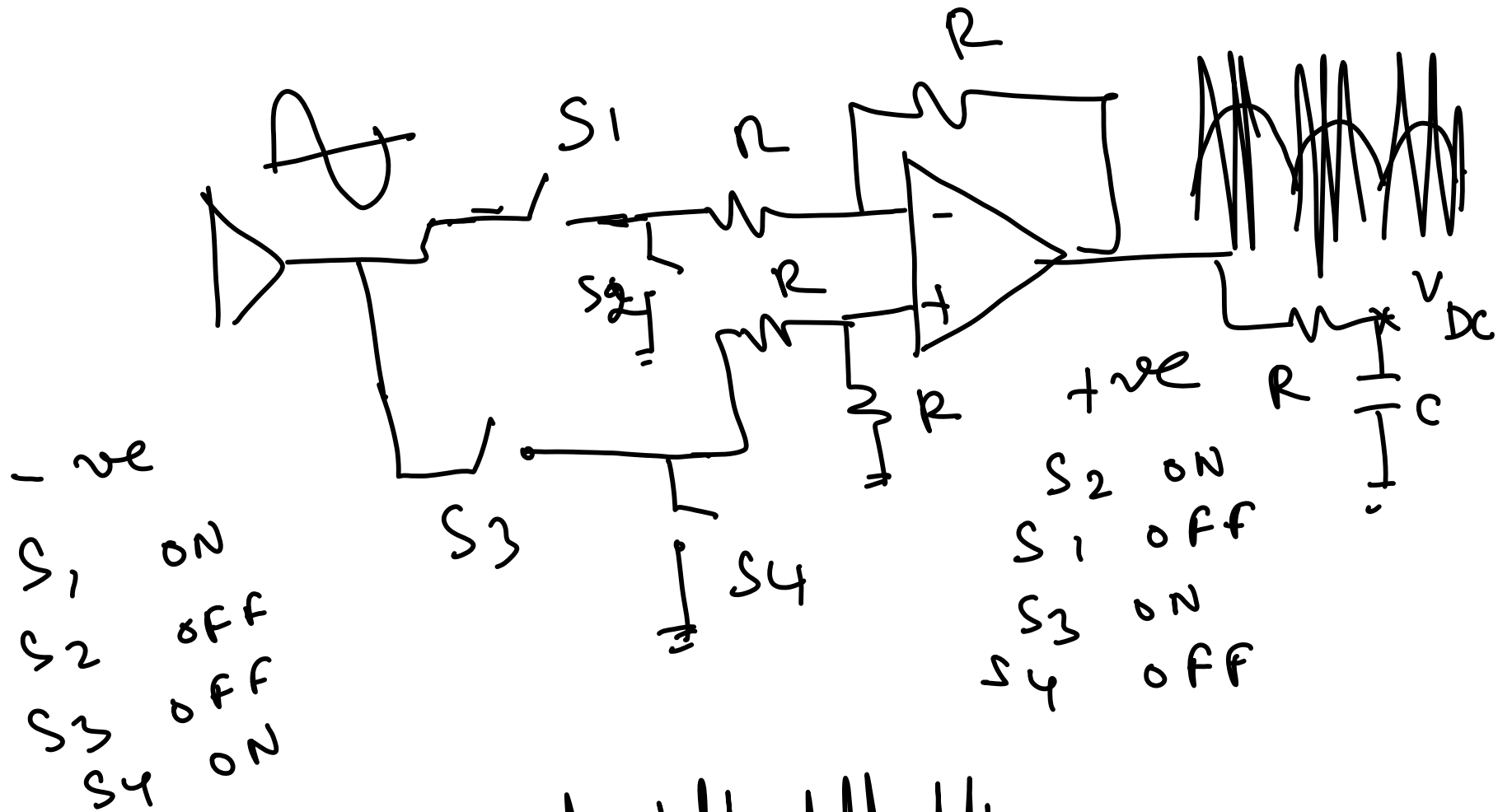
$$\text{of amp 2 error} = \frac{1.5 \text{ mV}}{2 \text{ mV}} = \frac{3}{4} = 0.75^\circ \text{C}$$

$$\text{of amp 3 error} = \frac{1.5 \text{ mV}}{2 \text{ mV}} = 0.75^\circ \text{C}$$

$$\begin{array}{r} \text{Total error} = 1.25 + \\ 0.75 \\ 0.75 \\ \hline 2.75^\circ \text{C} \end{array}$$

1 + ~ x - x -

Lecture no: 32



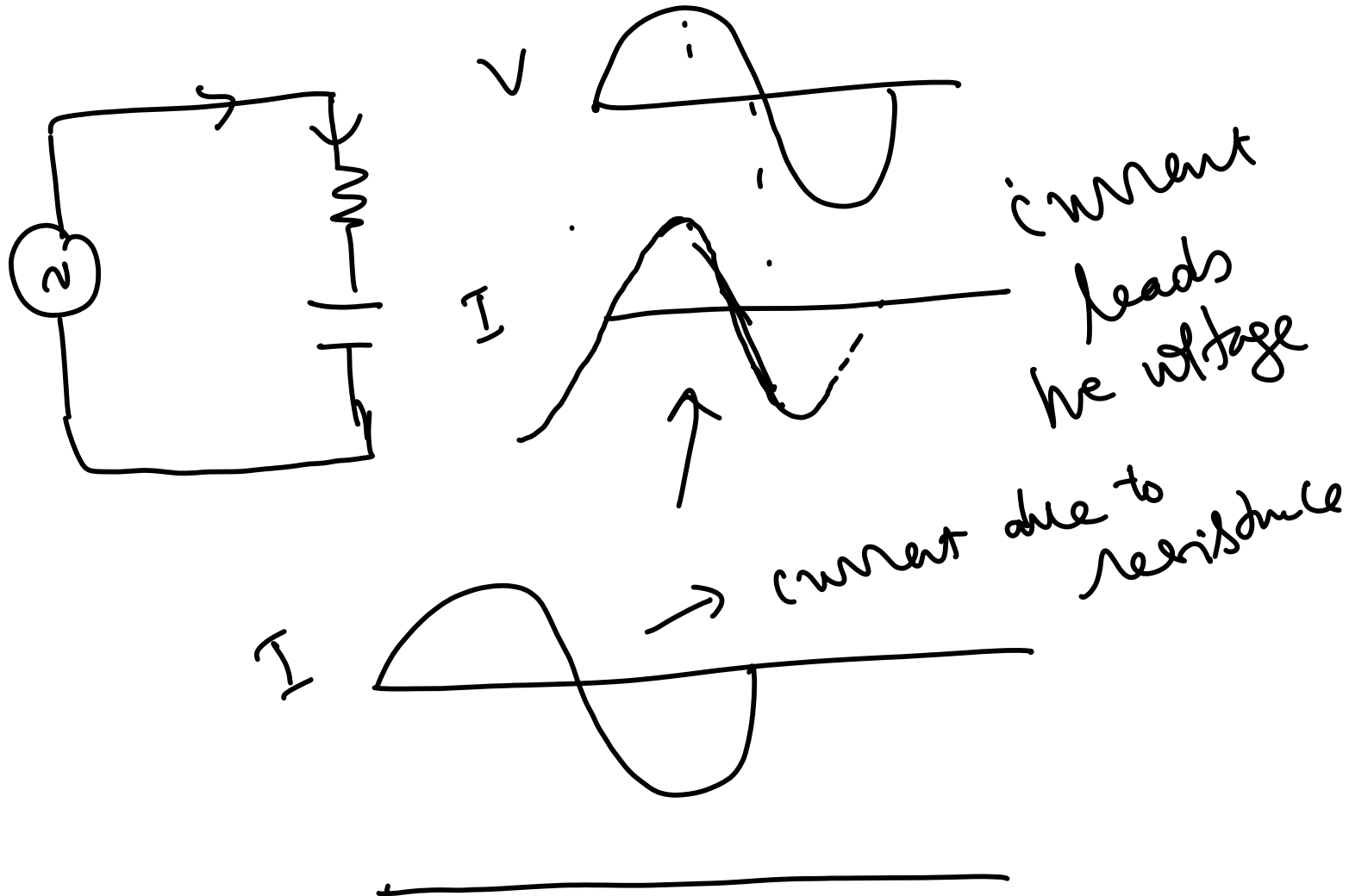
By means of averaging

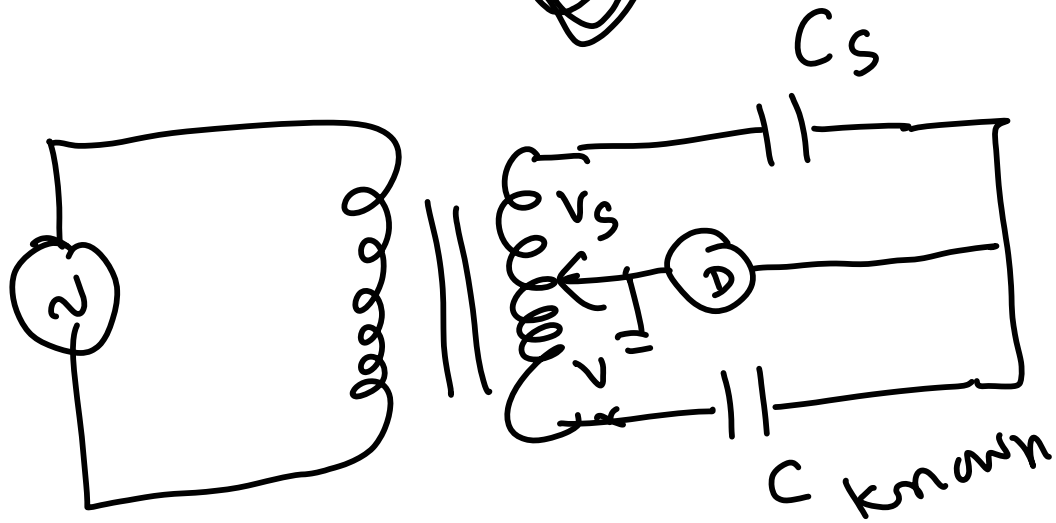
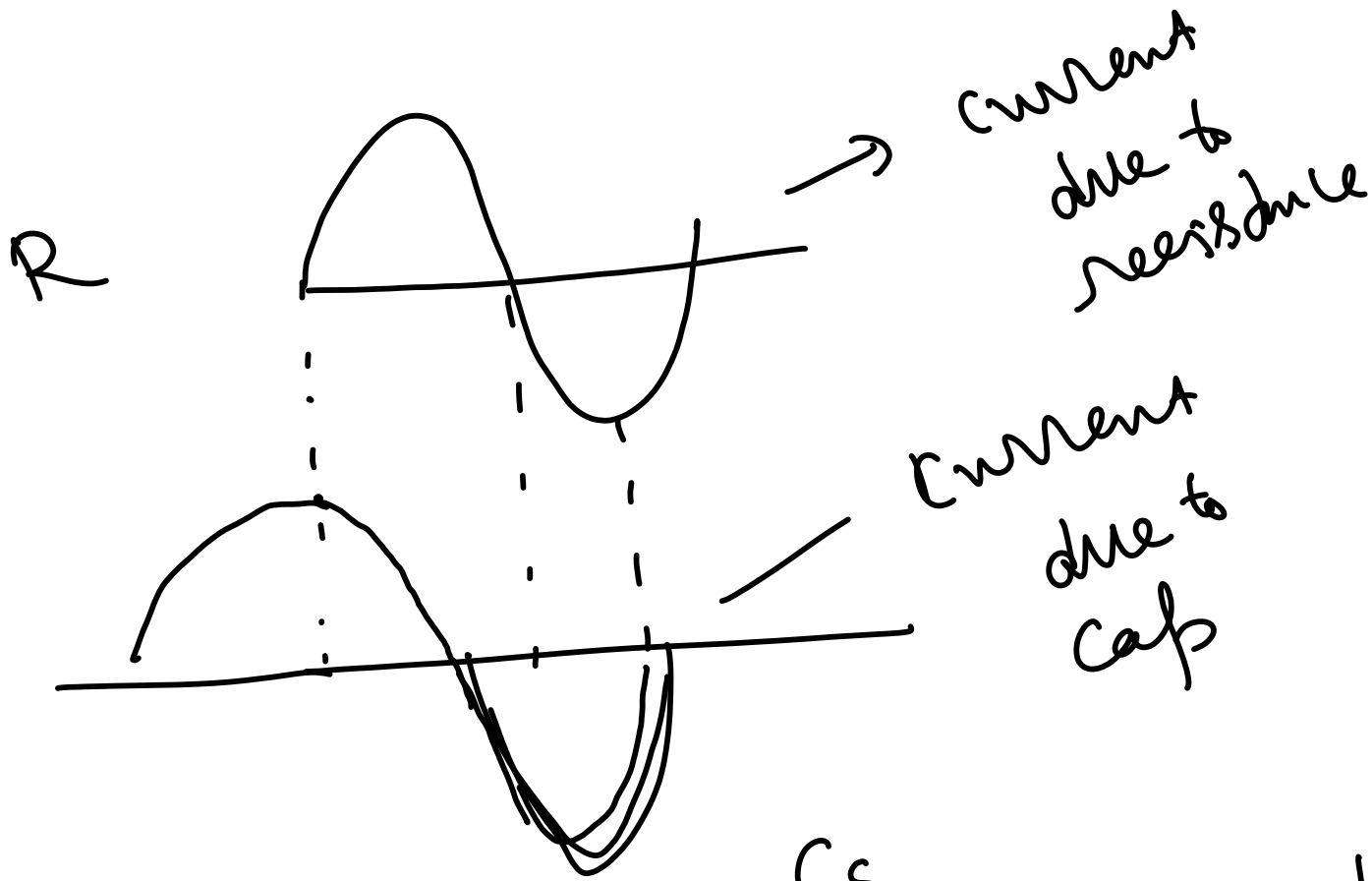
Noise is removed

For this to be effective

① RC time constant
much larger than
lowest noise frequency.

Lock in amplifier to
separate out in phase and
out of phase components

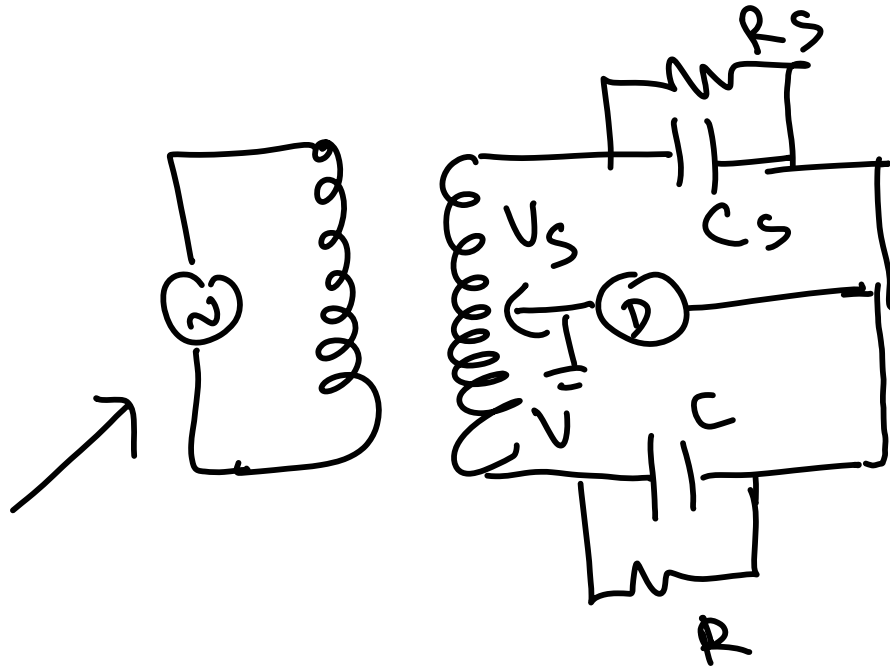




Radio transformer
bridge
for cap
measurement

$$V_s C_s \omega = V C \omega$$

$$\frac{R_s}{C} = \frac{V}{V_s}$$



The Detector current is due to both R and C

Assuming R_s and R is large

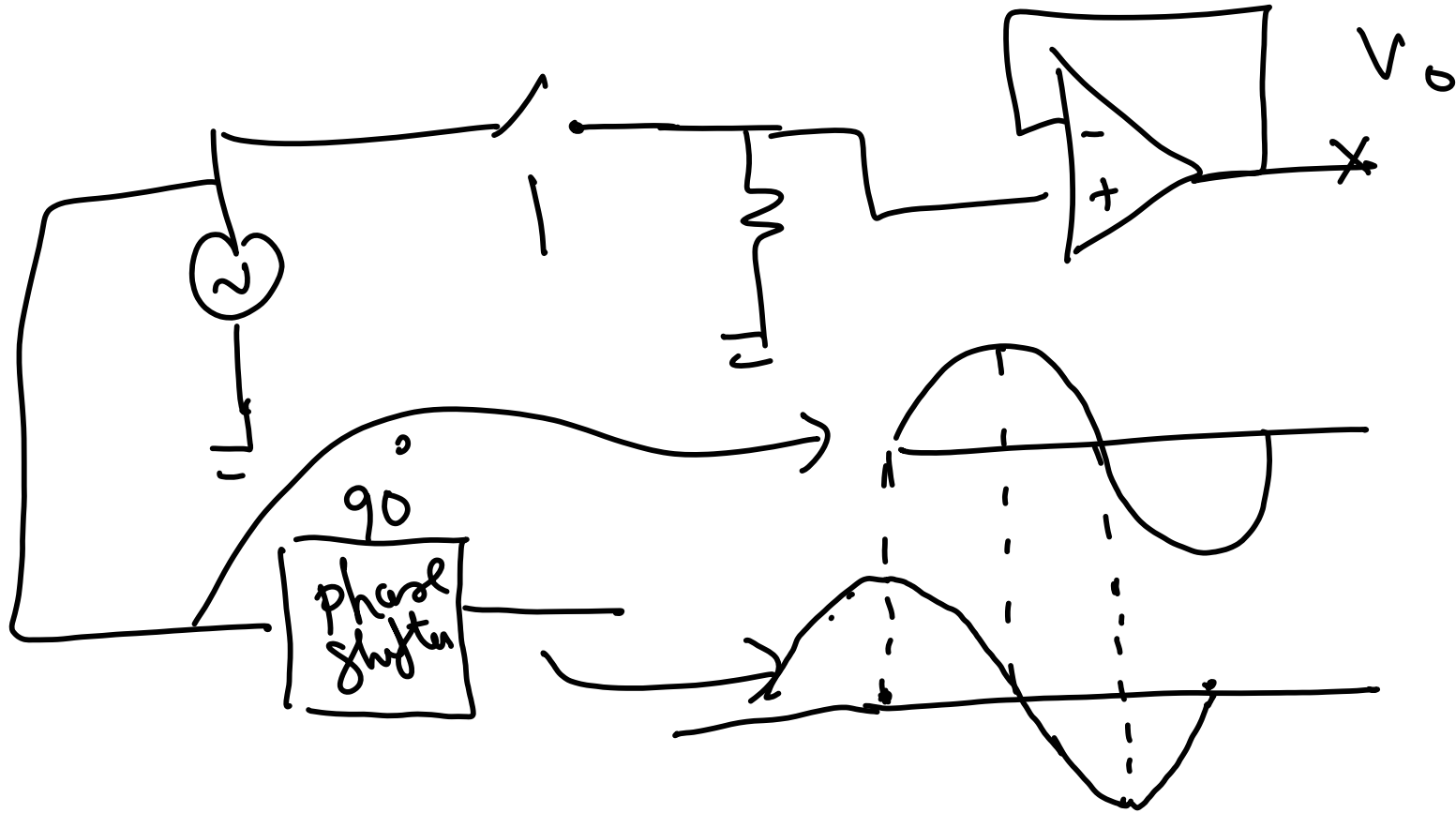
We can balance the bridge for resistance and capacitance separately.

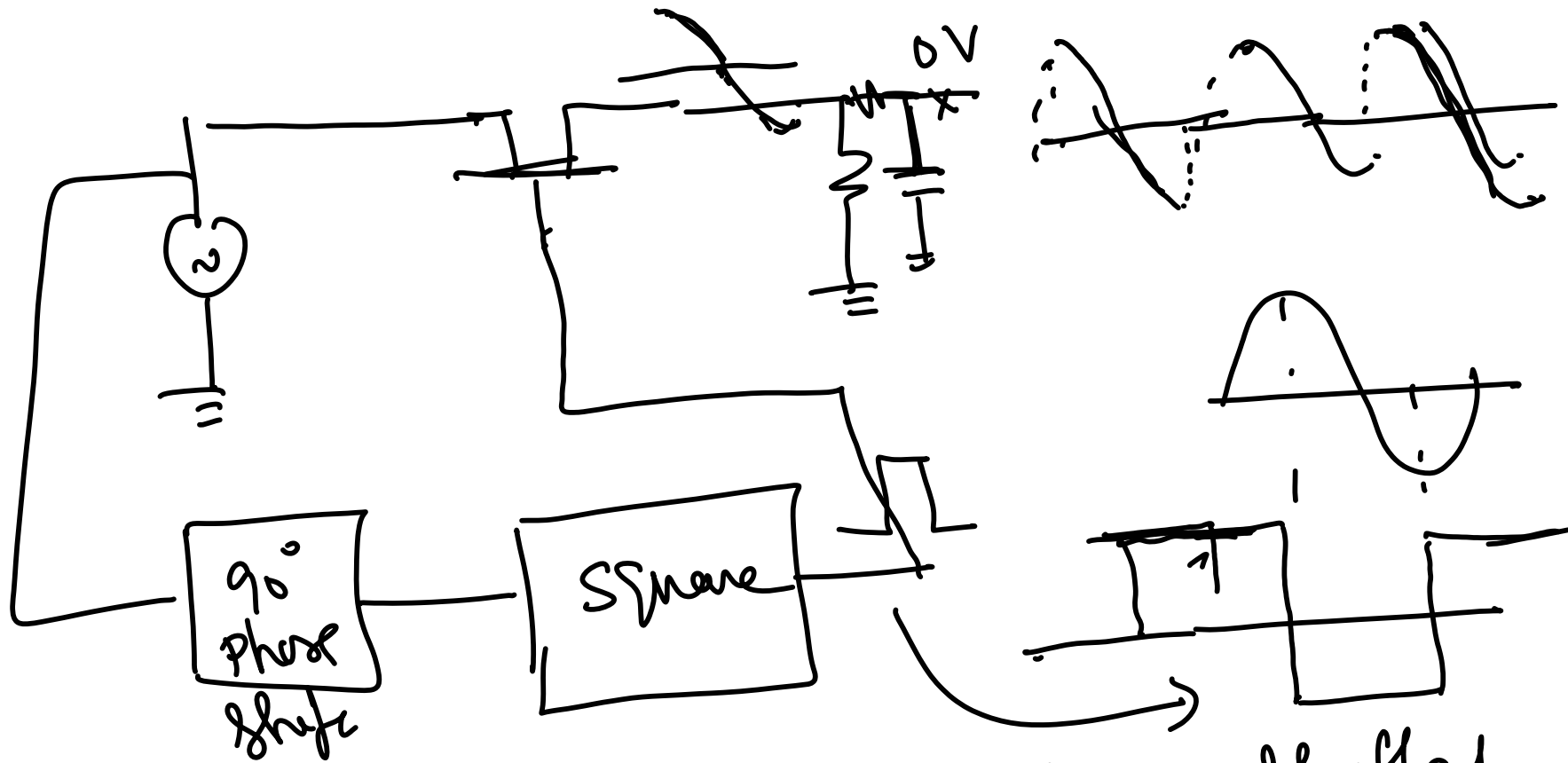
① To balance resistance make D sensitive to in phase comf. (in phase compared to the applied vol is V_S or V)

② To balance the capacitance make D sensitive to 90° out of phase comf.

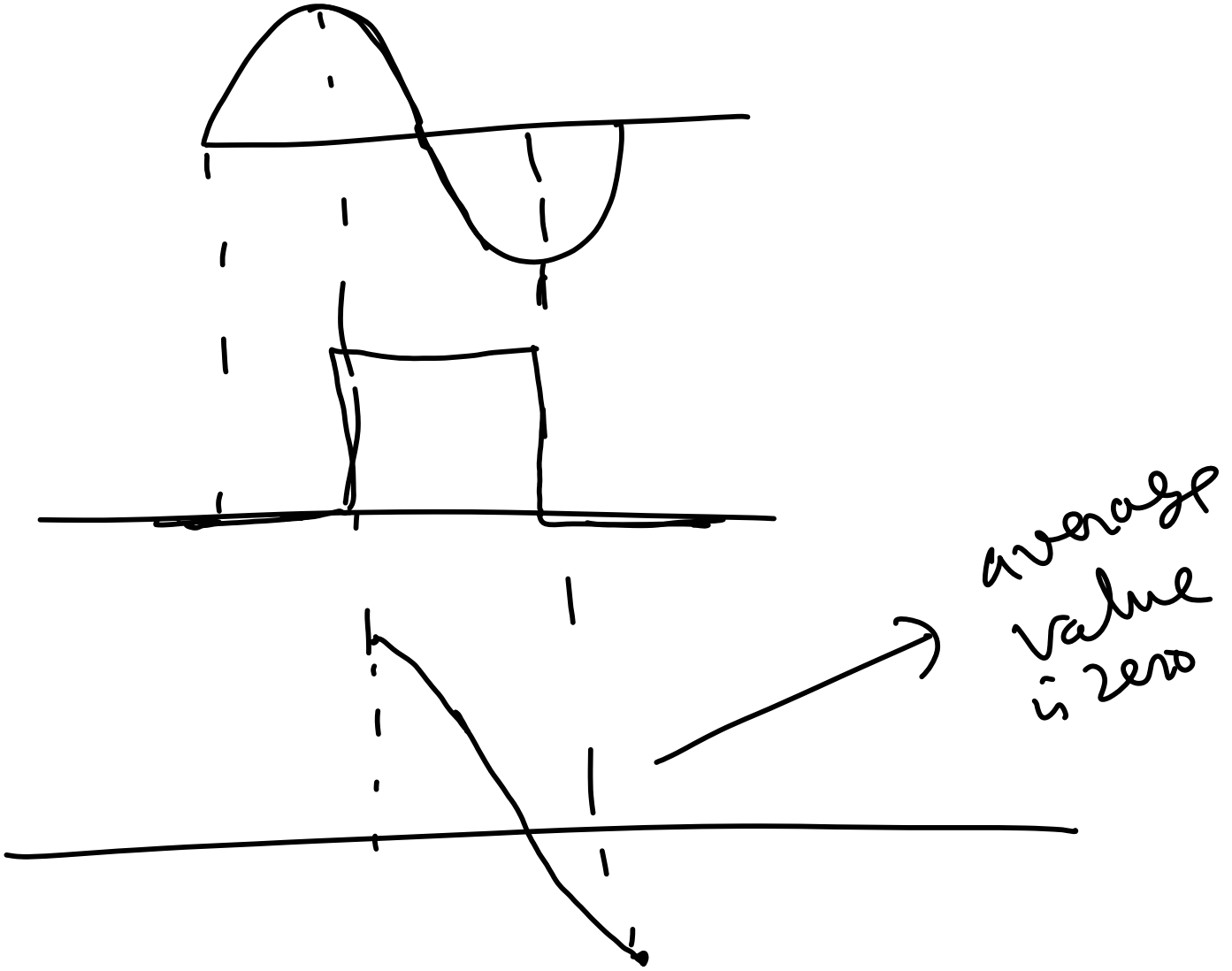
The Detector D is now
lock-in amplifier

How lock in amp is
sensitive to 90° phase comfot



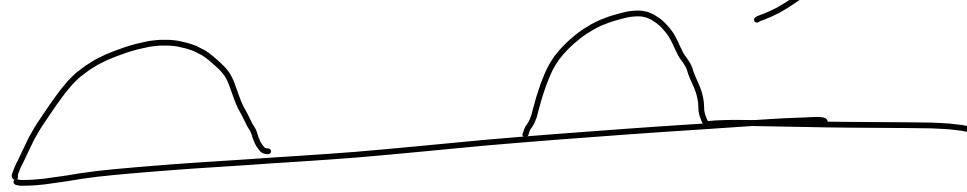
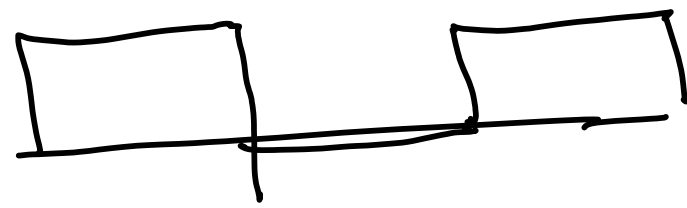
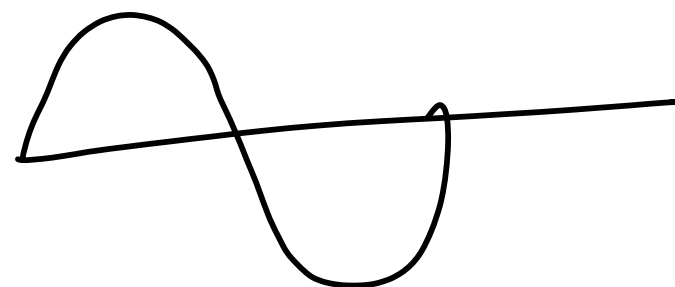


90° phase shifted square wave

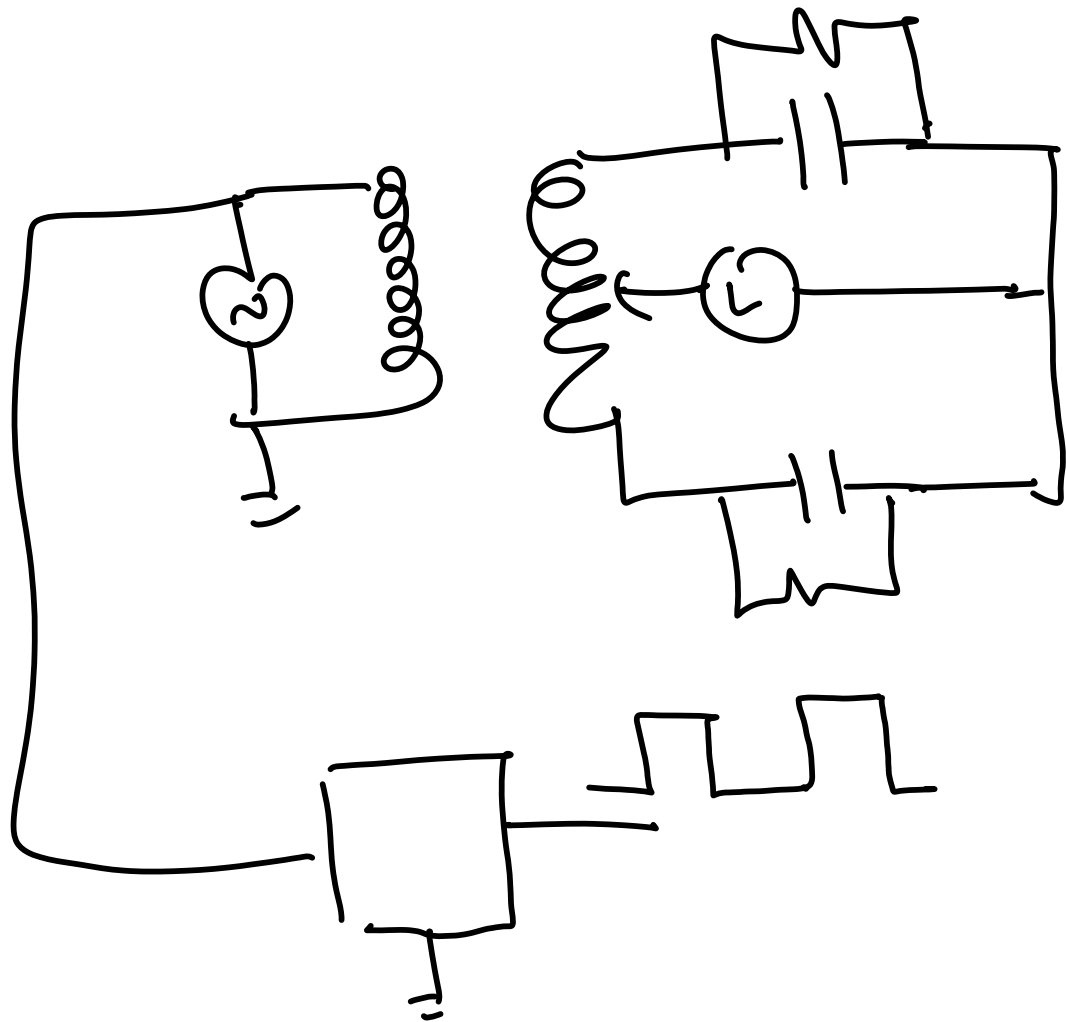


average
value
is zero

with out phase shifter

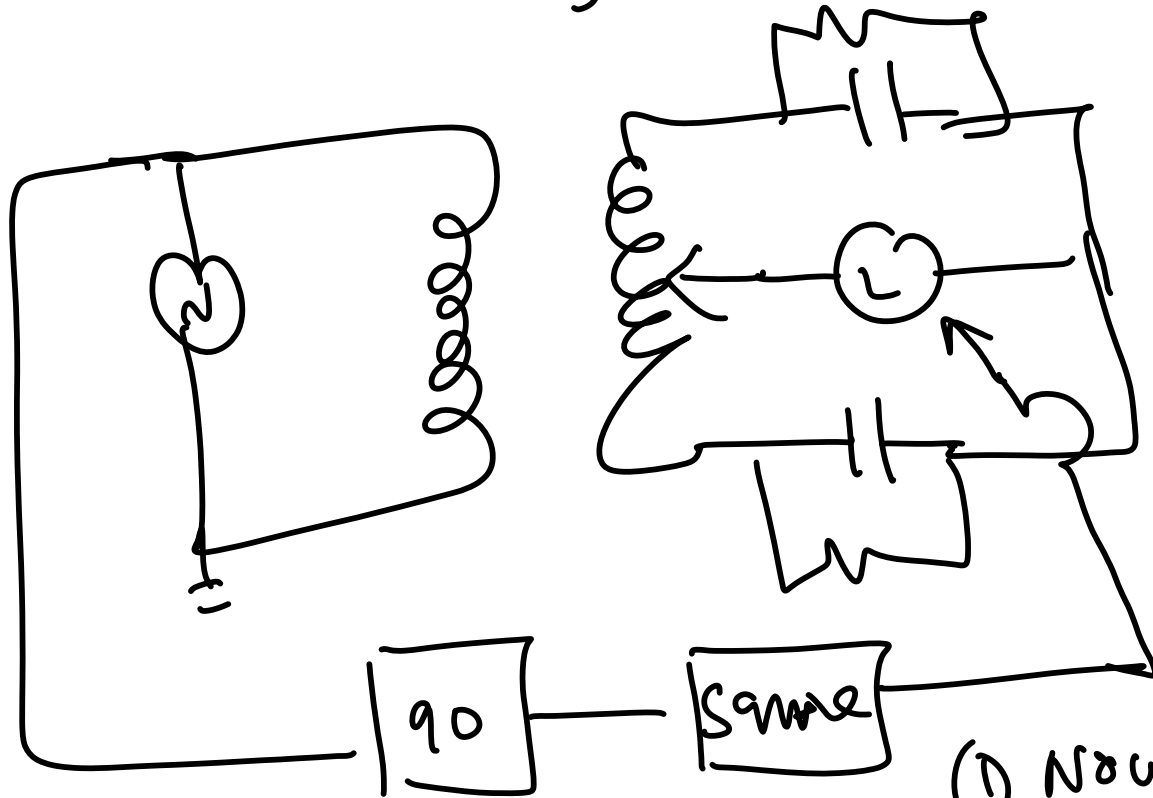


average
is not
zero



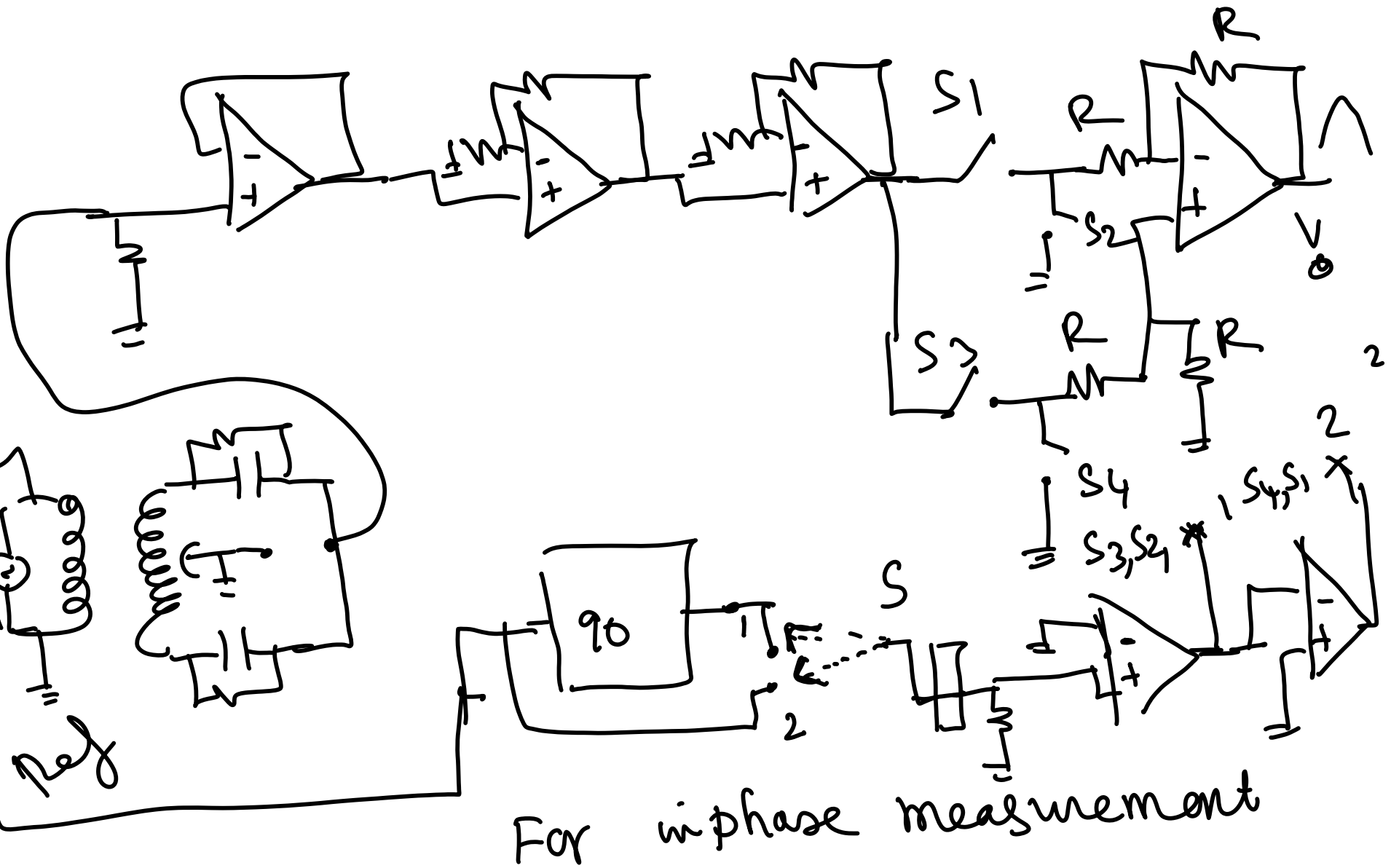
① If lock in
amp is
switched with
in phase source
were then
only resistance
current will
produce output.

(2) The capacitance current will not produce any output.



(1) Now lock in sensitive only to capacitance change and not for resistance change.

Designing of lock in amplifier



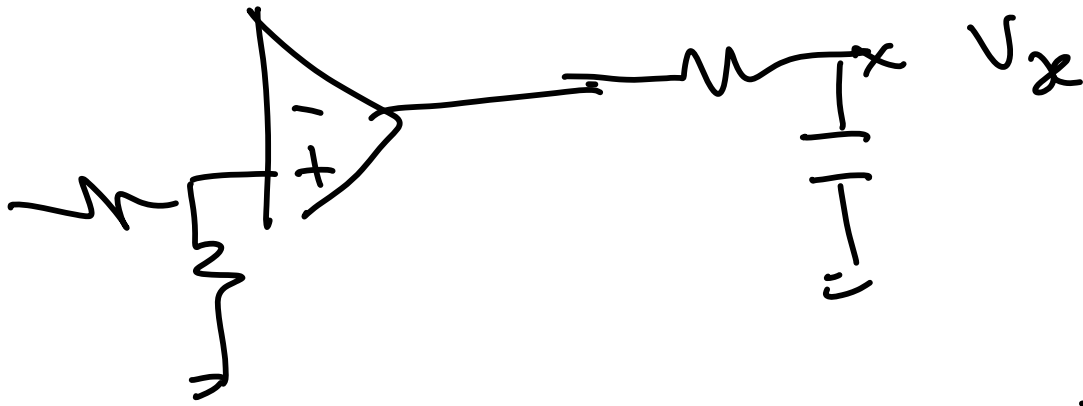
Connect S to point 2
 S_3 and S_2 will be ON, S_4, S_1 OFF
 S_0 output V_0 will be true

This measures the Resistance
i.e. it measures the in phase
comp. ϕ .

To measure the Capacitance

Connect Switch S_2 to position 1

Now the bridge is sensitive
for capacitance measurement

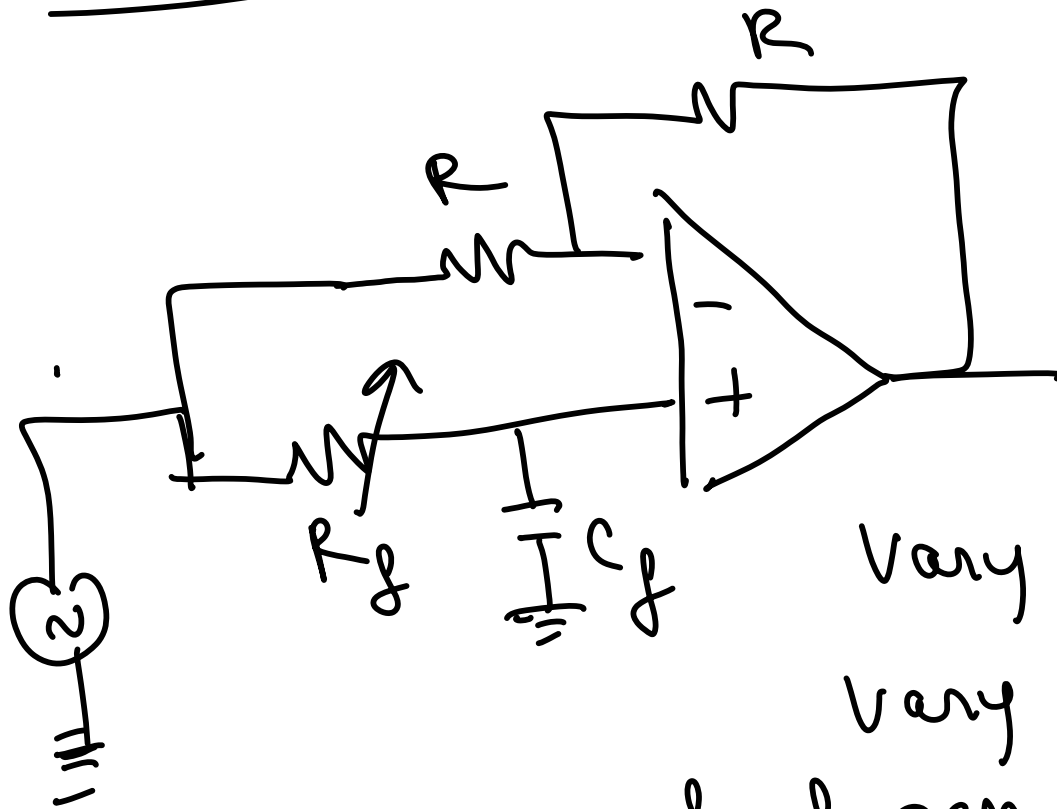


So using lock in amp

① Separate out the
in phase and
out of phase comp

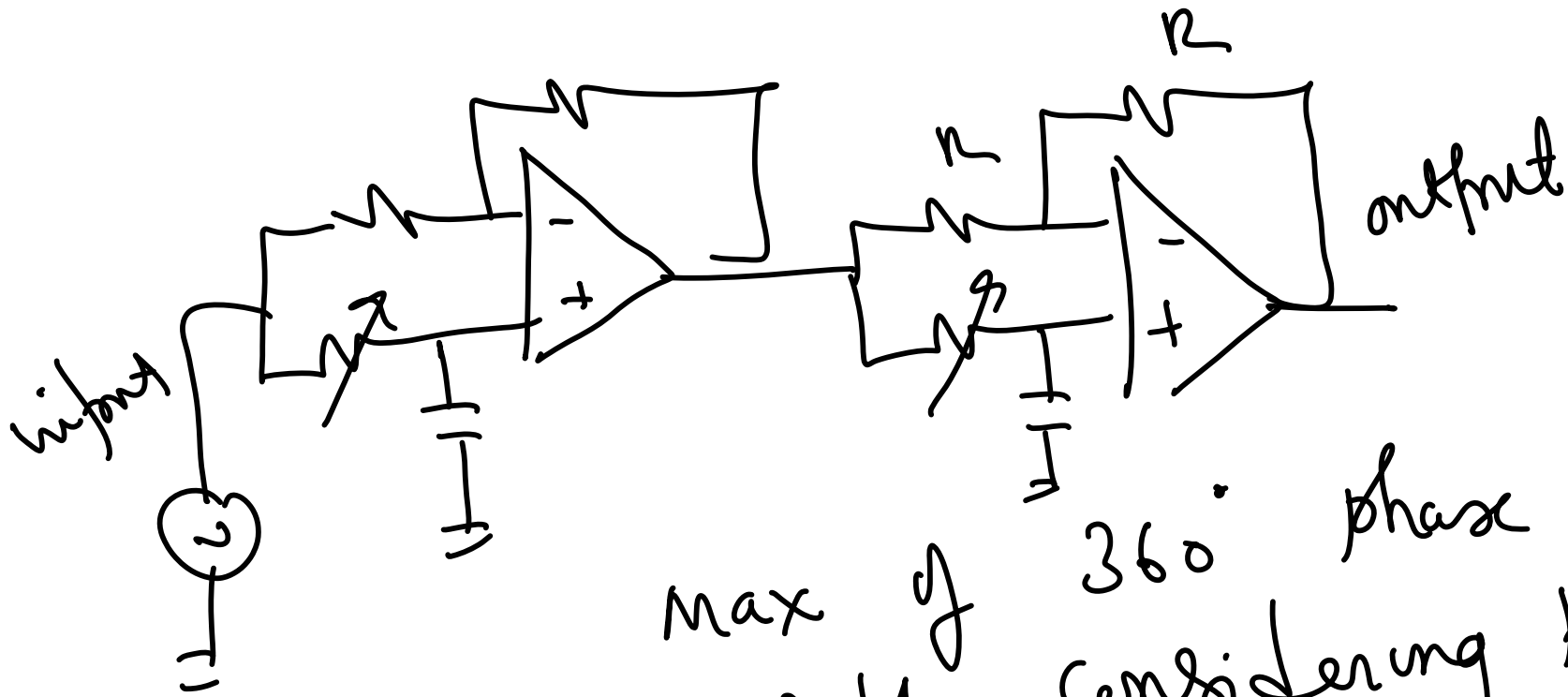
② Remove the noise
from the signal

Phase Shifter circuit

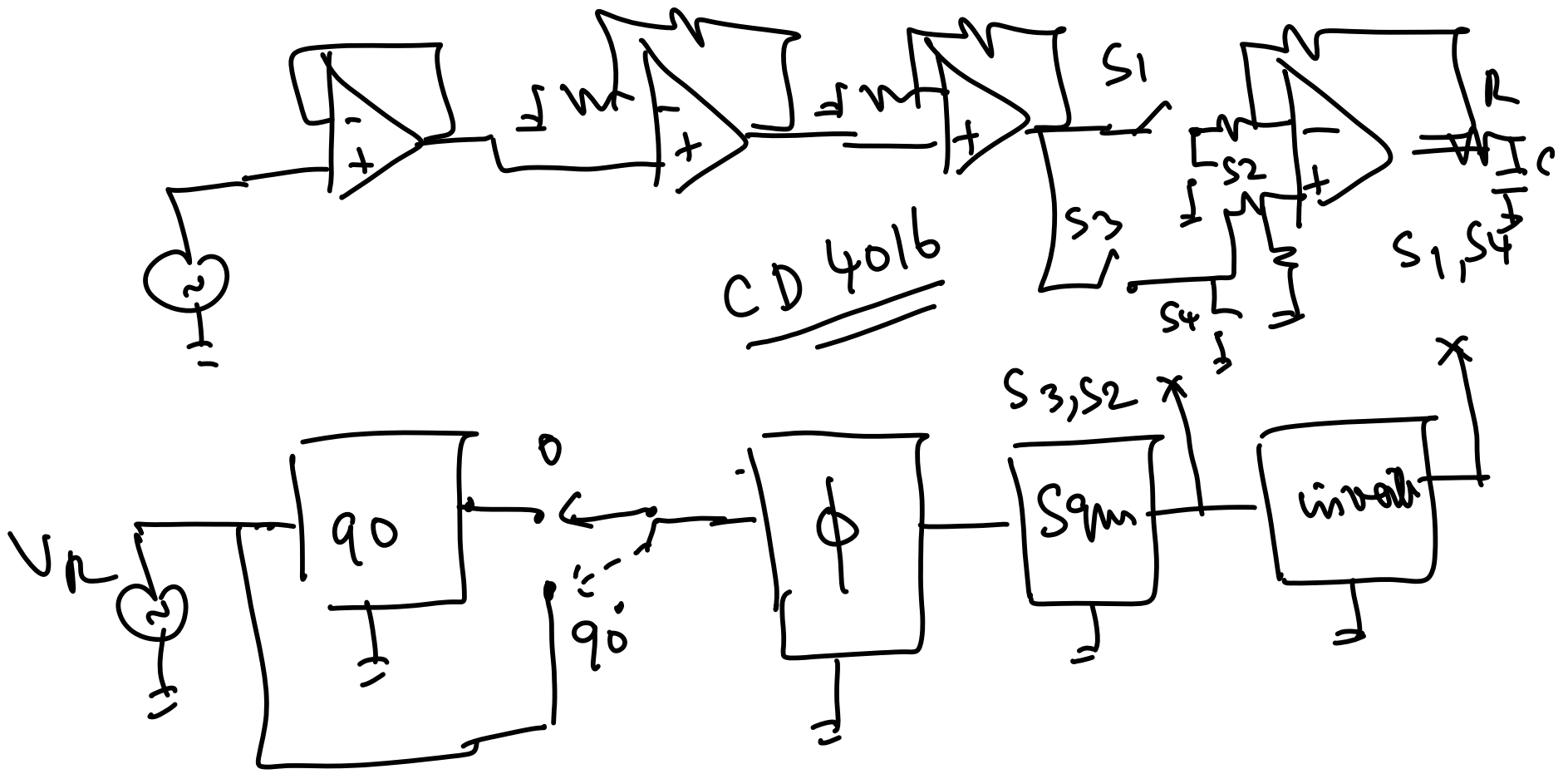


Vary the R_f to
vary the phase shift
between input and
output.

