

$$\langle t \rangle \text{ or } \bar{t} = \frac{t_1 + t_2 + t_3 + \dots + t_N}{N}$$

$$\sum_{i=1}^N t_i = t_1 + t_2 + t_3 + \dots + t_N$$

$$D_i = m_i - \langle m \rangle$$

$$D_i = x_i - \langle x \rangle = \text{"deviation"}$$

$$\sum_i D_i = 0$$

average deviation = 0

$$\sum_i (d_i)^2 = \text{non-zero}$$

"Variance"

$$\text{Variance} = \sum_i (x_i - \bar{x})^2$$

Root  
mean  
square } deviation

~~RMS~~

RMS

deviation

$$= \sqrt{\frac{1}{N} \sum_i (D_i)^2}$$

$$70 - 23 = \underline{\underline{47}}$$

$$60 \pm 3$$

$$60 \pm (30)$$

Average  $\pm$  Standard deviation.

$$\begin{aligned}
 & \downarrow \qquad \qquad \downarrow \\
 & \langle x^2 \rangle + \frac{\langle x^2 \rangle^2}{N} - 2\langle x \rangle \frac{1}{N} \sum x_i \\
 & \langle x^2 \rangle - \langle x \rangle^2 - 2\langle x \rangle \langle x \rangle
 \end{aligned}$$

$$v = \frac{1}{N} \sum_i (x_i - \langle x \rangle)^2$$

$$= \frac{1}{N} \sum_{i=1}^N [x_i^2 + \langle x \rangle^2 - 2x_i \langle x \rangle]$$

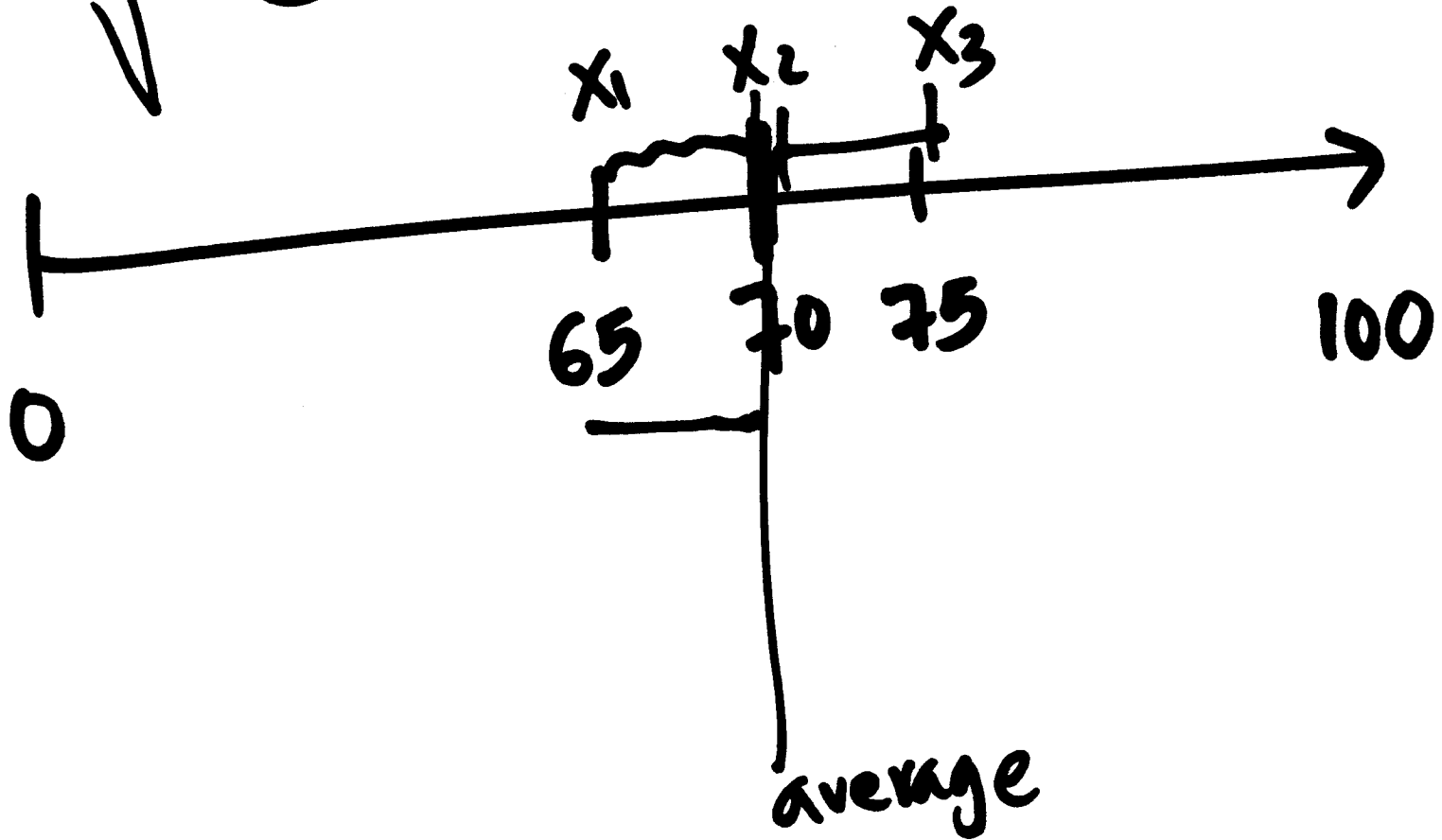
$$= \left( \frac{1}{N} \sum_{i=1}^N x_i^2 \right) + \frac{1}{N} \sum_{i=1}^N \langle x \rangle^2 - \frac{1}{N} \sum_{i=1}^N 2x_i \langle x \rangle$$