For 90° phase shift select suitable
 R_f and C_f



max of 360° phase shift
possible considering both
the stages



Lecture No. 33

Capacitive sensors

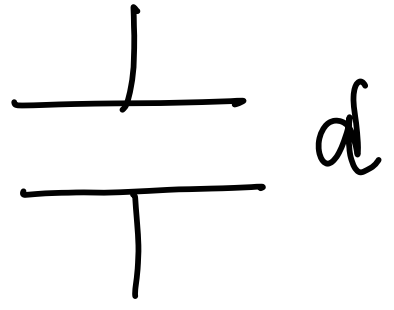
- ① Small in size
- ② low power consumption

Disadvantage

Noisy
Signal conditioning is difficult

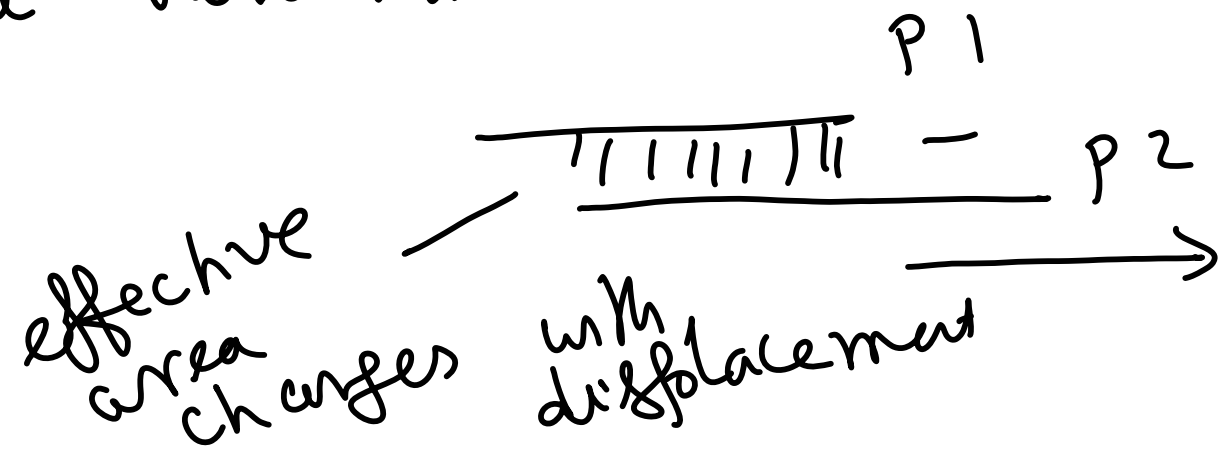
Problems

$$C = \frac{\epsilon_0 \epsilon_r (A)}{d}$$



Area
distance between
the two plates

① Area variation

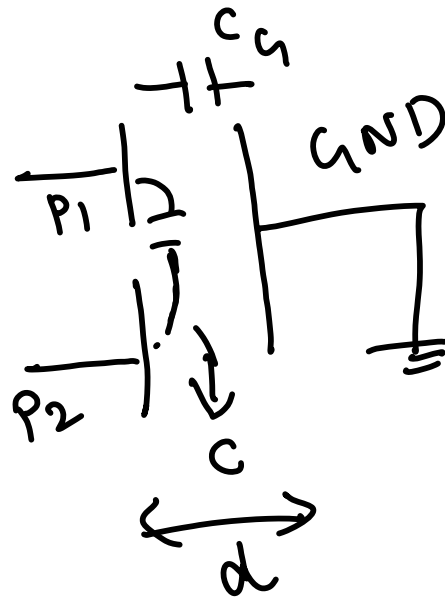


② Space variation



distance between the two plates varied and A is constant

③ proximity variation



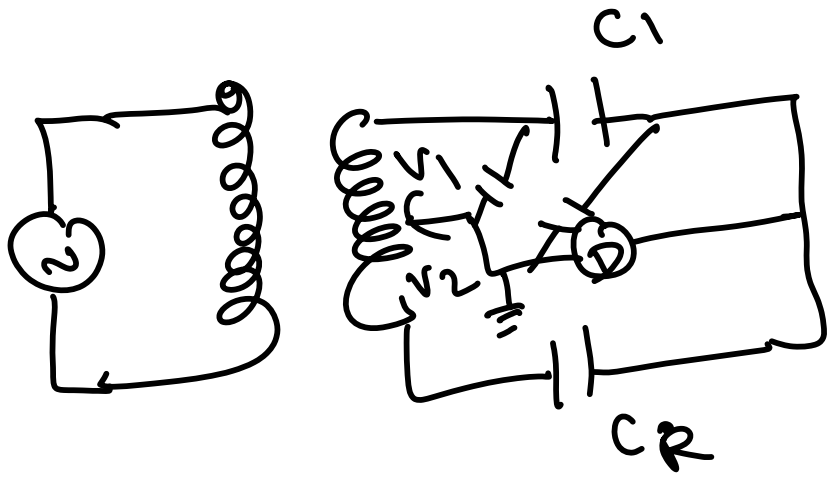
Here grounded electrode is moved and capacitance between the two fixed plates are measured.

① Using ratio transformer technique

② Triode pump circuit

③ How to use of amps

?



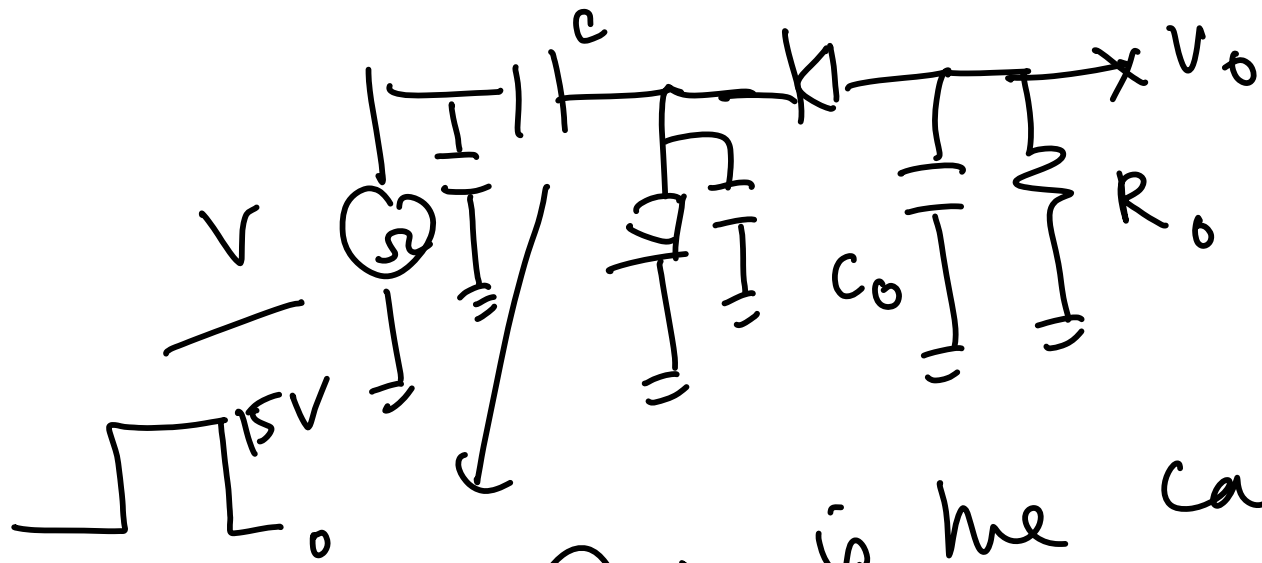
Ratio transformer bridge

$$V_1 C_1 \omega = V_2 C_2 \omega$$

$$\frac{V_1}{V_2} = \frac{C_2}{C_1}$$

Stray cap \rightarrow no role to play
in the balancing of the bridge

So balancing to be done
manually. This is the main
draw back for instrumentation work.



Diode pump
circuit

This is the cap under measurement

of f is the frequency of the source of vol V .

Total charge transferred per sec

$$Q = CVf$$

This charge is delivered
to the output capacitor

If output vol is V_o

The amount of charge

leaking through $R_o = \frac{V_o}{R_o}$

$= g_m$ coming charge $= CVf$

$$CVf = \frac{V_o}{R_o}$$

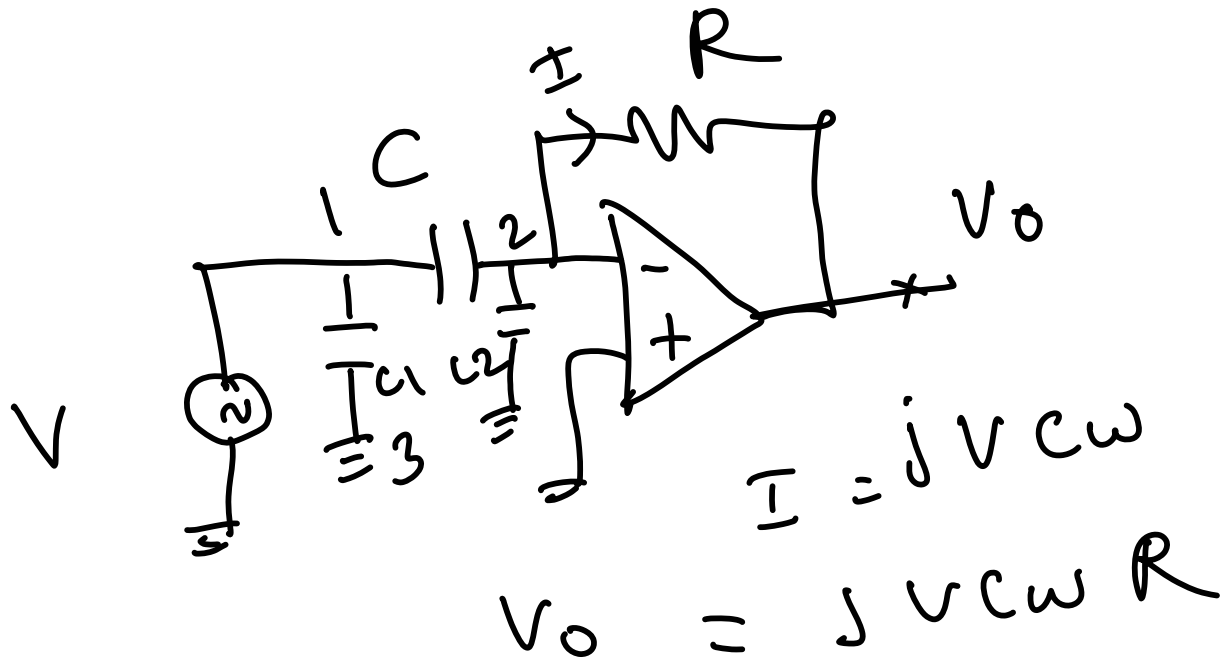
$$CVR_o f = V_o$$

$$C = \frac{V_o}{VR_o f}$$

This is valid only if
 V_o is small compared to V .

So keep V_o with in few mV
 by selecting R_o
 It is good for 1% to 2%
 accuracy level.

③ using op amp



$$V_o = V_{CWR}$$

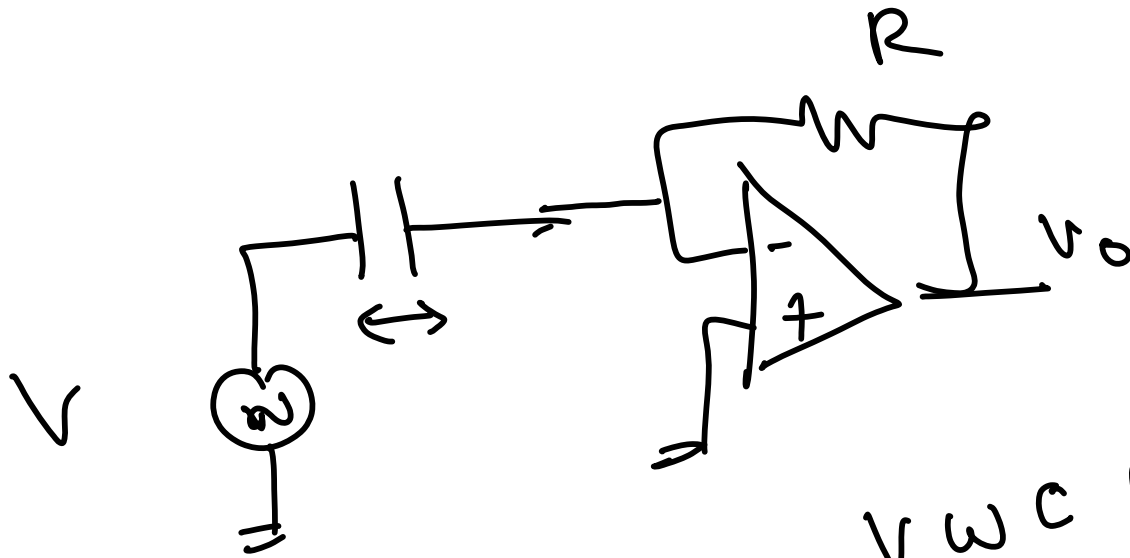
① Output vol is linear to C
Always consider cap as a 3 terminal device. This brings two stray caps.

② C_1 and C_2 will not produce any charge in V_o

It is valid ↓ provided

- ① Source impedance zero
- ② virtual ground is at zero

Displacement measurement



$$V_o = V \omega C R$$

$$= k V R \omega \left[\frac{A}{d} \right]$$

d changes V_o varies by $\frac{1}{d}$

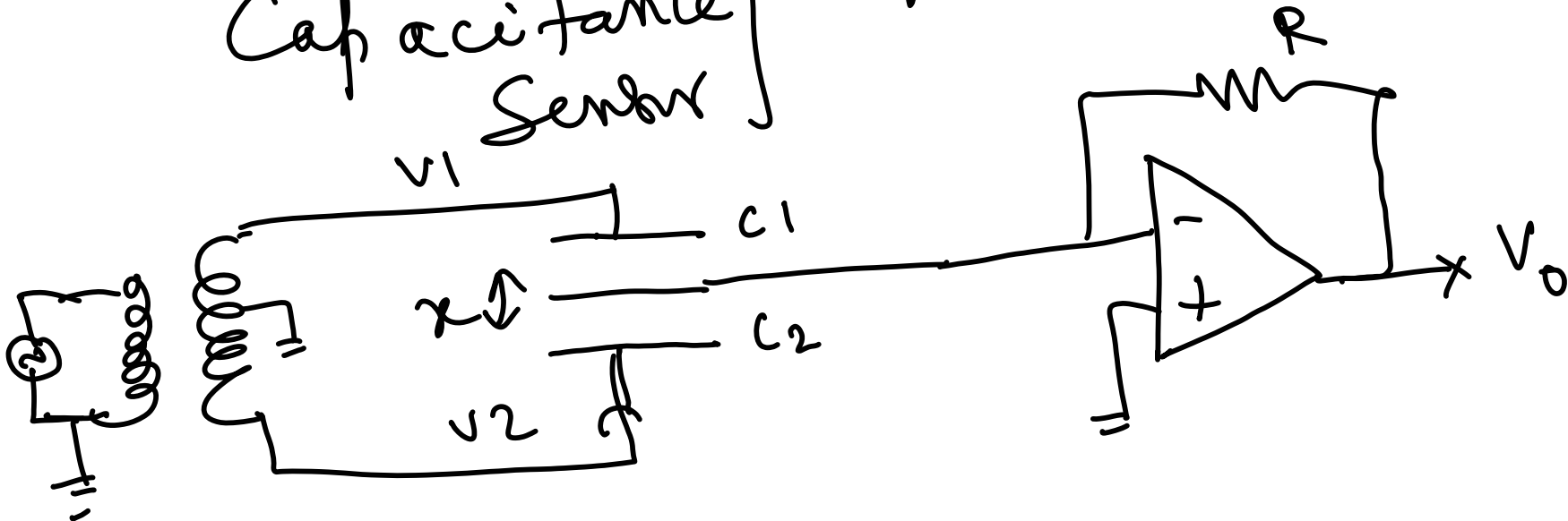
$$V_o = \frac{V \omega R \epsilon_0 t_r A}{d}$$

This is not as accurate as ratio transformer bridge

The errors are

- ① V variation
- ② ϵ_r variation \rightarrow moisture
- ③ ω variation

Capacitance Sensor with three plates



① current through C_1 and C_2
are 180° out of phase

$$\text{current through } C_1 = j V_1 C_1 \omega$$

$$\text{current through } C_2 = -j V_2 C_2 \omega$$

$$(V_1 C_1 \omega - V_2 C_2 \omega) R = V_0$$

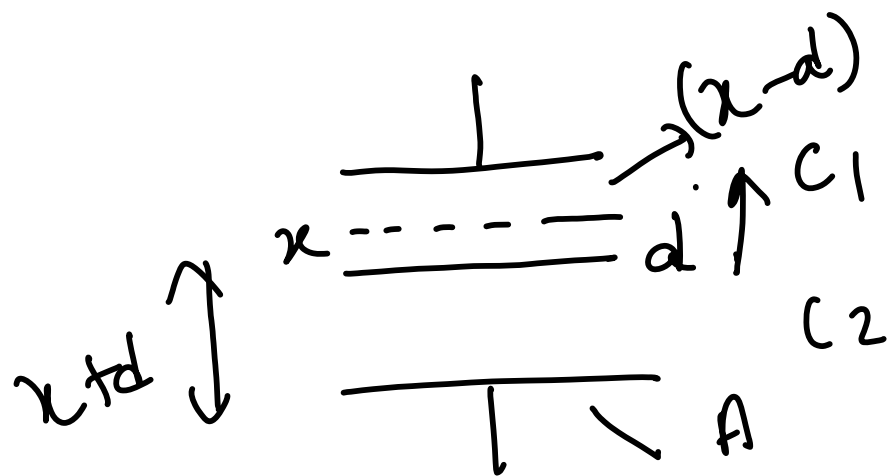
$$\omega R (V_1 C_1 - V_2 C_2) = V_0$$

$$V_1 = V_2 = V$$

$$V \omega R (C_1 - C_2) = V_0$$

① Area of the plates are A

② x is the displacement from the centre distance d



$$C_1 = \epsilon_0 \epsilon_r \frac{A}{d-x}$$

$$C_2 = \epsilon_0 \epsilon_r \frac{A}{d+x}$$

$$\begin{aligned} (C_1 - C_2) &= A \epsilon_0 \epsilon_r \left(\frac{1}{d-x} - \frac{1}{d+x} \right) \\ &= A \epsilon_0 \epsilon_r \left(\frac{d+x - (d-x)}{d^2 - x^2} \right) \end{aligned}$$

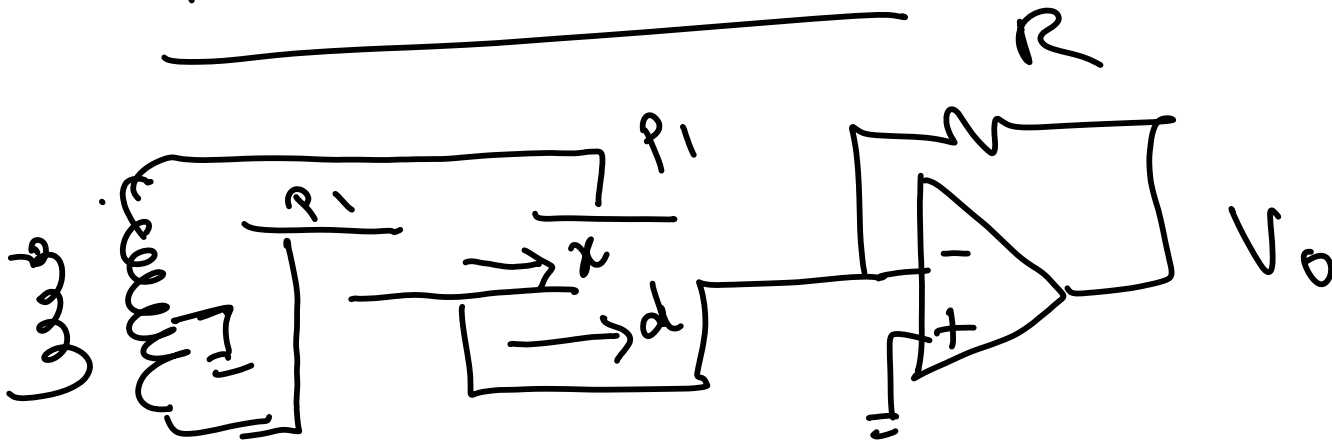
$$(C_1 - C_2) = A \epsilon_0 \epsilon_r \left(\frac{2x}{d^2 - x^2} \right)$$

$$V_0 = V W A \epsilon_0 \epsilon_r \left(\frac{2x}{d^2 - x^2} \right)$$

For $x \ll d$

$$V_0 \propto x$$

Area variation



For a die's placement x
area under one plate is
decreasing and equal area
is increasing in the other plate

$$A(1+x)$$

$$A(1-x)$$

$$V_0 = VRW(C_1 - C_2)$$

$$C_1 = \epsilon_0 \epsilon_r \frac{A(1+x)}{d}$$

$$C_2 = \epsilon_0 \epsilon_r \frac{A(1-x)}{d}$$

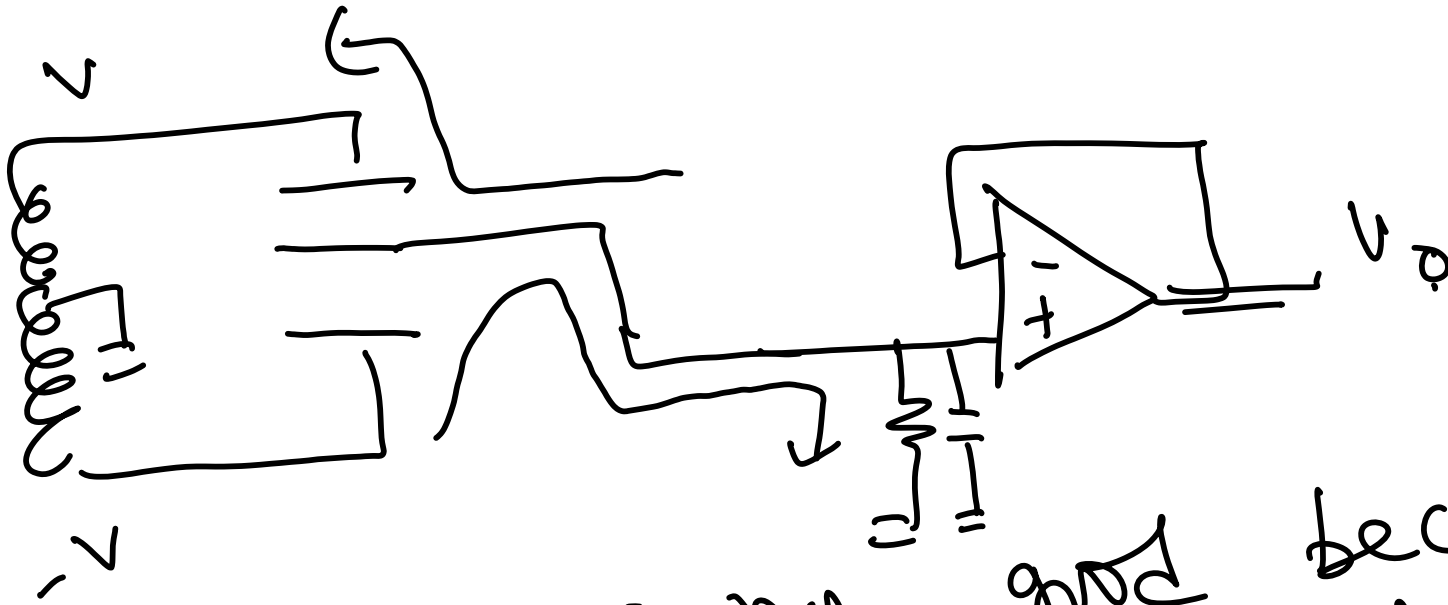
$$\begin{aligned}
 (C_1 - C_2) &= \frac{\epsilon_0 \epsilon_r A}{d} [(1+x) - (1-x)] \\
 &= \frac{\epsilon_0 \epsilon_r A}{d} [2x]
 \end{aligned}$$

$$V_o = \frac{V R \omega \epsilon_0 \epsilon_r A}{d} [2x]$$

Output voltage is linear for displacement x .

This is also not as accurate as ratio transformer bridge

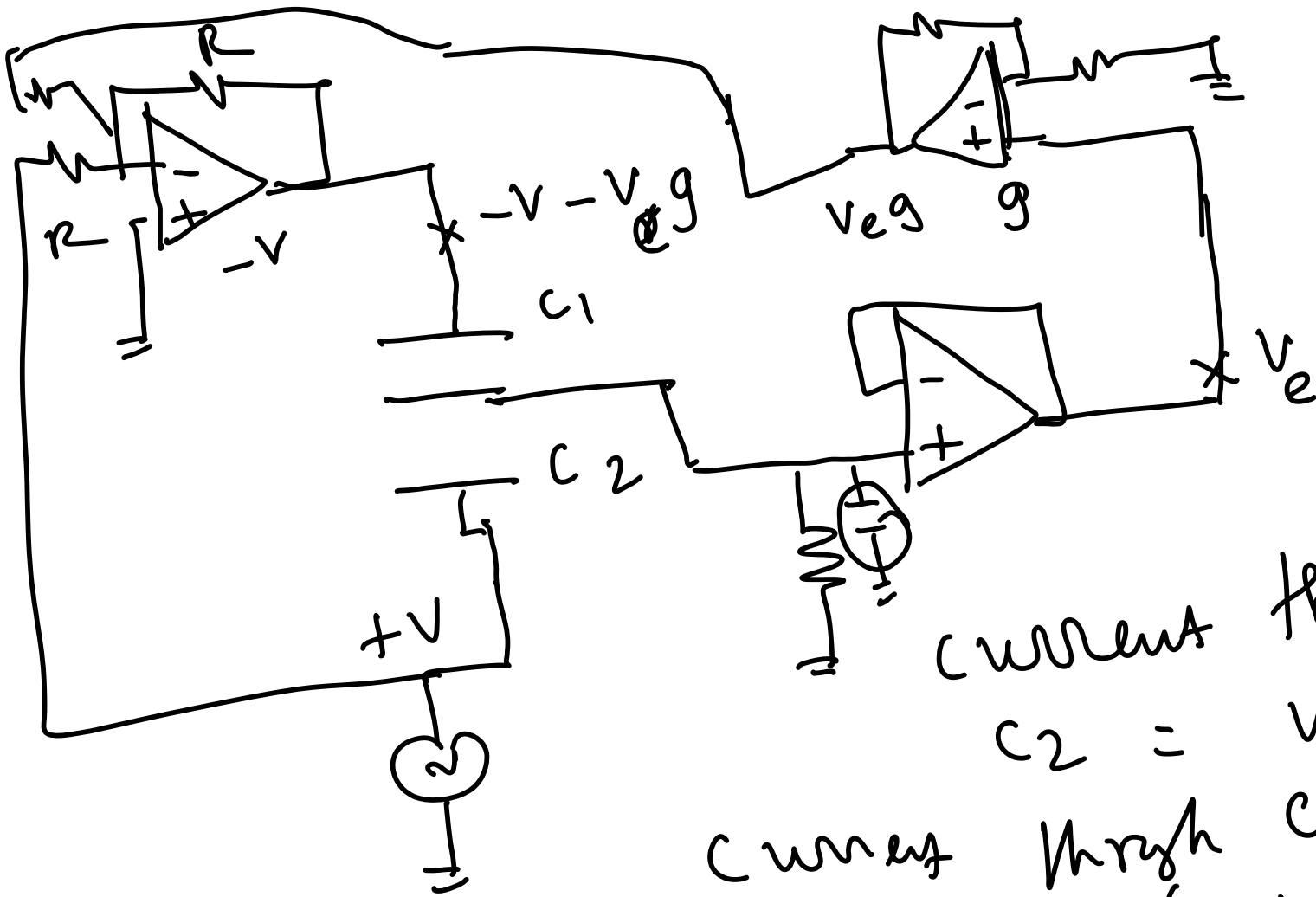
Use of non-inverting amp



This is not good because
it is sensitive to stray cap.
For this method to work

$$V_o = 0$$

How to make $V_o = 0$??



current through $C_2 = v C_2 \omega$

current through $C_1 = (-v - v_e g) C_1 \omega$

$$v C_2 \omega = (-v - v_e g) C_1 \omega$$

$$V C_2 = (V + v_e) C_1$$

v_e does the balancing technique
 v_e is small or large?

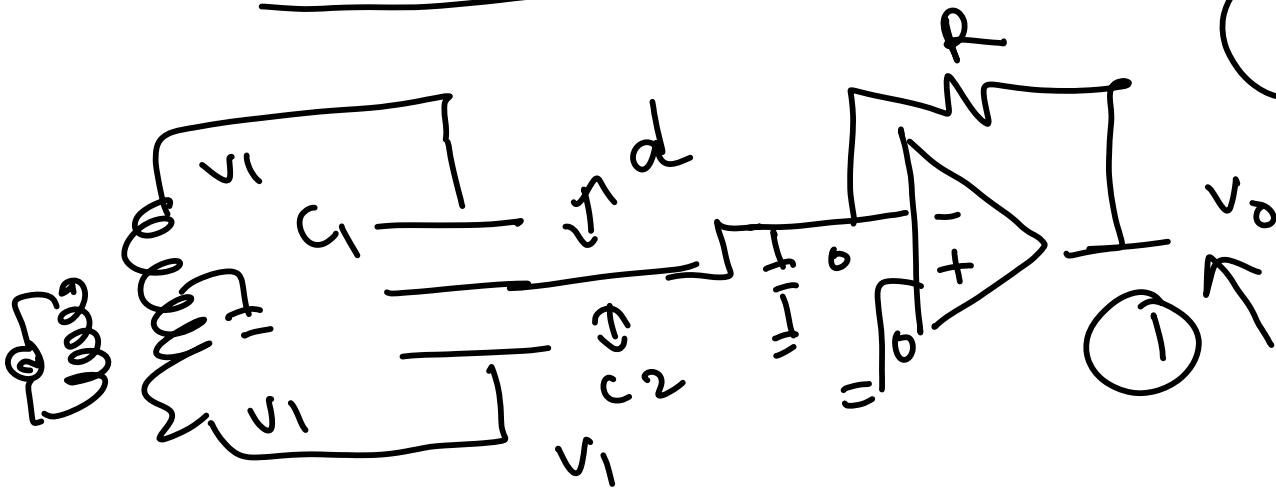
$$C_2 = \frac{t_o t_r A}{d+x}$$

$$C_1 = \frac{t_o t_r A}{d-x}$$

Non-inverting amp also can be used

~~Do~~ Linear or non linear or x ?

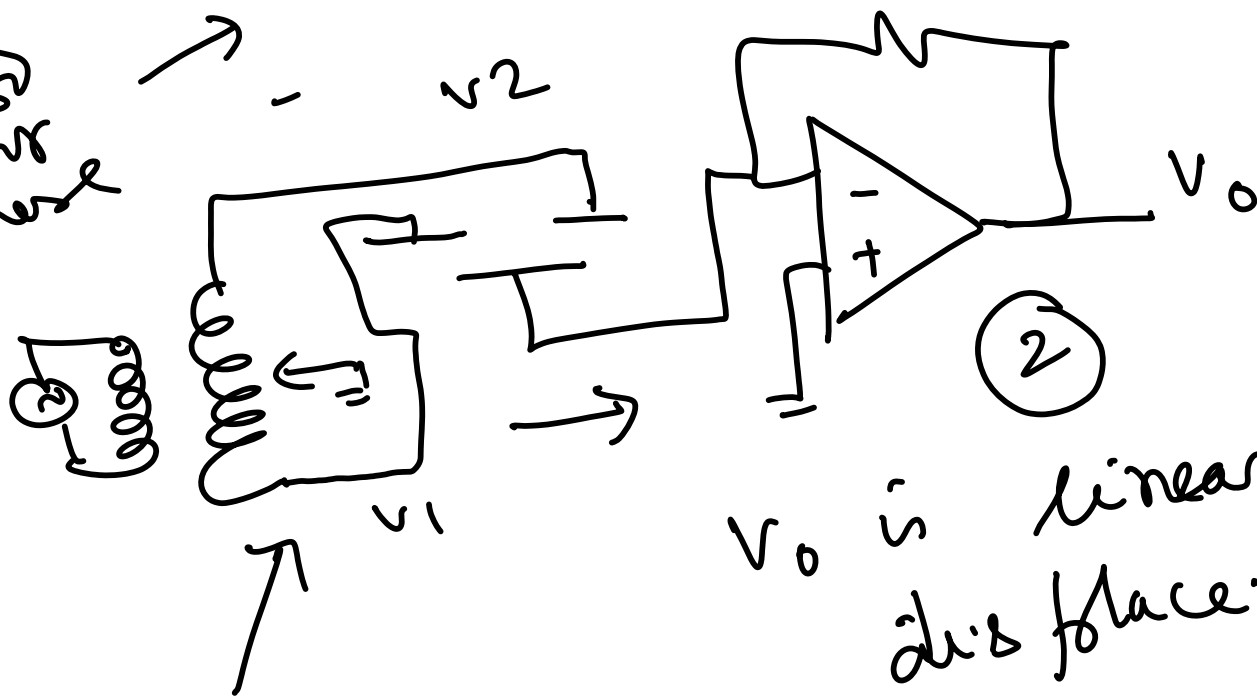
lec no: 34



Output is not linear with 'd'

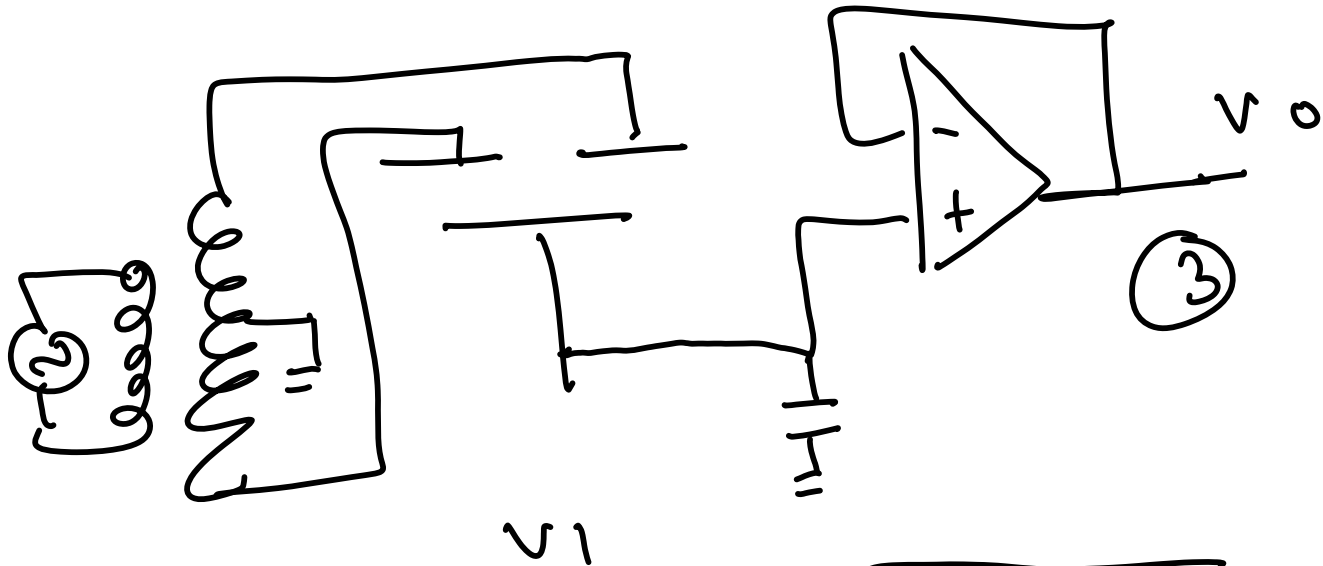
Low L
with space
variation

180° phase

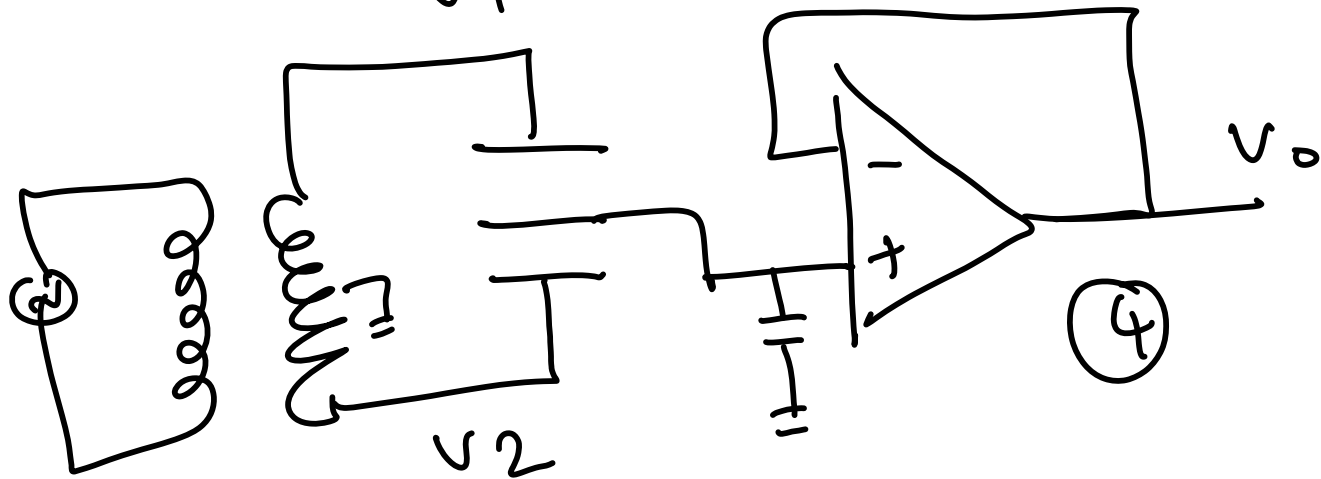


v_0 is linear with
displacement

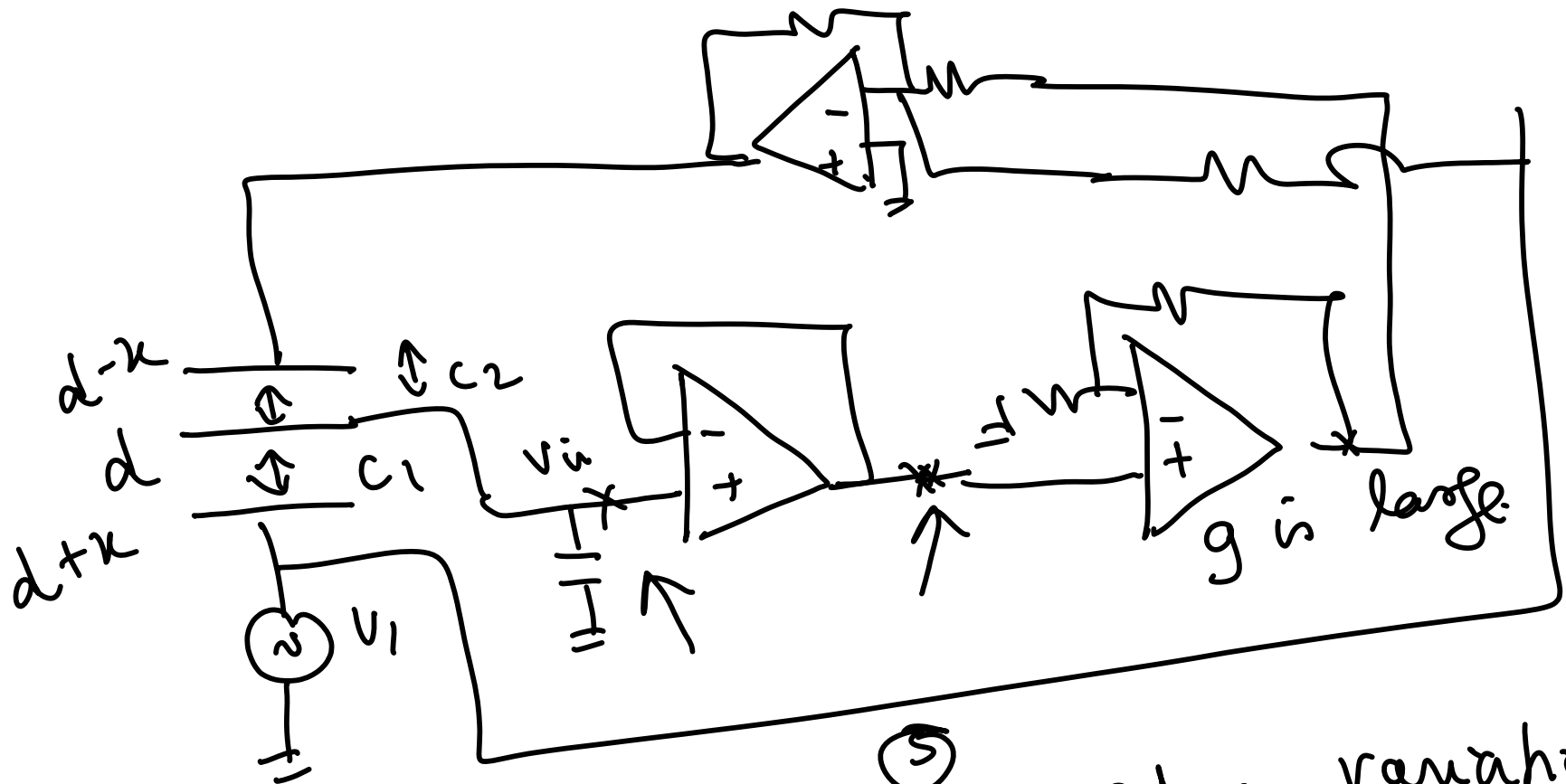
Low L
with area
variation



High Z
area variation



High Z
Space variation



High 2 amp with feed back Space vanaham

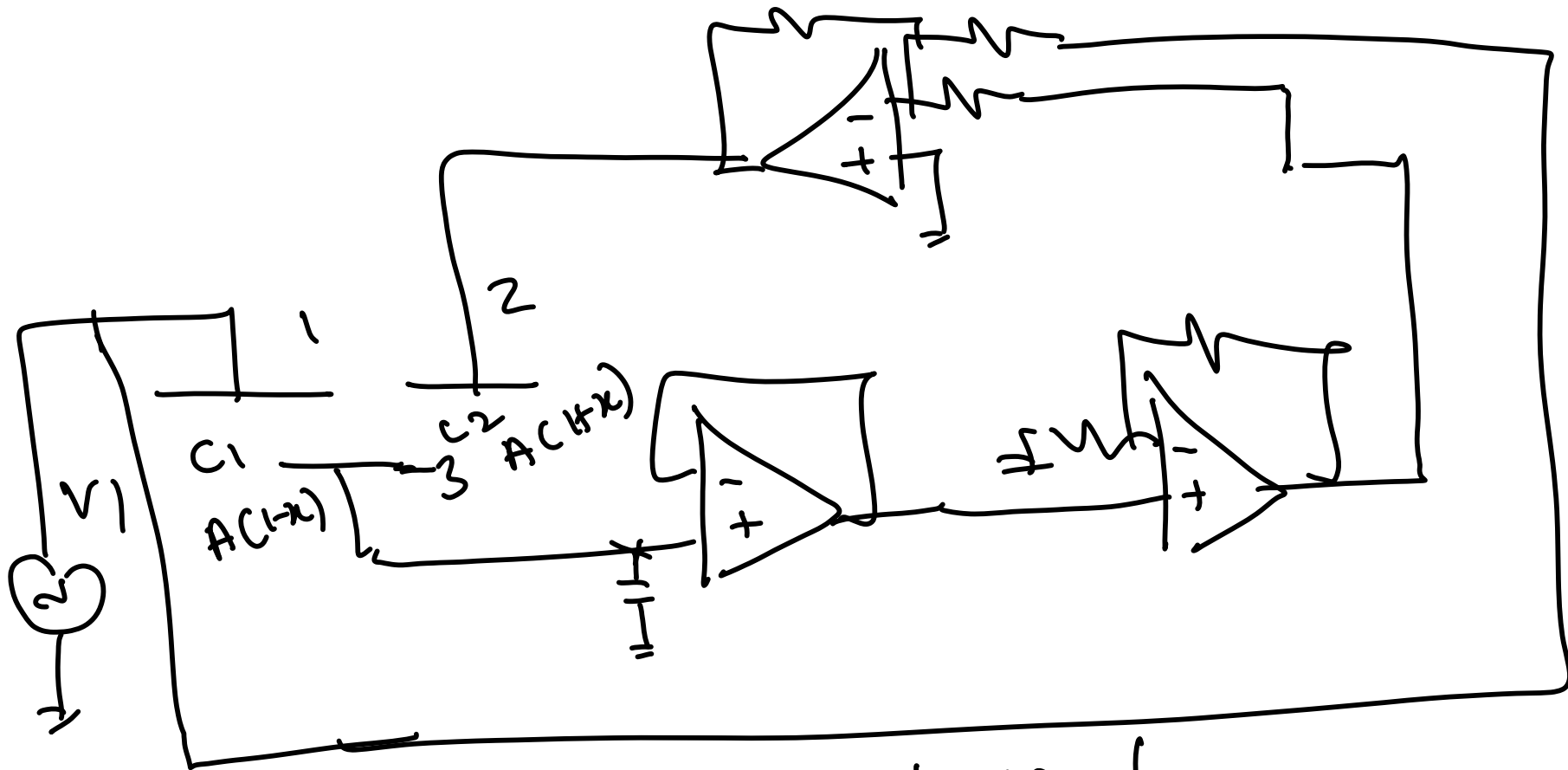
$v_{in} \approx 0$

$$v_1 C_1 \omega = v_2 C_2 \omega$$

$$\frac{v_1}{v_2} = \frac{C_2}{C_1}$$

$$= \frac{A}{d-x} \bigg| \frac{A}{d+x}$$

$$\frac{v_1}{v_2} = \frac{d+x}{d-x}$$



Circuit no. 6

High Z amplifier with area variation
 with feedback $V_1 C_1 \omega = V_2 C_2 \omega$

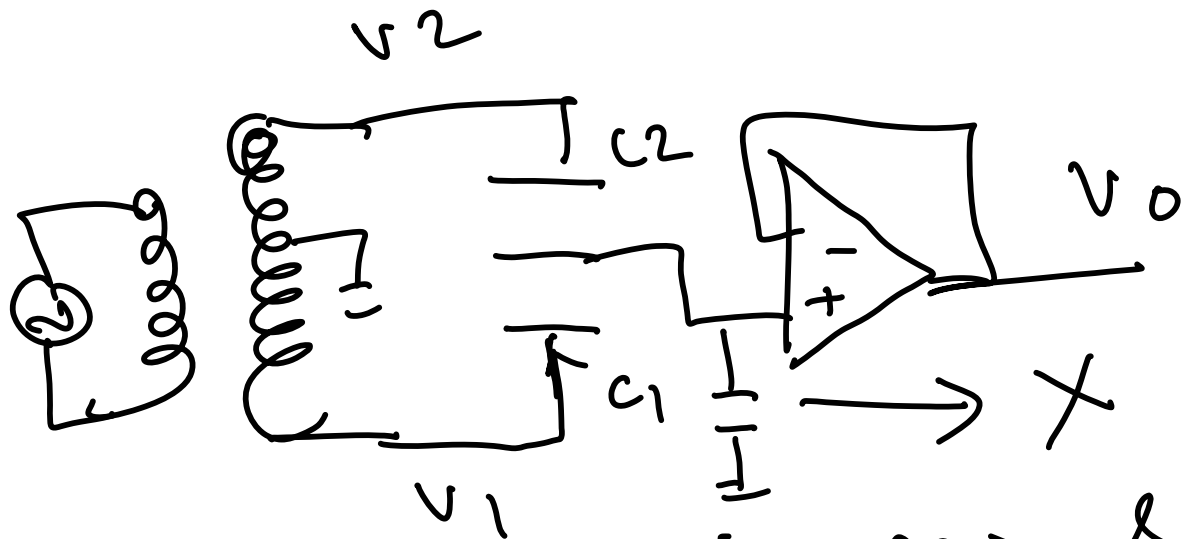
$$\frac{V_1}{V_2} = \frac{C_2}{C_1} = \frac{A(x)}{A(1-x)}$$

non linear with displacement

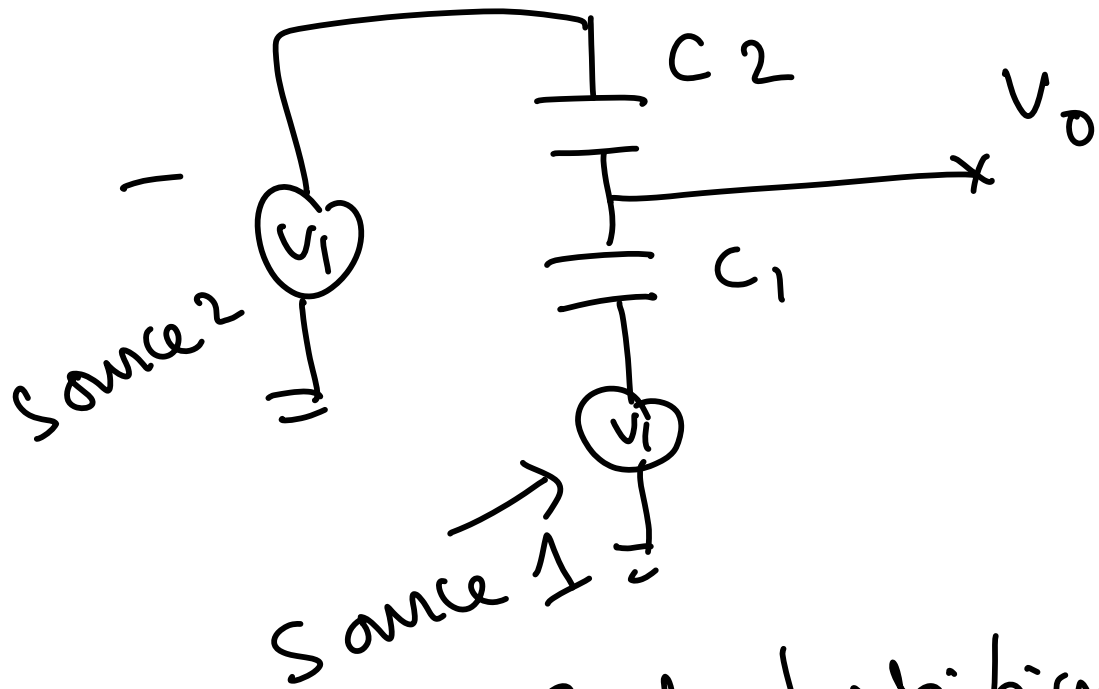
circuit 5 and circuit 6

Feed back keeps the non-inverting input of the first amplifier near to ground potential

This makes the stray caps are ineffective



- ① Assuming no stray cap at the input of the op amp and they
- ② Assuming $v_1 = v_2$ are 180° out of phase



Using Superposition theorem V_0 can be calculated

$$\frac{V_1 \times 2C_2}{2C_1 + 2C_2} \quad \rightarrow \quad I$$

Contribution due to V_1 by connecting V_2 to ground

Z_{C_2} is impedance of

cap C_2

Z_{C_1} is the impedance of cap C_1

II Contribution due to source 2

$$\rightarrow \frac{V_1 \times Z_{C_1}}{Z_{C_1} + Z_{C_2}} \quad \xrightarrow{\text{by ground; source 1}} \quad \text{II}$$

Adding I and II

$$V_0 = \frac{V_1 \times Z_{C_2}}{Z_{C_1} + Z_{C_2}} - \frac{V_1 Z_{C_1}}{Z_{C_1} + Z_{C_2}}$$

$$V_0 = \frac{V_1}{(Z_{C_1} + Z_{C_2})} [Z_{C_2} - Z_{C_1}]$$

$$Z_{C_1} = \frac{j\omega A}{d+x}$$

$$Z_{C_2} = \frac{j\omega A}{d-x}$$

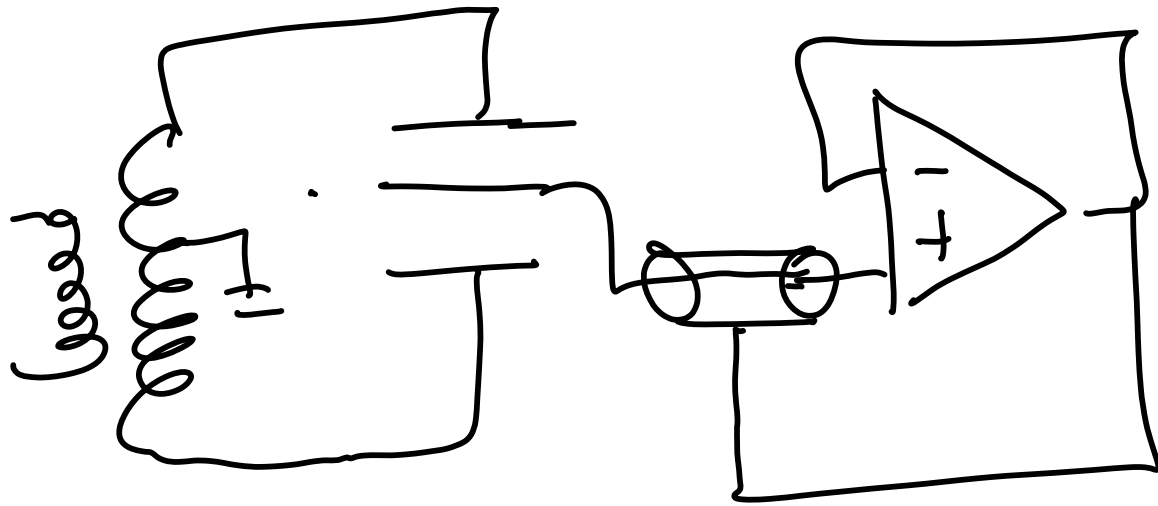
$$\begin{aligned} \frac{Z_{C_2} - Z_{C_1}}{Z_{C_1} + Z_{C_2}} &= \frac{\frac{1}{d-x} - \frac{1}{d+x}}{\frac{1}{d-x} + \frac{1}{d+x}} \\ &= \frac{d+x - (d-x)}{d+x + d-x} \end{aligned}$$

$$\frac{2c_2 - 2c_1}{2c_1 + 2c_2} = \frac{2\lambda}{2d} = \frac{\lambda}{d}$$

$V_0 = v_1 \times \frac{\lambda}{d}$

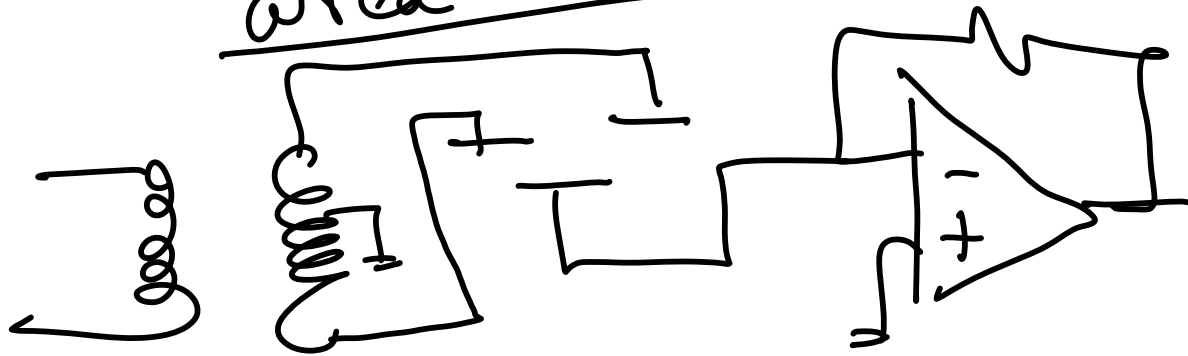
$\rightarrow v_1$ is fixed

$\rightarrow d$ is fixed

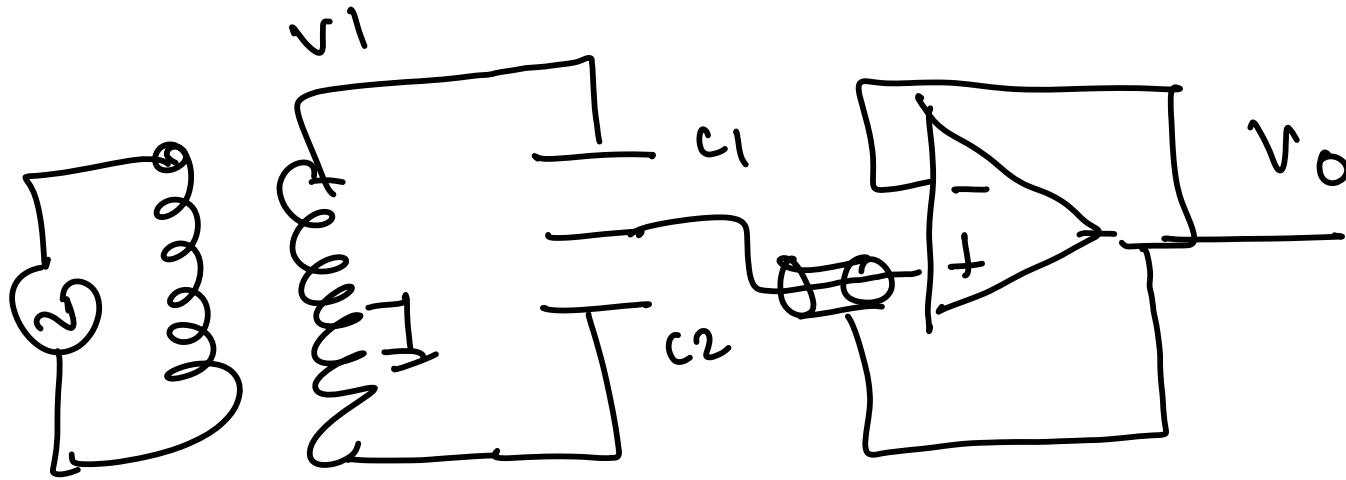


Linear for
displacement d
+ space variat.

Law 2 amp is linear for
area variation ✓



High Z amp for space
variation



$$V_0 = V_1 \frac{Z C_1}{2C_1 + 2C_2} - \frac{V_1 Z C_2}{2C_1 + 2C_2}$$

$$Z C_1 = \frac{A}{d+x} \times k$$

$$Z C_2 = \frac{A}{d-x} \times k$$

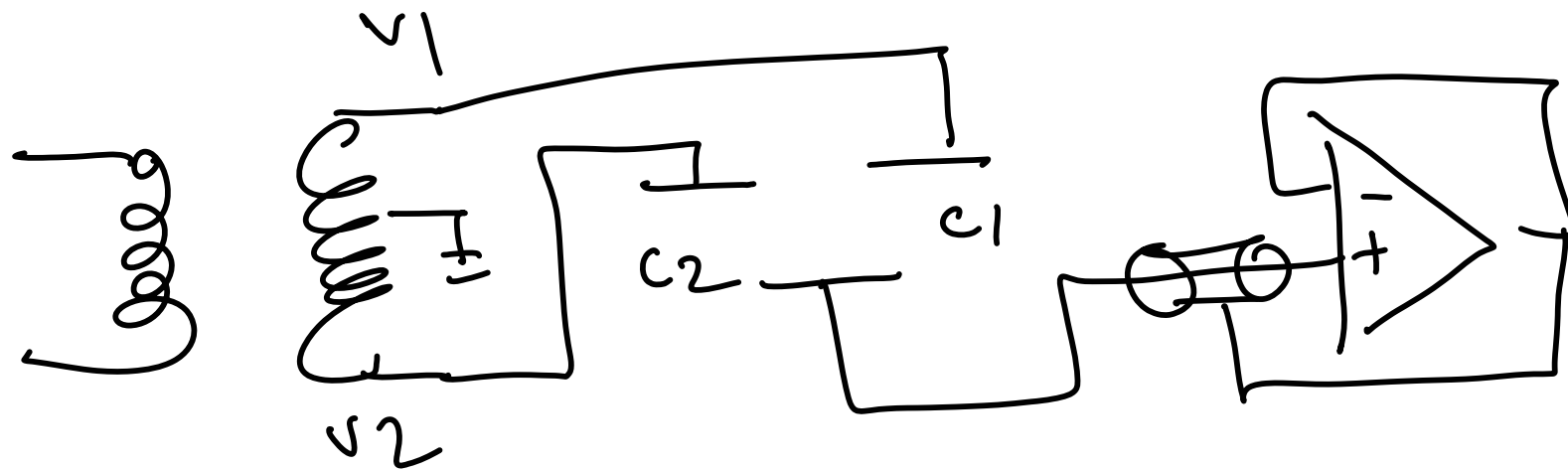
$$2c_1 + 2c_2 = \frac{A}{(d+x)} + \frac{A}{(d-x)}$$

$$2c_1 - 2c_2 = \frac{A}{(d+x)} - \frac{A}{(d-x)}$$

$$\frac{2c_1 - 2c_2}{2c_1 + 2c_2} = \frac{\frac{1}{d+x} - \frac{1}{d-x}}{\frac{1}{d+x} + \frac{1}{d-x}}$$

This is already done

High 2 for area variation



$$V_2 \frac{Z_{C_2}}{Z_{C_1} + Z_{C_2}} - V_1 \frac{Z_{C_2}}{2Z_{C_1} + Z_{C_2}} = V_o$$

$$Z_{C_1} = \frac{A(1+\kappa)}{d}$$

$$Z_{C_2} = \frac{A(1-\kappa)}{d}$$

$$2c_1 - 2c_2 = \frac{A}{d} [1+x - (1-x)]$$

$$2c_1 + 2c_2 = \frac{A}{d} [(1+x) + (1-x)]$$

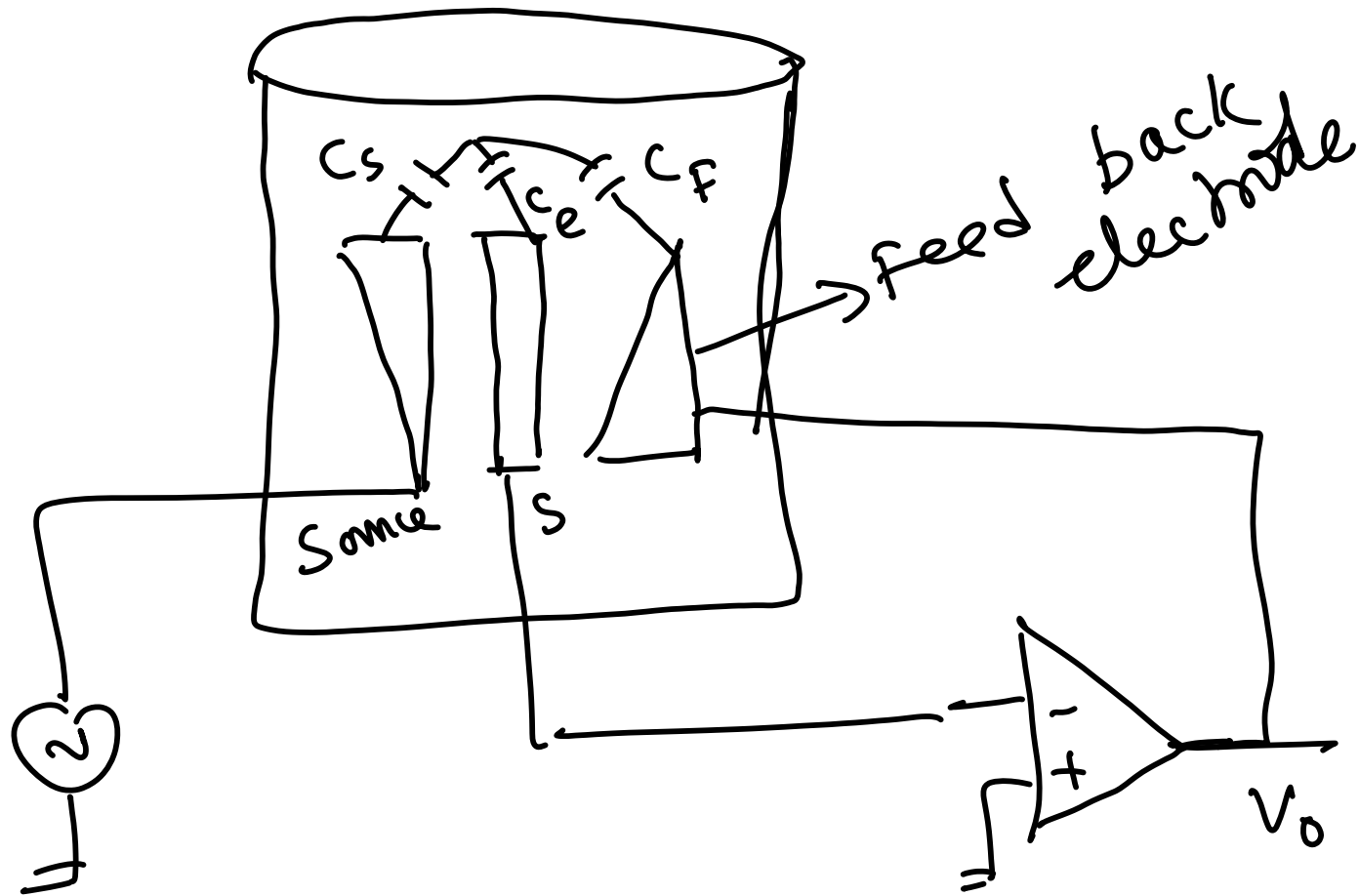
$$\frac{2c_1 - 2c_2}{2c_1 + 2c_2} = \frac{1+x-1+x}{1+x+1-x} = \frac{2x}{2} = x$$

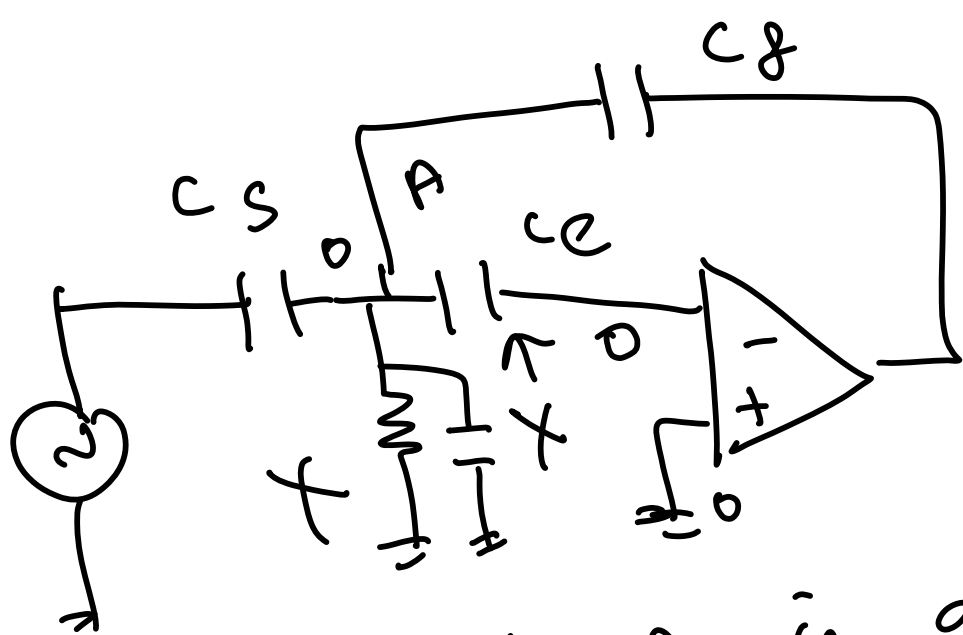
$$v_1 = v_2$$

$$v_0 = v_x$$

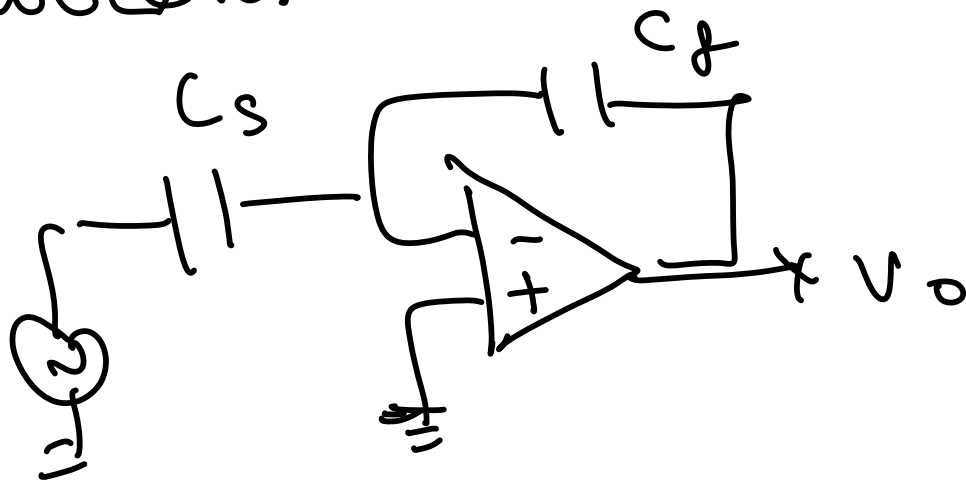


Water level measurement using Cap. Sensor





point A is at zero potential!
 This is because -ve terminal
 is at zero potential and no
 current through C_e



Both C_f and C_s depend
on the water level.

The plates are inverted

So with water level
 v_0 varies.

① Best circuit is

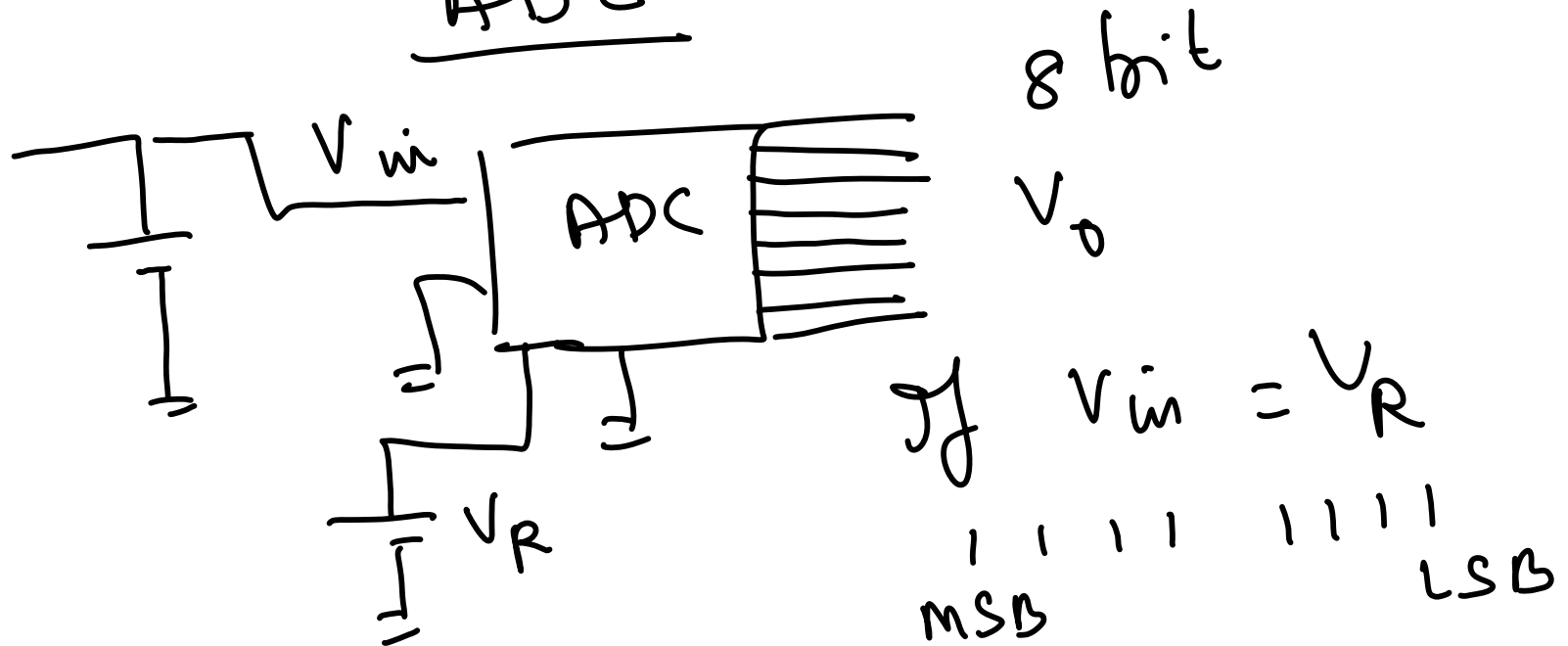
Ratio transformer
bridge.

② of amp is with in inverting
amp is ~~best~~ next best

Lecture - 35

Analog to Digital Conversion

ADC



$$\text{For } V_{in} \geq V_R$$

$$|V| = 1V$$

Then $\overset{\text{MSB}}{\uparrow} 111 \quad 111 \downarrow \overset{\text{LSB}}{\quad}$

All bits are high

$$\text{For } V = 0$$

0000 0000

All bits are zero

Total binary level = 2^8

$$= 256$$

1 LSB to change the reference

$$\text{Vol} = \frac{1}{256} \approx 4 \text{ mV}$$

In fact 4 mV



0000 0001

For 1 LSB the reference

$$Vol = \frac{V_R}{2^n} = \frac{V_R}{256}$$

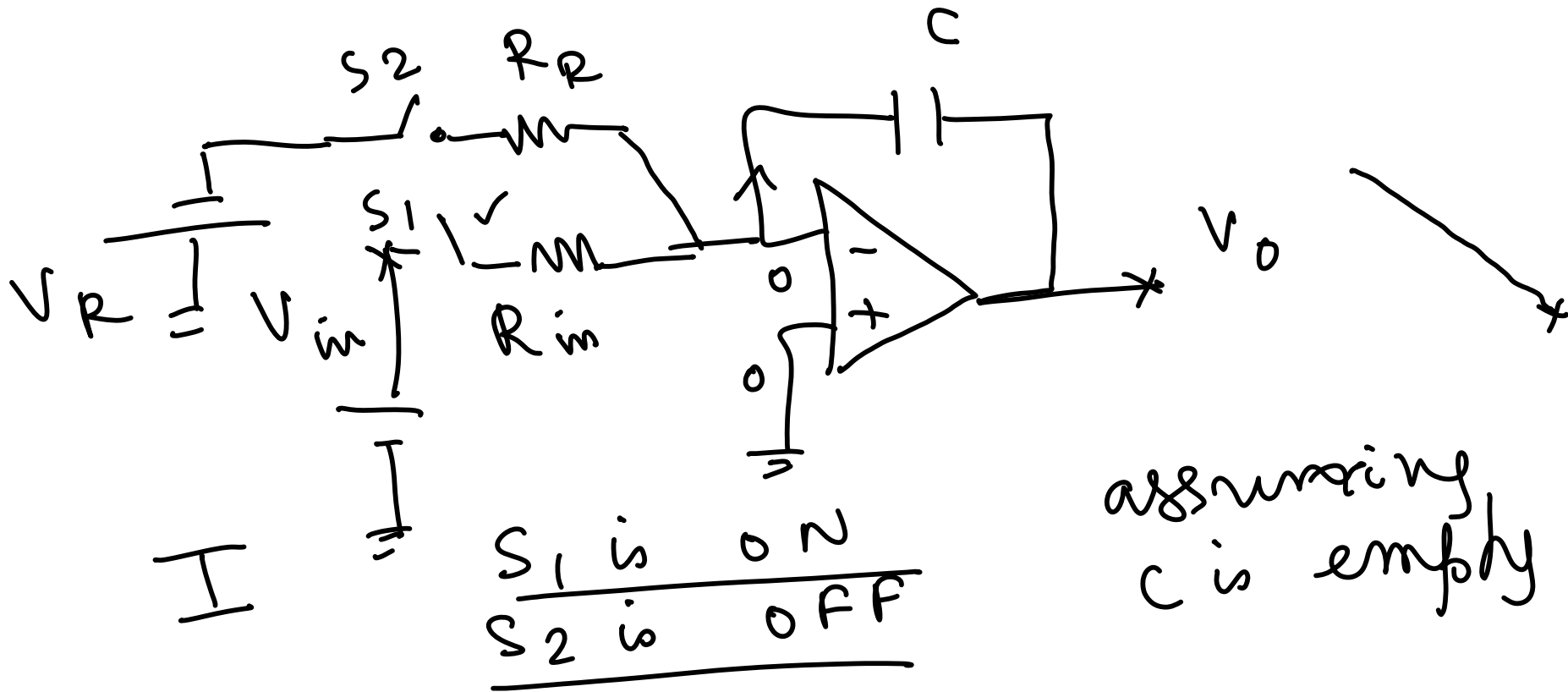
LSB gives us the minimum resolution one can get using this converter.

LSB value depends on the reference voltage

Types of Converters

- ① Dual Slope ADC
- ② Successive approximation ADC
- ③ Flash ADC
- ④ $\Sigma - D$ ADC

Dual slope ADC



when S_1 is ON
 I_{in} flows through the R_{in}
 -ve input is at zero V

$$I_{in} = \frac{V_{in}}{R_{in}} = \text{current through } C$$

i.e. the input source voltage charges the capacitor C at a constant rate

Capacitor vol will increase with time.

So output vol = capacitor vol.

Capacitor
w/

$$Q = it$$

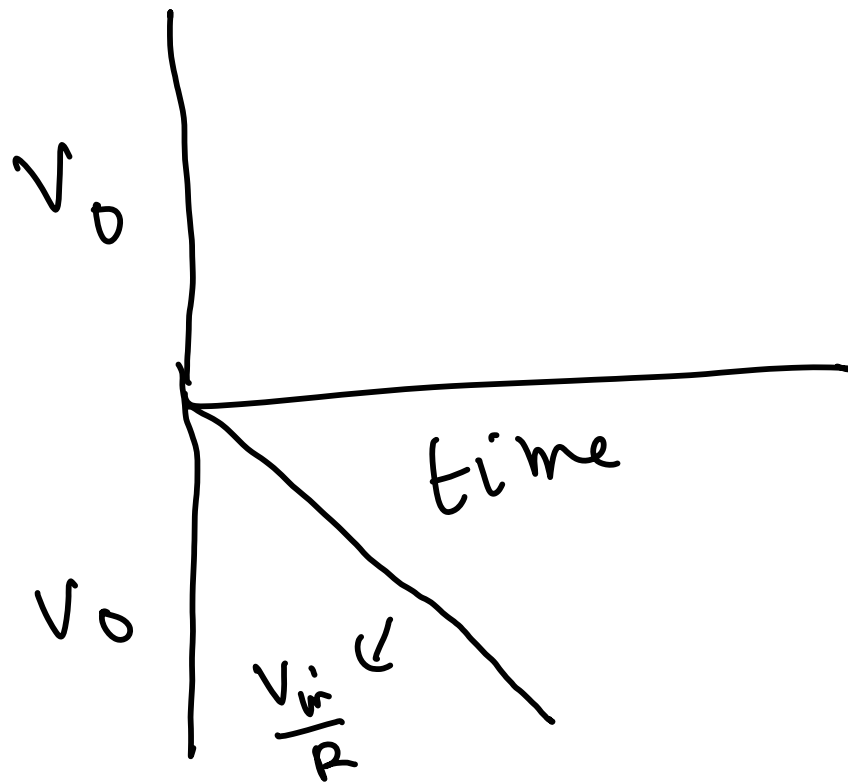
$$Q = cV$$

$$it = cV$$

$$V_o = \frac{c \cdot t}{c}$$

$$i = \frac{V_{in}}{R_{in}}$$

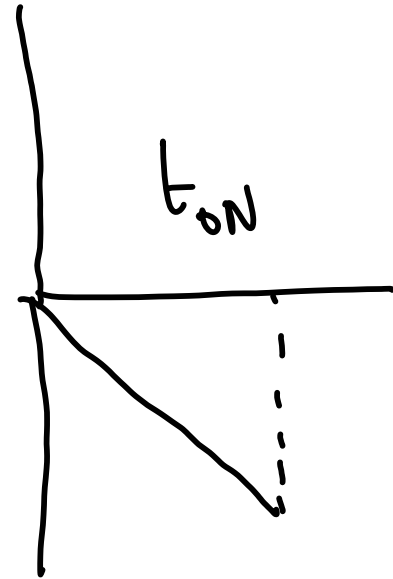
$$V_o = \frac{V_{in} \times t}{R_{in} \cdot c}$$



→ output w/

Due to of amp inversion

$$V_o = - \frac{V_{in} \times t}{R_{in} C}$$

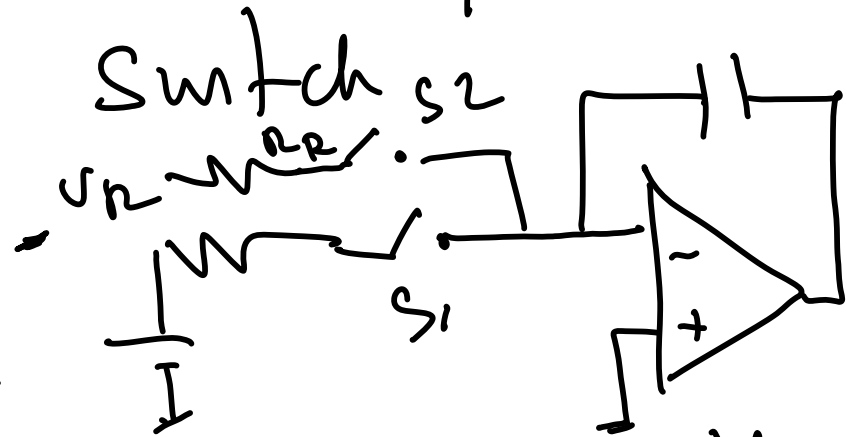


Keep S_1 ON only for a fixed time t_{ON}

After t_{ON} time OFF S_1

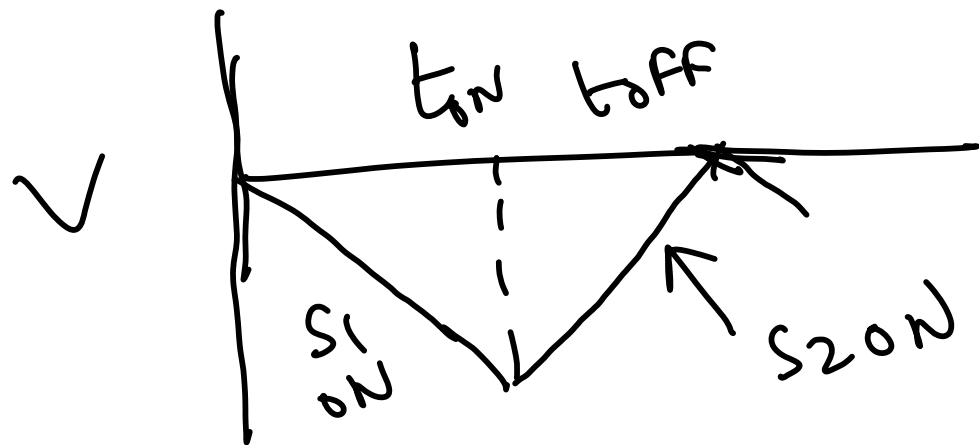
Switch ON S_2

Switch S_2 is connected to V_{Ref} through the Ref resistance R_{Ref}



The current through R_R is opp to that of R_{in}
 So capacitor C now discharges
 So output vol V_o will start coming down.