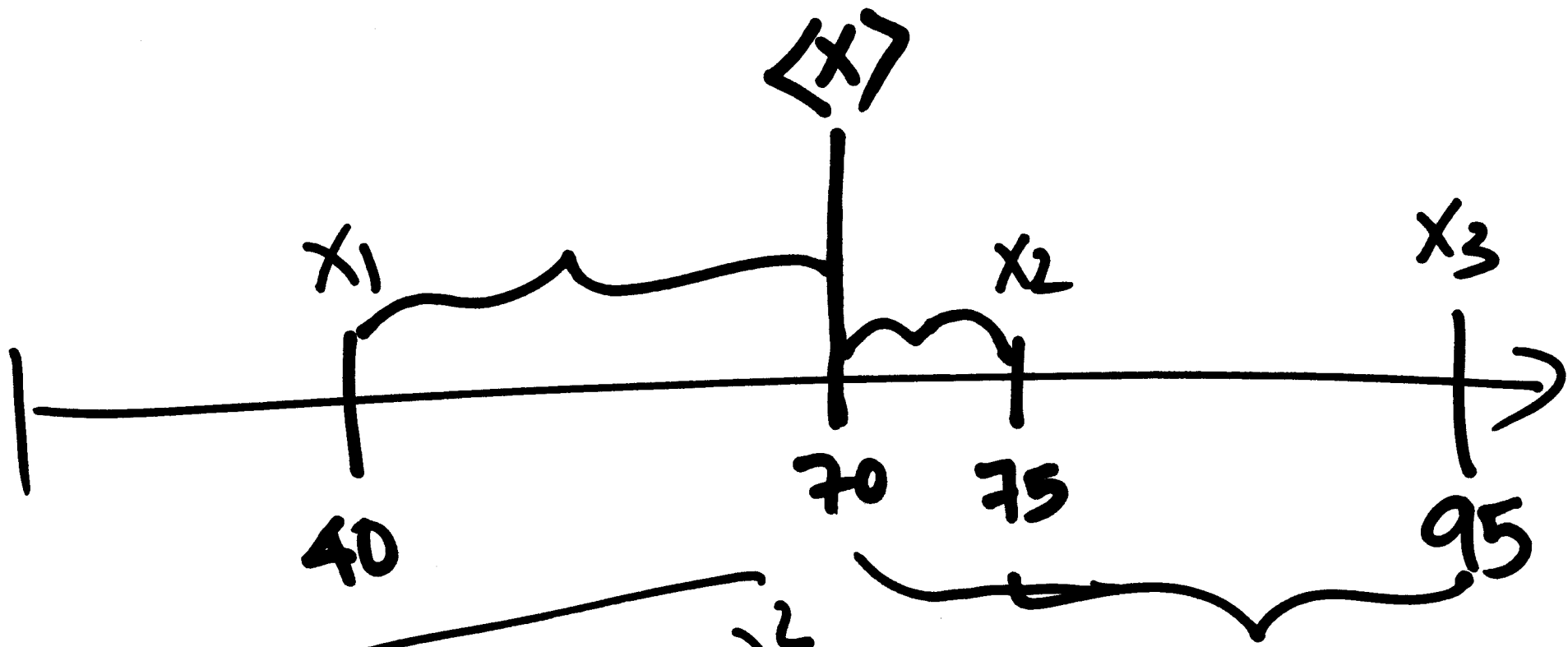


$$\text{Variance} = \langle x^2 \rangle - \langle x \rangle^2$$

$$\sigma = \sqrt{\langle x^2 \rangle - \langle x \rangle^2}$$

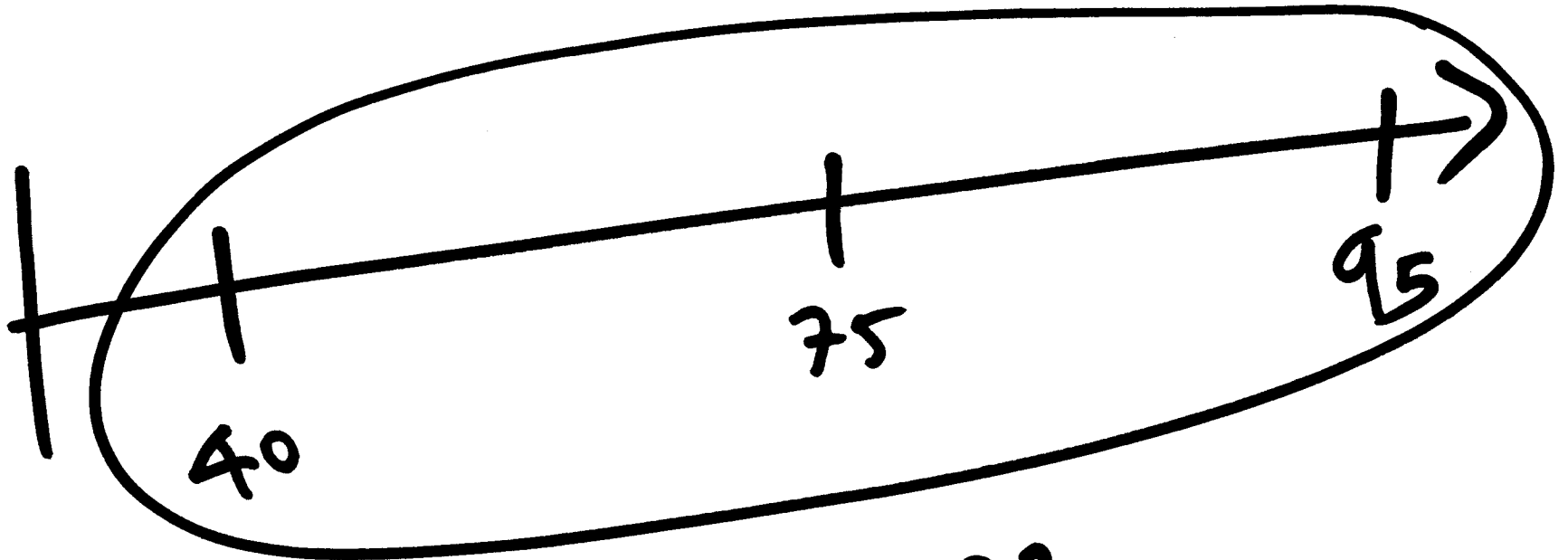