Keep S_2 ON so that V_o becomes zero after some time



Discharge equation

$$I_D = \frac{V_R}{R_R}$$

$$i t = C V$$

$$\frac{i t}{C} = V_0$$

Total charge delivered to C
when S_1 ON = $i t = \frac{V_{in} t_{ON}}{R_{in}}$

Total discharge
when S_2 ON = $\frac{V_R t_{OFF}}{R_R}$

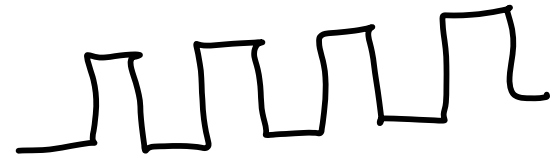
Total input charge = Total output charge

$$\frac{V_{in} t_{ON}}{R_{in}} = \frac{V_R t_{OFF}}{R_R}$$

$$R_{in} = R_R$$

$$V_{in} \xrightarrow{\text{fixed}} \frac{V_{in}}{V_R} = \frac{t_{OFF}}{t_{ON}} \xrightarrow{\text{fixed}}$$

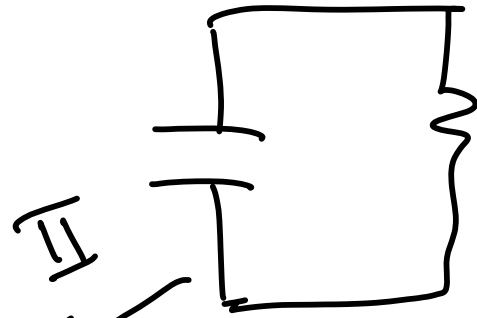
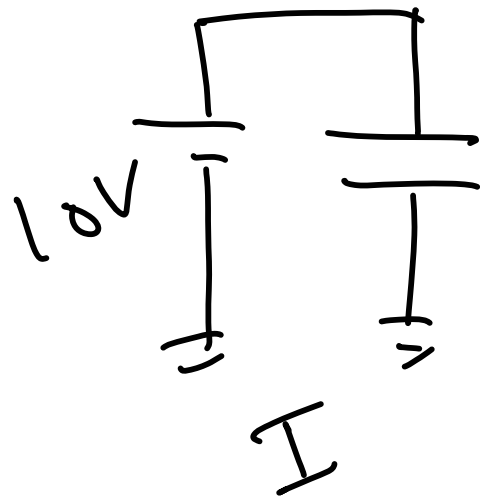
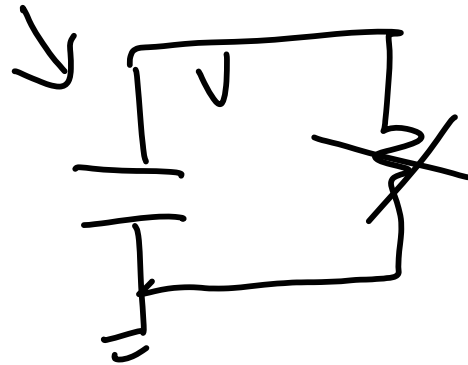
$$V_{in} \propto t_{OFF}$$



t_{OFF} period can be measured by counting the no. of pulses

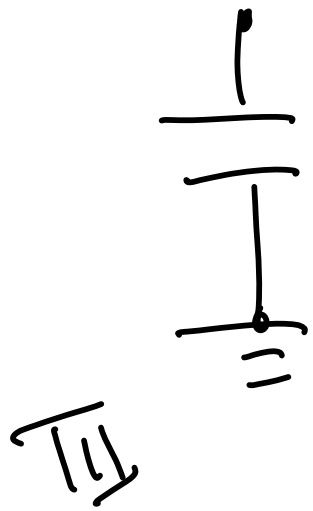
- ① The C is not appearing
in the final equation
So the long term drift of
the capacitor is not a issue
- ② The slow drift of the C
due to temp is not a
issue. Because t_{ON} and
 t_{OFF} are in milli seconds

③ The dielectric absorption of the capacitor is a major issue



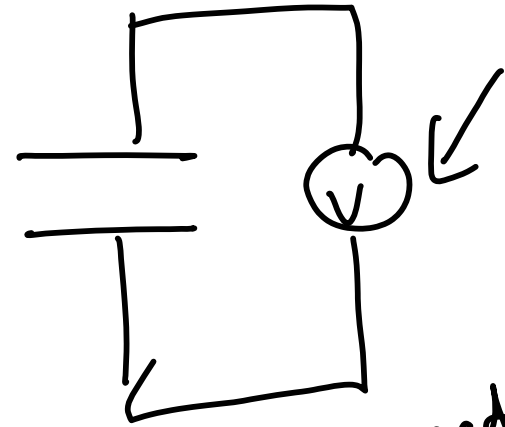
1 or 2 Ω
for few secs

Allow the cap to discharge fully



remove
the load

IV



now connect
a high impedance
multimeter (volt)

with time V is increasing
ie some of the charge re appears
in the cap
This is called dielectric absorption

For electrolytic cap $\bar{\tau}$ is about 10%

For ceramic 1-2%

For plastic film $\bar{\tau}$ is less
i.e. 0.01% to 0.1%



① assuming V_{in} large

Then c will charge to high vol

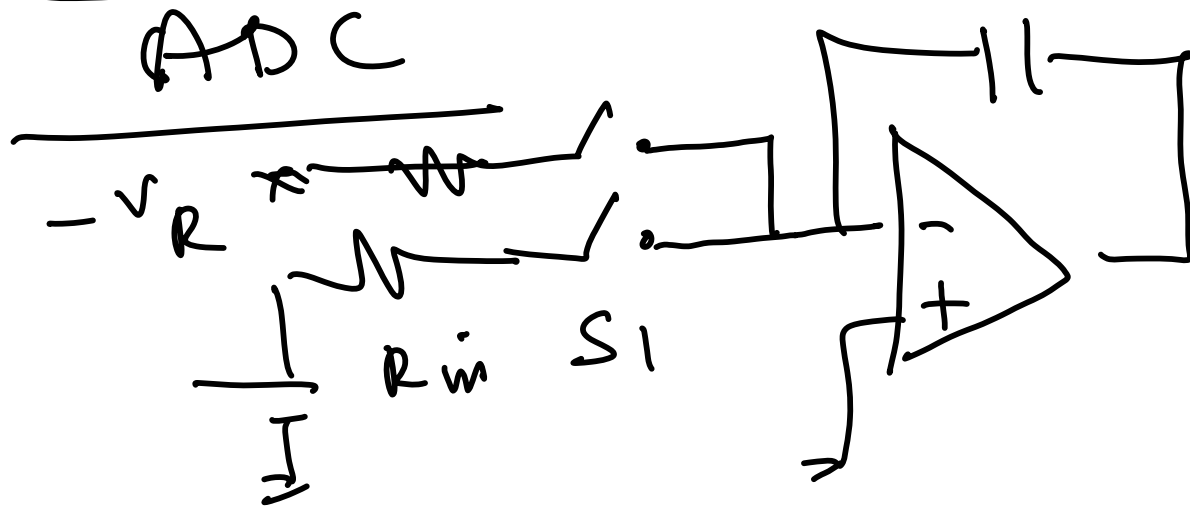
Then S_2 discharges C quickly
If the input vol is changed to
a lower value say from 1V to
10mV or so

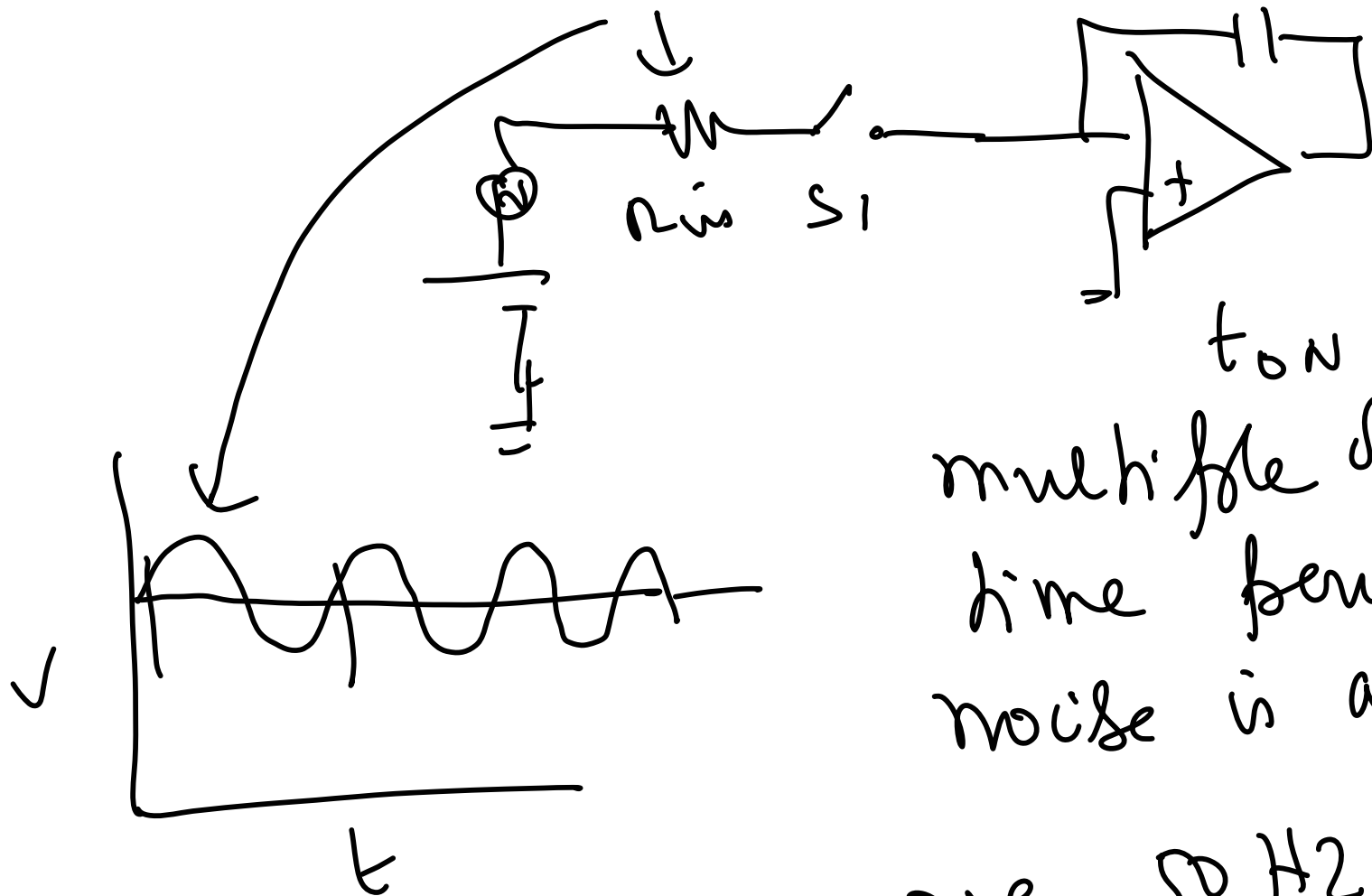
no when S_1 is on this 10mV
will deliver small charge to C
but in addition part of the
earlier charge also part re-appears
due to di-electric absorption

This will make our measurement
to go wrong.

So it is essential that c is
having very low dielectric
absorption.

Noise issues in dual slope





t_{ON} is integral
 multiple of noise
 time period then
 noise is averaged out

To remove 50 Hz noise
 $t_{ON} = 60 \text{ ms}$ (3 cycle time)

Then averaging is done for
3 ac cycles

The average charge due to
ac comp is zero

The ADC is not sensitive
to input noise.

This is the merit of the
Dual Slope ADC

Dis - advantage

Conversion is very slow

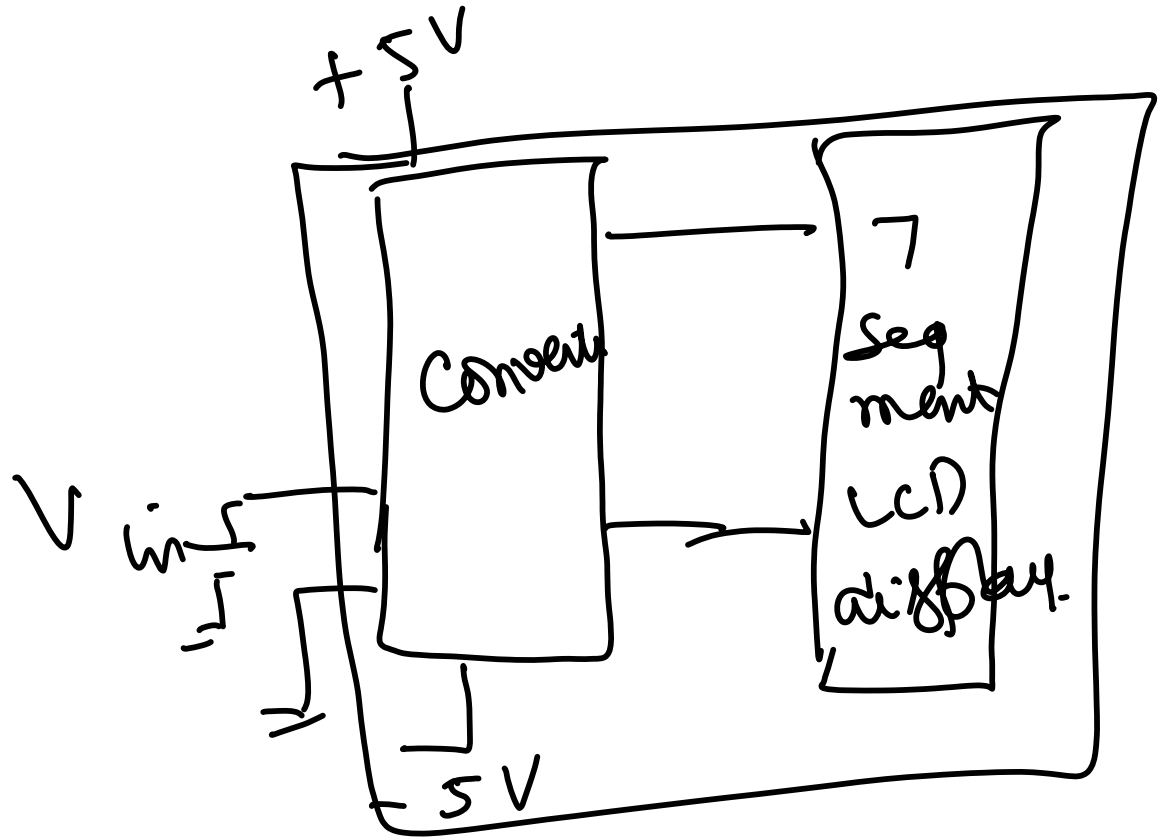
Advantage

It is sensitive to noise

This types of converters are used for LCD display etc

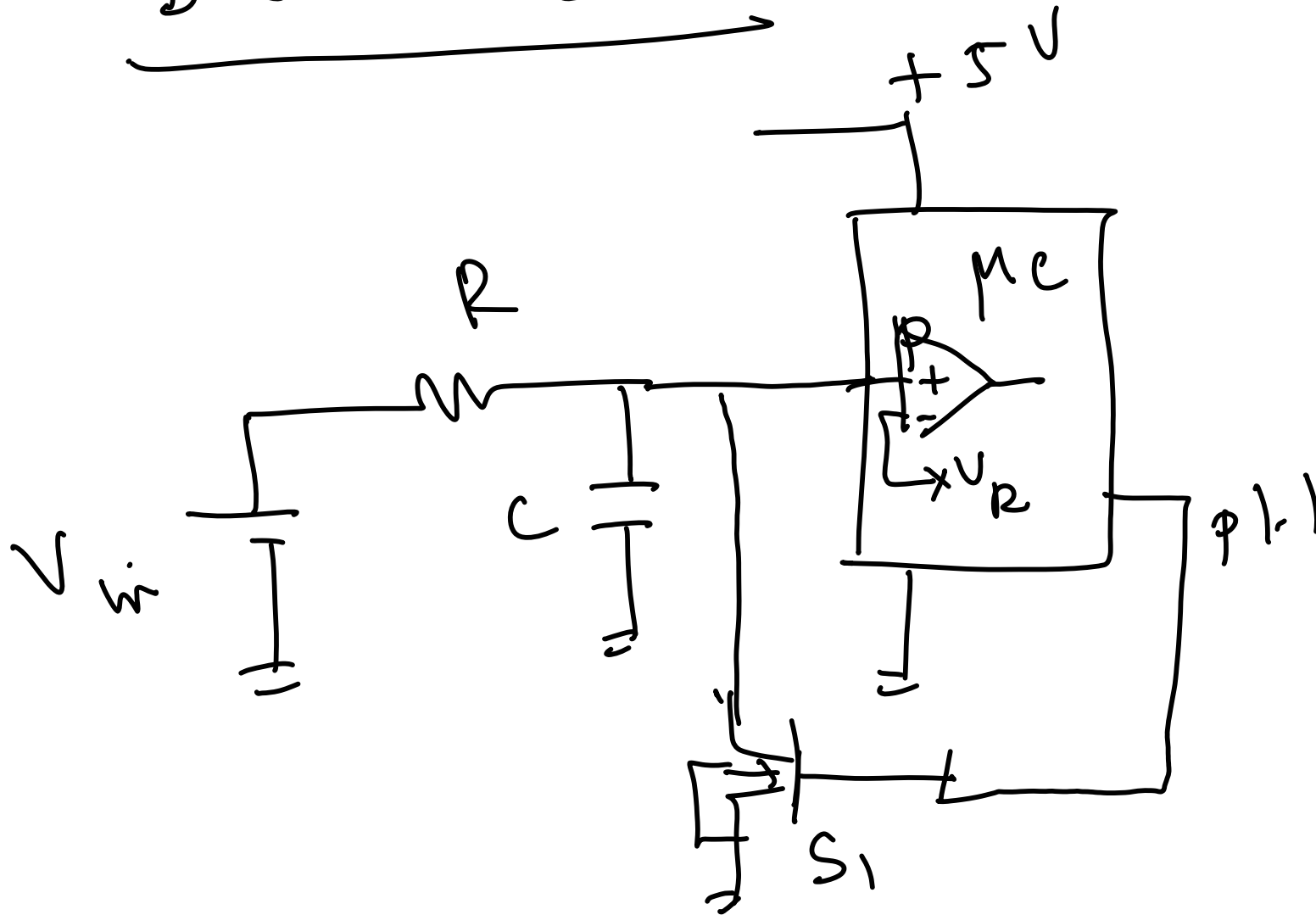
At the max 8 to 10 conversions are possible

All displays use this type
of converters.



Microprocessor/micro Controller

bases to ADC



Discharge C by switching on S_1

Then start the timer in μC
and simultaneously switch off S_1

Allow this OFF condition
for some time

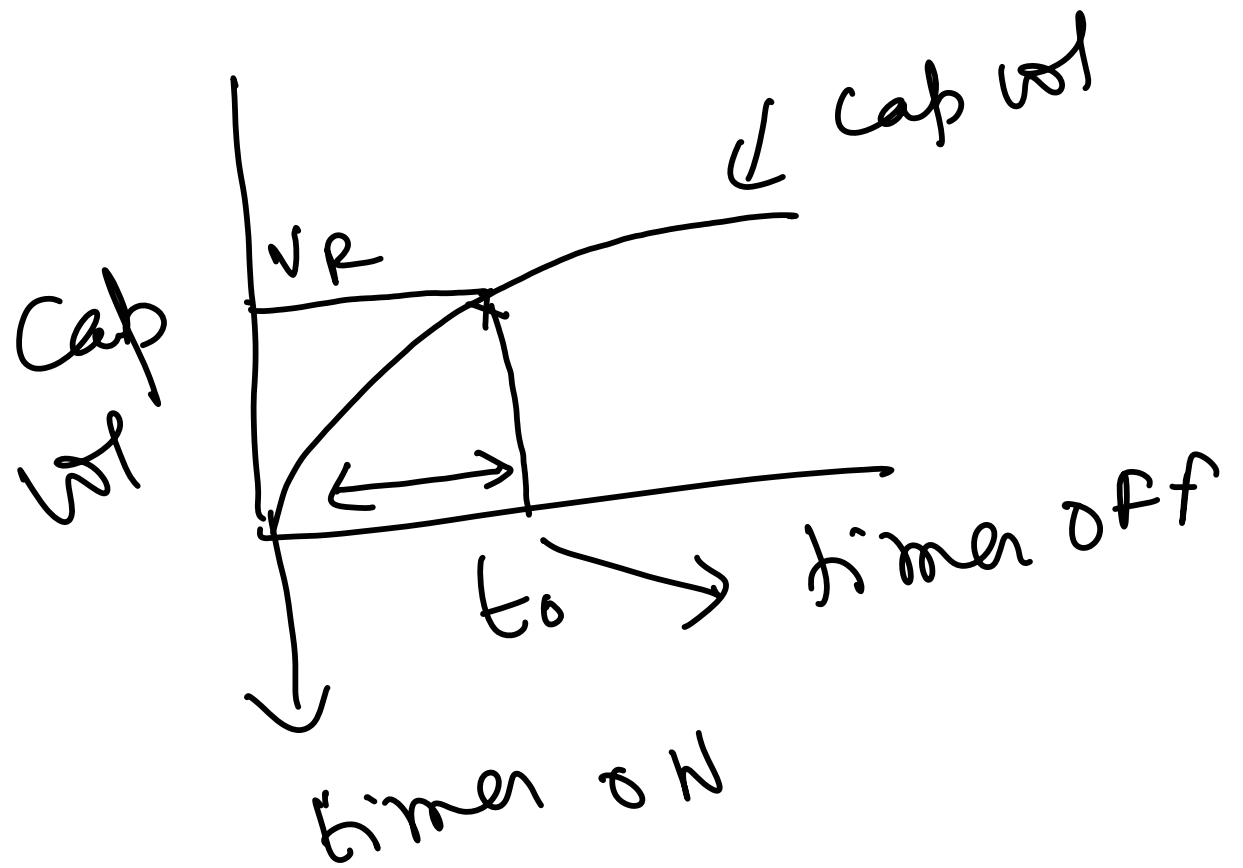
Now the capacitor C ^{voltage} will
slowly increase.

The comparator in the μC
will change state once

the capacitor voltage goes above reference fixed inside the μC .

once voltage change in the comparator occurs the timer is stopped.

The time period can be used to calculate the V_{in}



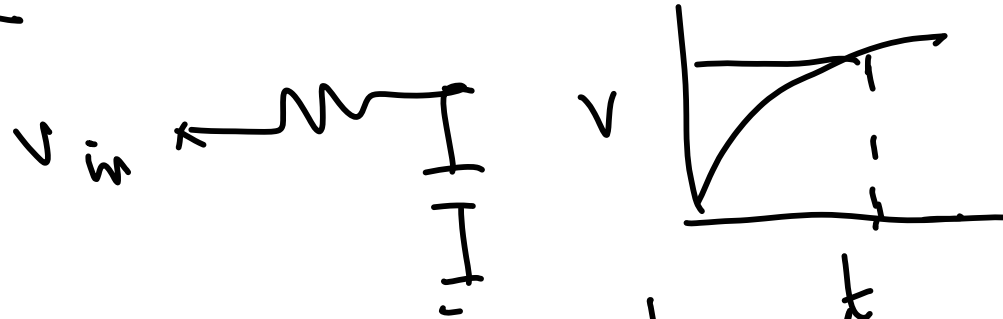
Period t_0
 gives you the
 This is not
 converter.

timer on
 input voltage
 a dual slope

① The capacitor drift
Resistor drift
all will give error

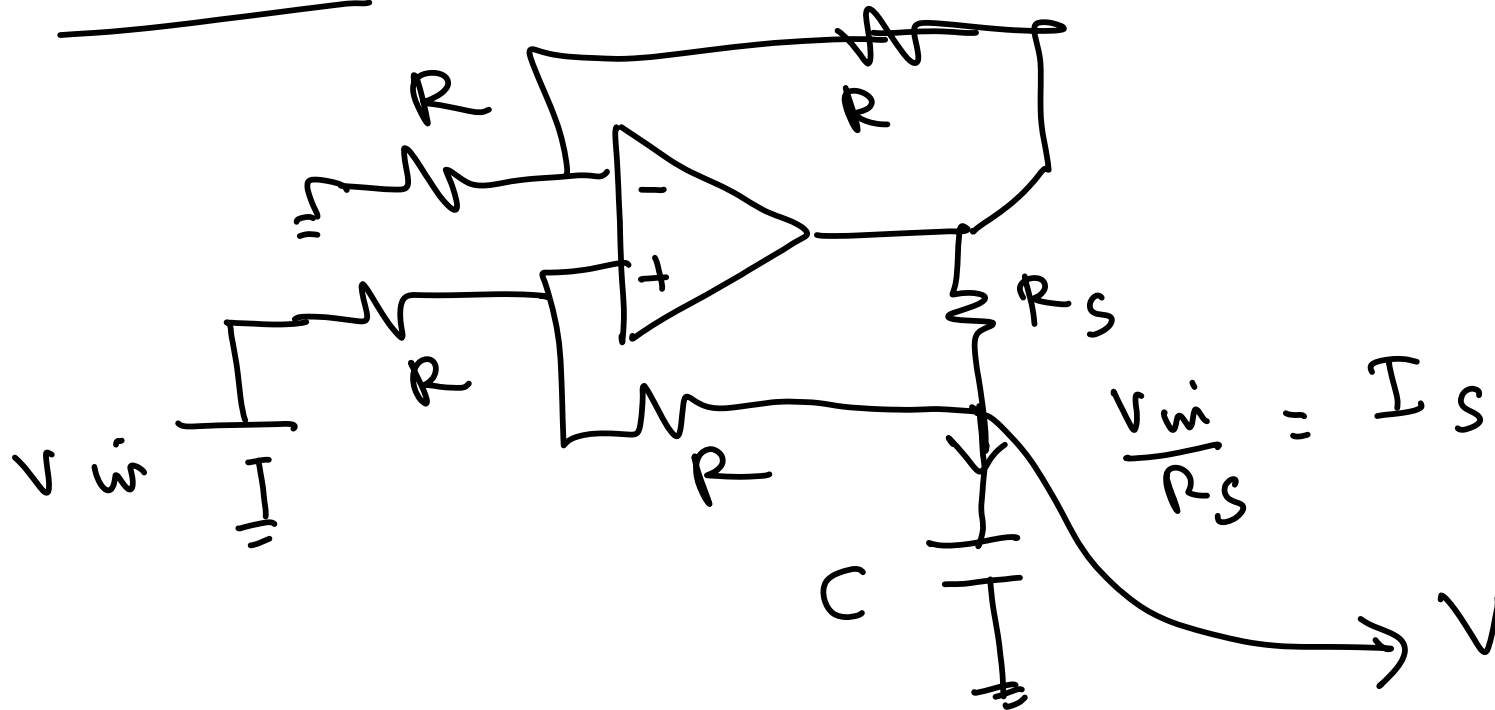
② The noise averaging
benefit is available.
but not completely because
 T_{ON} is not fixed. It
changes with V_{in}
This converter can be improved
by modifying the circuit.

Lecture no: 36



Constant current source based

ODC



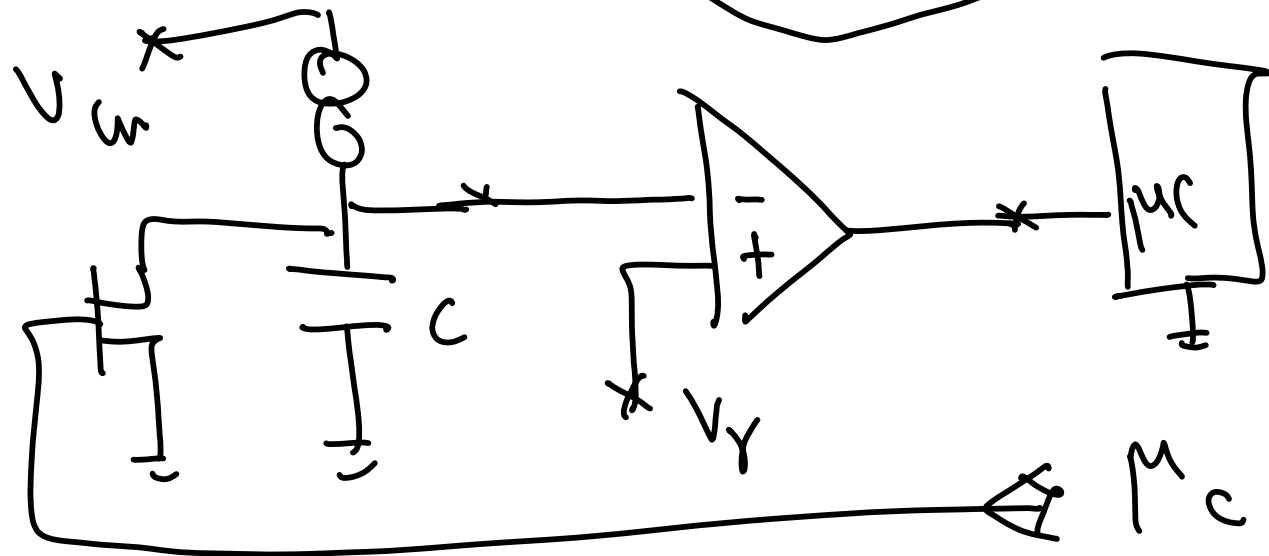
The capacitor C charges linearly
 with time

$$C V = i t$$

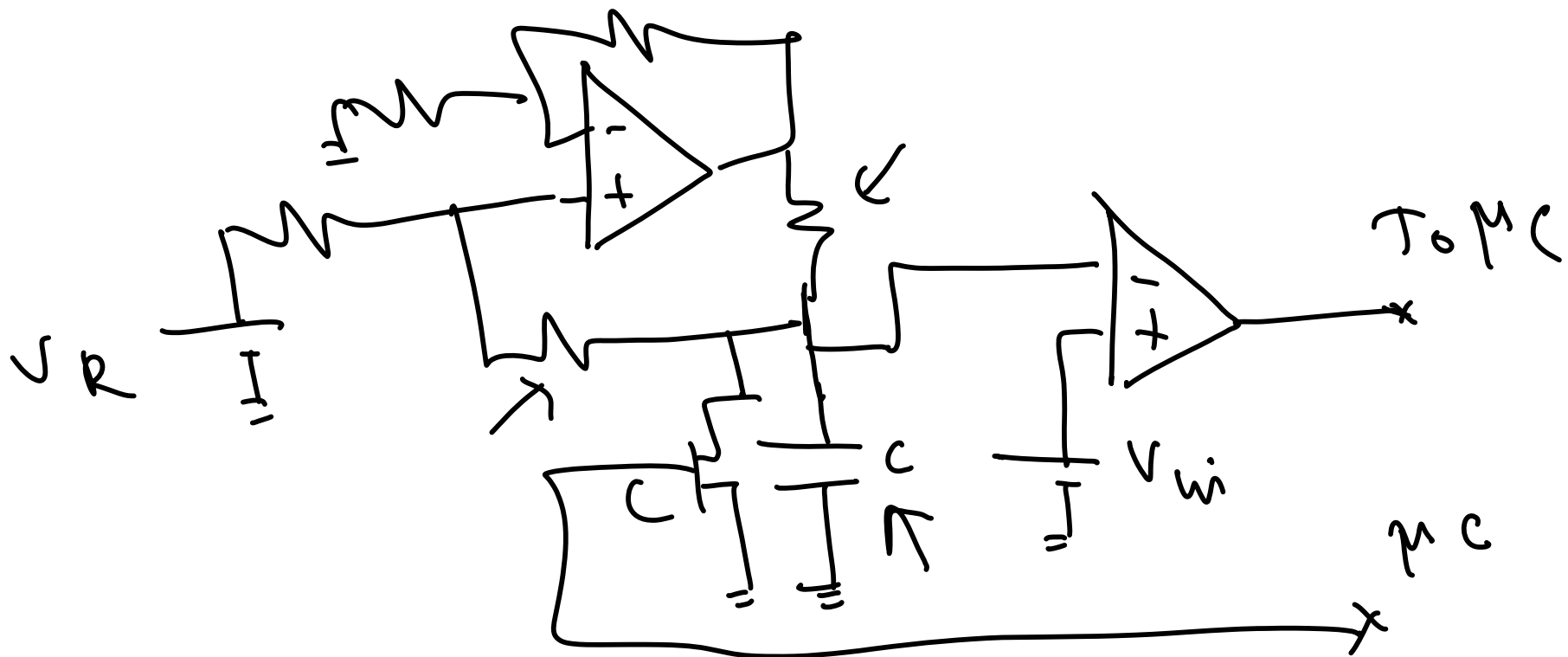
$$V = \frac{i t}{C} = \frac{V_{in} t}{R_s C}$$

V_{in} is the vol to be
 measured

Then $V_{in} = \frac{V R_s C}{t}$



- ① First discharge C
After discharge start the timer
- ② Wait for Comparator roll over
Then Stop the timer



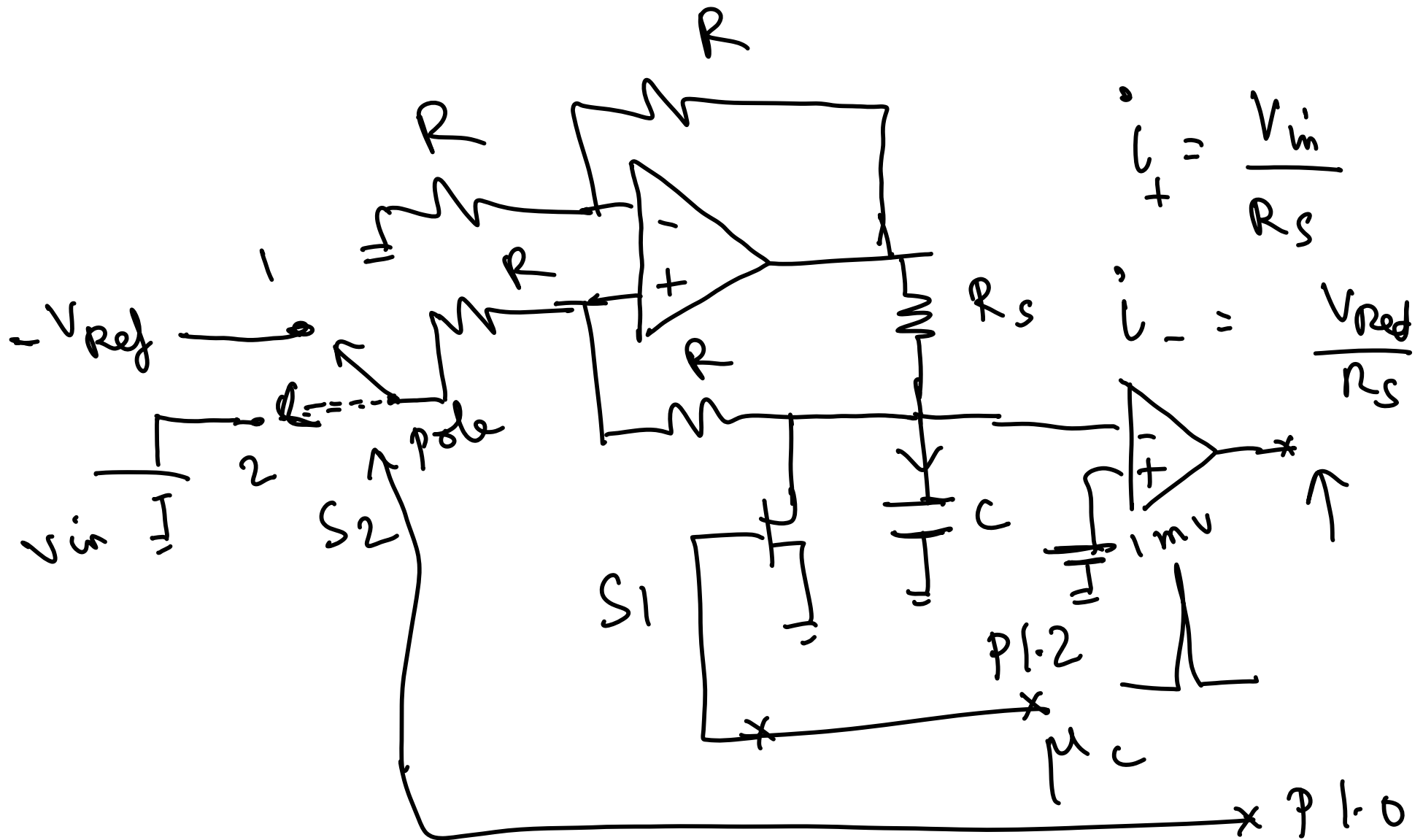
$$i t = C V_{in}$$

$$V_{in} = \frac{i(t)}{C}$$

$$V_{in} \propto t$$

- ① discharge C and start the timer
- ② wait for comparator roll over and stop the timer

Dual Slope Converter with μc



① Discharge C using the switch S_1

② Allow the switch S_2 to connect to V_{in}

③ Keep the switch S_2 for a fixed time 't' or
$$V = \frac{it}{C} = \frac{V_{in} \times t_{ON}}{R_{SC} C}$$

④ Now change the switch S_2 to $-V_{ref}$

This discharges the capacitor C
 Time required
 discharge

to
 can be computed
 $it = CV$

$$\frac{V_{ref} \times t_{dis}}{R/s \times \phi}$$

$$= V$$

$$= \frac{V_{in} \times t_{on}}{R/s \times \phi}$$

$$V_{ref} \times t_{dis}$$

$$= V_{in} t_{on}$$

$$\frac{V_{ref} \times t_{dis}}{t_{on}}$$

$$= V_{in}$$



① This is very accurate

② noise averaging can be controlled \rightarrow we are fixing the on time

Select the on time in multiples

of noise frequency

To remove 10dB noise t_{ON} can be in multiples of 20ms.

③ Low dielectric capacitor must be used

④ Discharge can be checked
by the μc using the
comparator

Advantage

① Good noise rejection

Dis advantage

①

It is very slow

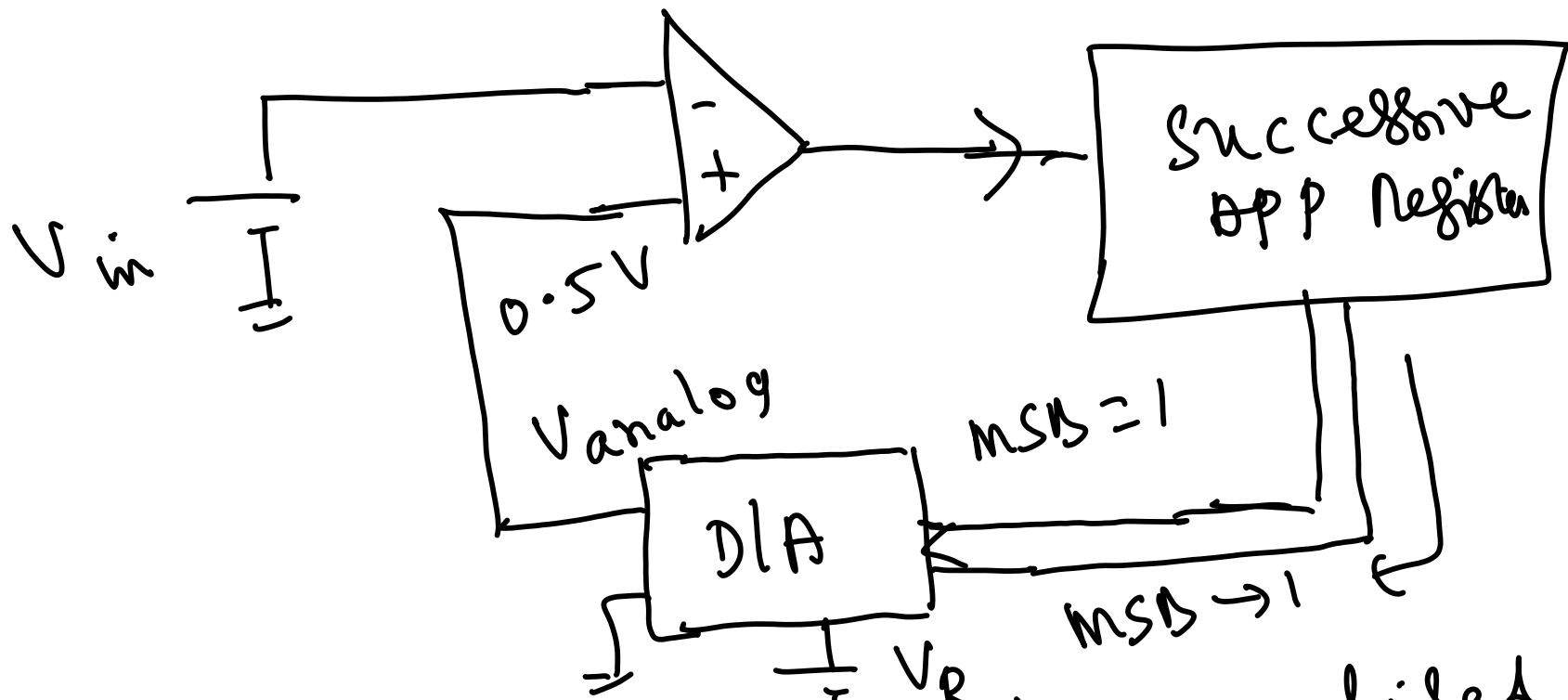
②

5 to 6 conversions
possible per sec
only

Successive approximation

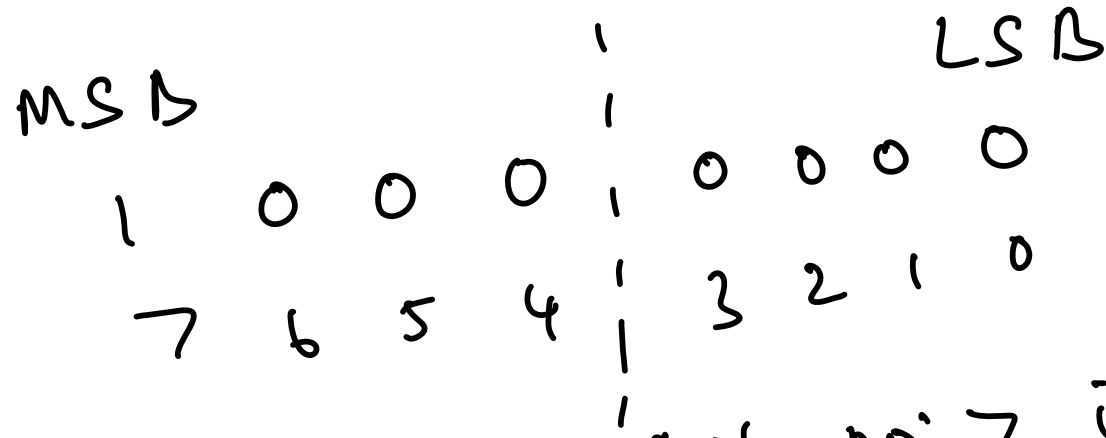
Adv ADC
① Very Fast

dis-adv
② noise rejection is very poor



ADC
 a
 Digital to analog converter
 is realised using

For 8 bit converter



- ① Keep MSB i.e. bit no. 7 is high
all the other bits 0-6 are low
- ② The D/A converter responds
for this by outputting its
analog voltage

③ If the DAC $V_R = 1V$

Then $V_0 = 0.5V$

$$V_0 \text{ of DAC} = \frac{\text{Digital Value} \times V_R}{2^n}$$

$$= \frac{128 \times 1}{256} = 0.5$$

④ If the input $V_{in} > 0.5V$
Then comparator output is zero

⑤ Now SAR it's next trial
Since there is no change
in the comparator output

② The MSB i.e. bit 7 is kept as it is at 1
Then bit 6 is kept 1
and other bits i.e. 0-5 are kept low
Now bit 6 and 7 are high

③ DAC gives out
 $0.5 + 0.25 \rightarrow 0.75V$
↑ bit 7 ↓ bit 6

④ Now the comparator output i.e. goes high chases its

if the input is $> 0.75V$
 it goes low if $V_{in} < 0.75V$
 Then bit 7, 6 are kept as one
 bit 7 is kept as 1
 bit 6 is put back to zero

Third trial

Here bit 5 is kept as 1
 bits 0-4 are kept 0

Now DAC \rightarrow

7	6	5	0	0.75
0.5	0.25	0.125		.12
				0.875

 $\rightarrow 0.875$

Now the comparator goes
high if it is < 0.875

like this

8 trials are made

In each trial if the comparator

goes up
as zero

that bit is put back
otherwise it is left as

one

By this at the end of
eight trial the converted
digital output is ready.

It needs only eight trials
to get the conversion completed

For example

If 1ms is required for
one conversion

Then only 8ms is required
to complete the conversion

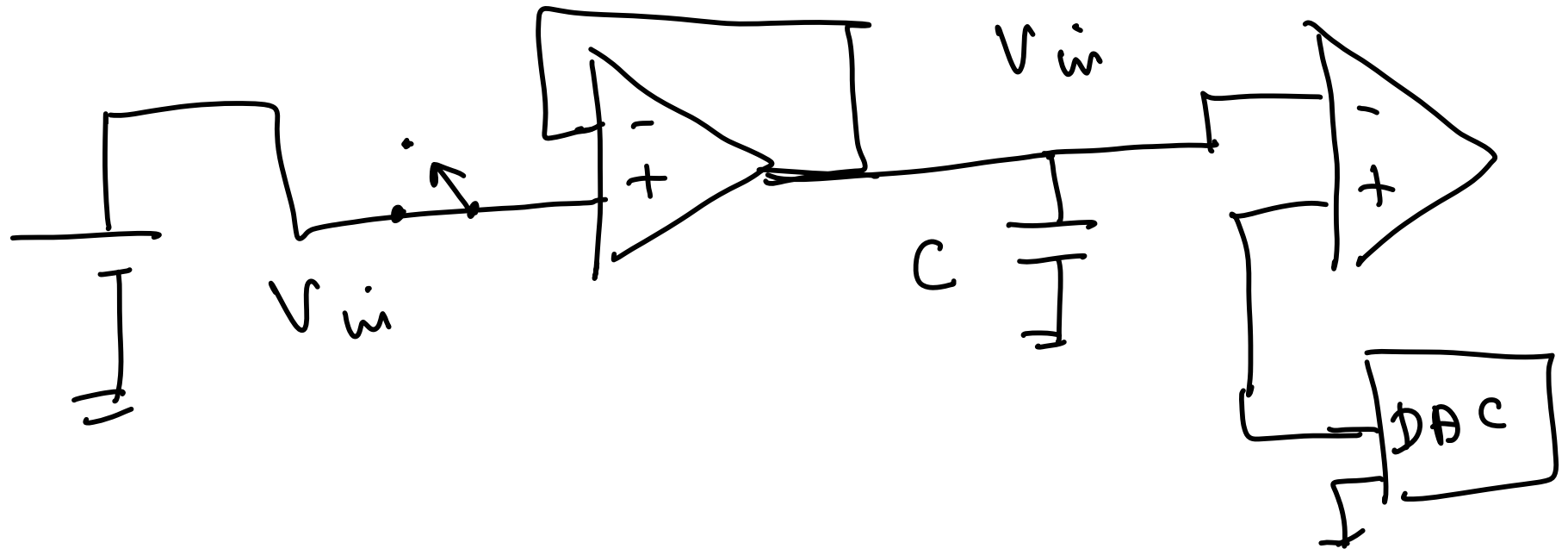
So it is very fast

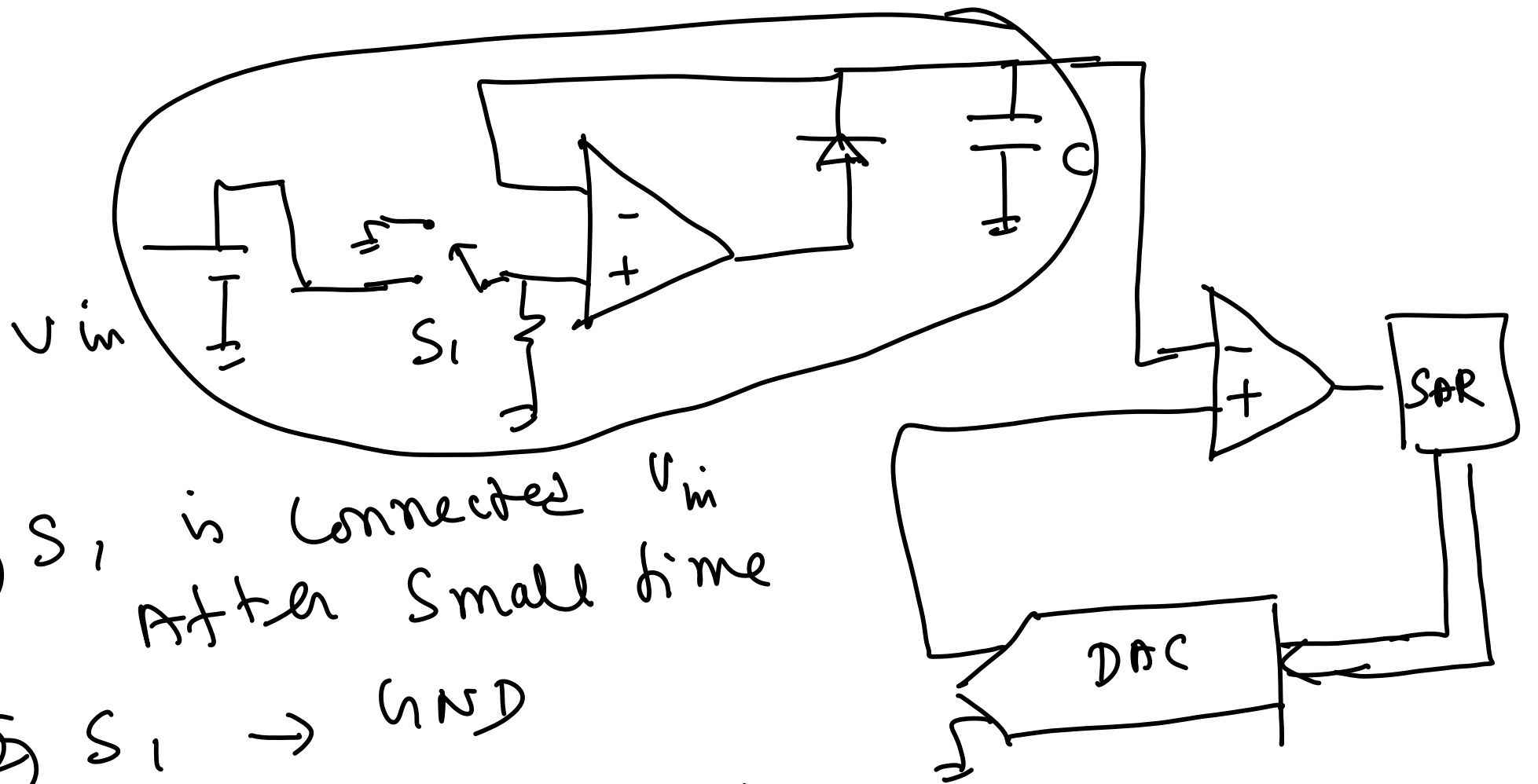
Important

This is valid i.e.
Converted output is valid only
if the input voltage is
constant during the conversion time

If the V_{in} changes
during $(t \times 8)$ period
then result is wrong.

How to keep the
input vol constant?
Latch the V_{in} using sample
and hold circuit





- ① S_1 is connected V_{in}
After small time
- ② $S_1 \rightarrow \text{GND}$
 V_{in} remains constant
- ③ Start the SAR

Conversion

This way of acquiring
the V_{in} to the ADC
is called Sample and hold
amplifiers

Sample and hold amplifiers
are commercially available

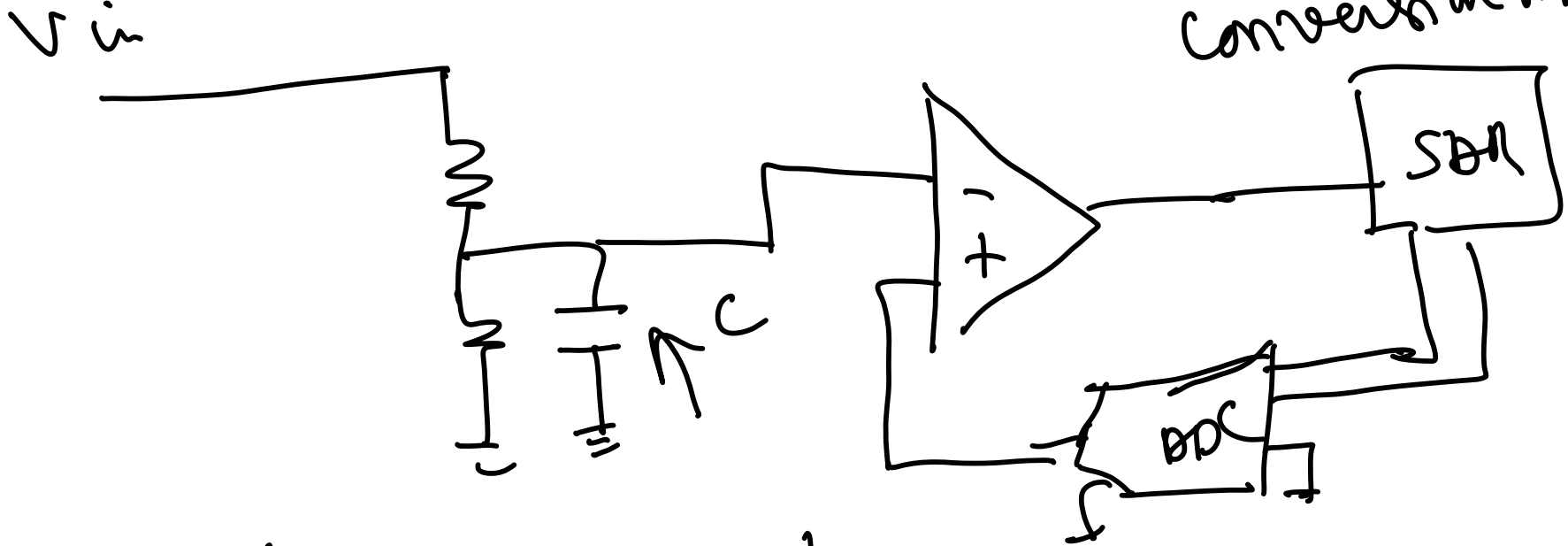
Total Conversion time

$$T_{ac} + T_{con} = T_{total}$$

If Sample and hold Amp is
(S H A)

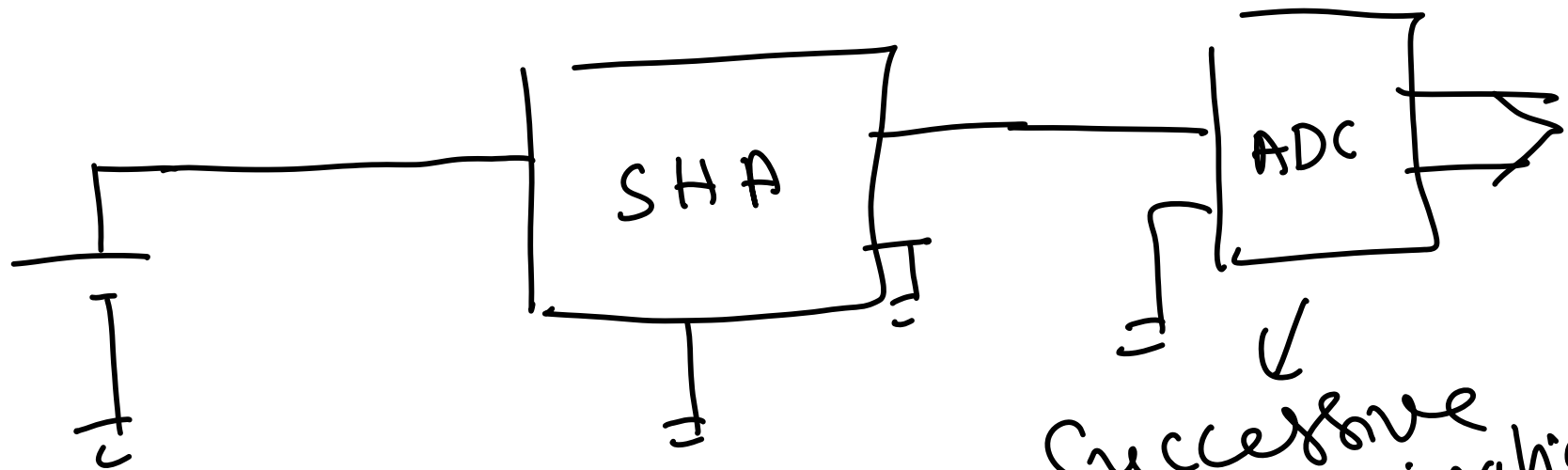
not used

Then $\Delta V_{in} \leq \frac{1}{2} \text{LSB}$
(during the conversion time)

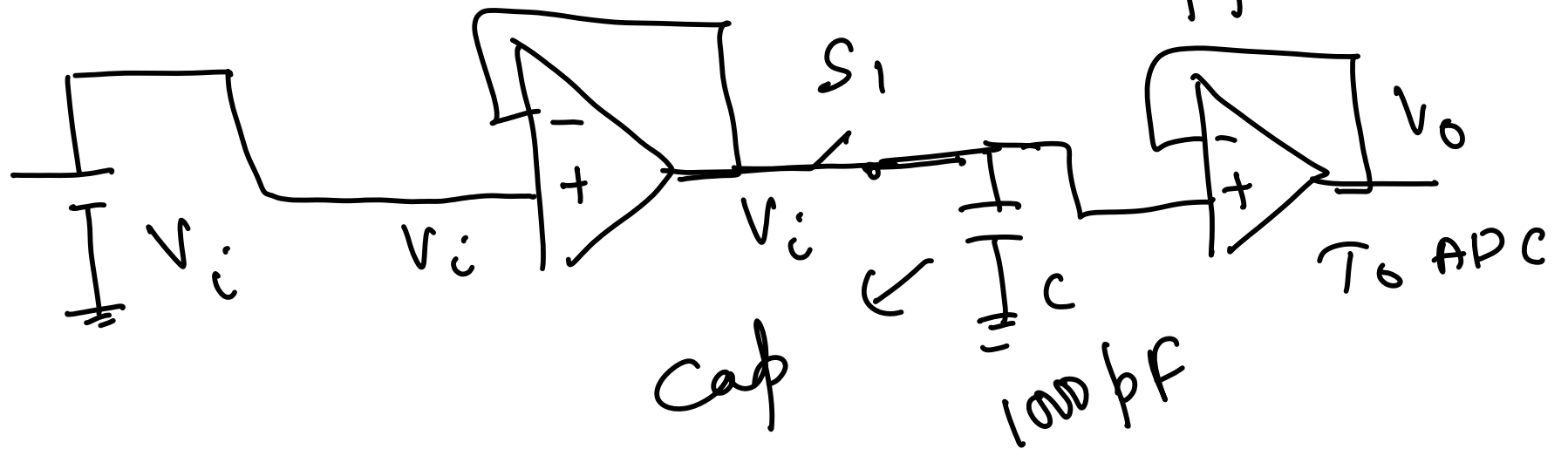


If C is very large
so that $\Delta V_{in} \leq \frac{1}{2} \text{LSB}$

Lecture no: 37



Successive approximation



When S_1 is closed

The cap charges up to V_i

Since R_o of the op amp is

very low

The charging is very fast

Normally it is the settling

time of the op amp

determines the charging time

is $< 1 \mu s$

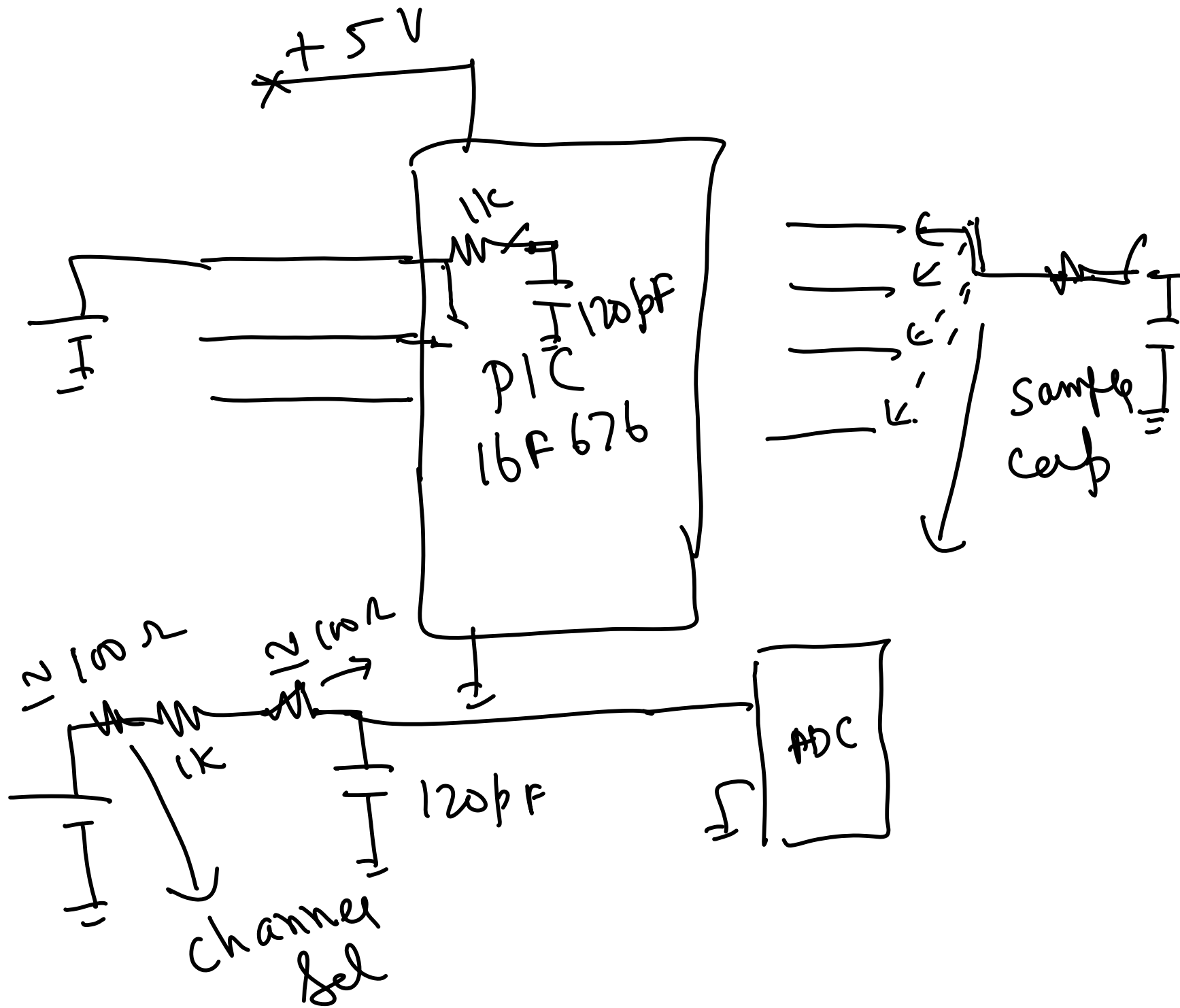
Then Switch of S₁

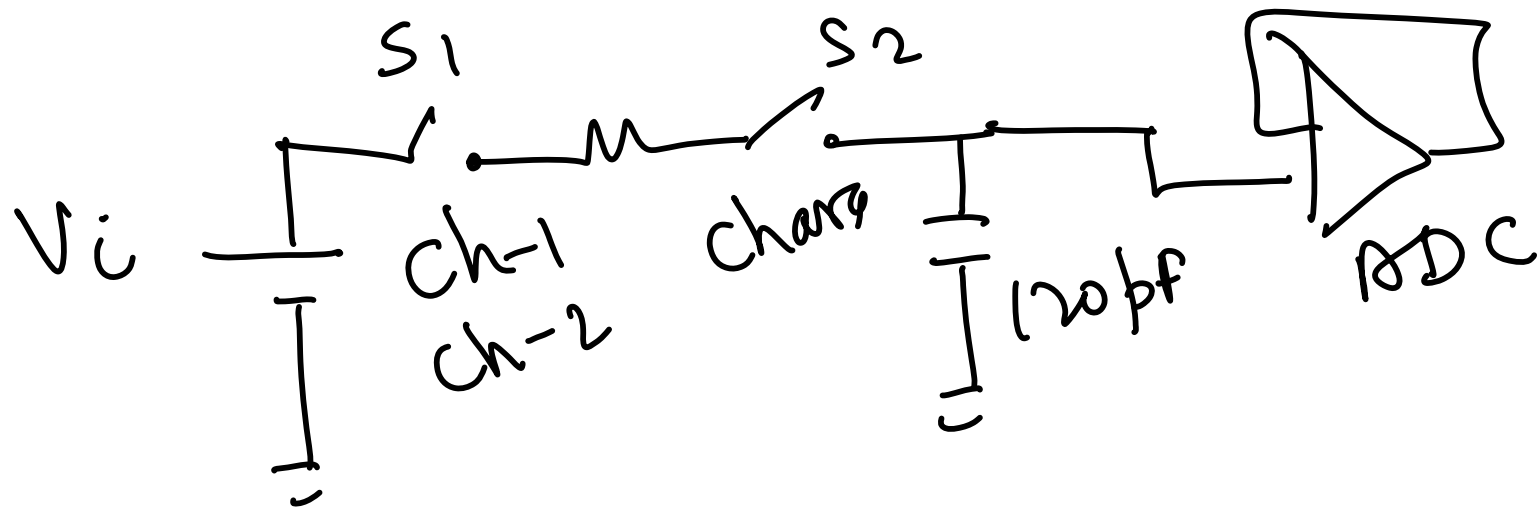
Now ADC Start Command
can be given.

ADC takes normally few
μs for conversion
During conversion the voltage
in the capacitor should not
decrease

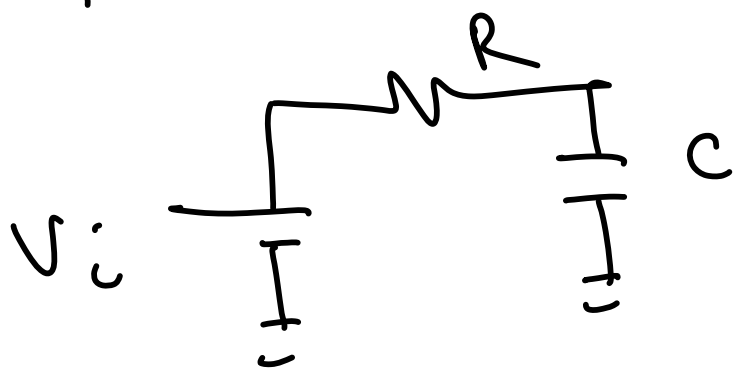
PIC MC

- ① In build 10 bit ADC
- ② Multiple Analog input channels
- ③ In build S+A





- ① S_1 and S_2 are on
- ② Allow the cap to charge
 up to $1/2$ LSB
- $$V = V_i e^{t/RC}$$



How much time
 I have to wait for charging
 up to $(V_i - 1/2 \text{ LSB})$

$$V = V_i e^{t/RC}$$

$$\frac{V}{V_i} = e^{t/RC}$$

$$\frac{2^{10} - 1/2 \text{ LSB}}{2^{10}} = e^{t/RC}$$

$$\frac{2^{10} \times 4}{1024}$$

$$\ln \left(\frac{1024 - 1/2}{1024} \right) = \frac{t}{RC}$$

$$\ln \left(1 - \frac{1}{2048} \right) = t/RC$$

$$\ln \left(\frac{1}{2048} \right) = t/RC$$

$$RC \ln \left(\frac{1}{2048} \right) = t$$

For $R = 1k$

$$C = 120 \text{ pF}$$

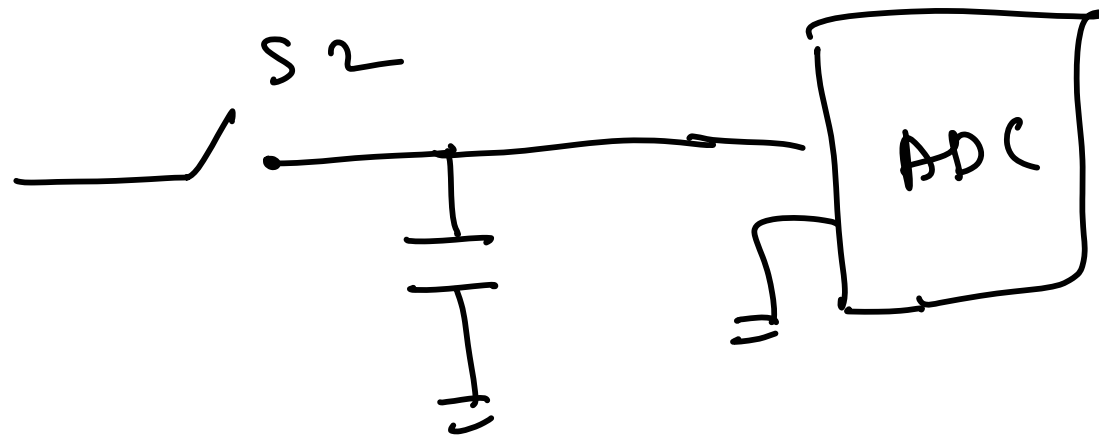
$$t = 20 \text{ MS}$$

③

After waiting for t secs
Start Conversion Command
is given to ADC

④

At this stage S_2 is
Switched off



In PIC MC

For 10 bit ADC it needs
 $10 + 1$ cycle time for
conversion.

The conversion is done
from MSB onwards
↓
1 1 1 1 1 1 1 1
↑
2nd 3rd
LSB
1 1

Minimum cycle time is $2\mu\text{s}$

For 10 bit complete conversion
wait for $11 \times 2 = 22\mu\text{s}$

SHA time + conversion time
 $20\mu\text{s}$ $22\mu\text{s}$

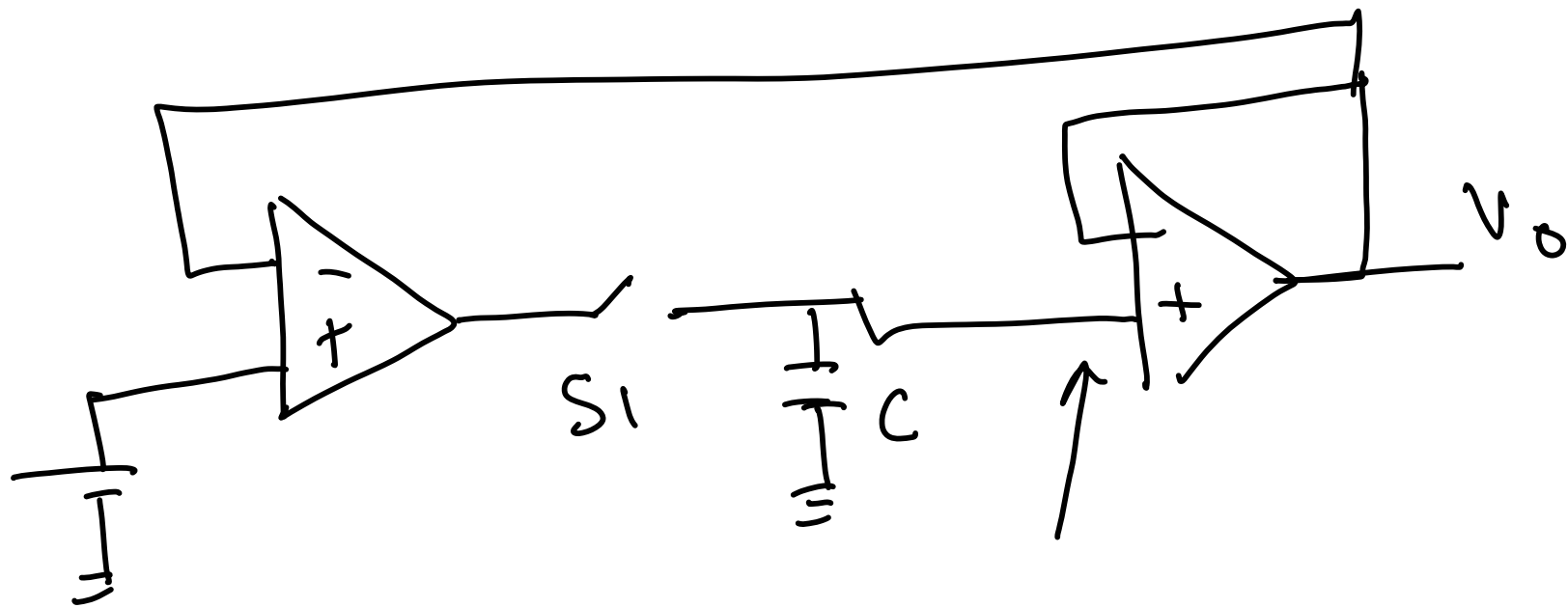
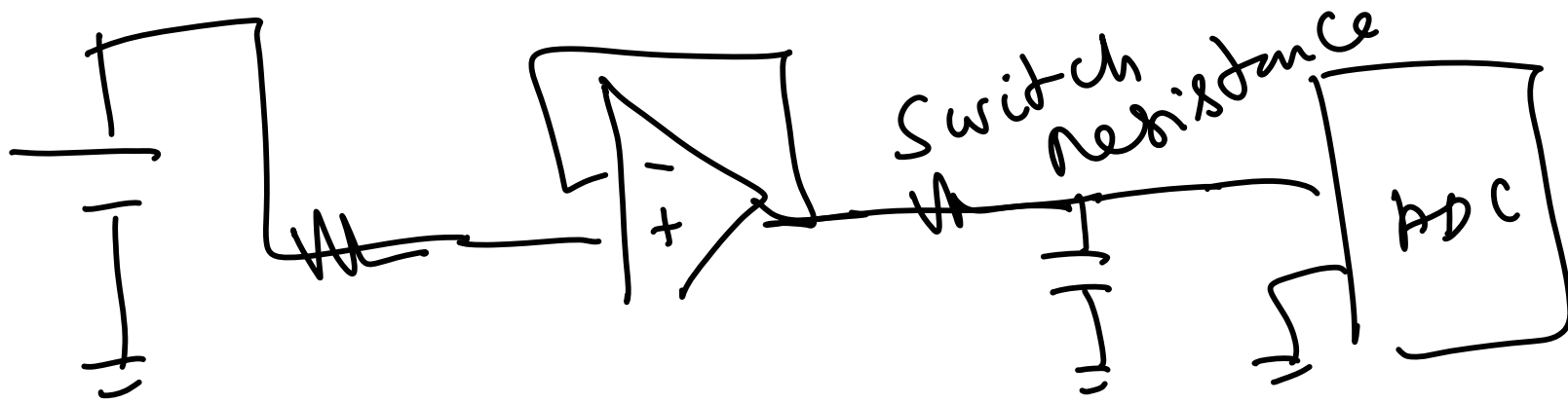
→ $42\mu\text{s}$

In actual case
we need to configuration of
channel

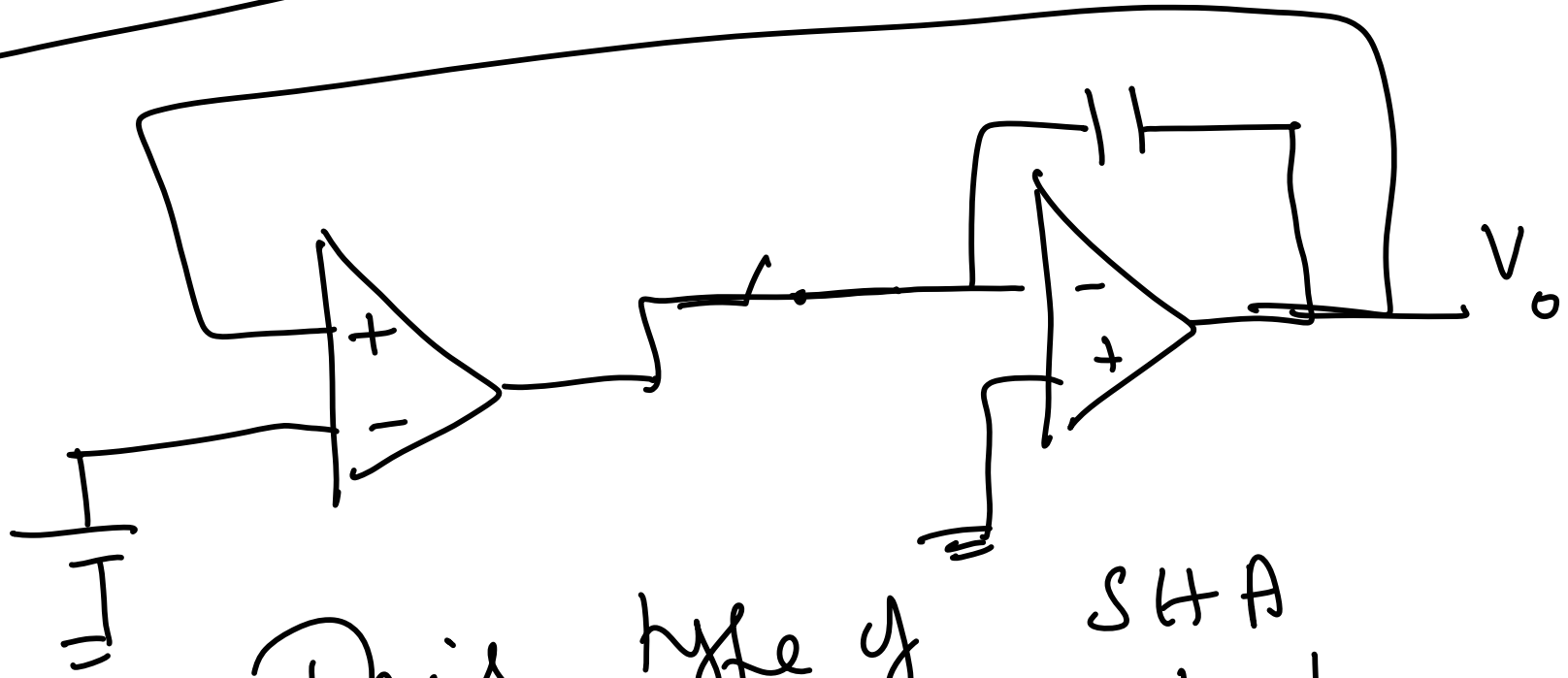
All the "setting" instructions
can take up to 10 μ S

① How to reduce the
Sampling time?

② How to reduce the
Conversion time of ADC

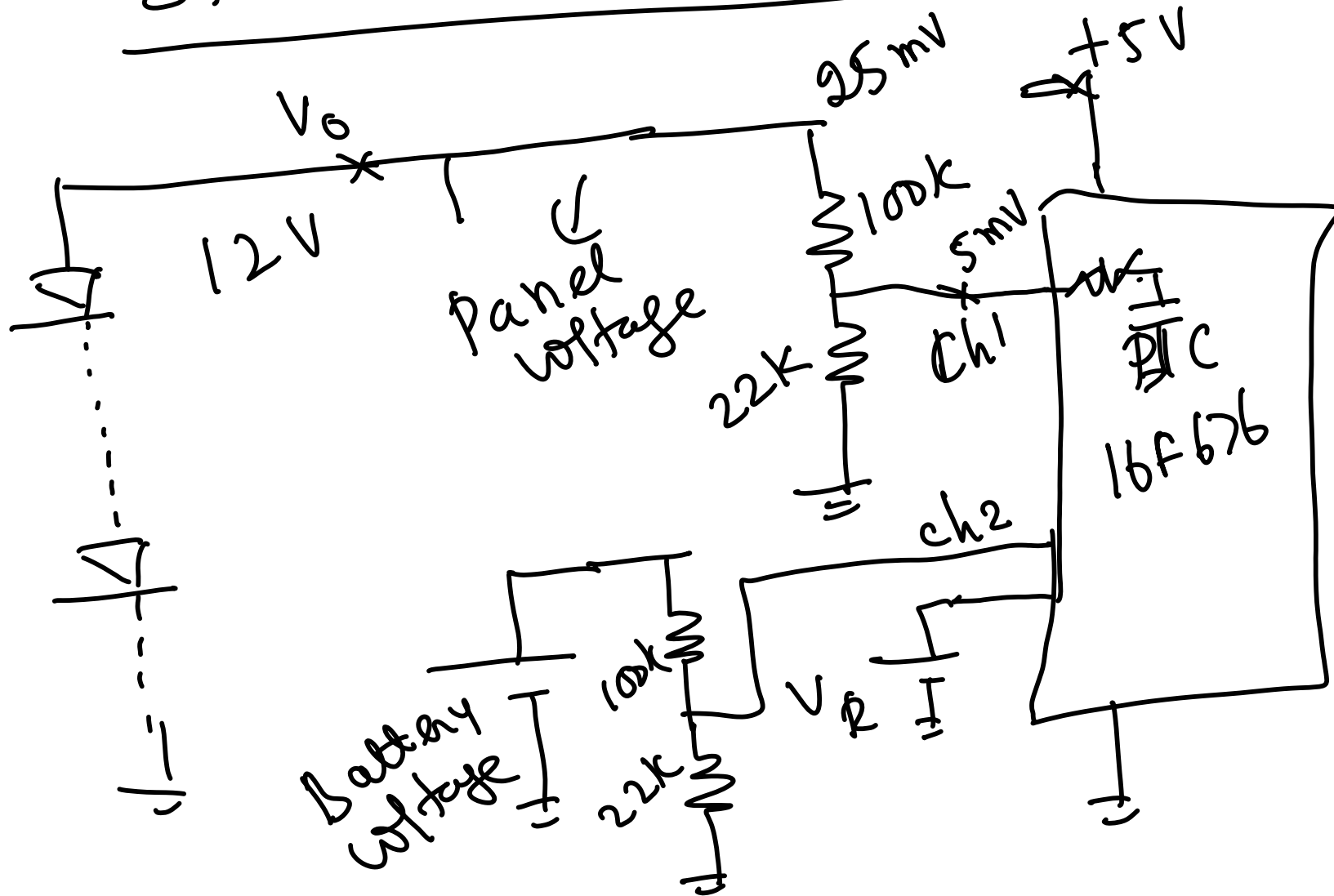


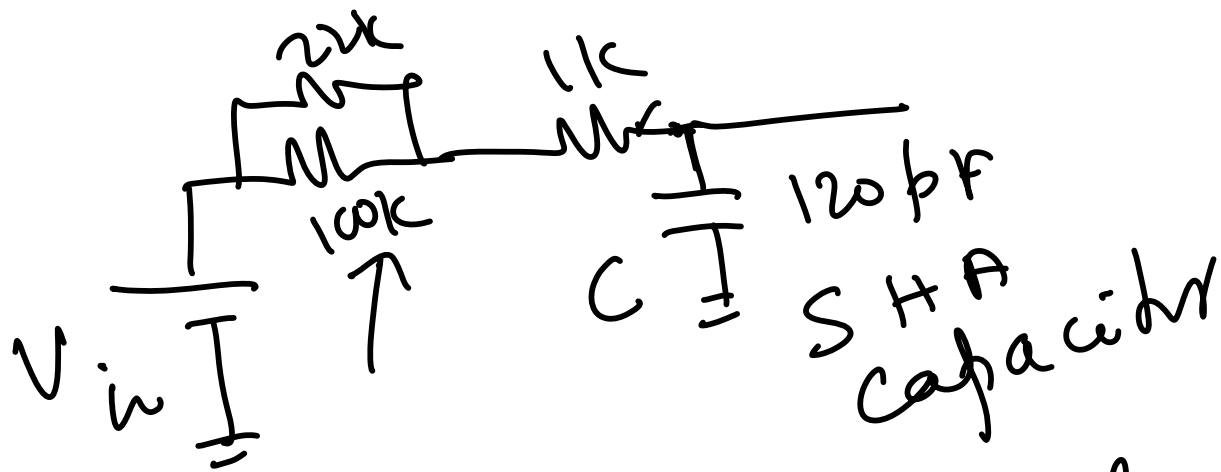
II nd type



This type of STT
will not ~~not~~ introduce
additional charge to the Cap

Solar cell based Street lighting

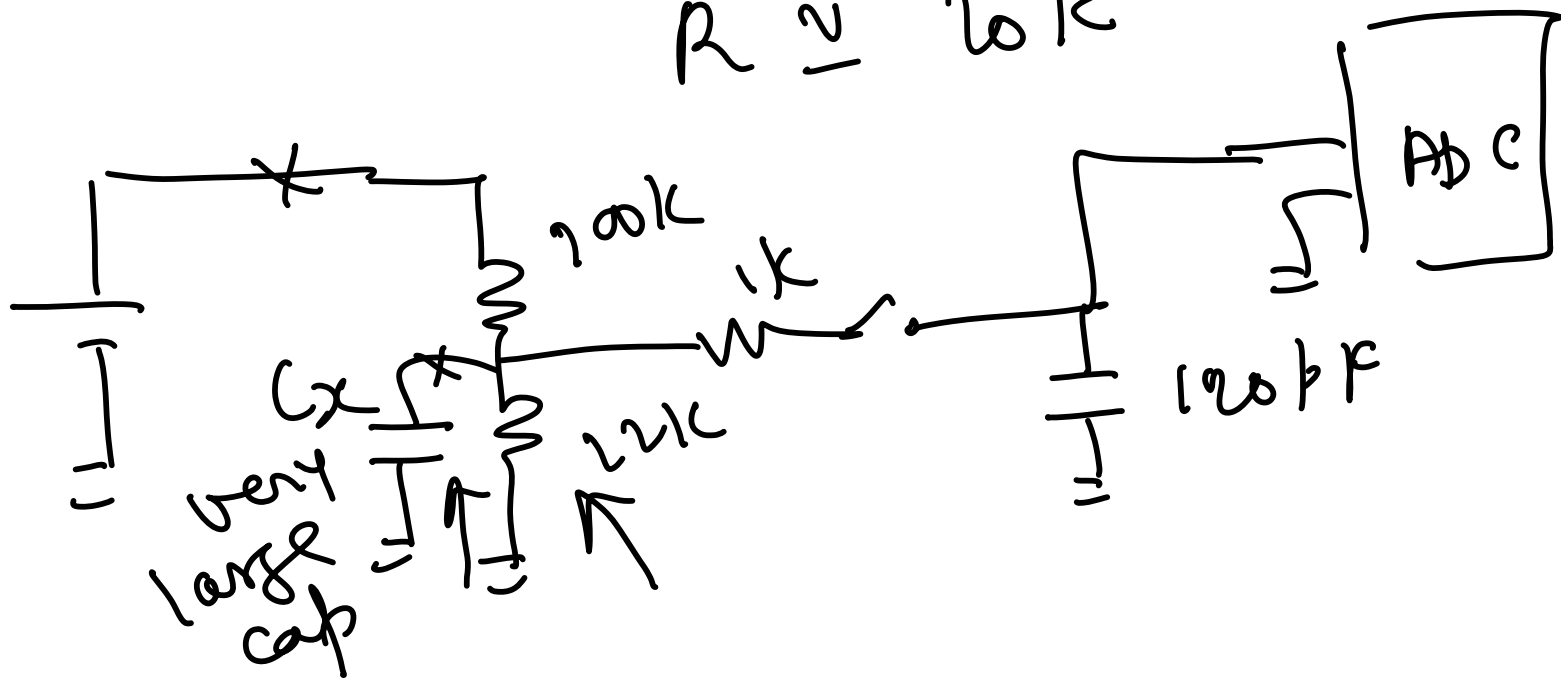


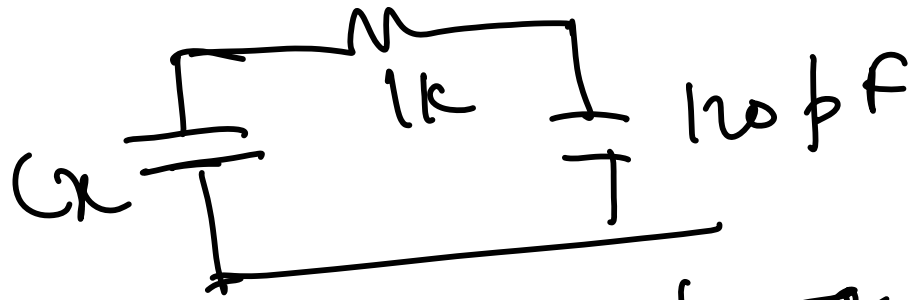


We have to wait for

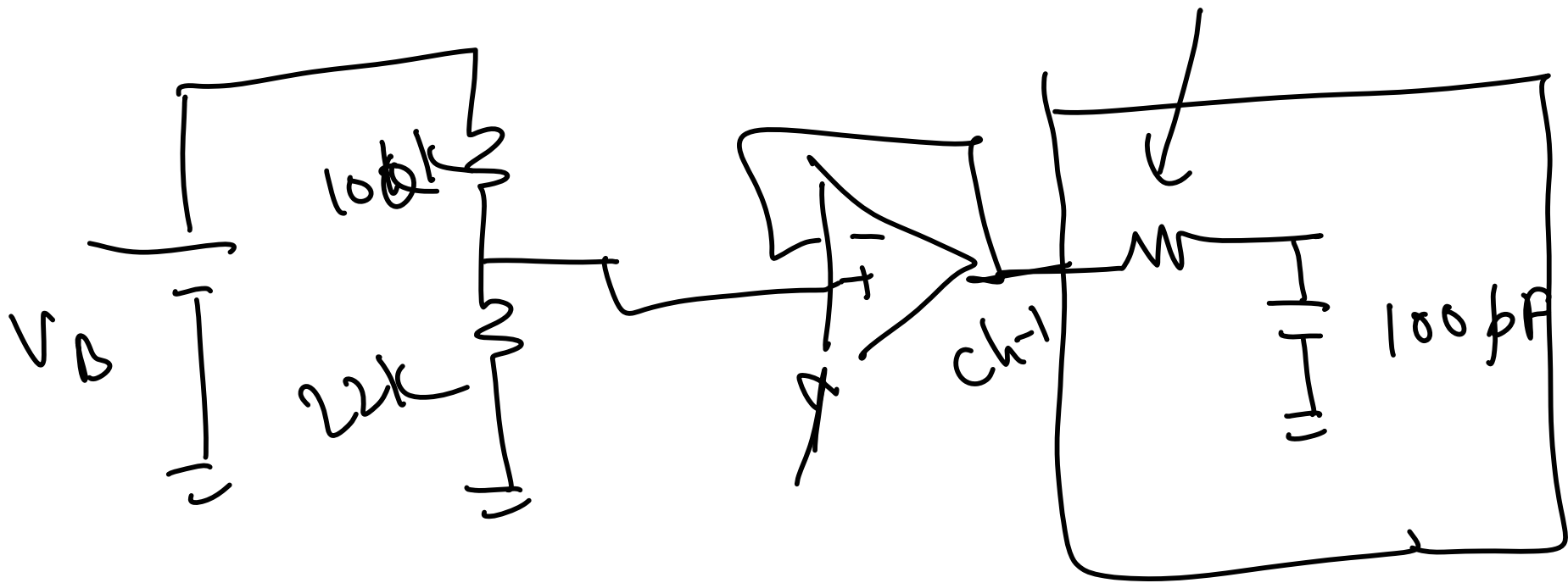
$$t = \ln\left(\frac{1}{2048}\right) \times RC$$

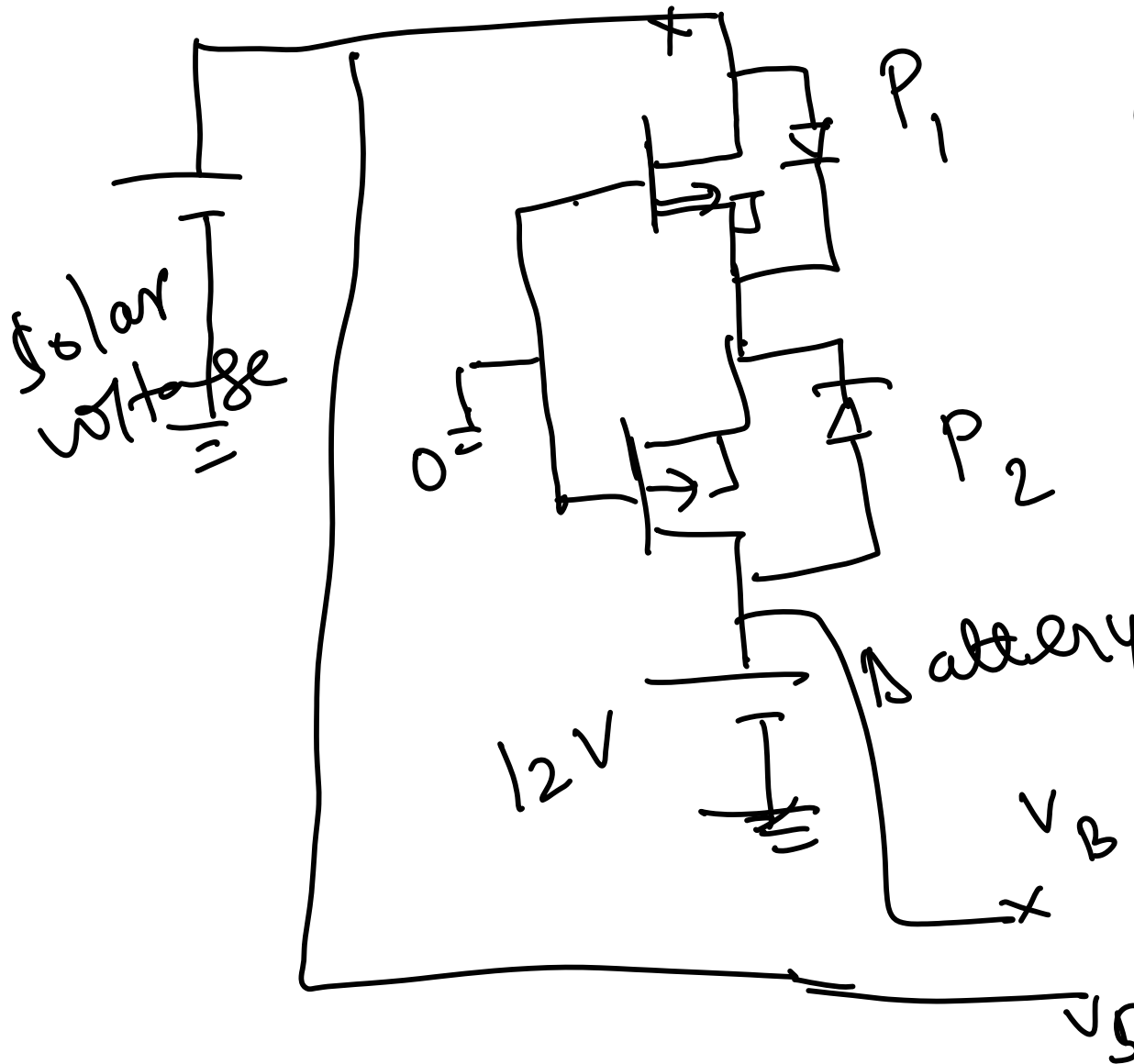
$$R \approx 20k$$





This method charges the hold cap very rapidly. But it is not fast enough to respond to the battery voltage change





Gates are grounded
 Both P₁ and P₂ are on
 If gates are left at 12V
 Then P₁ and P₂ are OFF

If $V_S > V_D$

put gates to zero

then charging of the battery
takes place

However

If V_S comes down

suddenly due to cloud

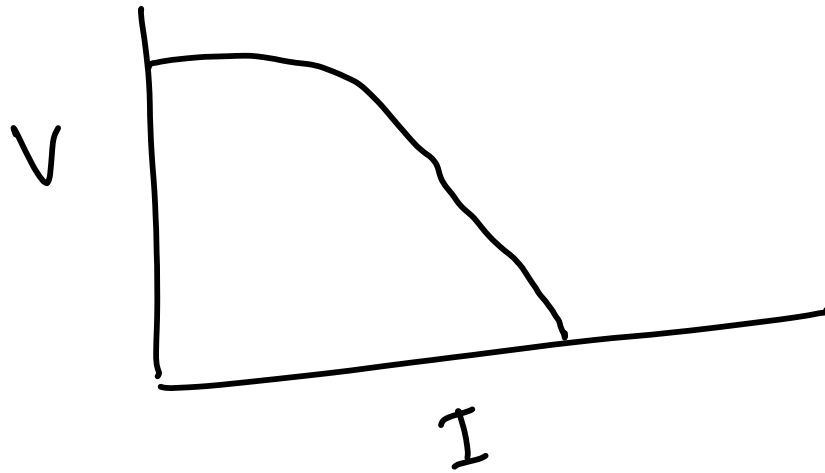
or any thing else

then battery will discharge
to the panel

This must be stopped
immediately

i.e. if $V_B > V_S$

P_1 and P_2 must be
switched off quickly



For example

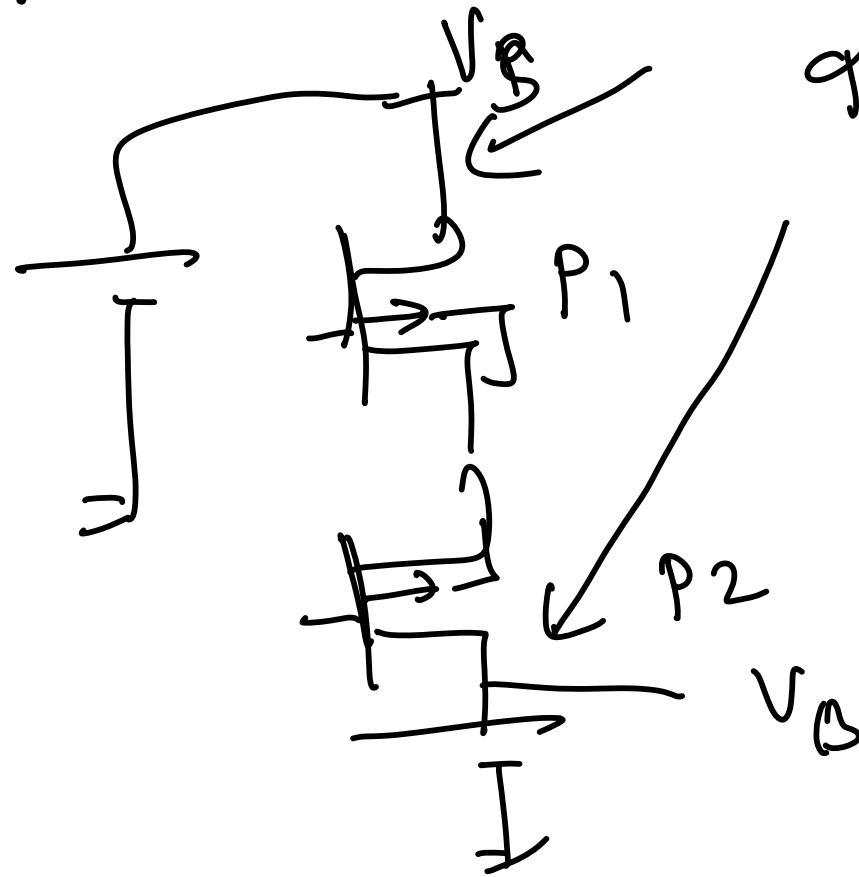
in this case $V_R = 5V$
it is a 10 bit converter

$$1 \text{ LSB} = \frac{5}{2^{10}} = \frac{5}{1024} = 5 \text{ mV}$$

Considering the voltage divider
the minimum detectable voltage
at the panel is

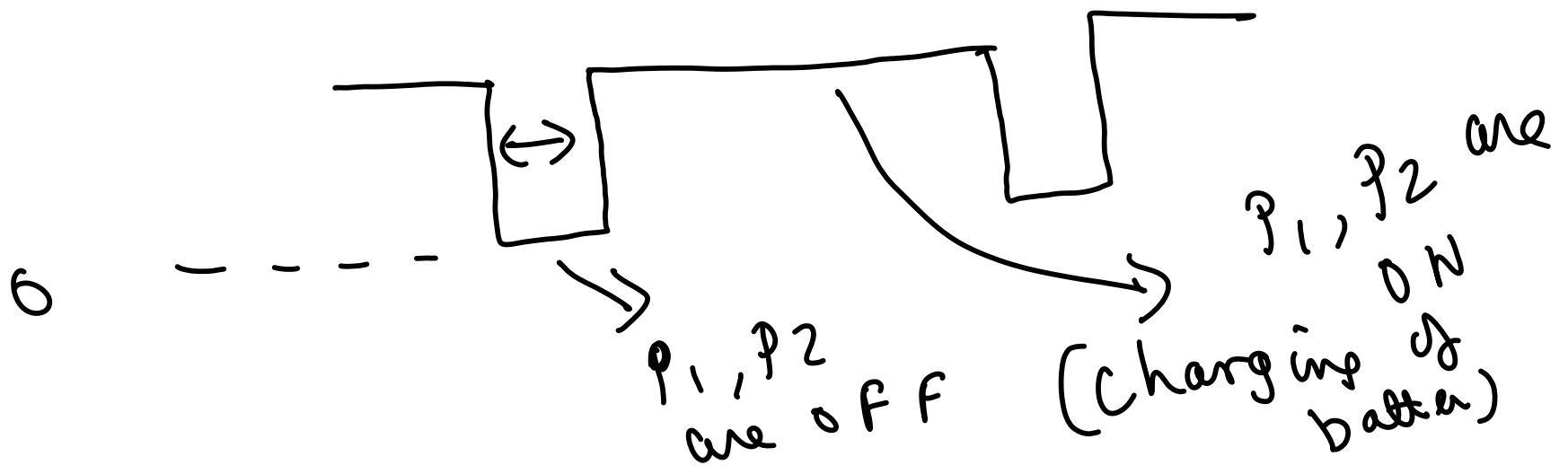
$$5 \text{ mV} \times \frac{100 \text{ k}}{22 \text{ k}} = 30 \text{ mV}$$

Minimum vol level at the
panel is 30mV



If it is
less than
30mV

- ① Switch off P_1 and P_2
- ② Measure quickly V_S and V_B
- ③ If $V_S > V_B$ Switch on $P_1 P_2$
- ④ Keep this ON state for about 3 to 5 ms
- ⑤ Repeat from step 1



During P_1, P_2 energy is
not drawn from the solar cell
ie we are not utilising
the cell fully.