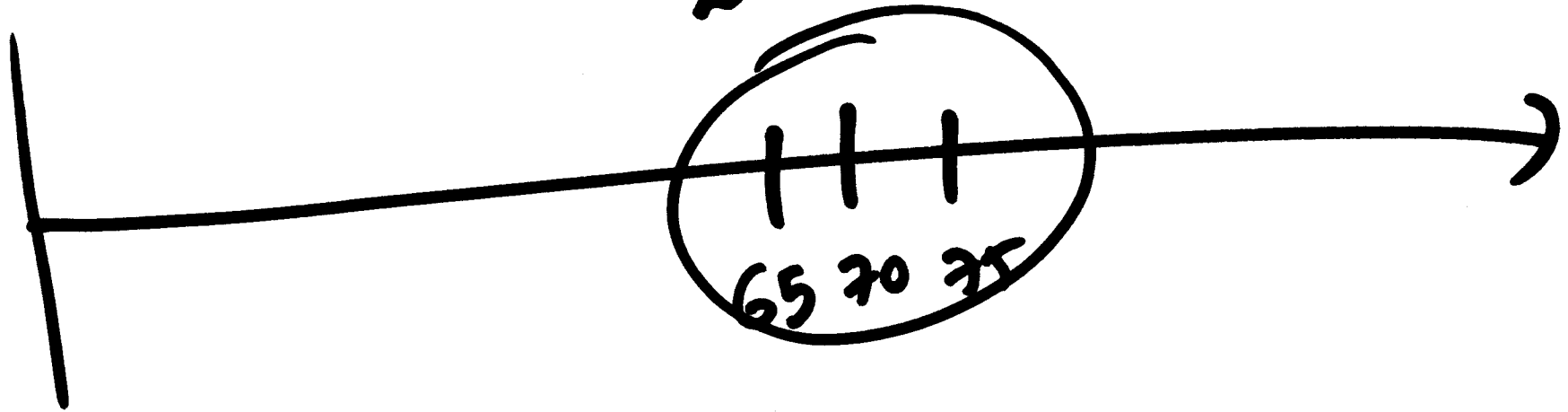
$$\sqrt{(x_1 - \mu)^2 + (x_2 - \mu)^2 + 0}$$





$$\begin{aligned} & (x_1 - \boxed{x})^2 + \\ & (x_2 - \boxed{x})^2 + \\ & (x_3 - \boxed{x})^2 + \end{aligned}$$

$$\approx 70 \pm 4 -$$



$$\approx 70 + 23$$