So the OFF time should
be very short compared to

the ON time

ie ADC must be very fast
why not longer ON time?

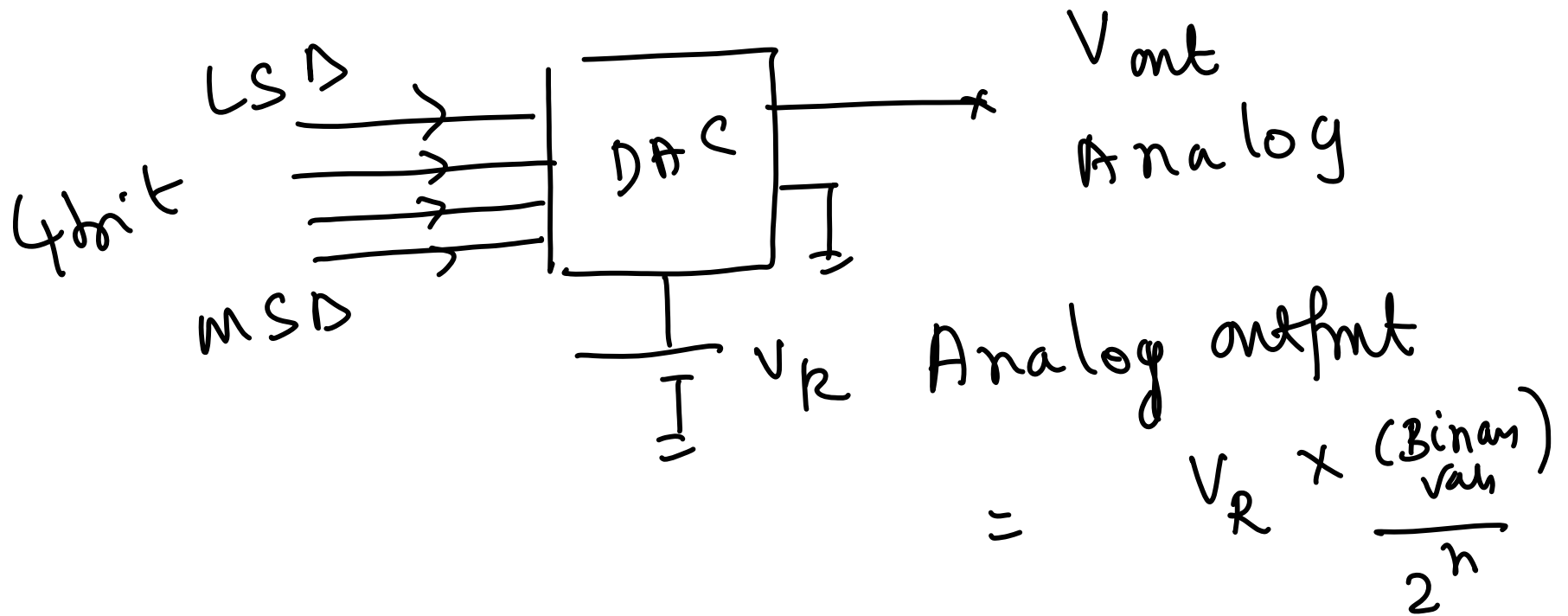
This is bad because
if $V_D > V_S$ during ON Time
battery will be discharging
to the panel.

Diode is not used to block
the reverse flow. because
the diode will eat away $0.4V$
 Φ_0

Lecture no: 38

Digital to Analog Converters

DAC



$$V_R = 1 \text{ V}$$

$$n = 4 \quad (4 \text{ bit converter})$$

$$V_0 = \frac{1 \times (BV)}{2^4} = \frac{1 \times 1}{16} = \frac{1}{16} \text{ V}$$

F-ur

1111

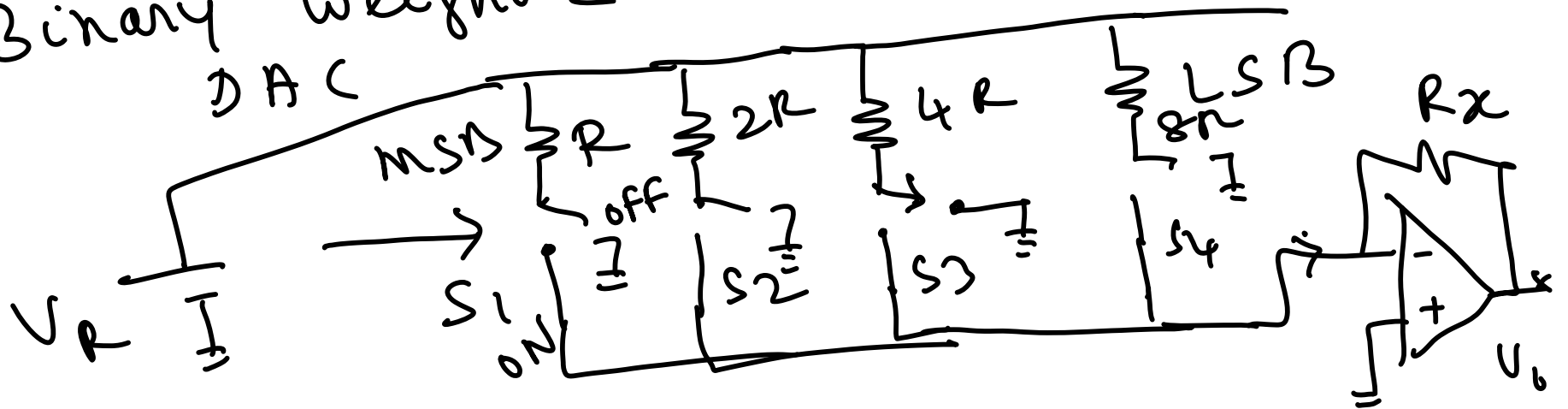
$$V_0 = \frac{1 \times 15}{16} \text{ V}$$

0001

Two types of DAC

- ① binary weighted DAC
- ② R-2R based DAC

Binary weighted DAC



MSB $\rightarrow 1$ and All other bits are zero

Input $\rightarrow 1000$ then
 S_1 ON \rightarrow connected to op amp
 S_2, S_3, S_4 \rightarrow OFF connected to GND

Then current I to the
inverting input of op amp

$$= \frac{V_R}{R} + 0 + 0 + 0$$

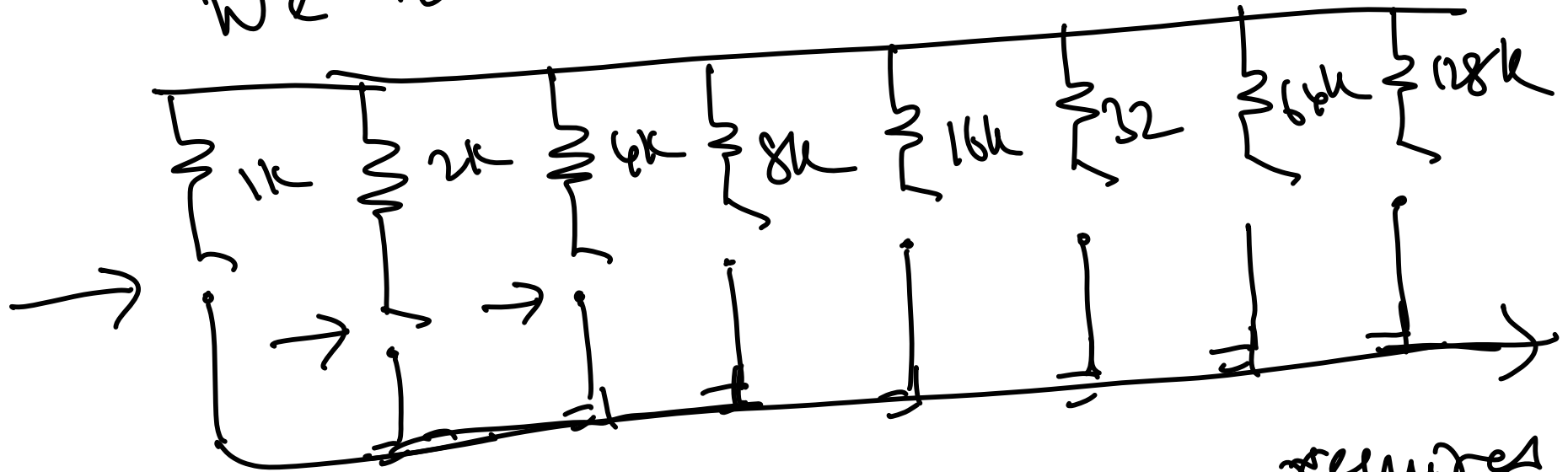
For digital

input 1111

then $I = \frac{V_R}{R} + \frac{V_R}{2R} + \frac{V_R}{4R} + \frac{V_R}{8R}$



For 8 bit Converter
we need 8 resistors



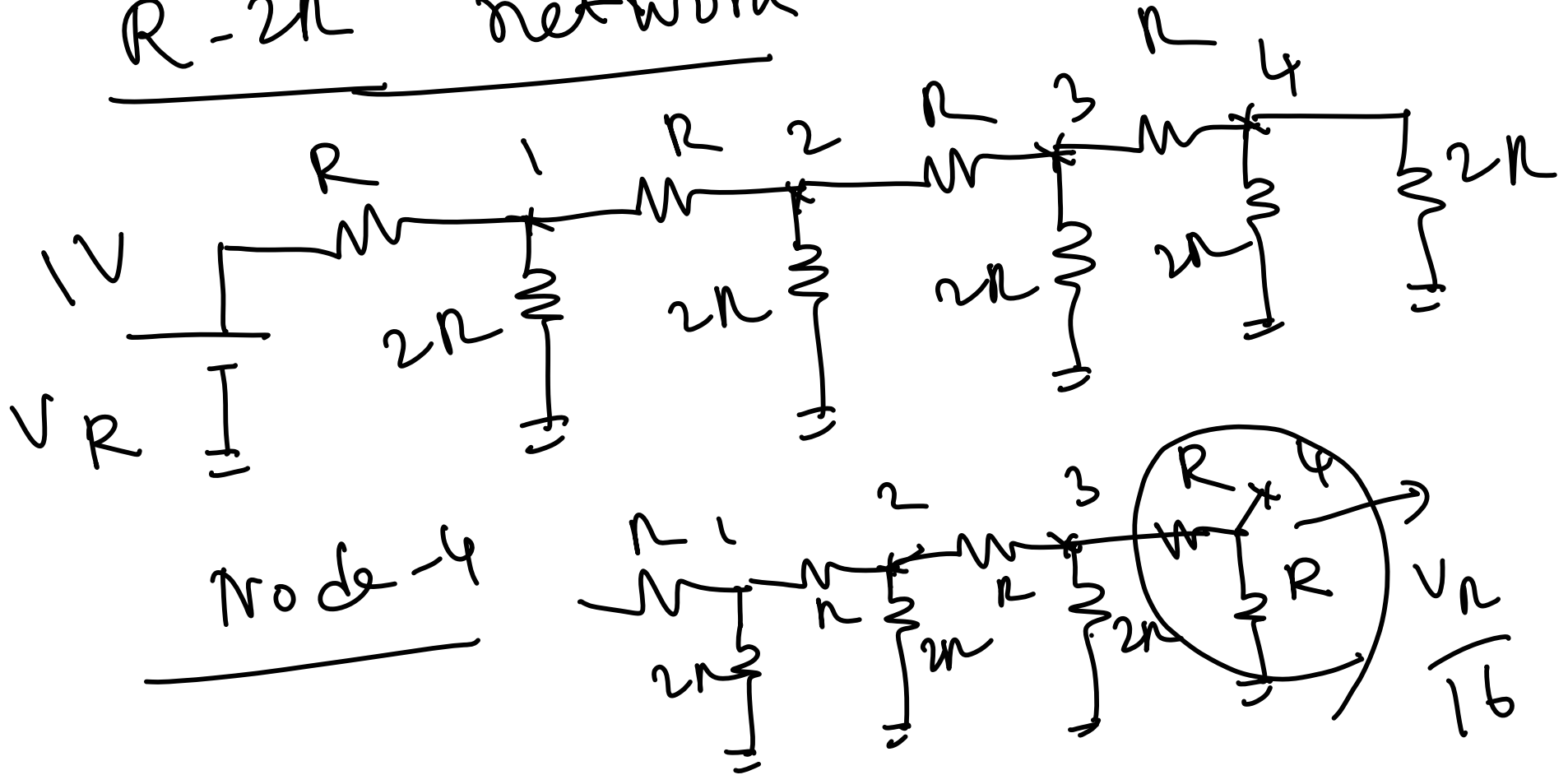
$\frac{1}{2^8}$ Accuracy required
for all the 8 resistors

In binary weighted resistor
based DAC

Accuracy requirement for
resistors are difficult to
achieve particularly for
high bit DACs

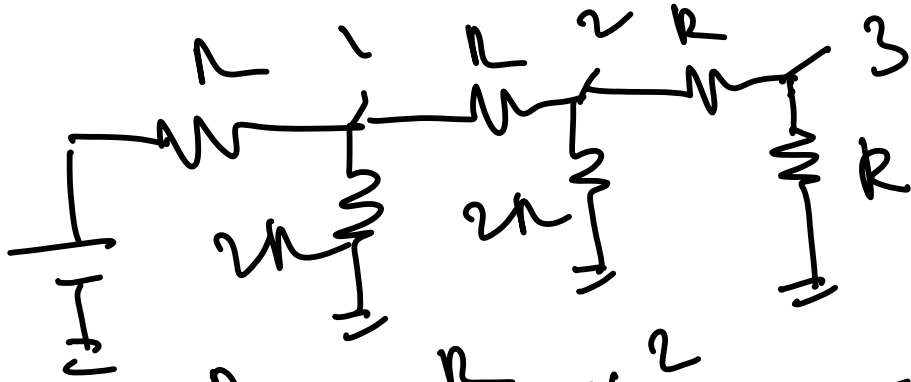
R-2R network based DAC

R-2R network



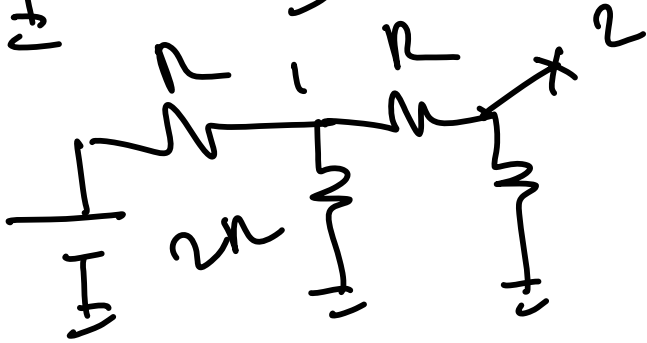
Node-4

③



$$\frac{8R}{8} = \frac{V}{4}$$

②



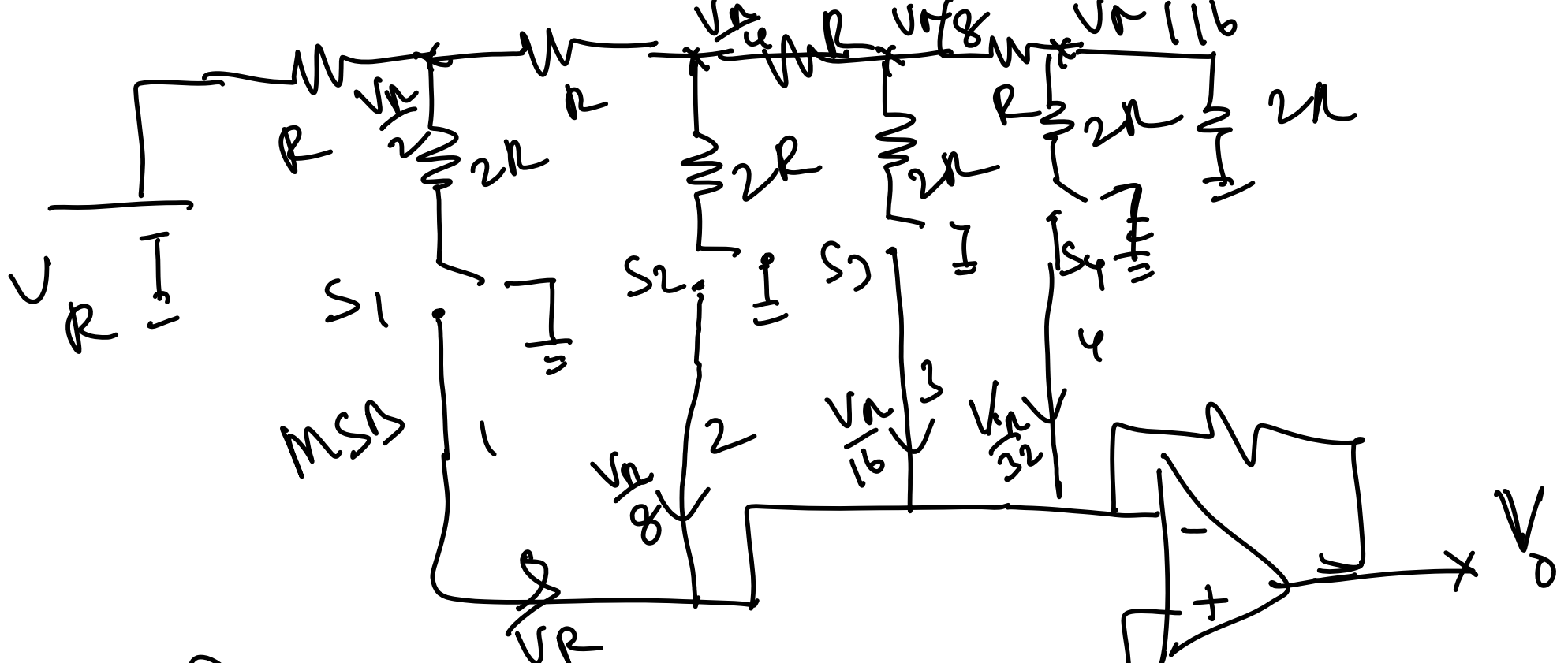
$$0.25$$

①



$$0.5V = \frac{V}{2}$$

one can get binary weights using only two different resistors (R and 2R)



For digital input } 1 1 1 1

S_1, S_2, S_3, S_4 ↓

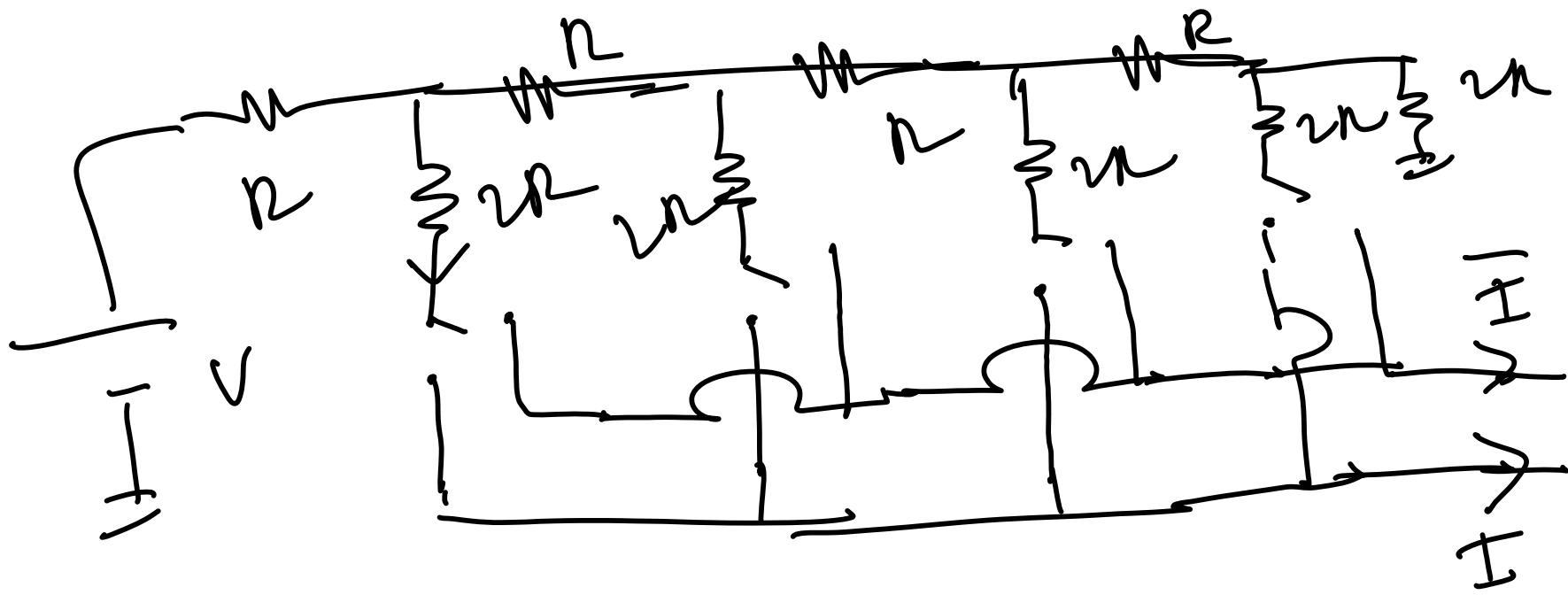
all delivering current to inverting input of op amp

For digital input } 0 0 0 0

↪ S_1, S_2, S_3, S_4 all grounds to op amp

For digital input 1
current is delivered to
of amp by the corresponding
resistor

For digital input 0
current from the corresponding
resistor is grounded



R_x $|||$

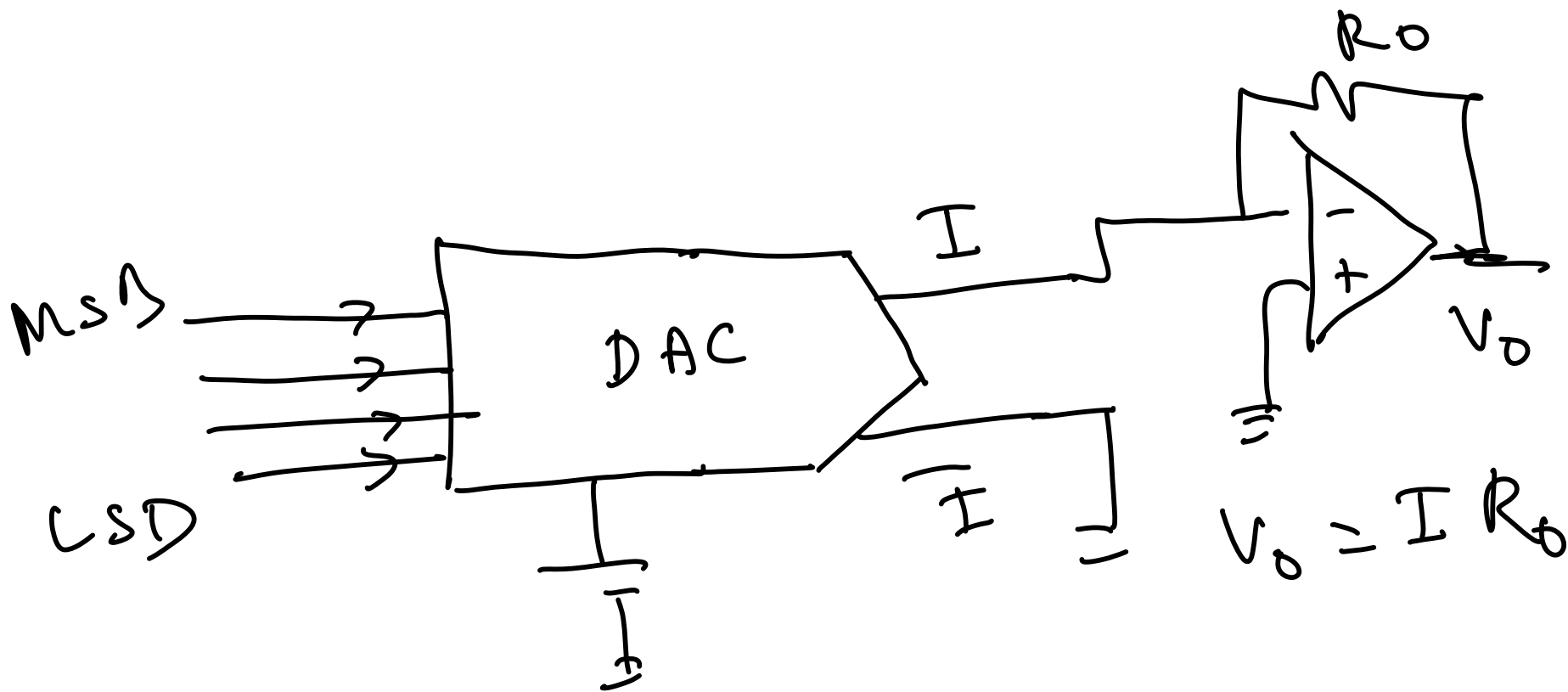
$$I = \frac{V}{4R} + \frac{V}{8R} + \frac{V}{16R} + \frac{V}{32R}$$

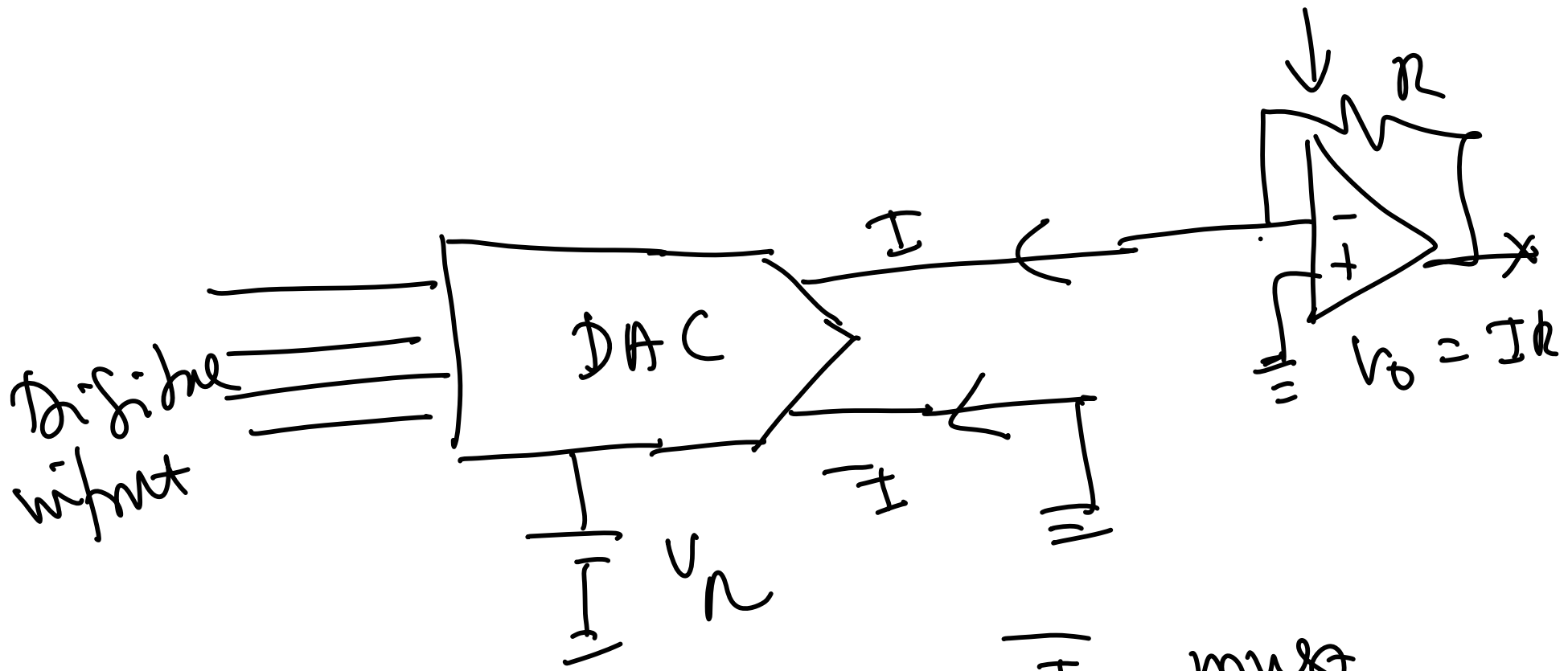
$$I = 0$$

For 0000

$$I = 0$$

$$I = \frac{V}{4R} + \frac{V}{8R} + \frac{V}{16R} + \frac{V}{32R}$$

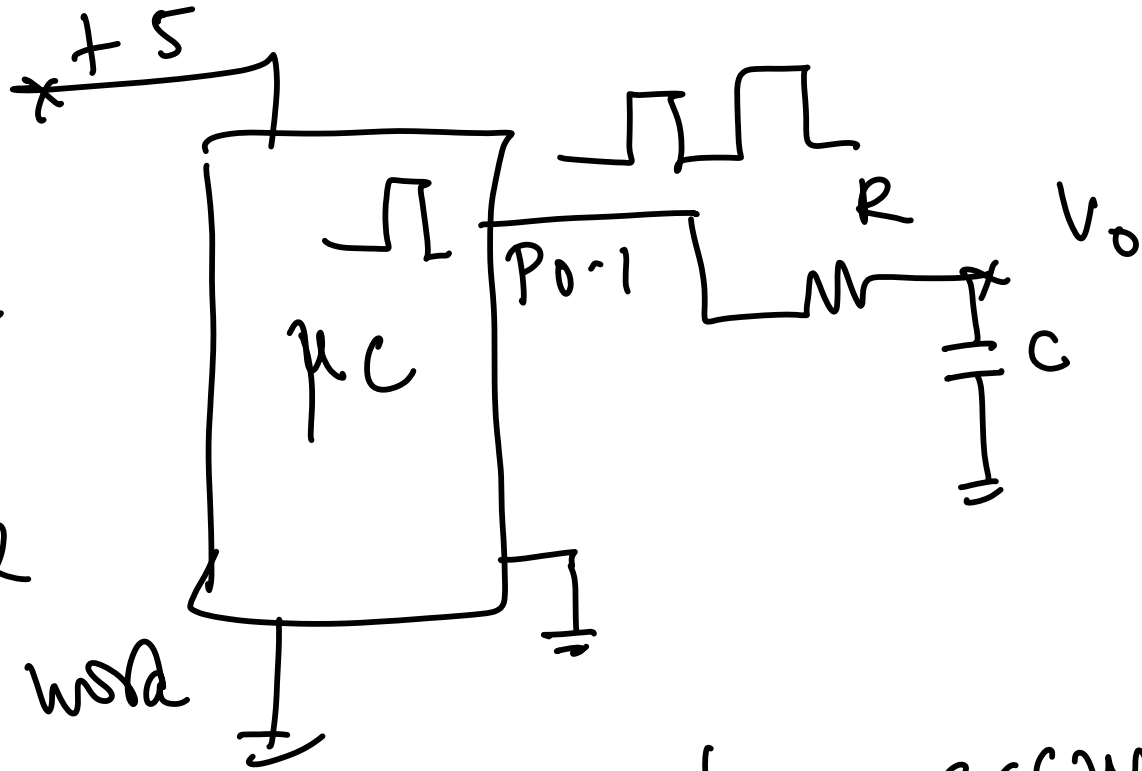




Both I and $-I$ must always ground potential

PWM based DAC

Pulse width must be proportional to digital word

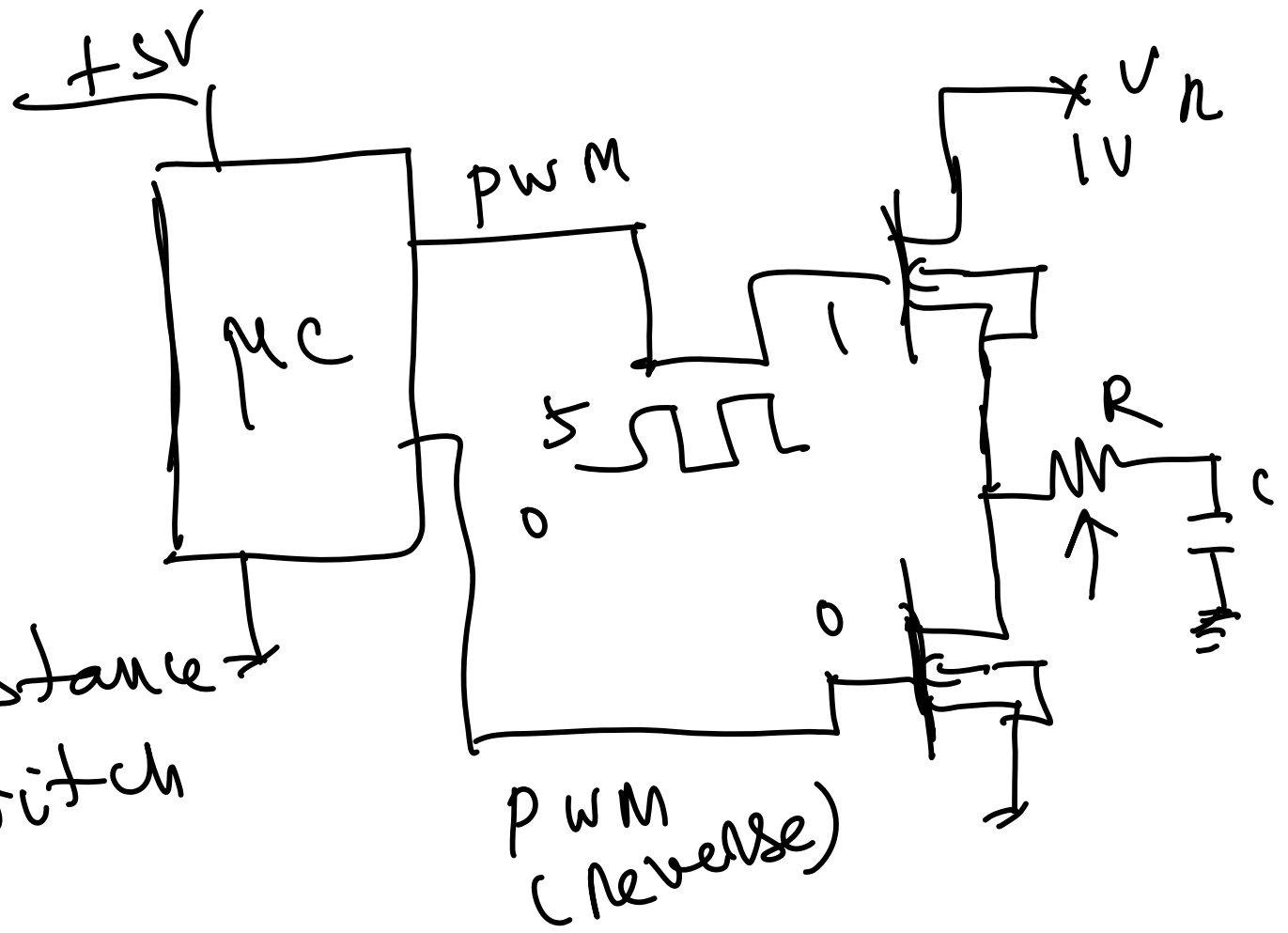


The output may not be accurate because

- 1
- 2

Supply vol error
Switches may not be accurate (voltage loss in the switches may be con)

∴ ON resistance of the switch must be very small compared to R



*: It is very slow DAC

However it is very simple
cost effective DAC for μC
systems

ADC

①

Dual Slope ADC

②

Successive approximation
ADC

③

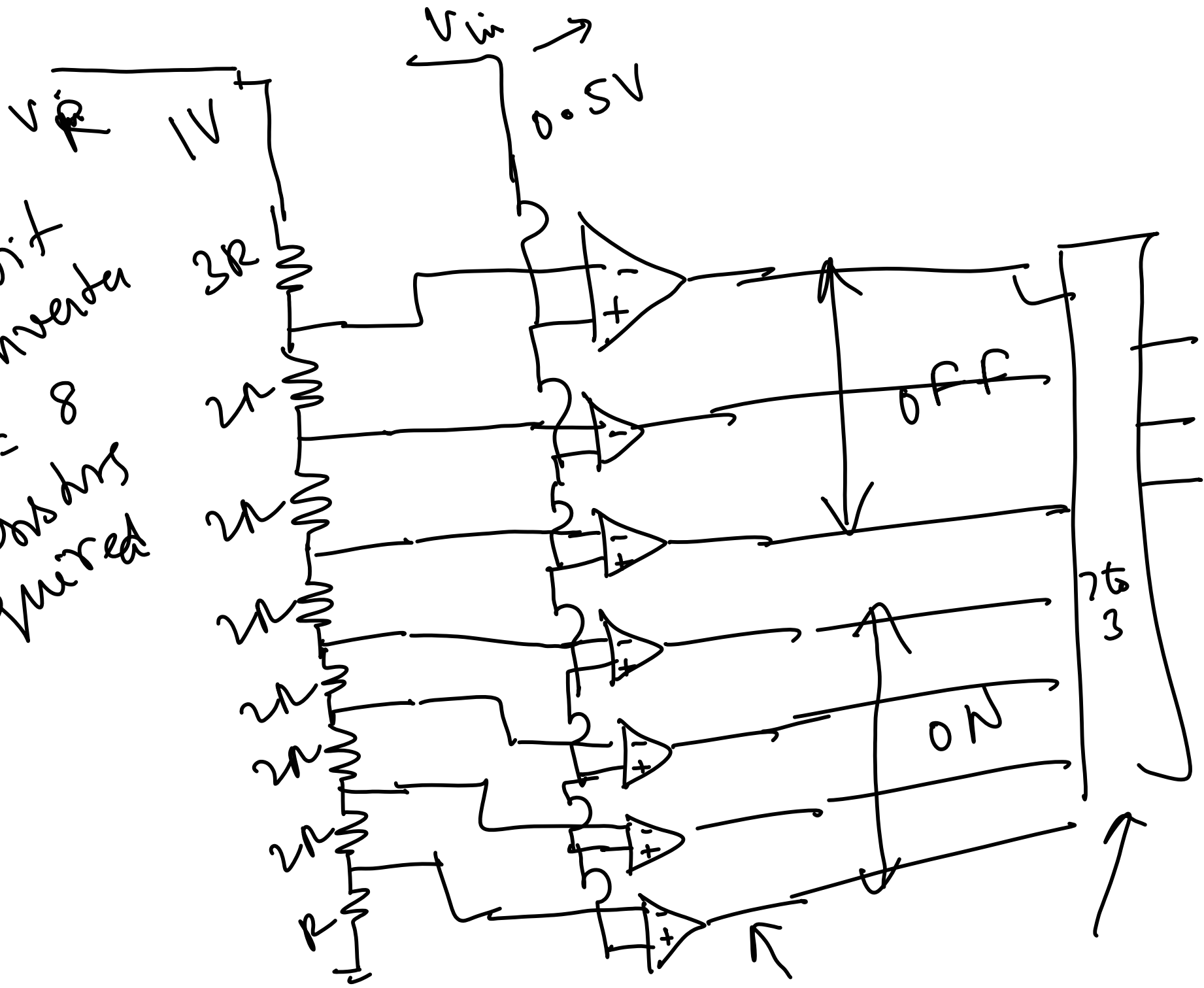
Flash ADC

Dual Slope ADC → 5 to 10 conversions
per sec

SA / ADC → 10 to 20 ~~µ~~ ^{ms} / sec

Flash ADC

3 bit
Converter
2³ = 8
levels
required



Conversion time is
very small

Comparator response time + logic conversion time

Advantage → less conversion time

This advantage → large hardware
matched resistors
comparators

- ① 2^n
- ② 2^n

For 8 bit Converter

- ① Huge Conversion logic
- ② 255 resistors — matches
- ③ 256 comparators

For 16 bit Converter

- ① $2^{16} \rightarrow 64,000$ resistors
- ② $64,000$ comparators

$$\frac{0.4}{16}$$

- ③ Conversion logic to convert $64,000$ (2^{16}) to 16 bit output

For $V_U \rightarrow V_{ref}$
16 bit Converter required

$$\text{total error } \approx \frac{1}{2^{16}} \approx 16 \mu\text{V}$$

Use two 8 bit Flash ADC
to get one 16 bit Flash ADC

This is called sub-ranging
ADC

Lecture - 39

8 bit Flash ADC

① 2^8 Comparators
required

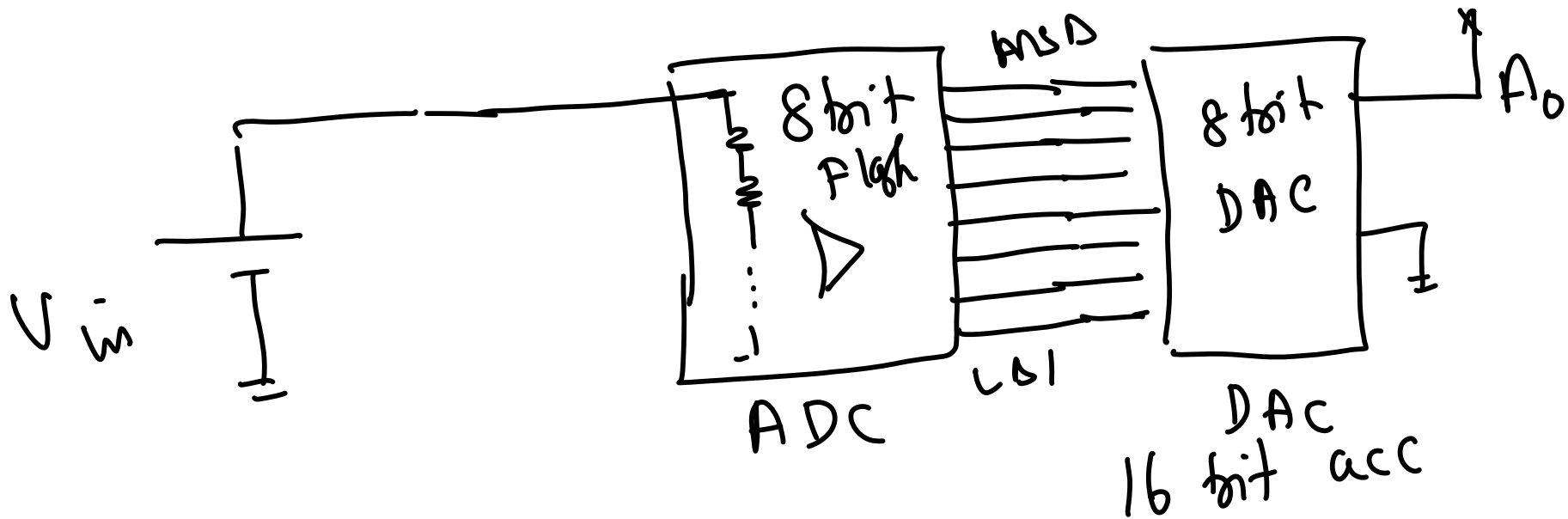
② 2^8 Dividers

16 bit Flash ADC

① 2^{16} Comparators

② 2^{16} Dividers

Sub ranging ADC is used for
12 bit or 16 bit Flash ADC

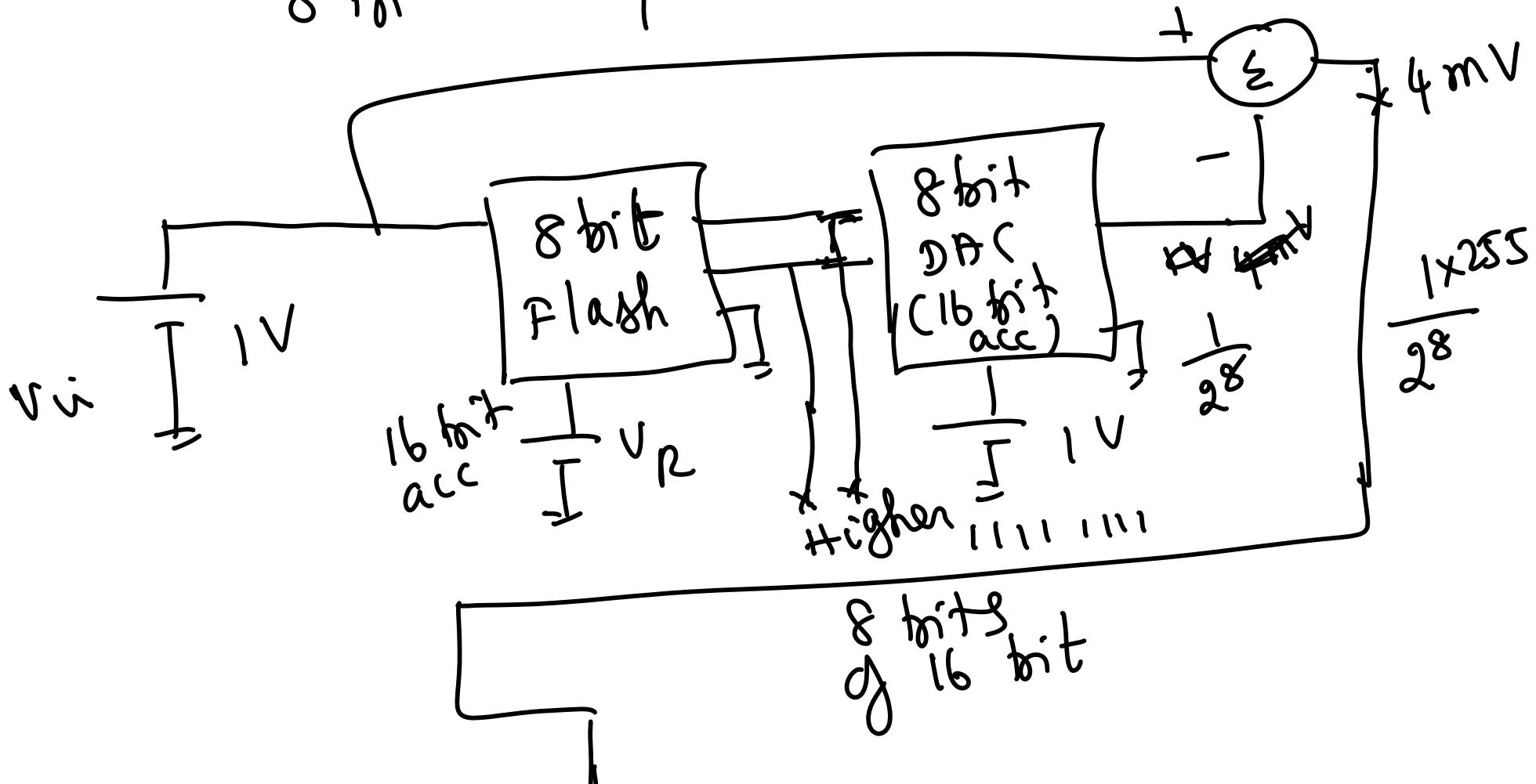


8 bit DAC 8 bit acc → error will be 1st LSB of 8 bit

8 bit DAC 16 bit acc → 1 LSB of 16 bit

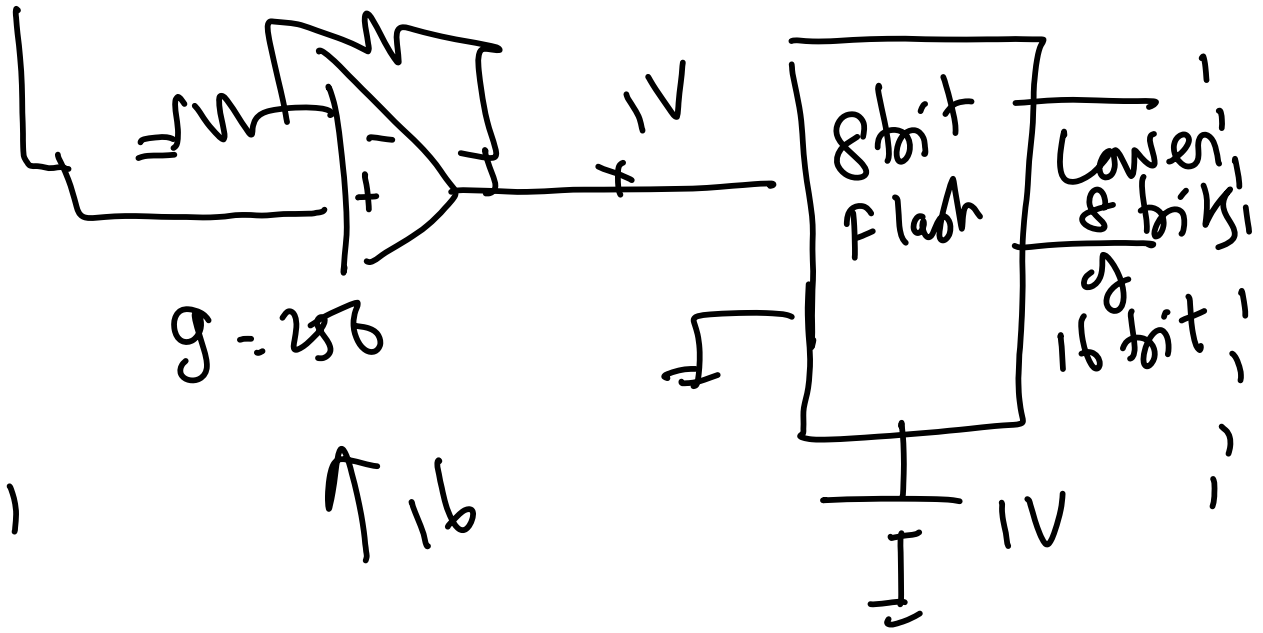
For 1 volt ref
 8 bit DAC / 8 bit acc $\rightarrow \frac{1}{256} \approx 4 \text{ mV}$

For 1 volt ref
 8 bit DAC / 16 bit acc $\rightarrow \frac{1}{2^{16}} = \frac{1}{64000} \approx 16 \mu\text{V}$

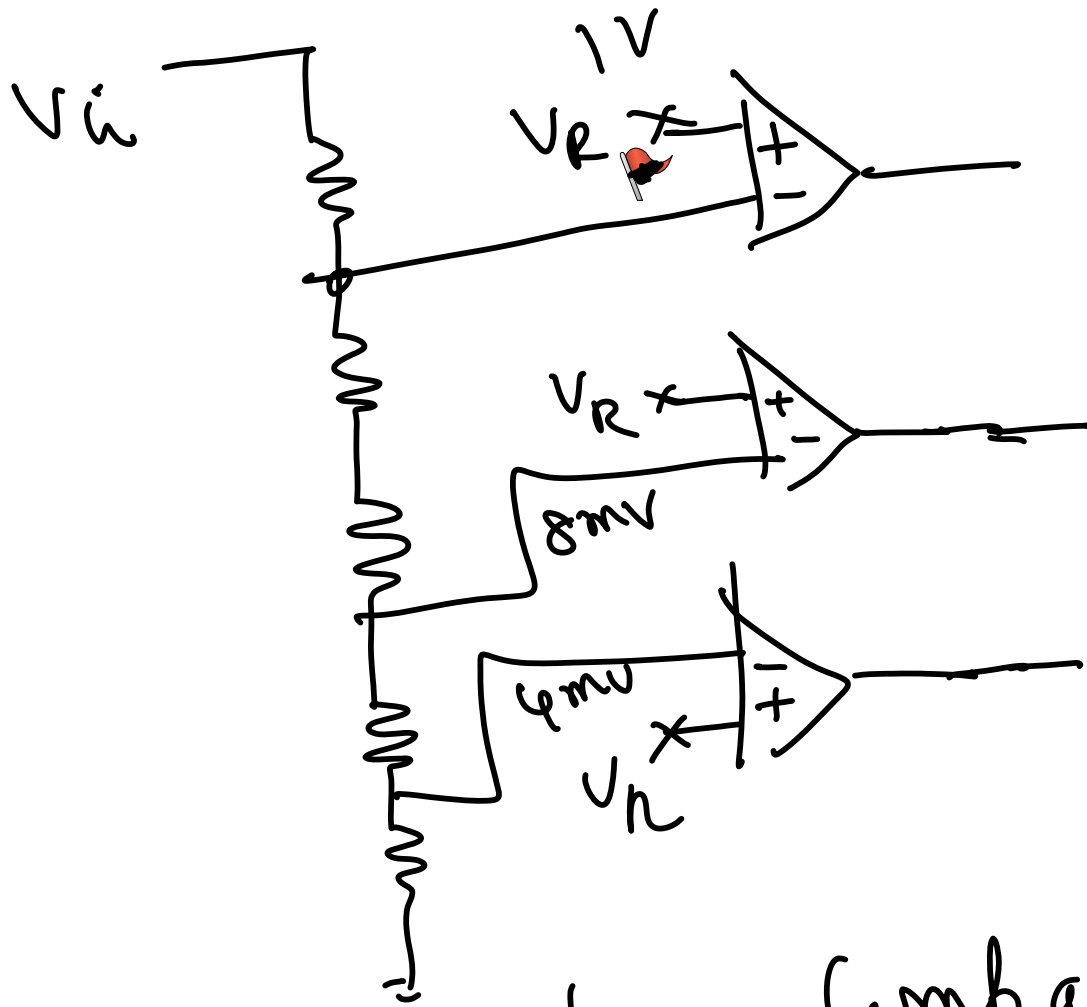


$V_{in} = 1V$
Digital

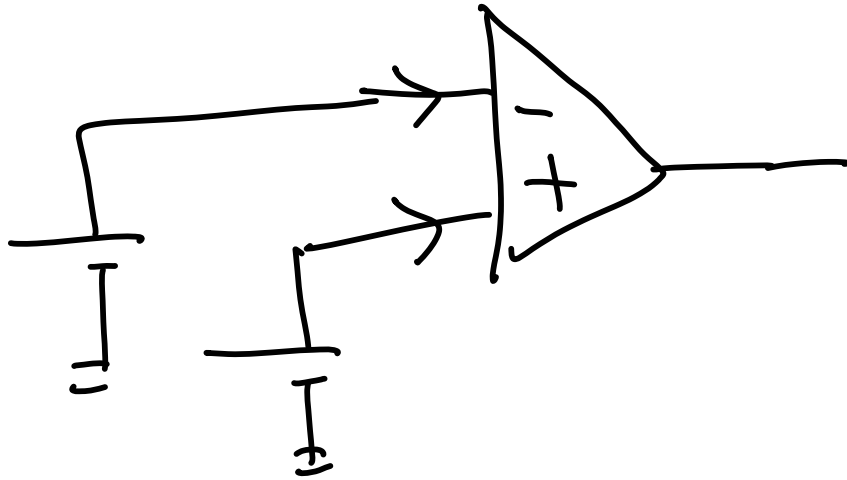
$V_o = 11111111$
 11111111



Adv \rightarrow Very short Con time
Dis \rightarrow costly

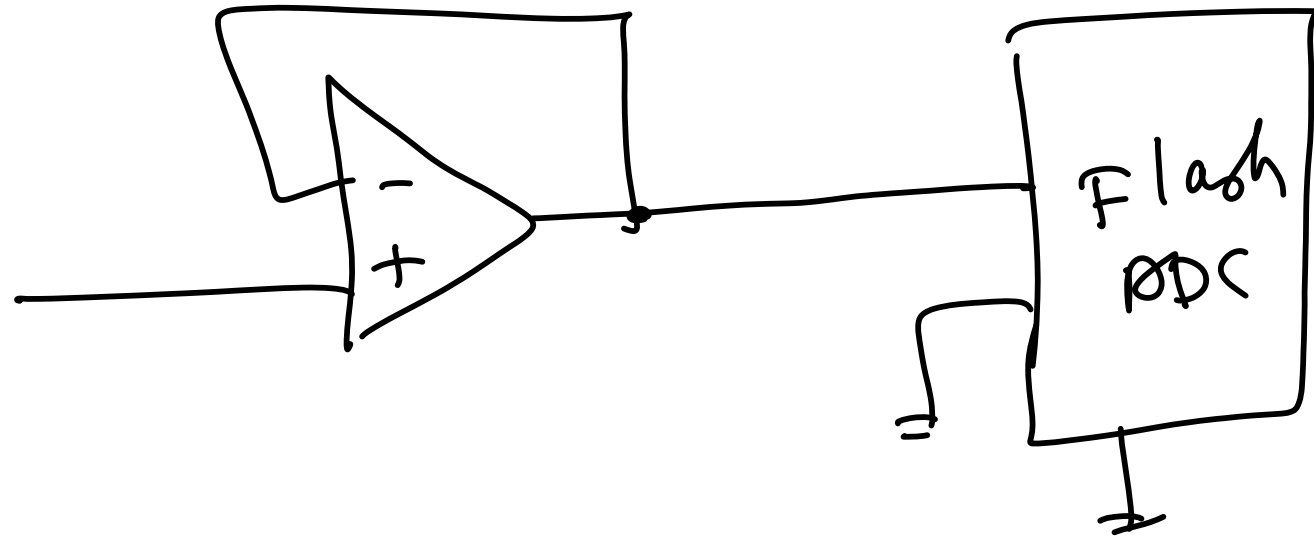


Always all the comparators are
 in saturation mode only



In saturation
 mode
 the input bias
 current is higher

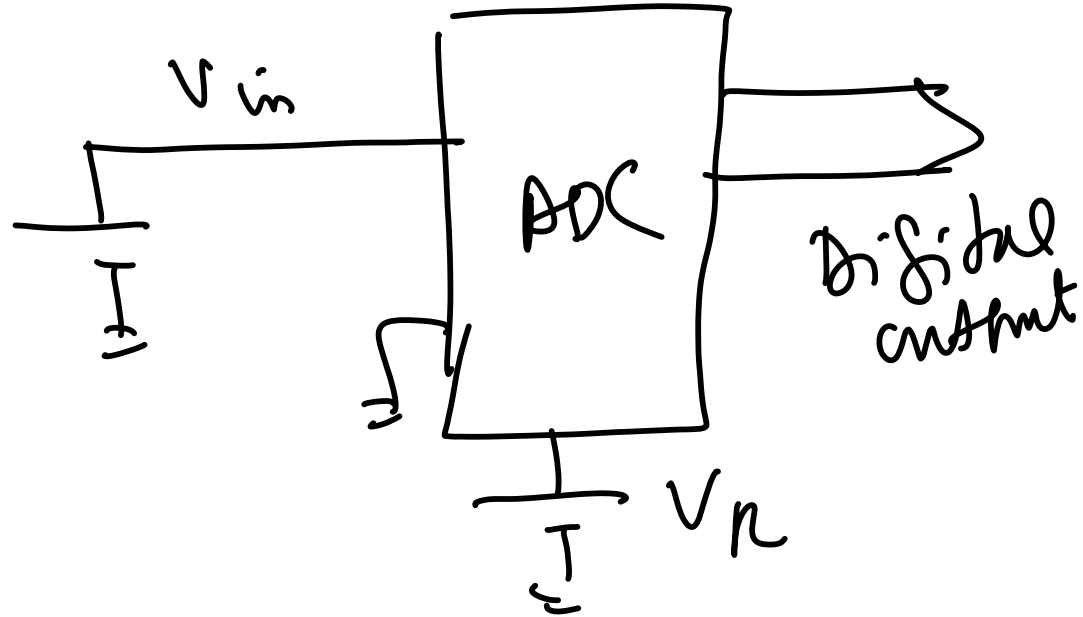
Drive with source Flash ADC output resistance
 with source Very low



Always drive the Flash ADC
with low output resistance

- 8-10 ① Dual slope ADC \rightarrow display
- 1 MS ② Successive approx ADC
- 50 ns \leftarrow
10 ns \leftarrow ③ Flash ADC

Errors



$$\text{Resolution} = \frac{1}{2^n}$$

$$\text{For } \epsilon_{\text{int}} = \frac{1}{256}$$

- ① Reference w/ drift
 - ② OFF set w/ drift
 - ③ gain drift
- For $b_{in} = 0$ $v_o \neq 0$
- Temp
relat
errs

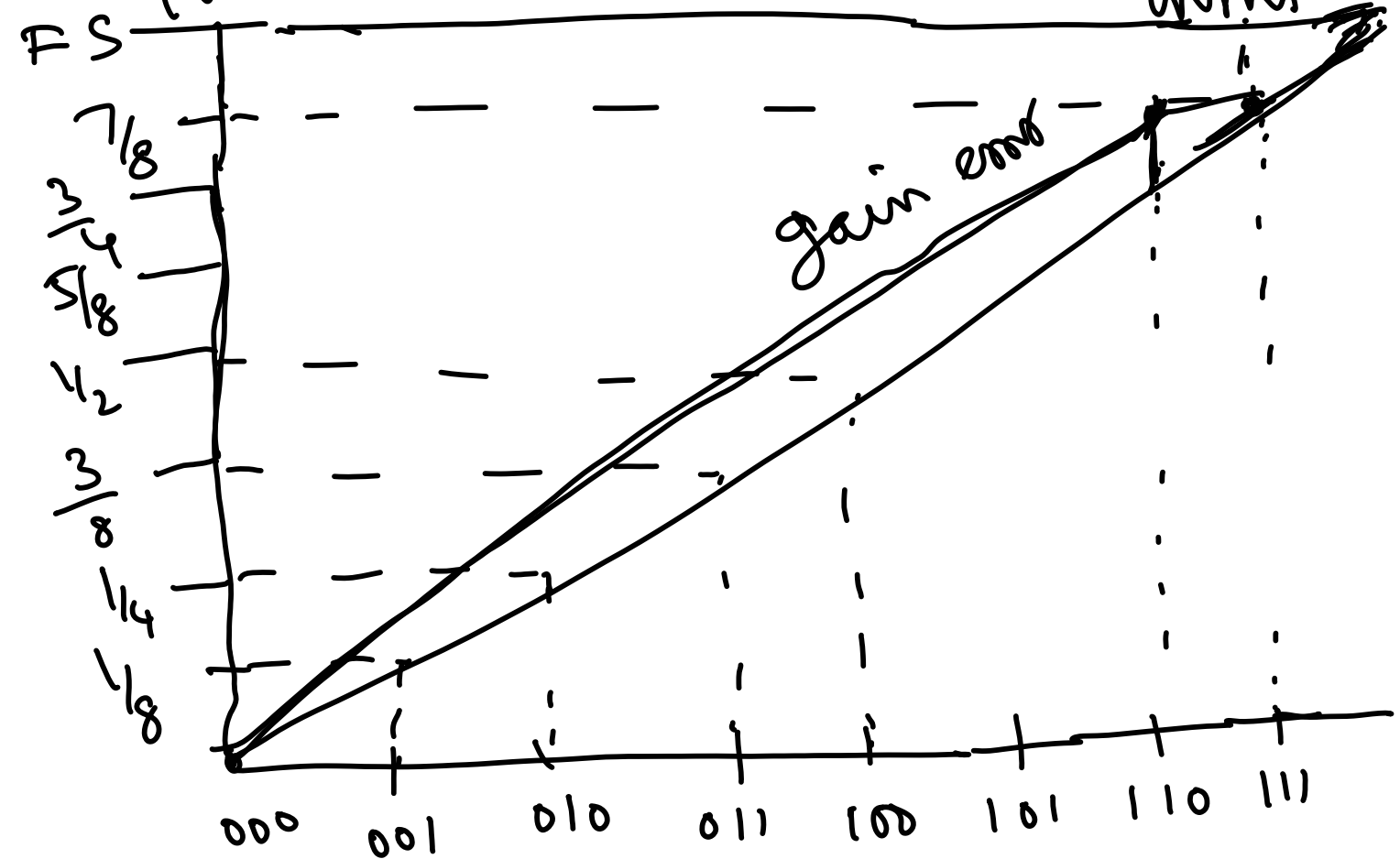
The static errors (not related to temp)

- ① gain error
- ② offset voltage error
- ③ linearity error
- ④ differential linearity error

Example with 3 bit

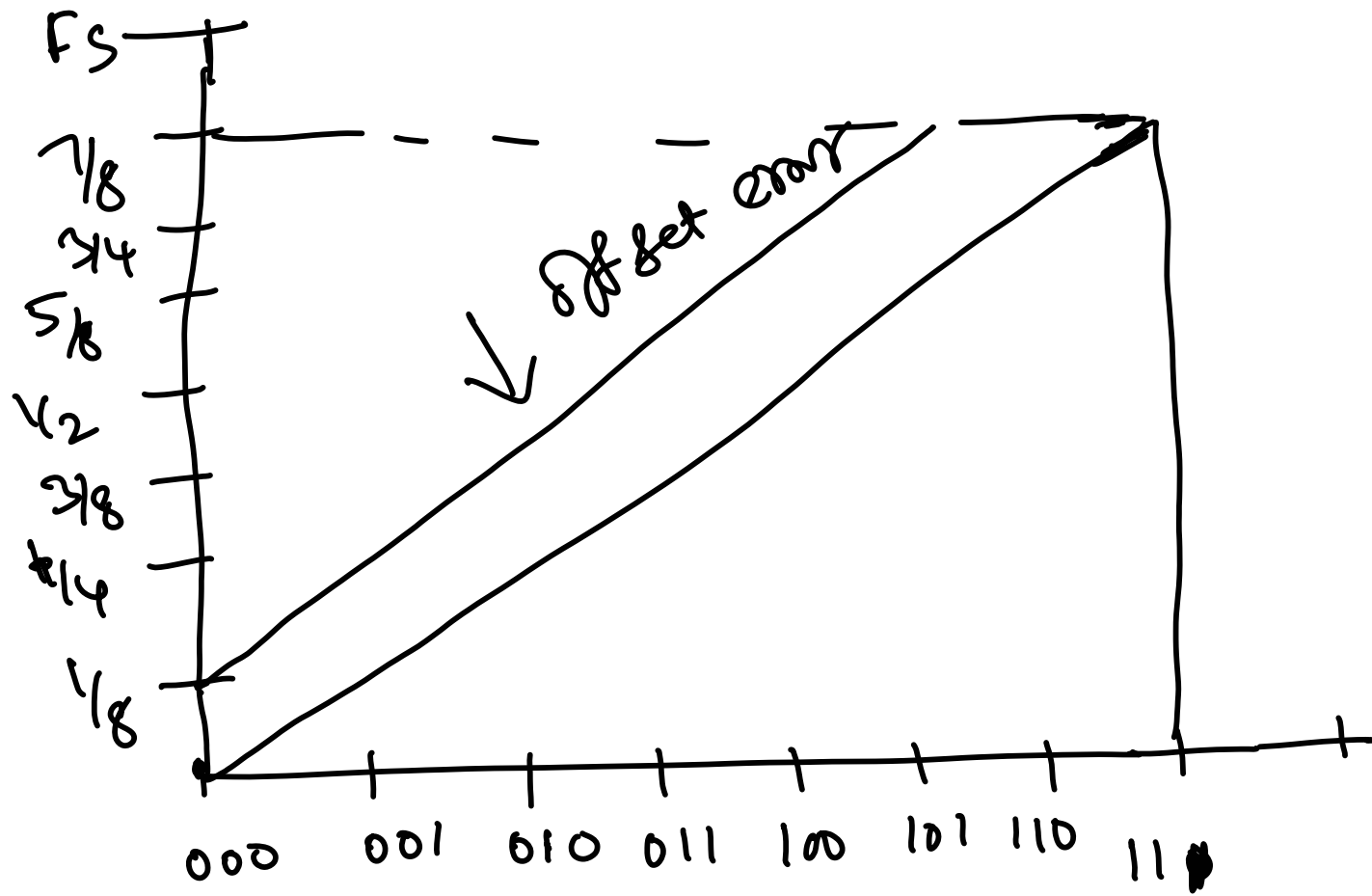
111 → digital

$V_R = 1V$

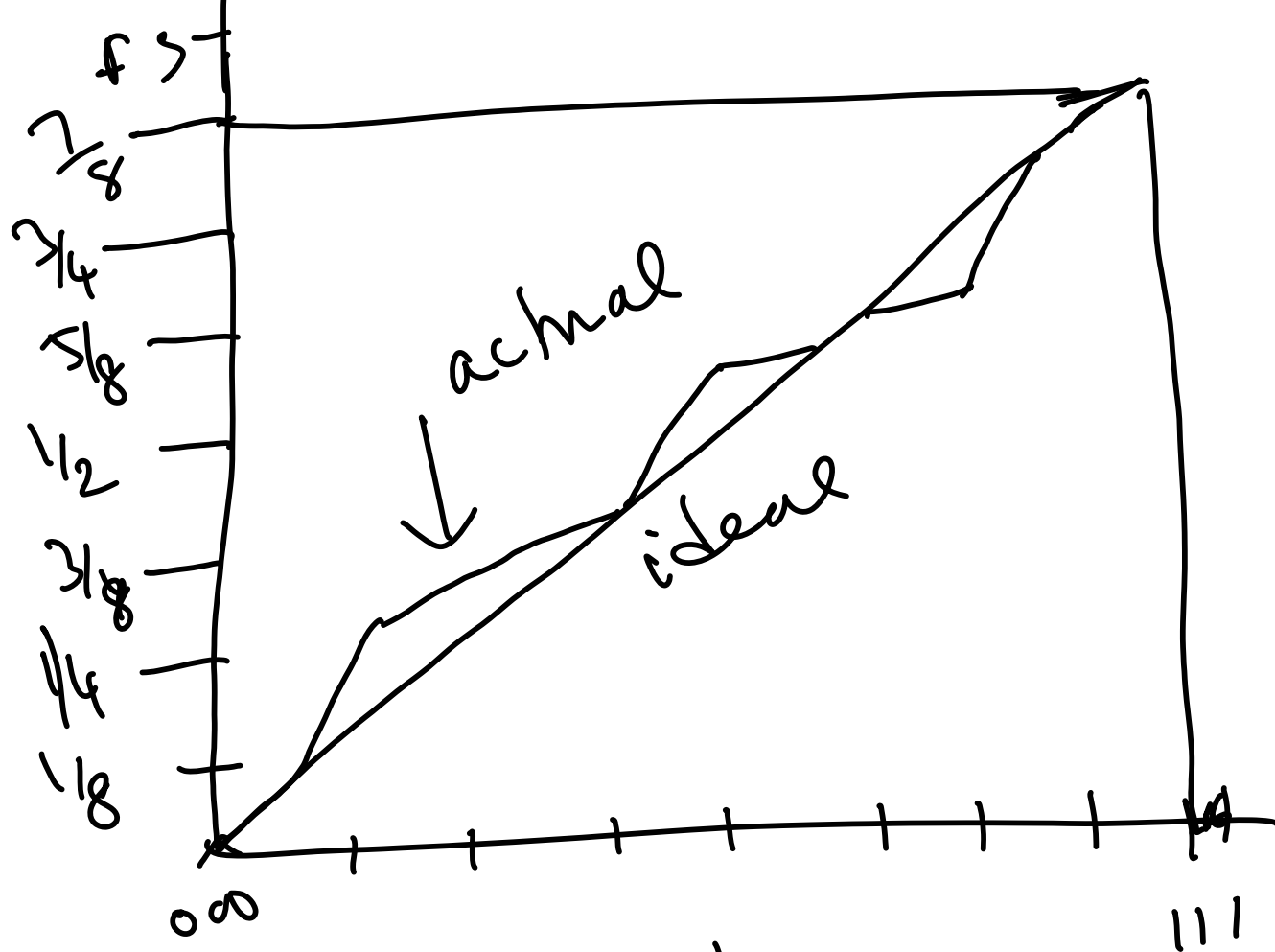


$\frac{7}{8}$ bit at 111 → ideal
 $\frac{7}{8}$ bit at 110 → real value

OFF set
error



Linearity error



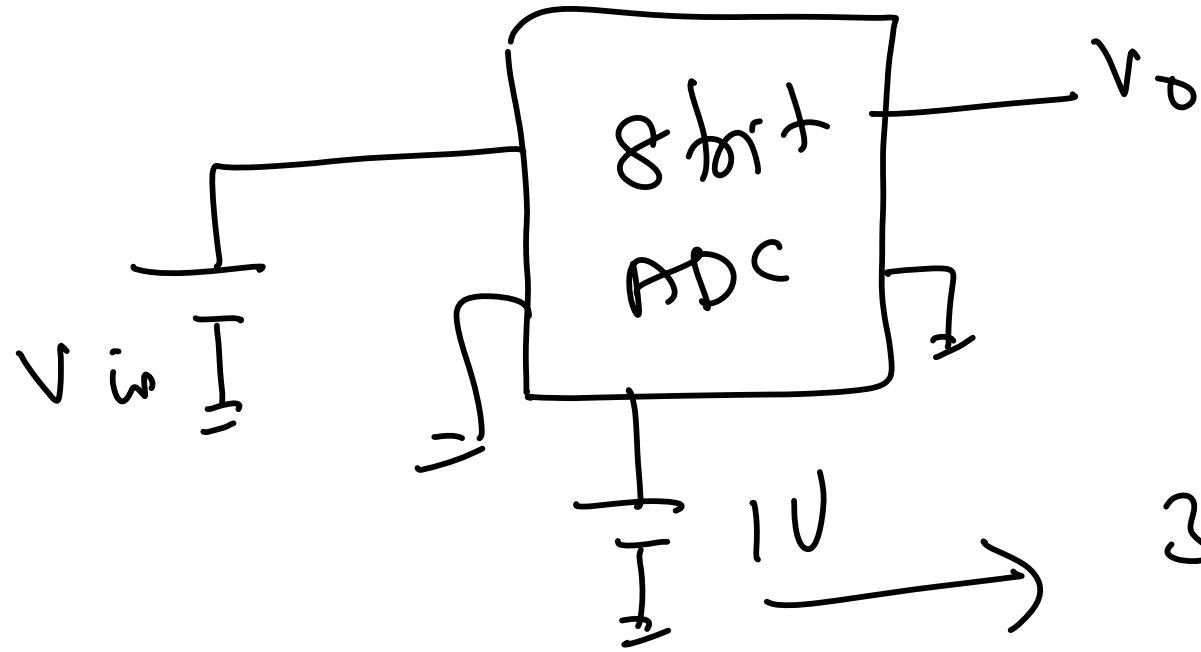
Differential linearity error

$110 \rightarrow \frac{3}{4} \text{ Volt}$
 $111 \rightarrow \frac{7}{8} \text{ Volt}$

} 1 LSB

For differential
non linearly the
difference \approx 1 LSB

These 4 errors are correctable
but temp related errors are
not correctable



30 ppm/°C

For $\Delta T = 100 \text{ } ^\circ\text{C}$

The V_R drift

$$= \frac{30 \times 100 \times 1}{10^6} = \frac{3000}{10^6} = 3 \text{ mV}$$

For 8 bit Converter

$$1 \text{ LSD} = \frac{1}{2^8} \approx 4 \text{ mV}$$

For 16 bit Converter

$$1 \text{ LSD} = \frac{1}{2^{16}} \approx 16 \mu\text{V}$$

For 16 bit converter

$$\text{total error} = \frac{3000}{16} \text{ LSBs}$$

$$\approx \underline{\underline{200}} \text{ LSBs}$$

For $(1 \text{ PPM})_c$ drift error

$$\text{the total drift} \approx \frac{100}{10^6} \approx 10^{-4} \text{ V} \\ = 100 \mu\text{V}$$

$$\approx \underline{\underline{6}} \text{ LSBs}$$

II Offset drift error

offset w/ drift at the
input of ADC \rightarrow 1 to 5 $\mu\text{V}/c$

For example

For $5 \mu\text{V} \cdot \text{C}$ drift case

For $\Delta T = 100 \text{ C}$

Then total drift = $500 \mu\text{V}$

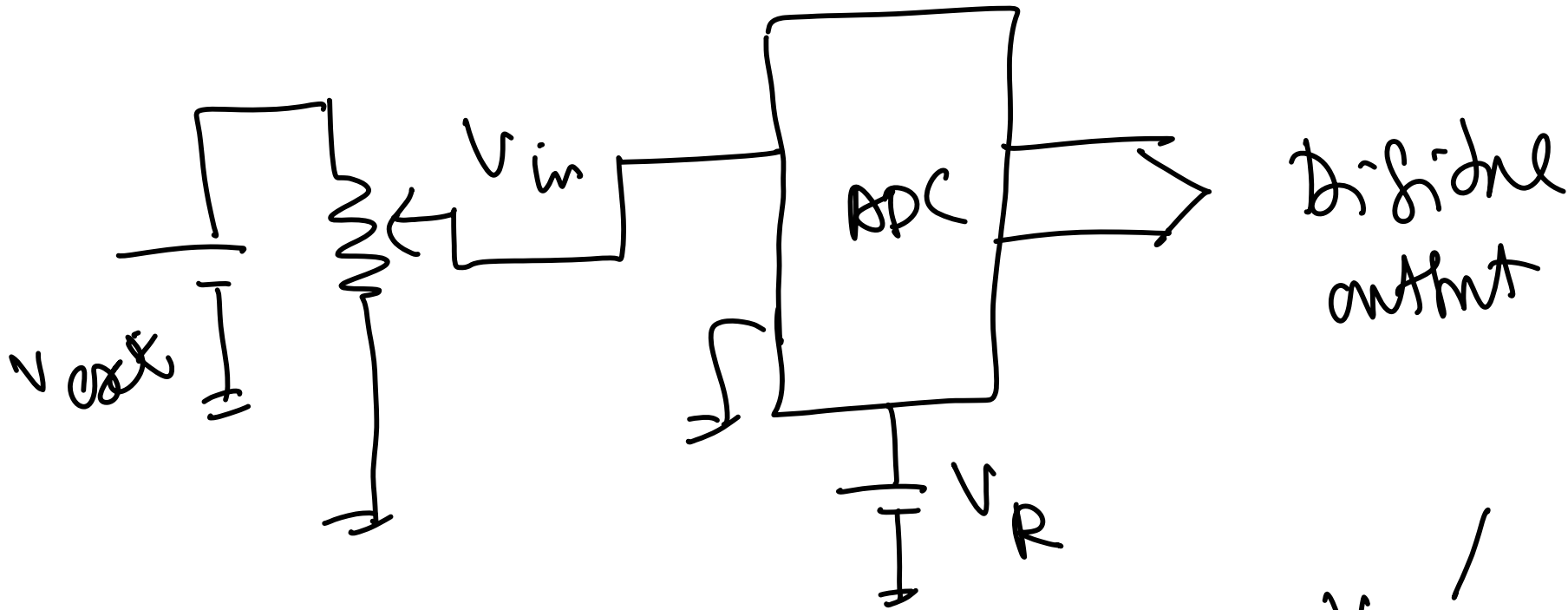
For 16 bit converter

$$\text{this drift} = \frac{500}{16} = 32 \text{ LSB}$$

① For 8 bit converters
Resolution and accuracy
will be more or less same
i.e. it is possible to get
8 bit accuracy against
ambient temp variation

② For 16 bit converters
it is difficult to get
16 bit accuracy.

Ratio metric conversion



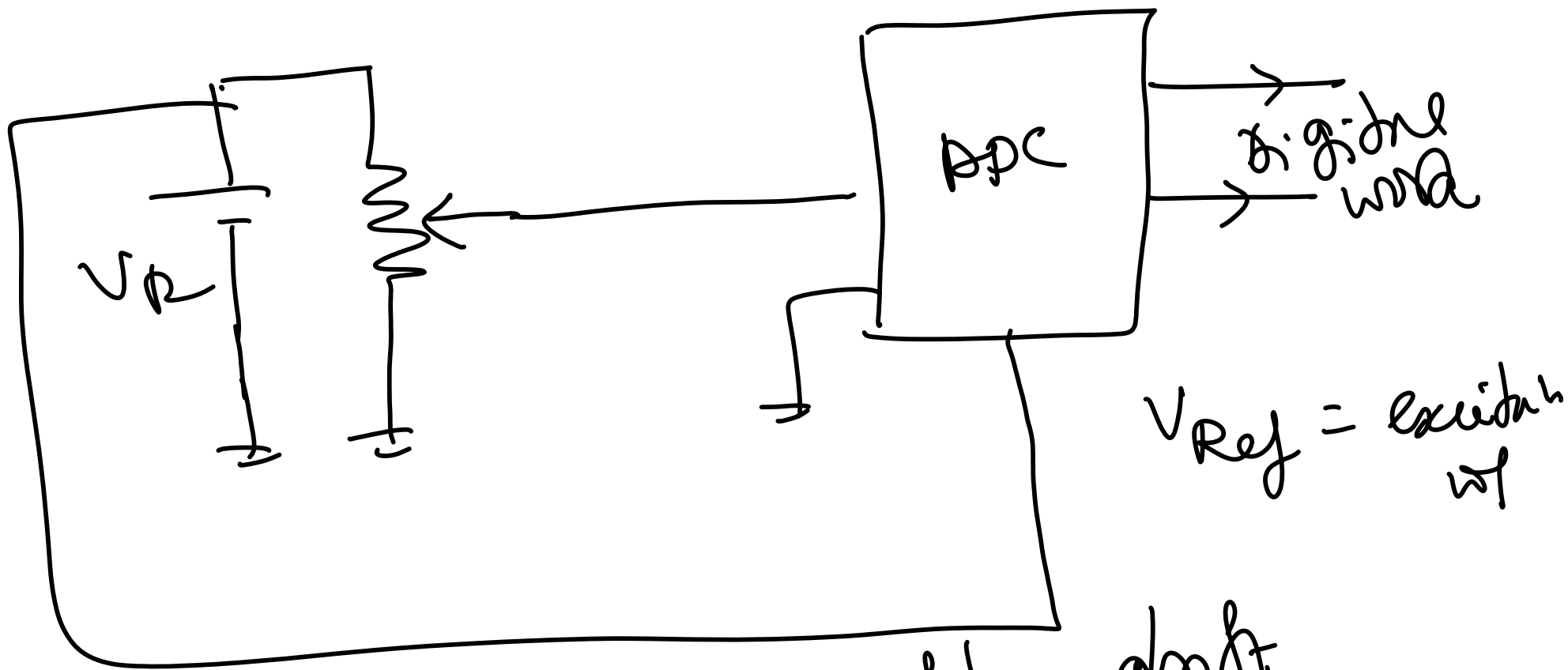
Digital output

Full Scale Digital
conversion

$$\frac{V_{in}}{V_R}$$

If V_R changes
then For given V_{in}
Digital output is changing
 V_{in} depends on the excitation
w.t.

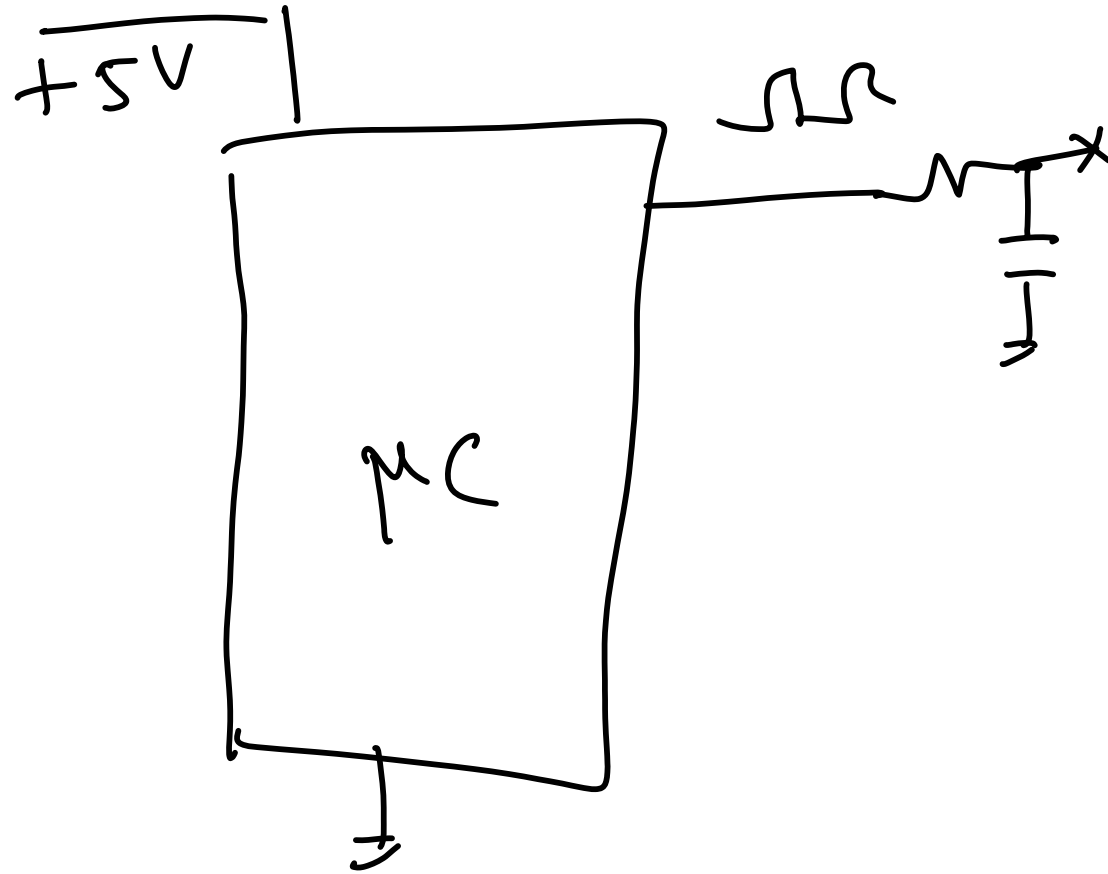
Make V_R as excitation w.t/daye
then no drift due to V_R



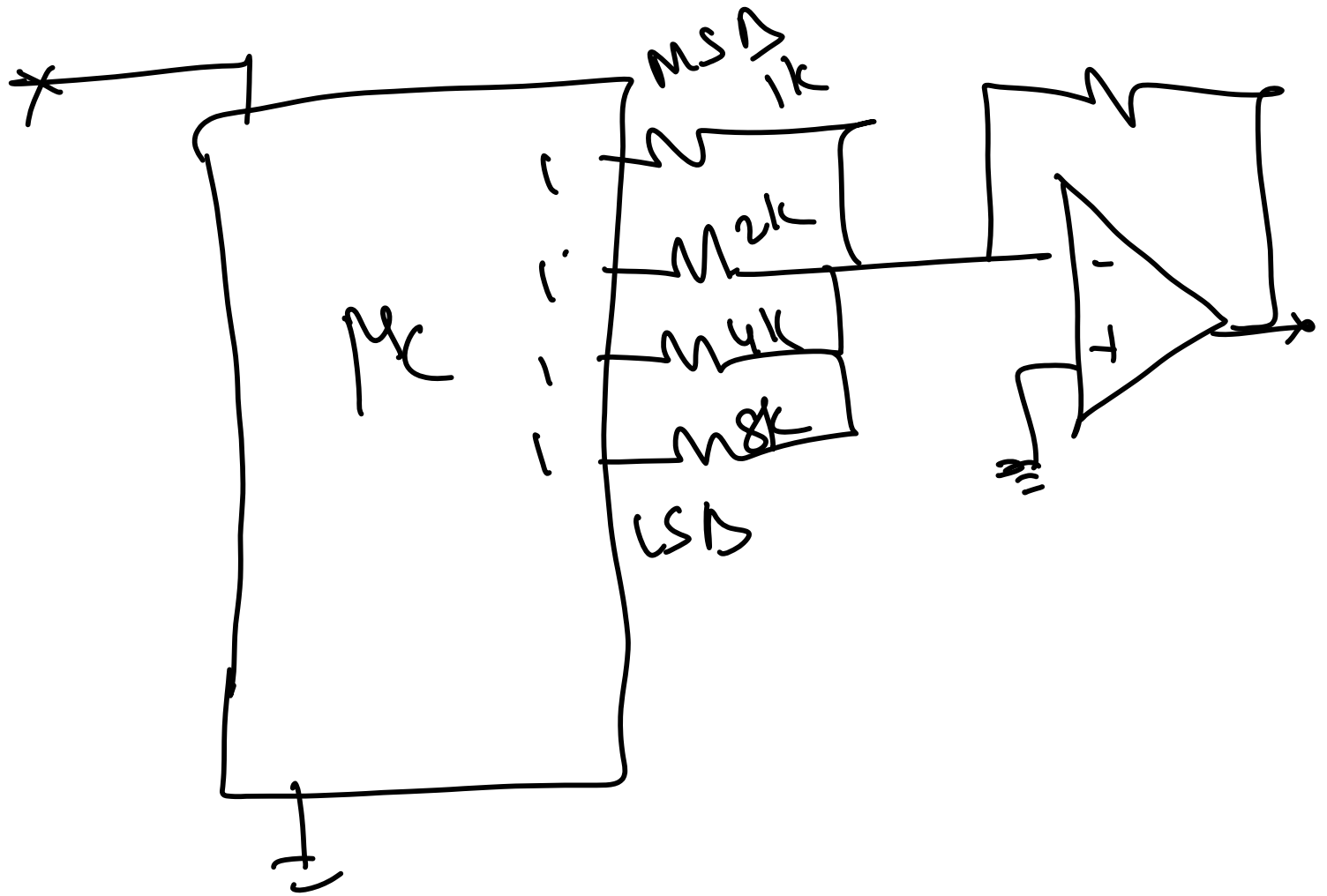
So reference will have no effect on the output

will have no effect on the output

DAC using MC



Binary weighted DAC using MC



Lecture no: 40

$\Sigma - D$ ADC

Dual Slope - noise rejection
good

but slow

Successive
app

— 2 μ s/bit
1 μ s/bit

getting 24 bit converter
is difficult ~~the~~ because we
need 24 bit DAC

When we need
say 24 bit or 32 bit resolution
but satisfied with 16 bit
accuracy then we can look for

$\Sigma - \rightarrow$ ADC

$\Sigma - \rightarrow$ ADC

Assume that $V_{in} = 0.5V$

Then if $V_o = 0.5$ at some time

Then $ADC \text{ output} = 10000000$
 $= 10000000$

$DAC \text{ output} = 0.5V$

This makes $adder \text{ output} = 0$

So $integrator$ will stop charging.

So V_o remains constant
ADC and DAC are also
fixed output

$$V_{in} = 0.5$$

$$V_{in} = 0.5 + 10 \mu V$$

For 16 bit Converter

1 LSB

$$= \frac{1}{2^{16}} = \frac{1}{64000} \text{ V}$$

$$= \frac{1}{64} \times 10^{-3} = \frac{1000}{64} \mu V$$

$$\approx 16 \mu V$$

$V_{in} = 0.5 \text{ V} \rightarrow$ a ADC input

is 0.5 V then

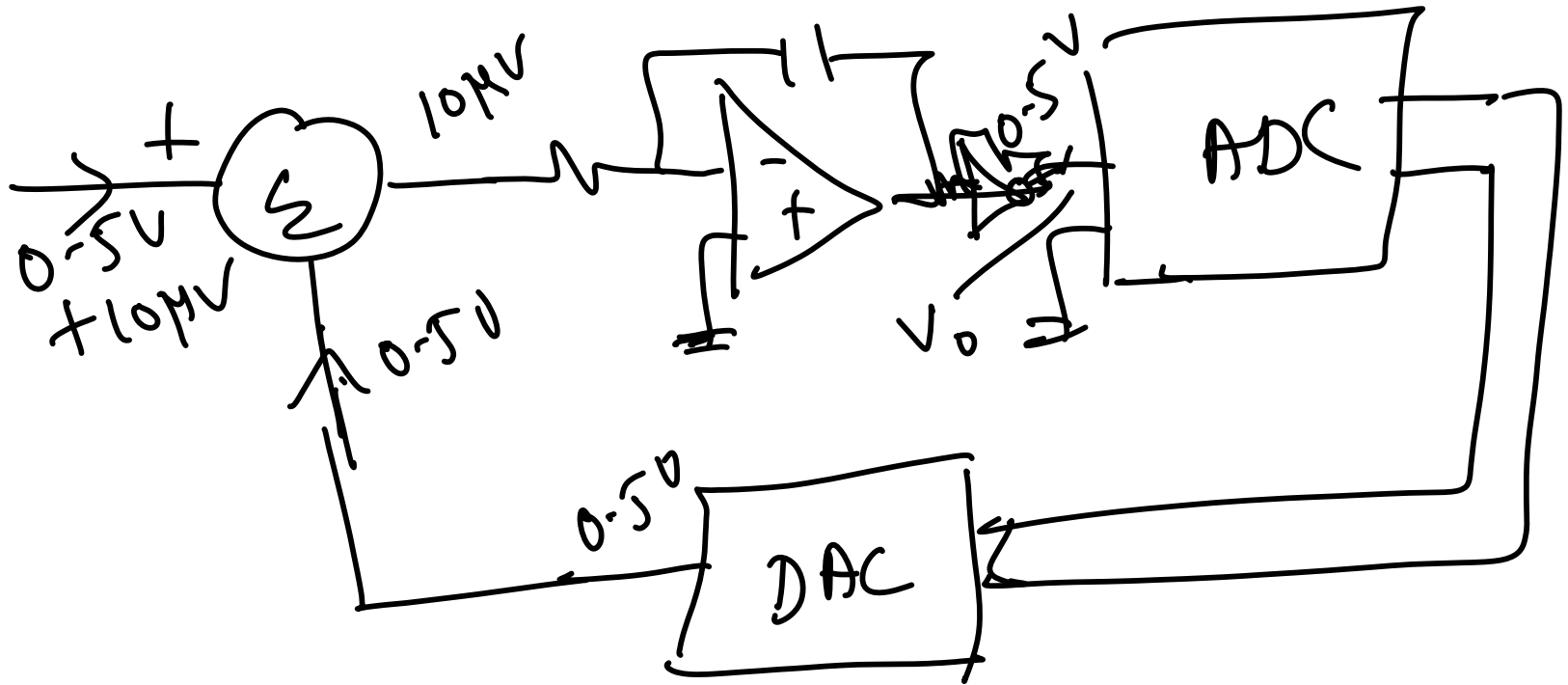
its output will be

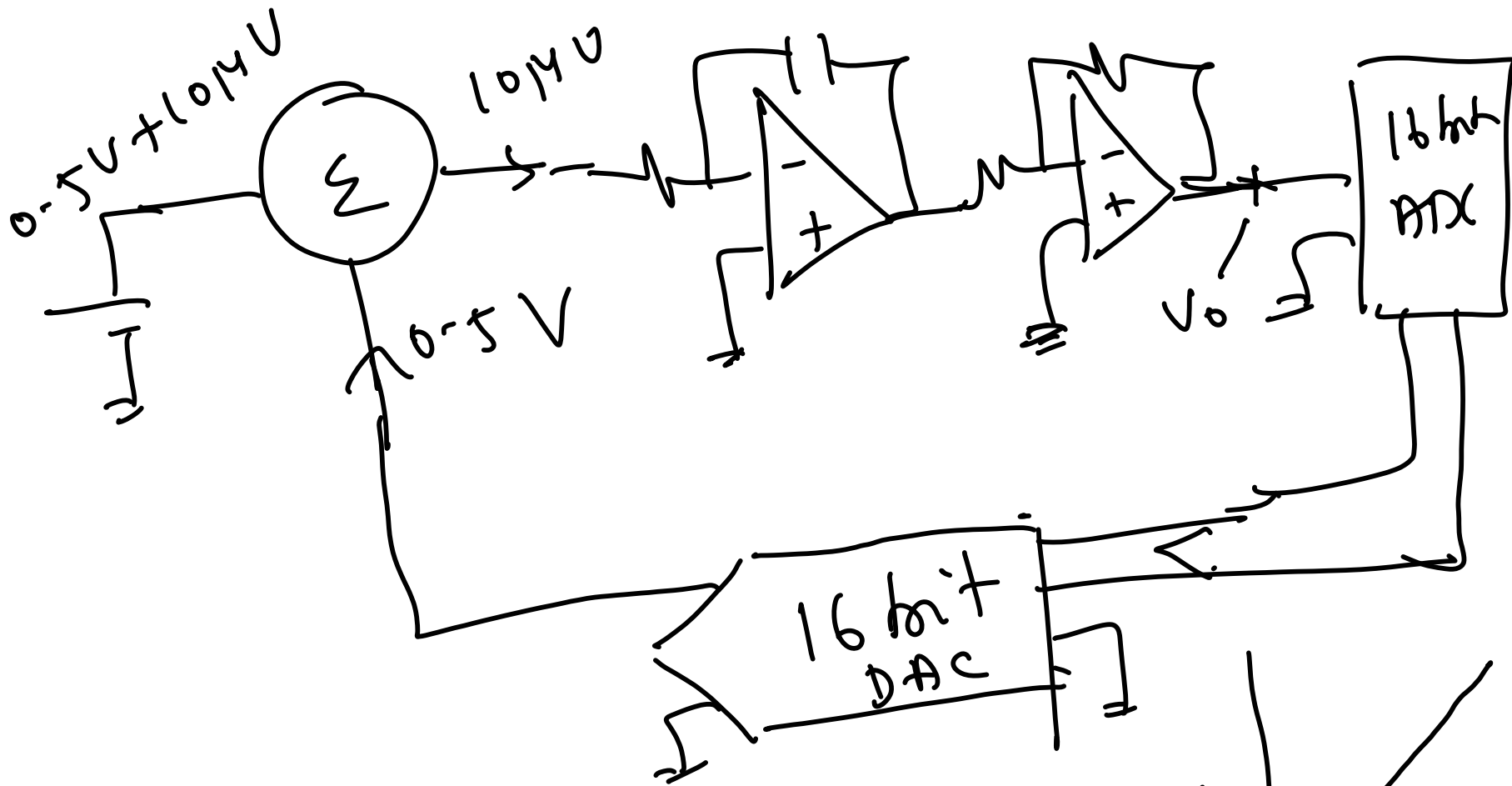
1000000
00000000

$$V_0 = 0.5 + 10 \mu V$$

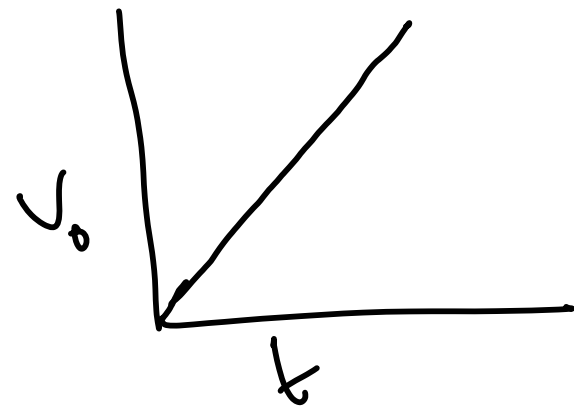
Den

$$\text{ADC} = 1000000000000000000$$
$$\text{DAC} = 0.5V$$

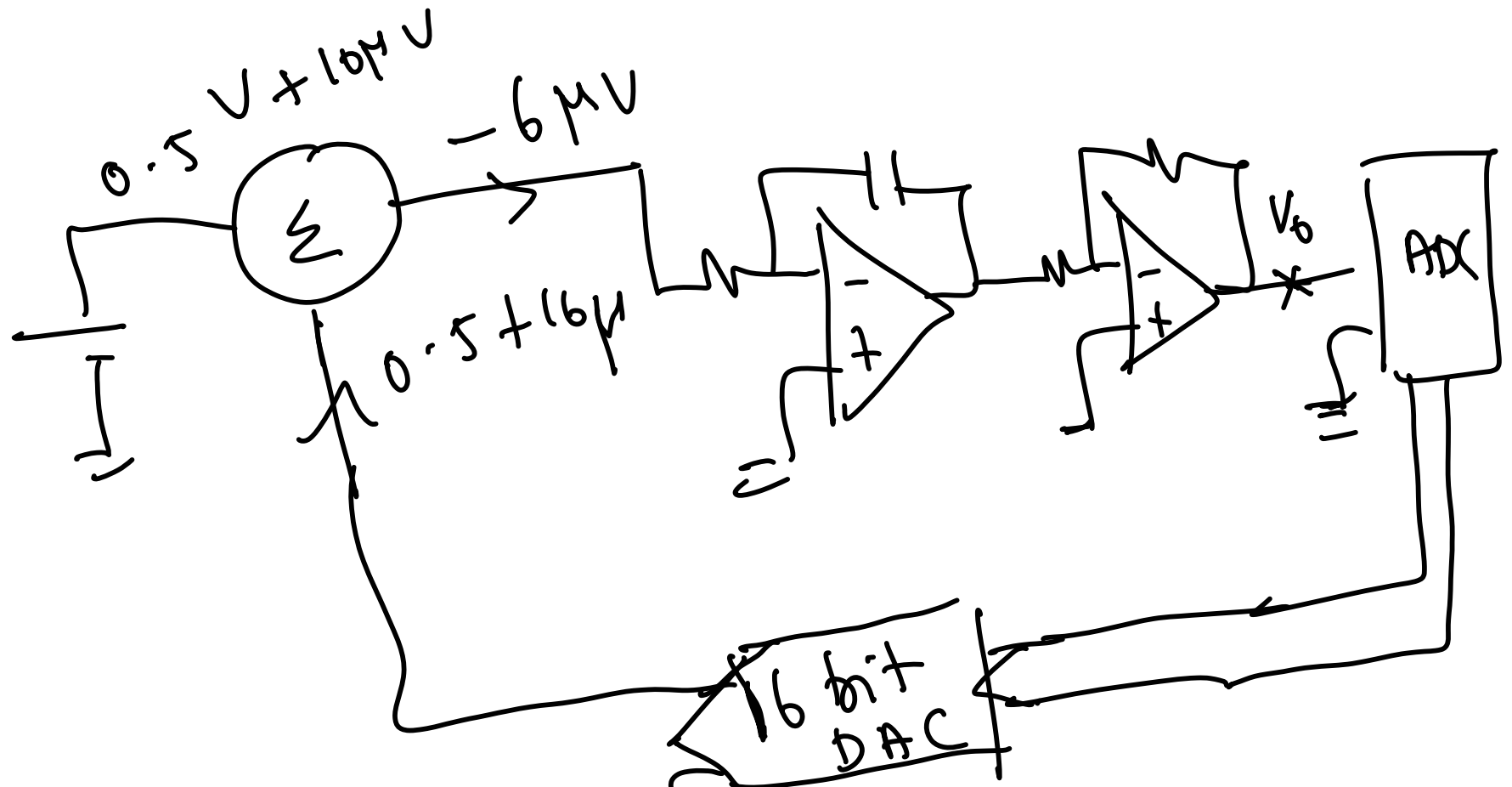




When v_o becomes $0.5V + 16\mu V$



ADC \rightarrow 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 =
 DAC \rightarrow 0.5 + 16μV



Integrator input is -ve
 So integrator started discharging
 So V_o started decreasing

When V_o becomes $0.5V$
 Then ADC \rightarrow 1000 0000 0000 0000 =
 DAC \rightarrow $0.5V$



That is ~~it~~ will make integrator
 to charge again. So V_o will

start increasing
 ADC \rightarrow 1000 0000 0000 0001 =
 DAC \rightarrow $0.5 + 16MV$

\bar{c} ADC \rightarrow 1000 0000 0000 0000
 0000
 0001
 ⋮

What is ADC output in time domain?

For 100 samples
 how many LSB's will be 1?
 and how many LSB's will be 0?

If the input is 0.5V
 Then All 100 LSB's will
 be zero

If the input is

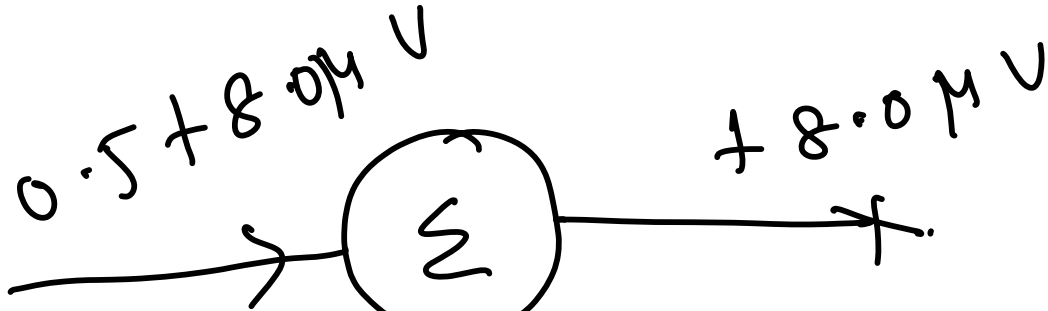
$$0.5V + 8\mu V$$

Then

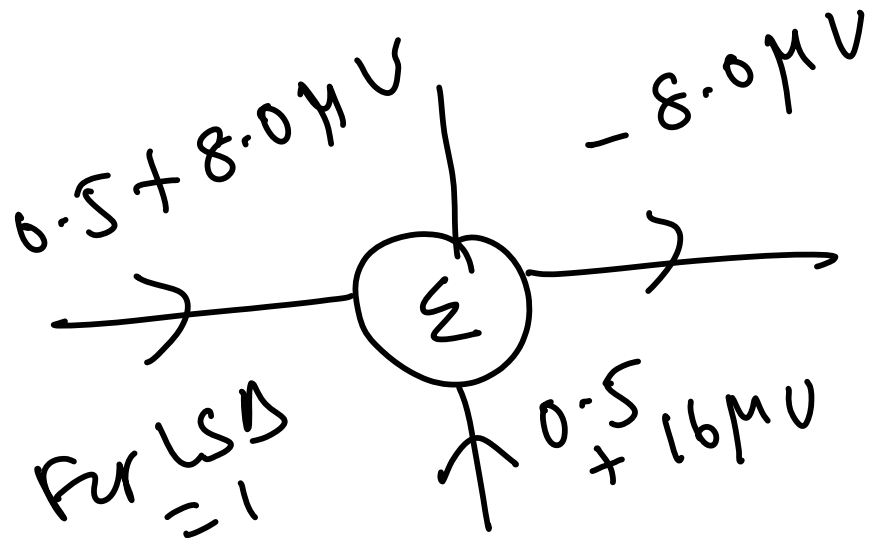
SD $\xrightarrow{\text{LSB}}$

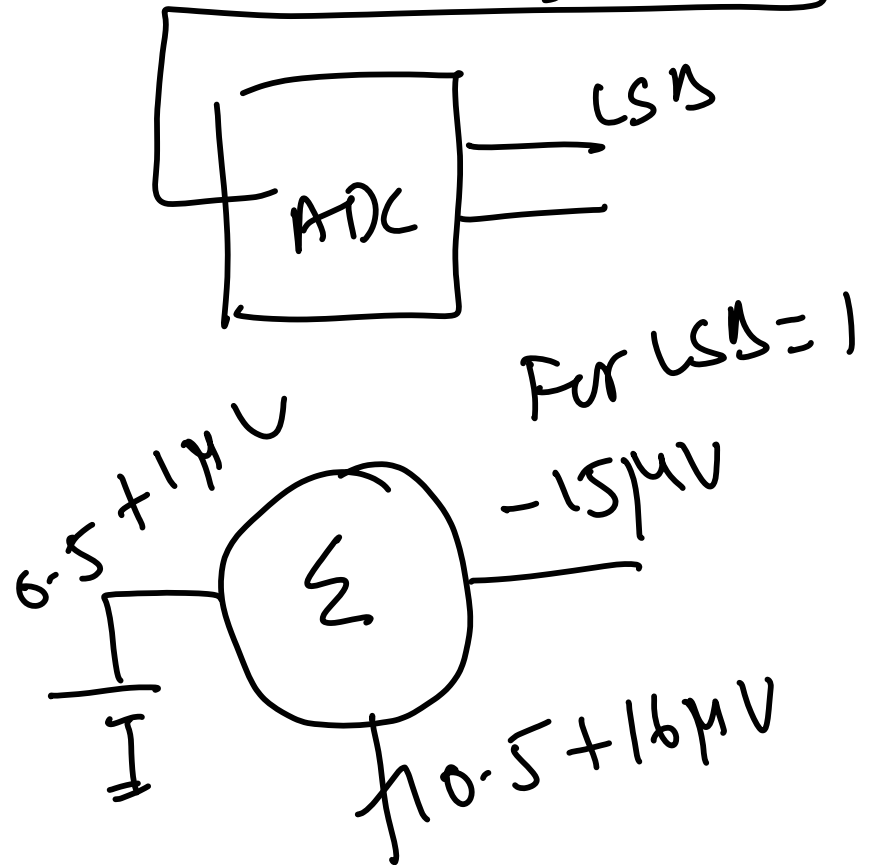
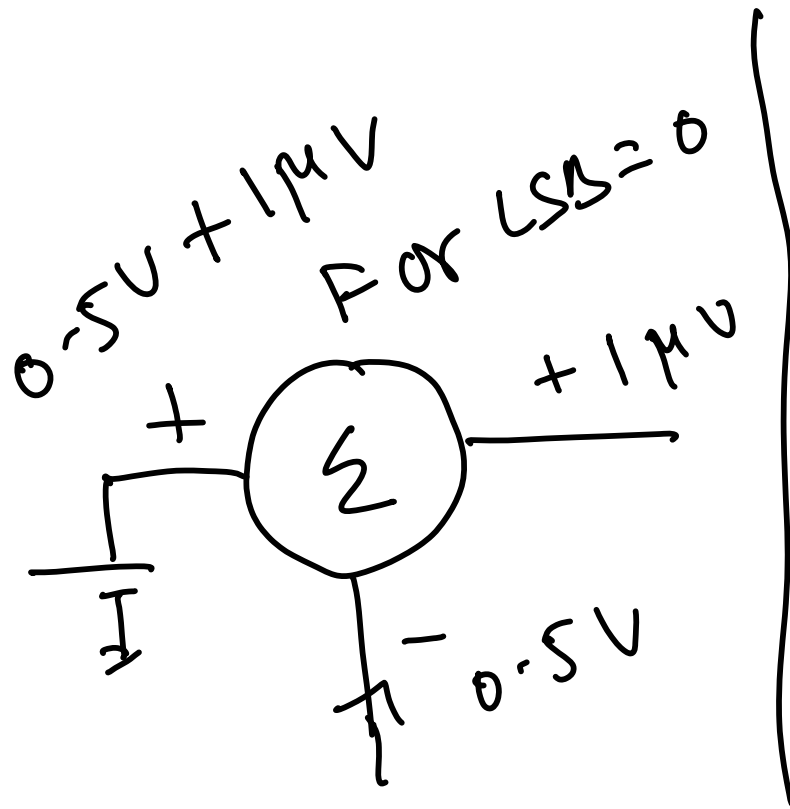
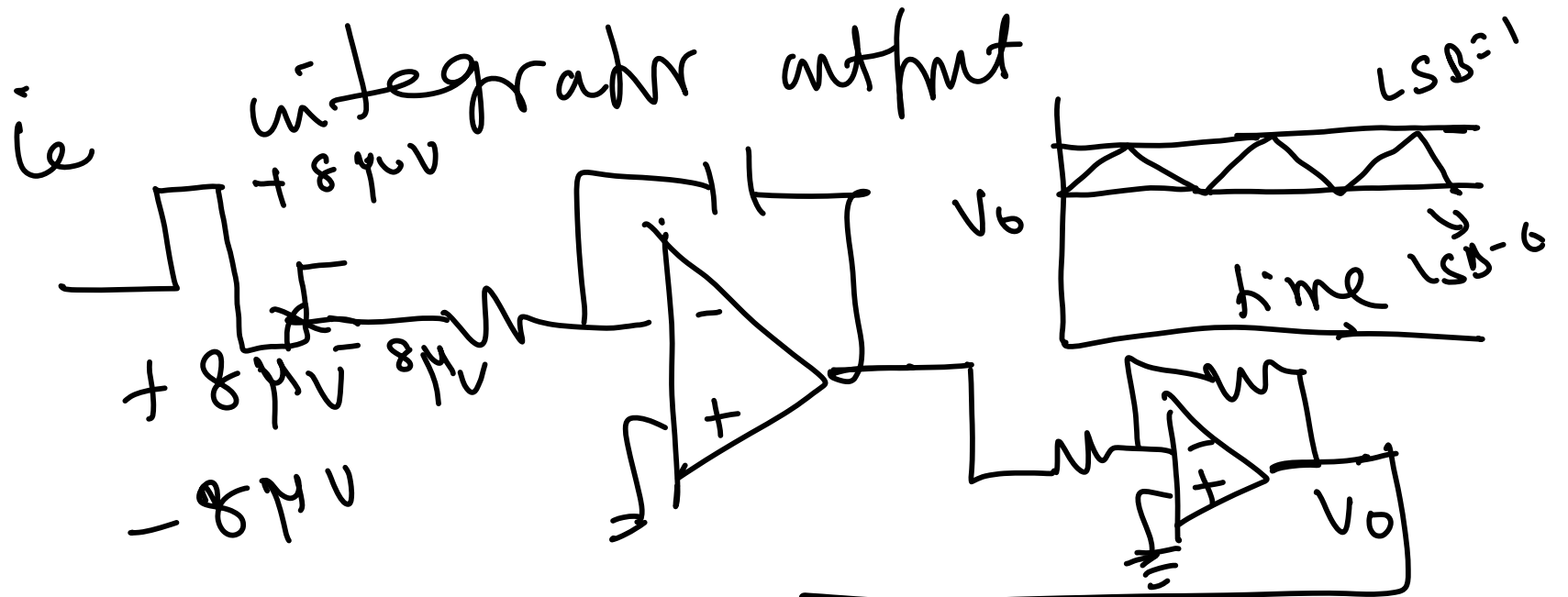
SD LSB'S

1 } analog
0 } 20

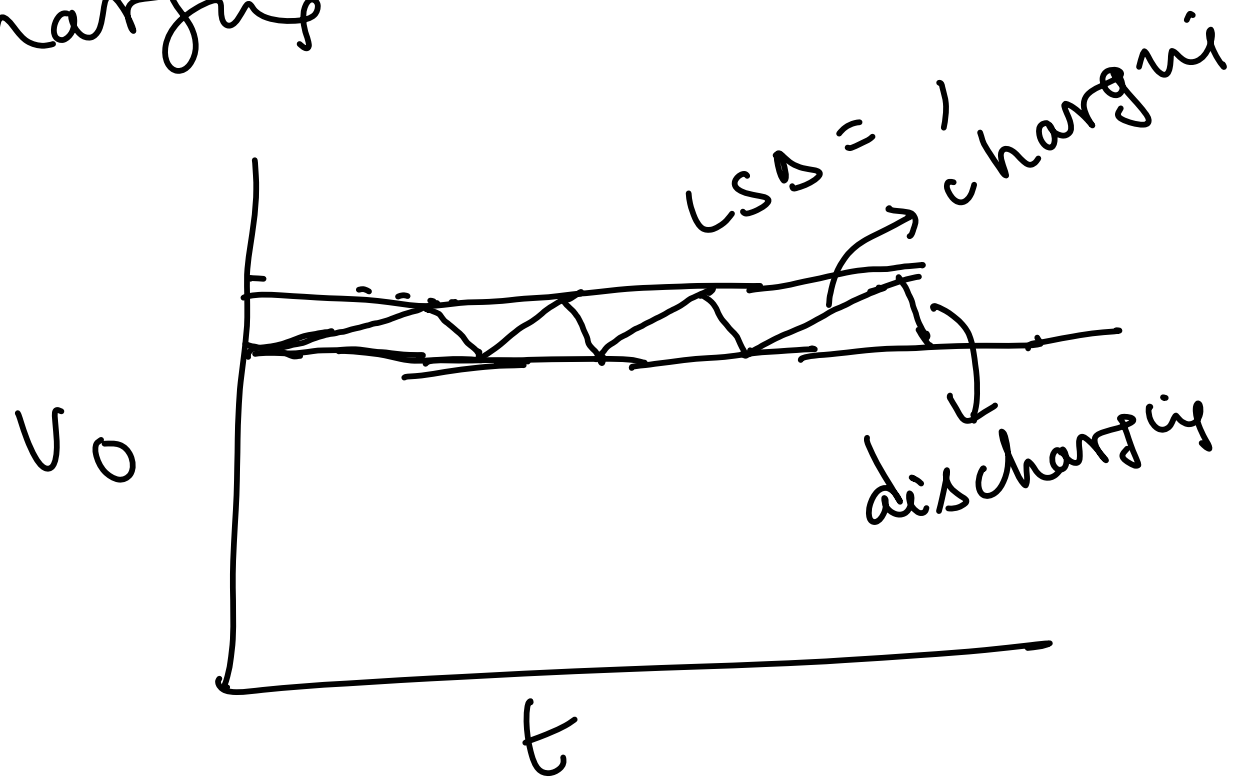


For
LSB = 0



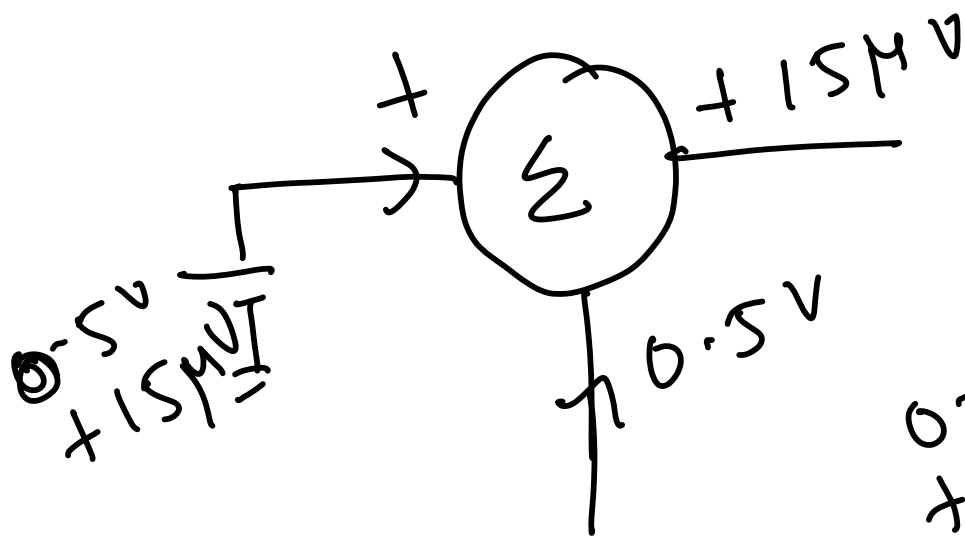


For this I_{nt} discharge is faster than charging

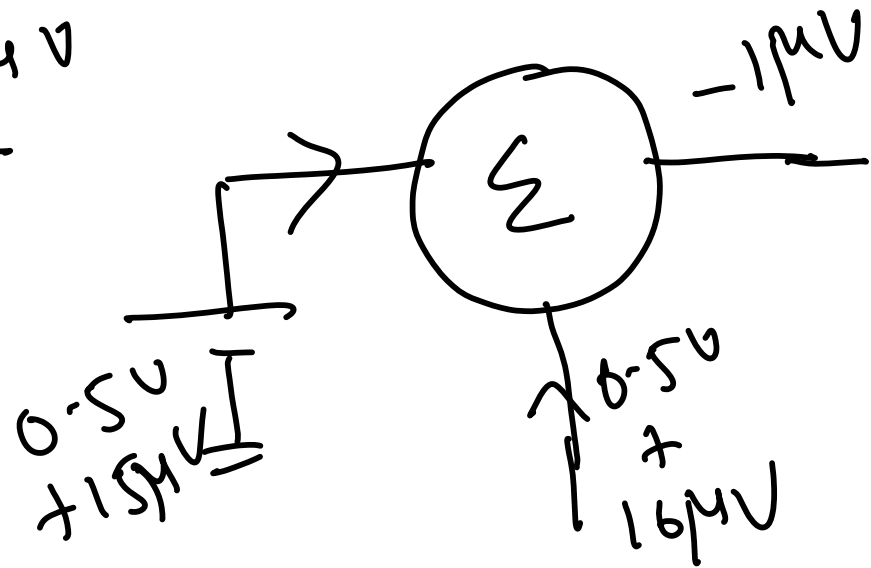


LSD 1 will be for less no. of time and LSD 0 will be obtained for more no. of times

For $V_m = 0.5 + 15\mu V$



$LSD = 0$



$LSD = 1$

As charging is fast and discharging is slow

For more no. of times

LSD is 1

less no. of times LSD = 0

Ratio between

LSD = 1

and LSD = 0

is same as ratio between

$$\frac{\text{fraction } V_{in}}{16}$$

and 16/4V

For example

$$\text{for } V_{in} = 0.5 + 1\mu V$$

Then the fraction is $\frac{1}{16}$

$$\text{for } V_{in} = 0.5 + 5\mu V$$

the fraction is $\frac{5}{16}$

The ADC LSB = 1 and $LSB = 0$
ratio also will be as as
 $\frac{1}{16}$ and $\frac{5}{16}$

over sample the ADC
and find out n and $n+1$
at the output

$$\frac{n}{n+1} = \frac{1}{16}$$

$$\text{or } 0.5 + 1 \mu\text{V}$$

$$\frac{n}{n+1} = \frac{5}{16}$$

$$\text{or } 0.5 + 5 \mu\text{V}$$

$$\frac{n}{n+1} = \frac{8}{16}$$

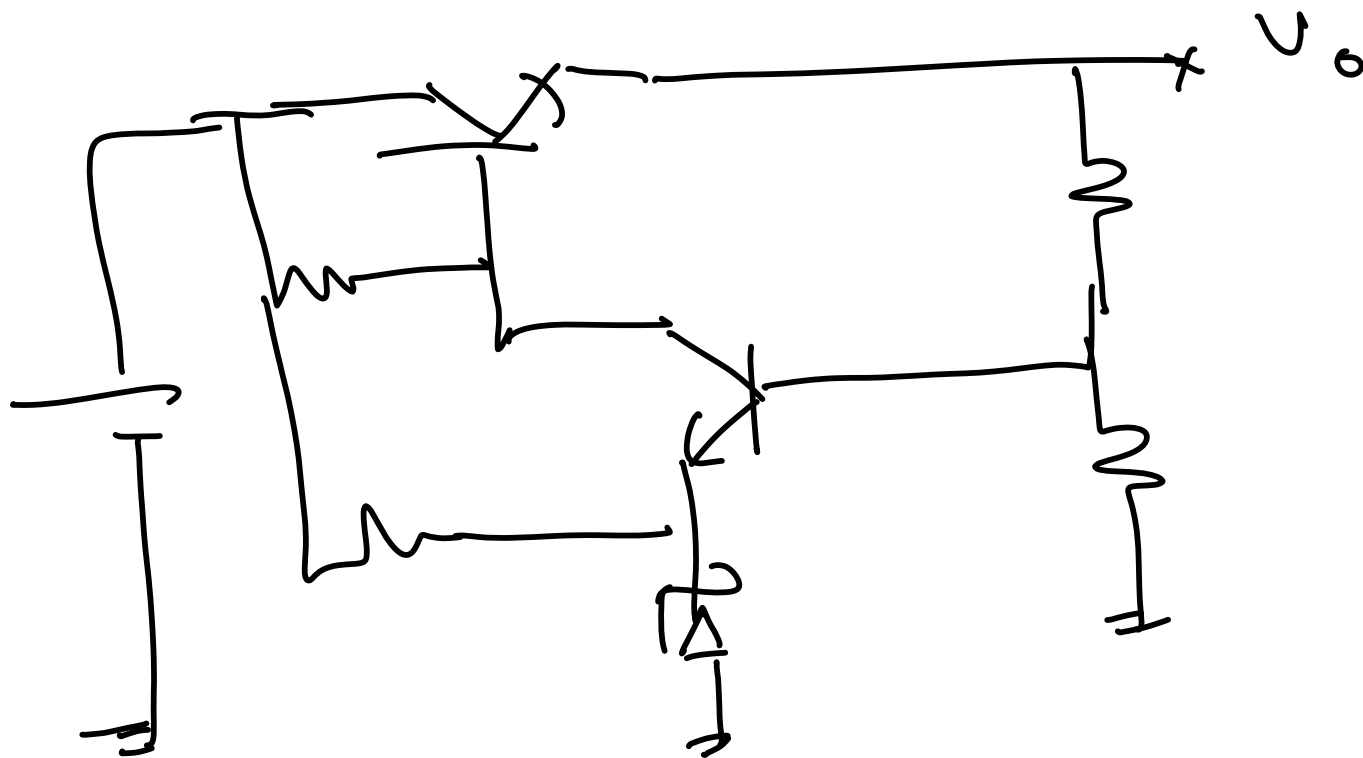
$$\text{or } 0.5 + 8 \mu\text{V}$$

By this way ADC Resolution
can be increased by over sampling

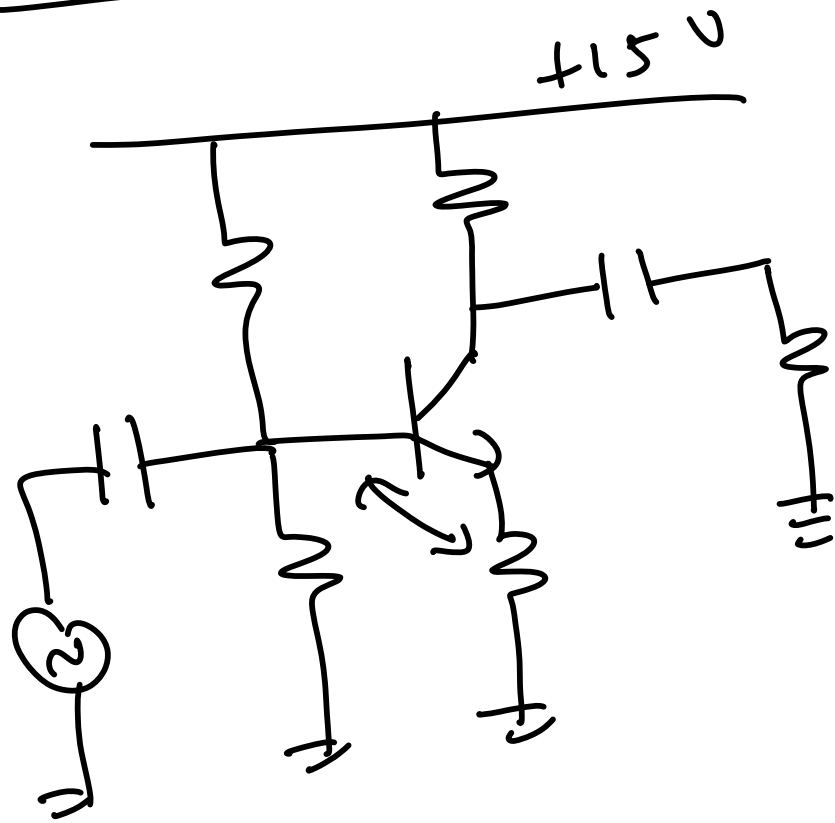
Using DSP over sampling
and the required calculations
are carried out.

So one can get resolution
more than 16 bit w/o
16 bit ADC and DAC
but accuracy is limited to
16 bit only.

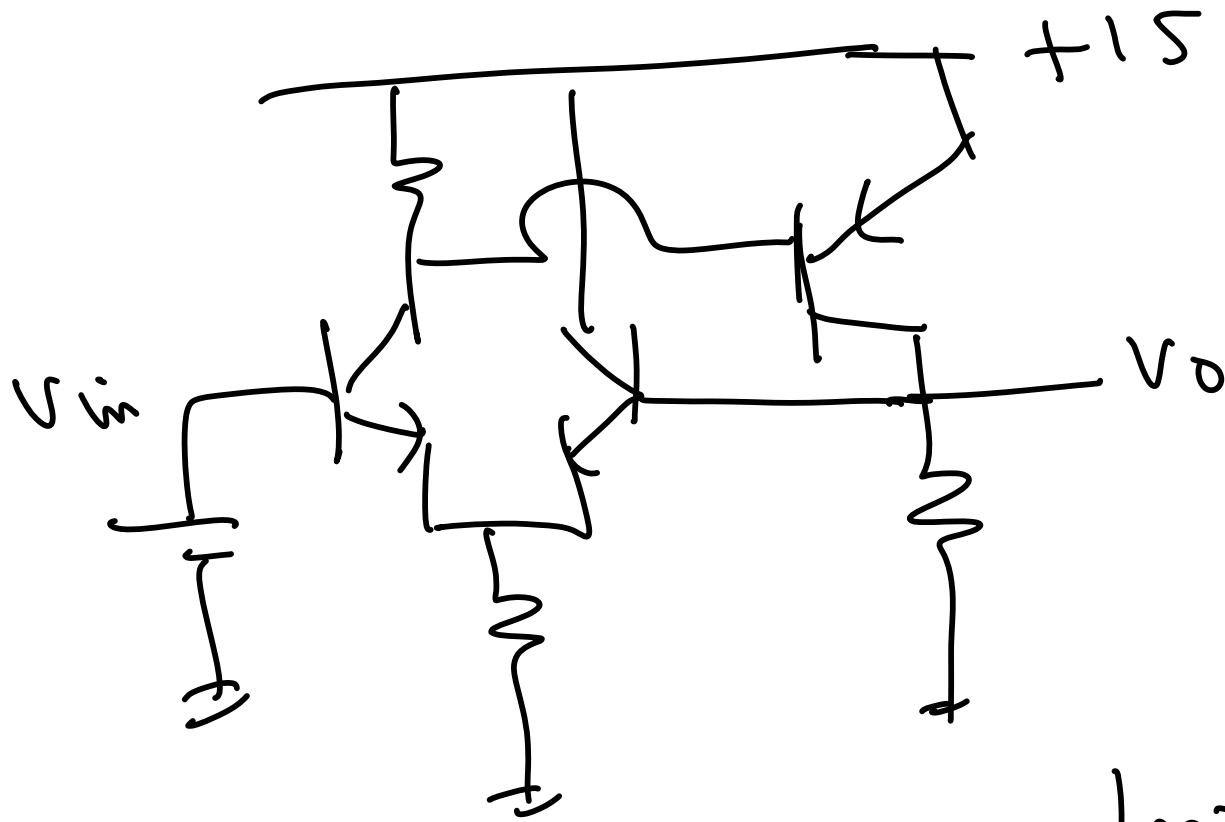
① Transistor applications
 ↳ as a switch $\begin{cases} \beta \gg 1 \\ \beta < 1 \end{cases}$
 as a latch
 to boost the current



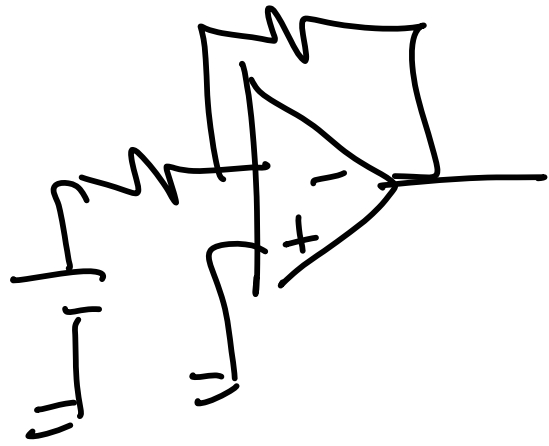
operational amplifiers



V_{BE} drift
creates problems
for DC amplification



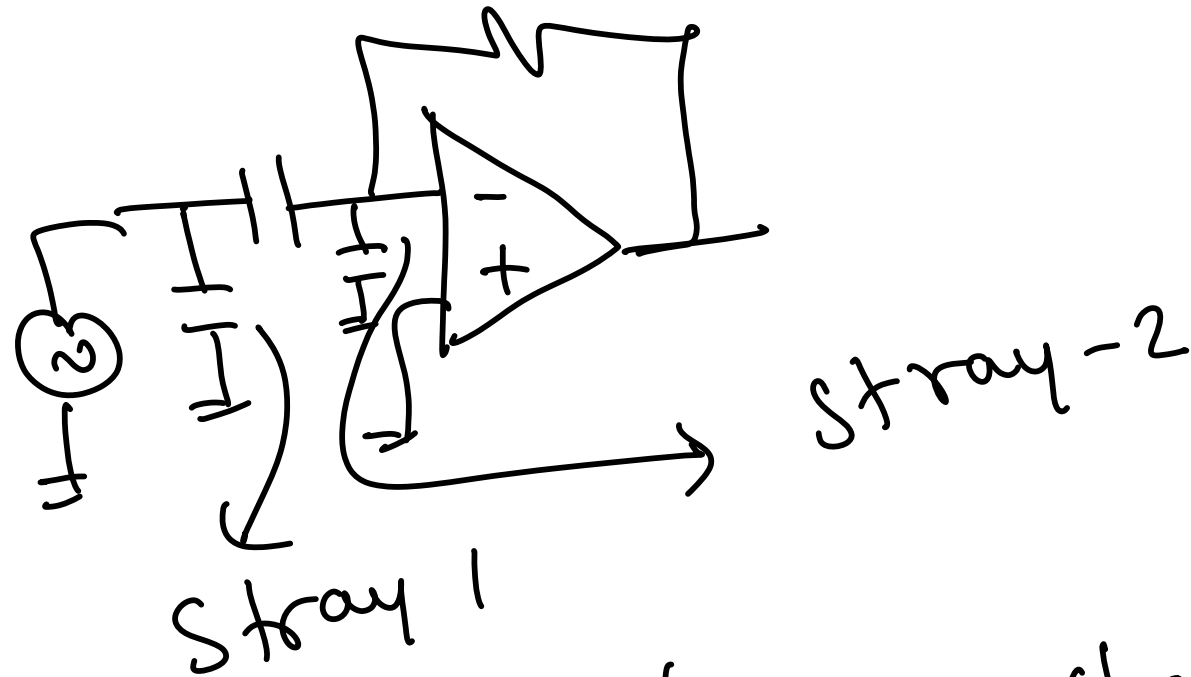
This v_o is not drifting
due to temp !!!



- ① Voltage regulator using op-amp
- ② Constant current source
- ③ 4 - 20 mA current transmitter
- ④ Transformer
- ⑤ LVDT signal conditioning
- ⑥ Capacitive transducers

⑦

Ratio transformer bridge applications



⑧

Solar based battery charging

Error budgeting

- ① Offset voltage drift
- ② Input resistance
- ③ Output resistance
- ④ Bias current errors
- ⑤ CMRR related errors

Making an error budget for the circuit is an important task for the analog circuit designer.

ADC / DAC

- ① Dual Slope ADC
- Dual slope ADC with MC

errors involved in these converters also discussed

- ② Successive approx

- ③ Flash ADC

- ④ $\Sigma - \Delta$ ADC

- ① Error budgeting
- ② Circuit design skill
- ③ Various techniques involved.

— x — x — x —